

COSI 127b

Introduction to Database Systems

Lecture 15: Normalization (4)

Review: Good DB Design

Three Approaches:

1. Ad hoc:

- use **Entity-Relationship Model** to model data requirements
- translate **ER** design into relational schema

Issue: How to tell if design is "good"?

2. Theoretical:

- construct **universal relations** (e.g., Borrower-All)
- **decompose** above using known **functional dependencies**

Issue: Time-Consuming and Complex

3. Practical:

- use ER Model to produce 1st cut DB design
- use FDs to refine and verify

Review: Functional Dependencies

Previously:

- What " $\mathbf{A_1, \dots, A_n} \rightarrow \mathbf{B}$ " means
- When sets of FDs are equivalent ($F \equiv G$)
 - if $F^+ = G^+$ (*FD set closures*)
 - *algorithms: Attribute Closures or Armstrong's Axioms*
- Minimal FD Sets (F_c = "Canonical Cover" of F)
- Canonical Cover Algorithm

Today:

- DB Design using FDs

Review: Canonical Cover (F_C)

One more algorithm over FD sets:

- **Canonical Cover (F_C)**: a "minimal" version of FD set, F
- F_C the "minimal" version of F ?
 1. equivalent to F ($F_C^+ = F^+$)
 2. "smaller" than other FD sets equivalent to F :
 - a) fewer FDs:
 $\{A \rightarrow B, B \rightarrow C\} < \{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$
 - b) fewer attributes in FDs:
 $\{A \rightarrow B, B \rightarrow C\} < \{A \rightarrow BC, B \rightarrow C\}$

Review: Canonical Cover (F_c)

Canonical Cover Algorithm

ALGORITHM Canonical-Cover (F : {FDs})

BEGIN

REPEAT UNTIL STABLE

1. Where possible, apply UNION rule to FD's in F
(Armstrong's Axioms)
2. Remove **extraneous** attributes from each FD in F
 - a) RHS: Is B **extraneous** in $A \rightarrow BC$?
$$\text{Is } (A \rightarrow B) \in (F - \{A \rightarrow BC\} \cup \{A \rightarrow C\})^+?$$
 - b) LHS: Is B **extraneous** in $AB \rightarrow C$?
$$\text{Is } (A \rightarrow C) \in F^+ ?$$

END

Review: Normalization

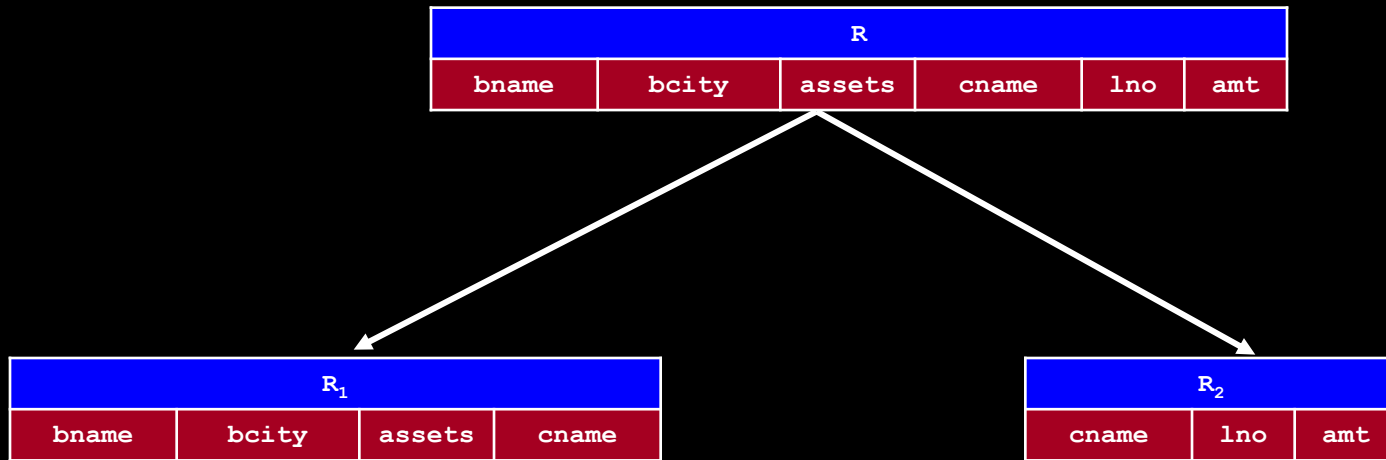
Basic Idea:

1. Start with **Universal Relation(s)**, R
 - all attributes in 1-2 tables
 - e.g., Borrower-All, Depositor-All

Borrower-All							
lno	cname	cstreet	ccity	bname	amt	bcity	assets
L-17	Jones	Main	Harrison	Downtown	1000	Brooklyn	9M
L-23	Smith	North	Rye	Redwood	2000	Palo Alto	2.1M
L-15	Hayes	Main	Harrison	Perry	1500	Horseneck	1.7M
L-17	Jackson	Senator	Brooklyn	Downtown	1000	Brooklyn	9M
L-93	Curry	Walnut	Stanford	Mianus	500	Horseneck	0.4M
L-11	Smith	North	Rye	R.H.	900	Horseneck	8M
L-16	Adams	Spring	Pittsfield	Perry	1300	Horseneck	1.7M

2. Determine FD set for R, F
3. **Decompose** R according to FDs in F^+

Review: Decomposition



Notation for schema decomposition:

$$R = R_1 \cup R_2$$

BTW: Not a Good Decomposition

Review: Decomposition Goals

1. Lossless Joins

- Avoid information loss

2. Redundancy Avoidance

- Avoid update anomalies

Relative Importance:

1: Primary Importance

2,3: Secondary Importance

3. Dependency Preservation

- Avoid expensive global integrity constraints

Review: Decomposition Goal Tests

Test of $R = R_1 \cup \dots \cup R_n$ with FD set F :

- Lossless Joins? iff for each decomposition step, $R_i = R_i \cup R_j$:
 $(R_1 \cap R_2 \rightarrow R_1)$ or $(R_1 \cap R_2 \rightarrow R_2)$

Review: Lossless Joins Test

Example 1: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$$R_1 = (A, C)$$

$$R_2 = (B, C)$$

$$F = \{ \mathbf{AB} \rightarrow \mathbf{C}, \mathbf{C} \rightarrow \mathbf{B} \}$$

Is the decomposition of R lossless?

A: 1) What are the candidate keys of R_1, R_2 ?

$$\mathbf{AC} \rightarrow \mathbf{R_1}$$

$$\mathbf{C} \rightarrow \mathbf{R_2}$$

2) What is $R_1 \cap R_2$?

C

3) Does $\mathbf{R_1} \cap \mathbf{R_2} \rightarrow \mathbf{R_1}$ or $\mathbf{R_1} \cap \mathbf{R_2} \rightarrow \mathbf{R_2}$?

Yes, $\mathbf{C} \rightarrow \mathbf{R_2}$

Therefore, decomposition of R is lossless

Review: Lossless Joins Test

Example 2: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$R_1 = (A, B, C)$

$R_2 = (B, C)$

$F = \{AB \rightarrow C, C \rightarrow B\}$

Is the decomposition of R lossless?

A: 1) What are the candidate keys of R_1, R_2 ?

$AB \rightarrow R_1, AC \rightarrow R_1$

$C \rightarrow R_2$

2) What is $R_1 \cap R_2$?

BC

3) Does $R_1 \cap R_2 \rightarrow R_1$ or $R_1 \cap R_2 \rightarrow R_2$?

Yes. $BC \rightarrow R_2$

Therefore, decomposition of R is lossless

Review: Decomposition Goal Tests

Test of $R = R_1 \cup \dots \cup R_n$ with FD set F :

- Lossless Joins? iff for each decomposition step, $R_i = R_i \cup R_j$:
 $(R_i \cap R_j \rightarrow R_i)$ or $(R_i \cap R_j \rightarrow R_j)$
- Redundancy Avoidance? iff for each R_i in decomposition result:
for each nontrivial, $X \rightarrow Y$ in F^+ covered by R_i , $X \rightarrow R_i$

Review: Redundancy Avoidance Test

Example 1: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$$R_1 = (A, C)$$

$$R_2 = (B, C)$$

$$F = \{ \mathbf{AB} \rightarrow \mathbf{C}, \mathbf{C} \rightarrow \mathbf{B} \}$$

Does decomposition of R have redundancy?

A: 1) What are the candidate keys of R_1, R_2 ?

$$\mathbf{AC} \rightarrow \mathbf{R_1}$$

$$\mathbf{C} \rightarrow \mathbf{R_2}$$

2) Which non-trivial FDs of F^+ are covered by R_1 ?

—



3) Which non-trivial FDs of F^+ are covered by R_2 ?

$$\mathbf{C} \rightarrow \mathbf{B}$$

$$(\mathbf{C} \rightarrow \mathbf{R_2})$$



Therefore, decomposition of R has no redundancy

Review: Redundancy Avoidance Test

Example 2: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$R_1 = (A, B, C)$

$R_2 = (B, C)$

$F = \{AB \rightarrow C, C \rightarrow B\}$

Does decomposition of R have redundancy?

A: 1) What are the candidate keys of R_1, R_2 ?

$AB \rightarrow R_1, AC \rightarrow R_1$

$C \rightarrow R_2$

2) Which non-trivial FDs of F^+ are covered by R_1 ?

$AB \rightarrow C$

$(AB \rightarrow R_1) \checkmark$

$C \rightarrow B$

$(C \not\rightarrow A \text{ so } C \not\rightarrow R_1) \times$

3) Which non-trivial FDs of F^+ are covered by R_2 ?

$C \rightarrow B$

$(C \rightarrow R_2) \checkmark$

Therefore, decomposition of R has redundancy

Review: Decomposition Goal Tests

Test of $R = R_1 \cup \dots \cup R_n$ with FD set F :

- Lossless Joins? iff for each decomposition step, $R_i = R_i \cup R_j$:
 $(R_1 \cap R_2 \rightarrow R_1)$ or $(R_1 \cap R_2 \rightarrow R_2)$
- Redundancy Avoidance? iff for each R_i in decomposition result:
for each nontrivial, $X \rightarrow Y$ in F^+ covered by R_i , $X \rightarrow R_i$
- Dependency Preserving? iff:

$$\left(\bigcup_{i=1}^n \{f \in F^+ \mid f \text{ covered by } R_i\} \right) = F^+$$

Review: Dependency Preservation Test

Example 1: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$$R_1 = (A, C)$$

$$R_2 = (B, C)$$

$$F = \{ \mathbf{AB} \rightarrow \mathbf{C}, \mathbf{C} \rightarrow \mathbf{B} \}$$

Is decomposition of R dependency preserving?

A: 1) Which non-trivial FDs of F^+ are covered by R_1 ?

—

2) Which non-trivial FDs of F^+ are covered by R_2 ?

$$\mathbf{C} \rightarrow \mathbf{B}$$

3) Does $(1 \cup 2)^+ = F^+$?

No. $(\mathbf{AB} \rightarrow \mathbf{C}) \in F^+$ but $(\mathbf{AB} \rightarrow \mathbf{C}) \notin \{\mathbf{C} \rightarrow \mathbf{B}\}^+$

Therefore, decomposition of R **is not** dependency preserving

Review: Dependency Preservation Test

Example 2: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$R_1 = (A, B, C)$

$R_2 = (B, C)$

$F = \{AB \rightarrow C, C \rightarrow B\}$

Is decomposition of R dependency preserving?

A: 1) Which non-trivial FDs of F^+ are covered by R_1 ?

$AB \rightarrow C$

$C \rightarrow B$

2) Which non-trivial FDs of F^+ are covered by R_2 ?

$C \rightarrow B$

3) Does $(1 \cup 2)^+ = F^+$?

Yes. $\{AB \rightarrow C, C \rightarrow B\}^+ = F^+$

Therefore, decomposition of R is dependency preserving

Review: Tests of Decomposition Goals

Example	Lossless Joins?	Avoids Redundancy?	Dependency Preserving?
$R_1 = (A, C)$ $R_2 = (B, C)$ $F = \{ \mathbf{AB} \rightarrow \mathbf{C}, \mathbf{C} \rightarrow \mathbf{B} \}$	yes	yes	no
$R_1 = (A, B, C)$ $R_2 = (B, C)$ $F = \{ \mathbf{AB} \rightarrow \mathbf{C}, \mathbf{C} \rightarrow \mathbf{B} \}$	yes	no	yes

Review: Goals of Decomposition

Goal	Motivation	Idea	Test
Lossless Joins	avoid info loss	recomposing tables should not add noise	For: $R = R_1 \cup R_2$ $(R_1 \cap R_2) \rightarrow R_1$ or $(R_1 \cap R_2) \rightarrow R_2$
Redundancy Avoidance	avoid update and deletion anomalies	only FD's with keys covered by decomposed tables	For any $X \rightarrow Y$ covered by R_i , X is a superkey of R_i
Dependency Preservation	efficient FD enforcement	fewer global ICs required to enforce FDs	For: $R = R_1 \cup \dots \cup R_n$ $(\text{FD's covered by each } R_i)^+ =$ $(\text{FD's covered by } R)^+$

Goals of Decomposition

Goal	Motivation	Idea	Test	Guaranteed By
Lossless Joins	avoid info loss	recomposing tables should not add noise	For: $R = R_1 \cup R_2$ $(R_1 \cap R_2) \rightarrow R_1$ or $(R_1 \cap R_2) \rightarrow R_2$	BCNF, 3NF
Redundancy Avoidance	avoid update and deletion anomalies	only FD's with keys covered by decomposed tables	For any $X \rightarrow Y$ covered by R_i , X is a superkey of R_i	BCNF
Dependency Preservation	efficient FD enforcement	fewer global ICs required to enforce FDs	For: $R = R_1 \cup \dots \cup R_n$ $(\text{FD's covered by each } R_i)^+ =$ $(\text{FD's covered by } R)^+$	3NF

Normalization

Normal Forms

- schema **in some normal form** if it satisfies certain properties
e.g., **BCNF**: lhs of FD covered by table is a key
- typically accompanied by **decomposition algorithm** that ensures result schema satisfies normal form

Normalization

Boyce-Codd Normal Form (BCNF):

- can result in many decompositions (schemas) for same relation + FD Set
- all result schemas satisfy
 1. lossless joins
 2. redundancy avoidance
 3. dependency preservation (sometimes, but not always possible)

Third Normal Form (3NF):

- can result in many decompositions (schemas) for same relation + FD Set
- all result schemas satisfy
 1. lossless joins
 2. dependency preservation (at least one schema satisfies)
 3. redundancy avoidance (sometimes, but not always possible)

Boyce-Codd Normal Form (BCNF)

Boyce-Codd Normal Form (BCNF):

- can result in many decompositions (schemas) for same relation + FD Set
- all result schemas satisfy
 1. lossless joins
 2. redundancy avoidance
 3. dependency preservation (sometimes, but not always possible)

Informally:

Relation schema R , with FD set F , is in BCNF if it avoids redundancy

Decomposition $R = R_1 \cup \dots \cup R_n$ with FD set F , is in BCNF if every
resulting relation, R_i , is in BCNF

Boyce-Codd Normal Form (BCNF)

Boyce-Codd Normal Form (BCNF):

- can result in many decompositions (schemas) for same relation + FD Set
- all result schemas satisfy
 1. lossless joins
 2. redundancy avoidance
 3. dependency preservation (sometimes, but not always possible)

Formally:

Relation schema R , with FD set F , is in BCNF if

for every nontrivial FD, $X \rightarrow Y$ in F^+ that is covered by R , $X \rightarrow R$

Decomposition $R = R_1 \cup \dots \cup R_n$ with FD set F , is in BCNF if every resulting relation, R_i , is in BCNF

Review: Redundancy Avoidance Test

Example 1: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$$R_1 = (A, C)$$

$$R_2 = (B, C)$$

$$F = \{ \mathbf{AB} \rightarrow \mathbf{C}, \mathbf{C} \rightarrow \mathbf{B} \}$$

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2) Which non-trivial FDs of F^+ are covered by R_1 ?

—



3) Which non-trivial FDs of F^+ are covered by R_2 ?

$$\mathbf{C} \rightarrow \mathbf{B}$$

$$(\mathbf{C} \rightarrow \mathbf{R_2})$$



Therefore, decomposition of R has no redundancy

Test for BCNF

Example 1: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$$R_1 = (A, C)$$

$$R_2 = (B, C)$$

$$F = \{ \mathbf{AB} \rightarrow \mathbf{C}, \mathbf{C} \rightarrow \mathbf{B} \}$$

Is decomposition of R in BCNF?

A: 1) What are the candidate keys of R_1, R_2 ?

$$\mathbf{AC} \rightarrow R_1$$

$$\mathbf{C} \rightarrow R_2$$

2) Which non-trivial FDs of F^+ are covered by R_1 ?

—



3) Which non-trivial FDs of F^+ are covered by R_2 ?

$$\mathbf{C} \rightarrow \mathbf{B}$$

$$(\mathbf{C} \rightarrow R_2) \checkmark$$

Therefore, decomposition of R is in BCNF

Review: Redundancy Avoidance Test

Example 2: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$R_1 = (A, B, C)$

$R_2 = (B, C)$

$F = \{AB \rightarrow C, C \rightarrow B\}$

Does decomposition of R have redundancy?

A: 1) What are the candidate keys of R_1, R_2 ?

$AB \rightarrow R_1, AC \rightarrow R_1$

$C \rightarrow R_2$

2) Which non-trivial FDs of F^+ are covered by R_1 ?

$AB \rightarrow C$

$(AB \rightarrow R_1) ? \checkmark$

$C \rightarrow B$

$(C \not\rightarrow A \text{ so } C \not\rightarrow R_1) \times$

3) Which non-trivial FDs of F^+ are covered by R_2 ?

$C \rightarrow B$

$(C \rightarrow R_2) ? \checkmark$

Therefore, decomposition of R has redundancy

Test for BCNF

Example 2: $R = R_1 \cup R_2$ ($R = (A, B, C)$)

$$R_1 = (A, B, C)$$

$$R_2 = (B, C)$$

$$F = \{AB \rightarrow C, C \rightarrow B\}$$

Is decomposition of R in BCNF?

A: 1) What are the candidate keys of R_1, R_2 ?

$$AB \rightarrow R_1, AC \rightarrow R_1$$

$$C \rightarrow R_2$$

2) Which non-trivial FDs of F^+ are covered by R_1 ?

$$AB \rightarrow C$$

$$(AB \rightarrow R_1) ? \checkmark$$

$$C \rightarrow B$$

$$(C \not\rightarrow A \text{ so } C \not\rightarrow R_1) \times$$

3) Which non-trivial FDs of F^+ are covered by R_2 ?

$$C \rightarrow B$$

$$(C \rightarrow R_2) ? \checkmark$$

Therefore, decomposition of R is not in BCNF

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

BCNF Decomposition Algorithm

Input: R : Relation, F : FD set

Output: Set of Relations forming decomposition of R

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

BCNF Decomposition Algorithm

Input: R : Relation, F : FD set

Output: Set of Relations forming decomposition of R

Initial result: $\{R\}$

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

BCNF Decomposition Algorithm

Input: R : Relation, F : FD set

Output: Set of Relations forming decomposition of R

Initial result: $\{R\}$

Repeat until all tables in result in BCNF

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

BCNF Decomposition Algorithm

Input: R : Relation, F : FD set

Output: Set of Relations forming decomposition of R

Initial result: $\{R\}$

Repeat until all tables in result in BCNF

Pick an R_i not in BCNF

Decompose on R_i

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

BCNF Decomposition Algorithm

Input: R : Relation, F : FD set

Output: Set of Relations forming decomposition of R

Initial result: $\{R\}$

Repeat until all tables in result in BCNF

Pick an R_i not in BCNF

i.e., some FD, $(\mathbf{X} \rightarrow \mathbf{Y}) \in F^+$ covered by R_i where X not a key of R_i

Decompose on R_i

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

BCNF Decomposition Algorithm

Input: R : Relation, F : FD set

Output: Set of Relations forming decomposition of R

Initial result: $\{R\}$

Repeat until all tables in result in BCNF

Pick an R_i not in BCNF

i.e., some FD, $(\mathbf{X} \rightarrow \mathbf{Y}) \in F^+$ covered by R_i where X not a key of R_i

Decompose on R_i

i.e., replace R_i with $\{R_{i1} = X \cup Y, R_{i2} = R_i - Y\}$ in result

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

Intuition: At each step until decomposition is in BCNF...

Decompose R_i on $(\mathbf{X} \rightarrow \mathbf{Y})$ (X not a key of R_i)

R_i					
A	B	C	D	E	H

decompose R_i on $(\mathbf{B} \rightarrow \mathbf{CD})$

$R_{i1} \leftarrow X \cup Y$

R_{i1}		
B	C	D

Observe: $\mathbf{B} \rightarrow \mathbf{CD}$ covered and $\mathbf{B} \rightarrow \mathbf{R}_{i1}$
Therefore, R_{i1} in BCNF

R_{i2}			
A	B	E	H

$R_{i2} \leftarrow R_i - Y$

R_{i1} may not be in BCNF, but we have made progress! ($\mathbf{B} \rightarrow \mathbf{CD}$ not covered)

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

```
ALGORITHM BCNF (R: Relation, F: FD set)
BEGIN
  Compute  $F^+$ 
  Result  $\leftarrow \{R\}$ 
  WHILE some  $R_i \in \text{Result}$  not in BCNF DO
    Choose non-trivial  $(\mathbf{X} \rightarrow \mathbf{Y}) \in F^+$  such that:
      • X not a key of  $R_i$ , and
      •  $(\mathbf{X} \rightarrow \mathbf{Y})$  covered by  $R_i$ 
    Decompose  $R_i$  on  $(\mathbf{X} \rightarrow \mathbf{Y})$ 
      •  $R_{i1} \leftarrow X \cup Y$ 
      •  $R_{i2} \leftarrow R_i - Y$ 
    Result  $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$ 
  RETURN Result
END
```

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

R		
A	B	C

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

R		
A	B	C

```
ALGORITHM BCNF (R: Relation, F: FD set)
BEGIN
  Compute  $F^+$ 
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  WHILE some  $R_i \in \text{Result}$  not in BCNF DO
    Choose non-trivial  $(X \rightarrow Y) \in F^+$  such that:
      •  $(X \rightarrow Y)$  covered by  $R_i$ 
      •  $X$  not a key of  $R_i$ 
    Decompose  $R_i$  on  $(X \rightarrow Y)$ 
      •  $R_{i1} \leftarrow X \cup Y$ 
      •  $R_{i2} \leftarrow R_i - Y$ 
    Result  $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$ 
  RETURN Result
END
```

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R		
A	B	C

What's the (Candidate) Key of R?

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R		
<u>A</u>	B	C

What's the (Candidate) Key of R?

A: A

```
ALGORITHM BCNF (R: Relation, F: FD set)
BEGIN
  Compute  $F^+$ 
  Result  $\leftarrow \{R\}$ 
  WHILE some  $R_i \in \text{Result}$  not in BCNF DO
    Choose non-trivial  $(X \rightarrow Y) \in F^+$  such that:
      •  $(X \rightarrow Y)$  covered by  $R_i$ 
      • X not a key of  $R_i$ 
    Decompose  $R_i$  on  $(X \rightarrow Y)$ 
      •  $R_{i1} \leftarrow X \cup Y$ 
      •  $R_{i2} \leftarrow R_i - Y$ 
    Result  $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$ 
  RETURN Result
END
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Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R		
<u>A</u>	B	C

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

 Compute F^+

Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN **Result**

END

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R		
<u>A</u>	B	C

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

 Compute F^+

Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN **Result**

END

Result = {R}

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R		
<u>A</u>	B	C

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

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- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Result = {R}

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R not in BCNF because of $B \rightarrow C$

R		
<u>A</u>	B	C

ALGORITHM BCNF (R : Relation, F : FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Result = {R}

Boyce-Codd Normal Form (BCNF)

A Simple Example:

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R not in BCNF because of $B \rightarrow C$

R		
<u>A</u>	B	C

Result = {R}

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

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- X not a key of R_i

Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

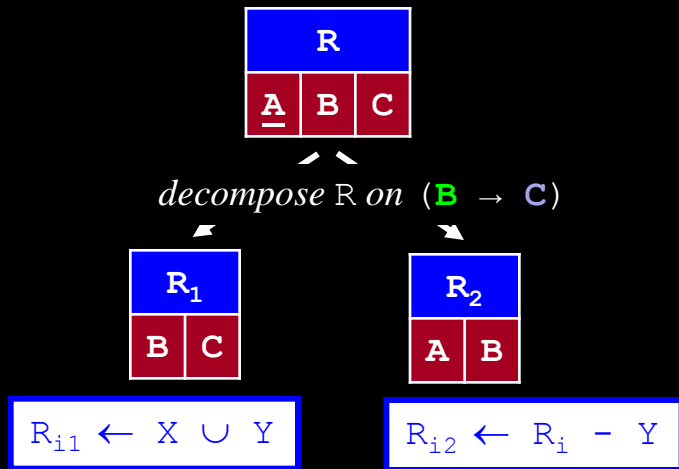
A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R not in BCNF because of $B \rightarrow C$



Result = {R}

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

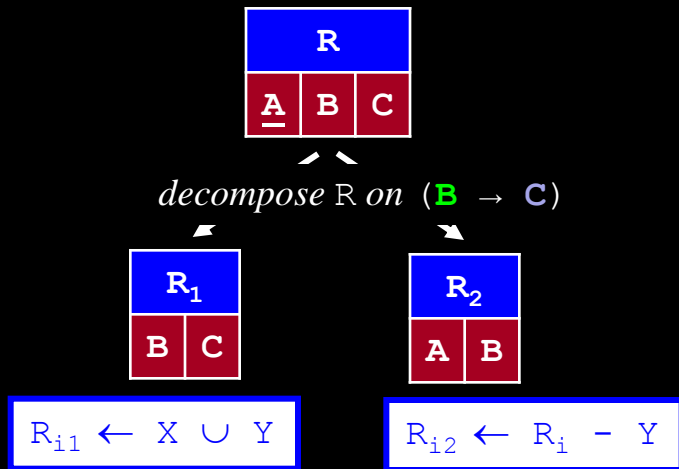
A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R not in BCNF because of $B \rightarrow C$



Result = {R}

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

Compute F^+

Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

Result \leftarrow **Result** - $\{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

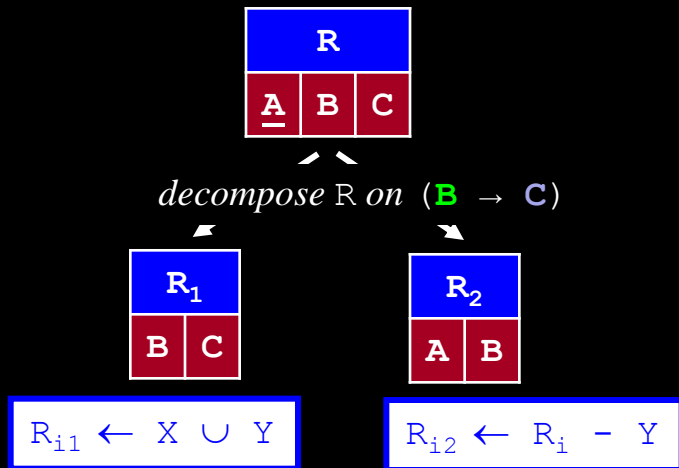
A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R not in BCNF because of $B \rightarrow C$



Result = {R₁, R₂}

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

Result \leftarrow **Result** - $\{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

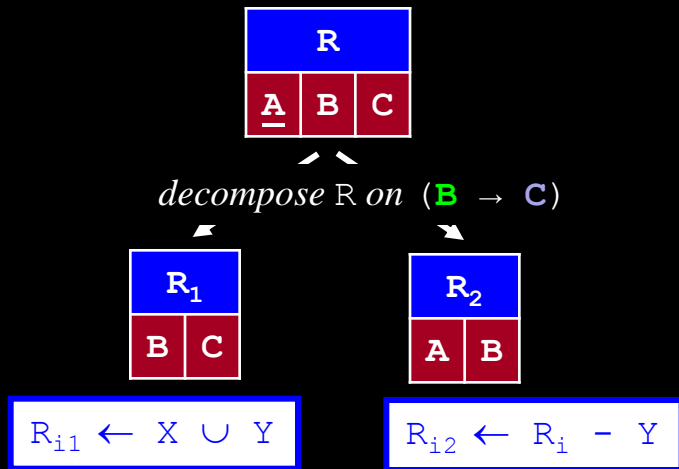
A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R not in BCNF because of $B \rightarrow C$



Result = $\{R_1, R_2\}$

ALGORITHM BCNF (R : Relation, F : FD set)

BEGIN

Compute F^+

Result $\leftarrow \{R\}$

WHILE some $R_i \in$ Result not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result \leftarrow Result $- \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R_1	
B	C

R_2	
A	B

- R_1 only covers $B \rightarrow C$
- B a key of R_1
- therefore in BCNF

- R_2 only covers $A \rightarrow B$
- A a key of R_2
- therefore in BCNF

Result = $\{R_1, R_2\}$

ALGORITHM BCNF (R : Relation, F : FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

R_1	
<u>B</u>	C

R_2	
<u>A</u>	B

- R_1 only covers $B \rightarrow C$
- B a key of R_1
- therefore in BCNF

- R_2 only covers $A \rightarrow B$
- A a key of R_2
- therefore in BCNF

Result = $\{R_1, R_2\}$

ALGORITHM BCNF (R : Relation, F : FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

A Simple Example:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

Result = $\{R_1, R_2\}$

R_1	
B	C

R_2	
A	B

ALGORITHM BCNF (R : Relation, F : FD set)

BEGIN

 Compute F^+

 Result $\leftarrow \{R\}$

WHILE some $R_i \in \text{Result}$ not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

Boyce-Codd Normal Form (BCNF)

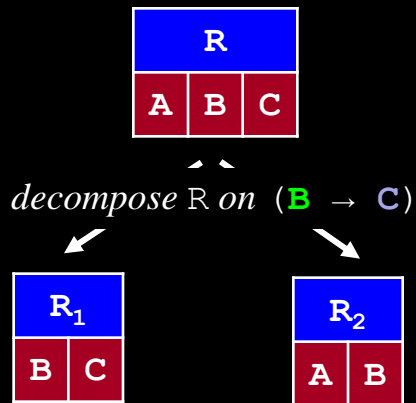
How derivations are usually expressed:

$R = (A, B, C)$

$F = \{A \rightarrow B, B \rightarrow C\}$

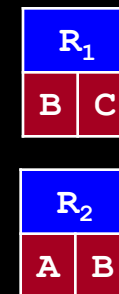
$F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C, \dots\}$

1. Derivation



2. Result

$$R = R_1 \cup R_2$$



Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

```
ALGORITHM BCNF (R: Relation, F: FD set)
BEGIN
  Compute  $F^+$ 
  Result  $\leftarrow \{R\}$ 
  WHILE some  $R_i \in \text{Result}$  not in BCNF DO
    Choose non-trivial  $(\mathbf{X} \rightarrow \mathbf{Y}) \in F^+$  such that:
      • X not a key of  $R_i$ , and
      •  $(\mathbf{X} \rightarrow \mathbf{Y})$  covered by  $R_i$ 
    Decompose  $R_i$  on  $(\mathbf{X} \rightarrow \mathbf{Y})$ 
      •  $R_{i1} \leftarrow X \cup Y$ 
      •  $R_{i2} \leftarrow R_i - Y$ 
    Result  $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$ 
  RETURN Result
END
```

Boyce-Codd Normal Form (BCNF)

An Algorithm to Decompose A Relation into BCNF:

ALGORITHM BCNF (R: Relation, F: FD set)

BEGIN

Compute F^+

Result $\leftarrow \{$

exponential cost (using either Attribute Closures, Armstrong's Axioms)!!

WHILE some $R_i \in$ Result not in BCNF **DO**

 Choose non-trivial $(X \rightarrow Y) \in F^+$ such that:

- $(X \rightarrow Y)$ covered by R_i
- X not a key of R_i

 Decompose R_i on $(X \rightarrow Y)$

- $R_{i1} \leftarrow X \cup Y$
- $R_{i2} \leftarrow R_i - Y$

 Result \leftarrow Result $- \{R_i\} \cup \{R_{i1}, R_{i2}\}$

RETURN Result

END

When an Algorithm Calls for F^+

Where We Have Seen It...:

- 1) Equivalence of FD sets ($F^+ = G^+$)
 - **avoid** by using canonical cover algorithm

2) Canonical Cover Algorithm

```
... 2. Remove extraneous attributes from each FD in X  
    a) RHS: B extraneous in  $A \rightarrow BC$ ?  
        True if  $(A \rightarrow B) \in (F - \{A \rightarrow BC\} \cup \{A \rightarrow C\})^+ \dots$   
  
    b) LHS: B extraneous in  $AB \rightarrow C$ ?  
        True if  $(A \rightarrow C) \in F^+ \dots$ 
```

- **avoid** by computing attribute closure (A^+)

3) BCNF algorithm

- **avoid** by ...?

When an Algorithm Calls for F^+

Strategy: Compute F^+ Lazily....:

- 1) Compute F_c using Canonical Cover Algorithm
- 2) Use F_c to derive FD's in F^+ as needed, using Armstrong's Axioms

official:

```
ALGORITHM BCNF (R: Relation, F: FD set)
BEGIN
  Compute  $F^+$ 
  Result  $\leftarrow \{R\}$ 
  WHILE some  $R_i \in \text{Result}$  not in BCNF DO
    Choose non-trivial  $(X \rightarrow Y) \in F^+$  such that:
      •  $(X \rightarrow Y)$  covered by  $R_i$ 
      •  $X$  not a key of  $R_i$ 
    Decompose  $R_i$  on  $(X \rightarrow Y)$ 
      •  $R_{i1} \leftarrow X \cup Y$ 
      •  $R_{i2} \leftarrow R_i - Y$ 
    Result  $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$ 
  RETURN Result
END
```

When an Algorithm Calls for F^+

Strategy: Compute F^+ Lazily....:

- 1) Compute F_c using Canonical Cover Algorithm
- 2) Use F_c to derive FD's in F^+ as needed, using Armstrong's Axioms

revised:

```
ALGORITHM BCNF (R: Relation, F: FD set)
BEGIN
  Compute  $F_c$ 
  Result  $\leftarrow \{R\}$ 
  WHILE some  $R_i \in \text{Result}$  not in BCNF DO
    Use  $F_c$  to derive non-trivial  $(X \rightarrow Y) \in F^+$  s.t:
      •  $(X \rightarrow Y)$  covered by  $R_i$ 
      •  $X$  not a key of  $R_i$ 
    Decompose  $R_i$  on  $(X \rightarrow Y)$ 
      •  $R_{i1} \leftarrow X \cup Y$ 
      •  $R_{i2} \leftarrow R_i - Y$ 
    Result  $\leftarrow \text{Result} - \{R_i\} \cup \{R_{i1}, R_{i2}\}$ 
  RETURN Result
END
```

When an Algorithm Calls for F^+

Example:

$$\begin{aligned} R &= (A, B, C, D, E) \\ F &= \{A \rightarrow B, C \rightarrow B, BC \rightarrow D\} \end{aligned}$$

$$F_c = ?$$

1. B extraneous in $BC \rightarrow D$? Yes: $(C \rightarrow D) \in F^+$
Proof: $C^+ = \{C, B, D\}$. Therefore, $D \in B^+$

$$F_c = \{A \rightarrow B, C \rightarrow BD\}$$

Boyce-Codd Normal Form (BCNF)

Example 1:

$$\begin{aligned} R &= (A, B, C, D) \\ F &= \{A \rightarrow B, AB \rightarrow D, B \rightarrow C\} \end{aligned}$$

Decompose R into BCNF

Compute F_c : $\{A \rightarrow BD, B \rightarrow C\}$

B extraneous in $AB \rightarrow D$? Yes: $(A \rightarrow D) \in F^+$

Proof: $A^+ = \{A, B, C, D\}$. Therefore, $D \in A^+$

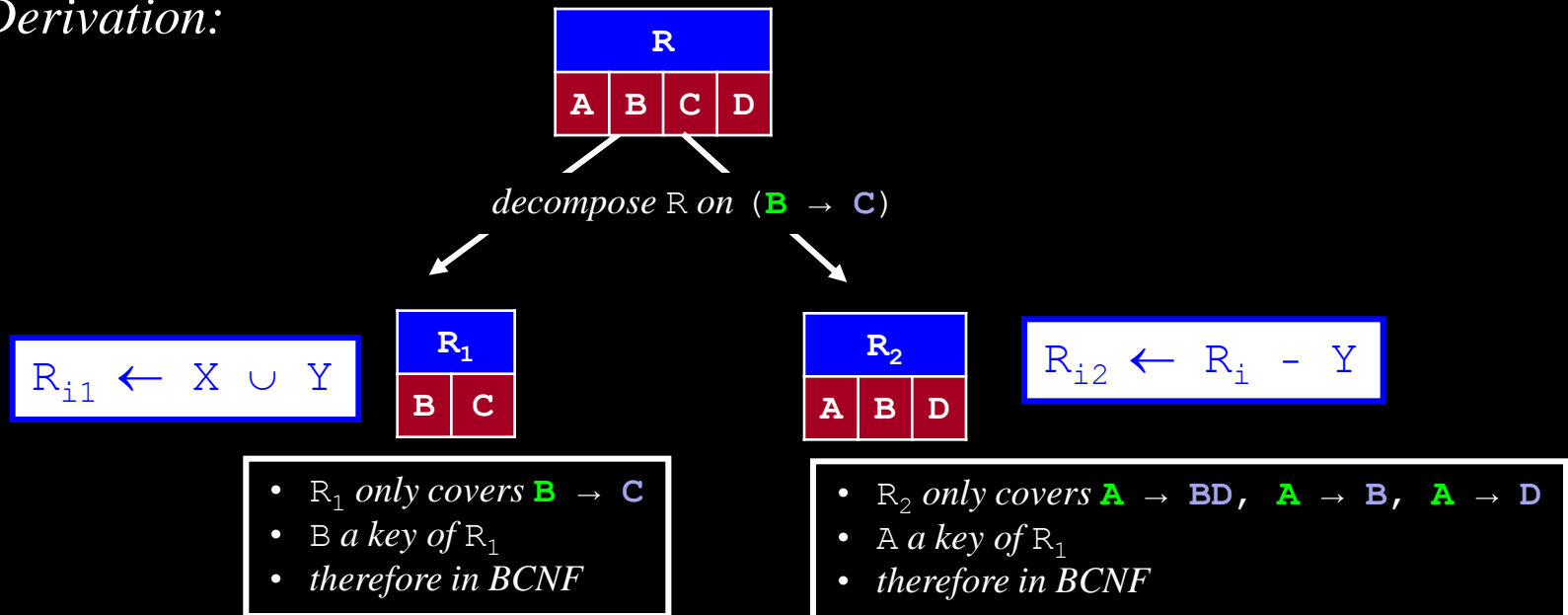
Boyce-Codd Normal Form (BCNF)

Example 1:

$$R = (A, B, C, D)$$
$$F_c = \{A \rightarrow BD, B \rightarrow C\}$$

Decompose R into BCNF

Derivation:



Boyce-Codd Normal Form (BCNF)

Example 1:

$$R = (A, B, C, D)$$
$$F_c = \{A \rightarrow BD, B \rightarrow C\}$$

Decompose R into BCNF

$$R = R_1 \cup R_2$$

R ₁	
B	C

R ₂		
A	B	D

covers $B \rightarrow C$

\cup

covers $A \rightarrow BD$

\Rightarrow *covers* $F_c \Rightarrow$ *covers* F^+

DP or not DP?

A: *DP*

Boyce-Codd Normal Form (BCNF)

Example 2:

$$\begin{aligned} R &= (A, B, C, D, E, H) \\ F_c &= \{ \textcolor{red}{A} \rightarrow \textcolor{blue}{BC}, \textcolor{red}{E} \rightarrow \textcolor{blue}{HA} \} \end{aligned}$$

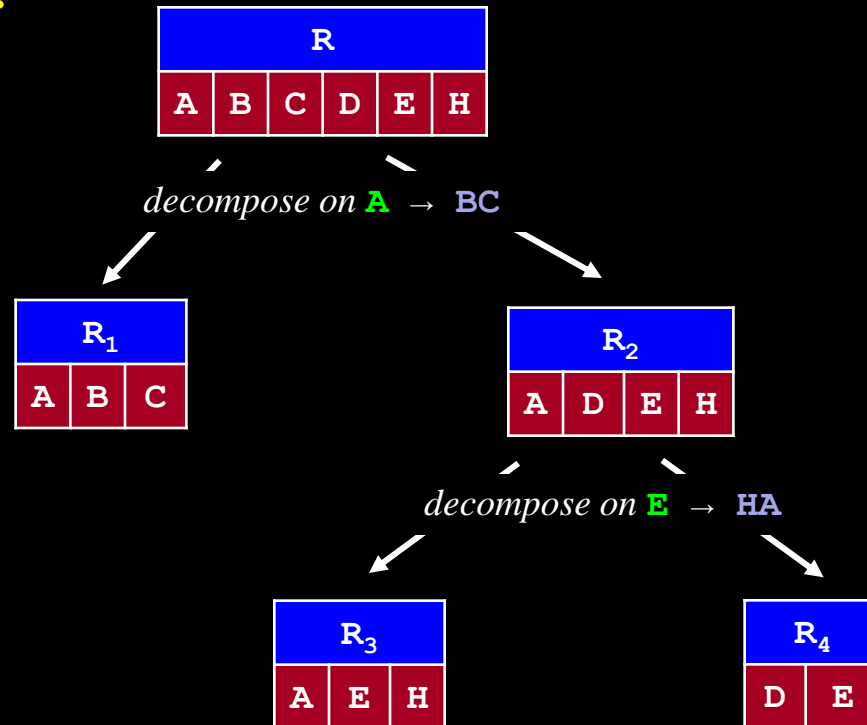
Produce 2 BCNF decompositions: one that is DP and one that isn't

Boyce-Codd Normal Form (BCNF)

Example 2:

$$R = (A, B, C, D, E, H)$$
$$F_c = \{A \rightarrow BC, E \rightarrow HA\}$$

Decomposition #1:



Boyce-Codd Normal Form (BCNF)

Example 2:

$$R = (A, B, C, D, E, H)$$
$$F_c = \{A \rightarrow BC, E \rightarrow HA\}$$

Decomposition #1:

$$R = R_1 \cup R_3 \cup R_4$$

R ₁		
A	B	C

covers $A \rightarrow BC$

\cup

R ₃		
A	E	H

covers $E \rightarrow HA$

\cup

R ₄	
D	E

covers -

$\Rightarrow \text{covers } F_c \Rightarrow \text{covers } F^+$

DP or not DP?

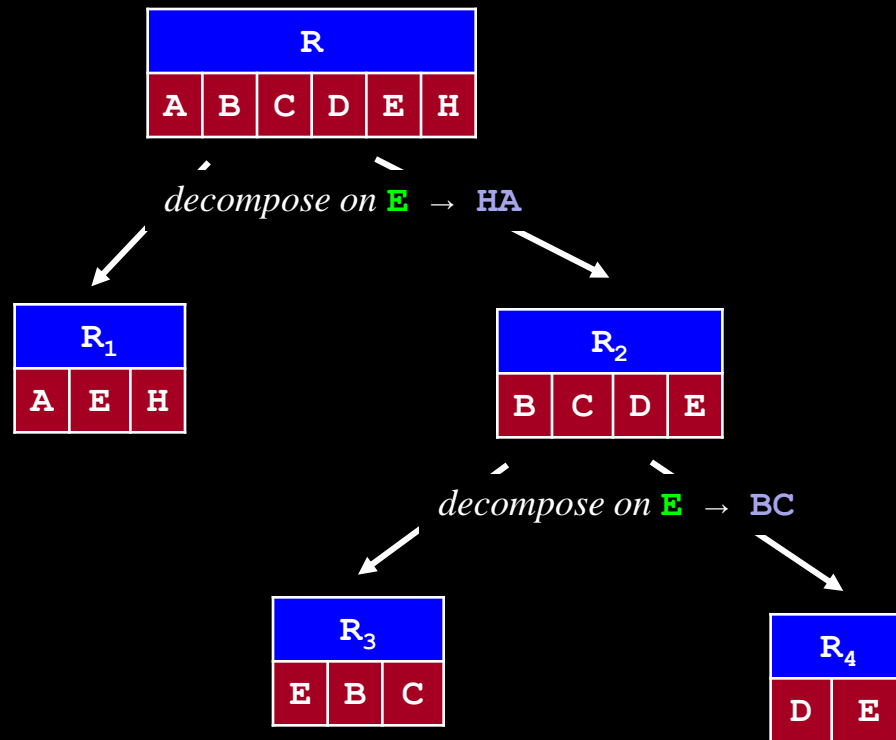
A: DP

Boyce-Codd Normal Form (BCNF)

Example 2:

$$R = (A, B, C, D, E, H)$$
$$F_c = \{ \textcolor{red}{A} \rightarrow \textcolor{blue}{BC}, \textcolor{red}{E} \rightarrow \textcolor{blue}{HA} \}$$

Decomposition #2:



Boyce-Codd Normal Form (BCNF)

Example 2:

$$R = (A, B, C, D, E, H)$$
$$F_c = \{ \textcolor{red}{A} \rightarrow \textcolor{blue}{BC}, \textcolor{red}{E} \rightarrow \textcolor{blue}{HA} \}$$

Decomposition #2:

$$R = R_1 \cup R_3 \cup R_4$$

R_1		
$\textcolor{red}{A}$	$\textcolor{red}{E}$	$\textcolor{blue}{H}$

covers $\textcolor{red}{E} \rightarrow \textcolor{blue}{HA}$

\cup

R_3		
$\textcolor{red}{E}$	$\textcolor{red}{B}$	$\textcolor{red}{C}$

covers $\textcolor{red}{E} \rightarrow \textcolor{blue}{BC}$

\cup

R_4	
$\textcolor{red}{D}$	$\textcolor{red}{E}$

covers -

\Rightarrow *does not cover* $\textcolor{red}{A} \rightarrow \textcolor{blue}{B}$

DP or not DP?

$\textcolor{red}{A}$: *Not DP*

Boyce-Codd Normal Form (BCNF)

Example 3:

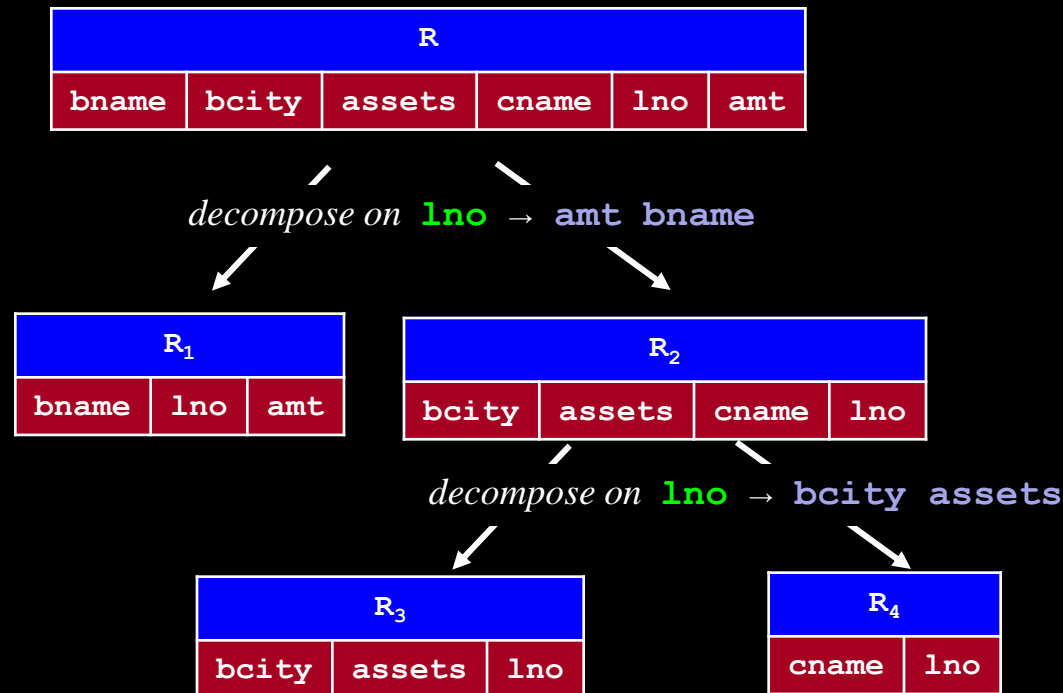
```
R = (bname, bcity, assets, cname, lno, amt)
Fc = { lno → amt bname,
       bname → bcity assets }
```

Decompose R into BCNF, ensuring DP if possible

Boyce-Codd Normal Form (BCNF)

Example 3:

$R = (\text{bname}, \text{bcity}, \text{assets}, \text{cname}, \text{lno}, \text{amt})$
 $F_c = \{ \text{lno} \rightarrow \text{amt bname}, \text{bname} \rightarrow \text{bcity assets} \}$



Boyce-Codd Normal Form (BCNF)

Example 3:

$R = (\text{bname}, \text{bcity}, \text{assets}, \text{cname}, \text{lno}, \text{amt})$
 $F_c = \{ \text{lno} \rightarrow \text{amt bname}, \text{bname} \rightarrow \text{bcity assets} \}$

Result:

$$R = R_1 \cup R_3 \cup R_4$$

R_1		
bname	lno	amt

R_3		
lno	bcity	assets

R_4	
cname	lno

covers $\text{lno} \rightarrow \text{amt bname}$

\cup

covers $\text{lno} \rightarrow \text{bcity assets}$

\cup

covers -

\Rightarrow *does not cover* $\text{bname} \rightarrow \text{bcity}$

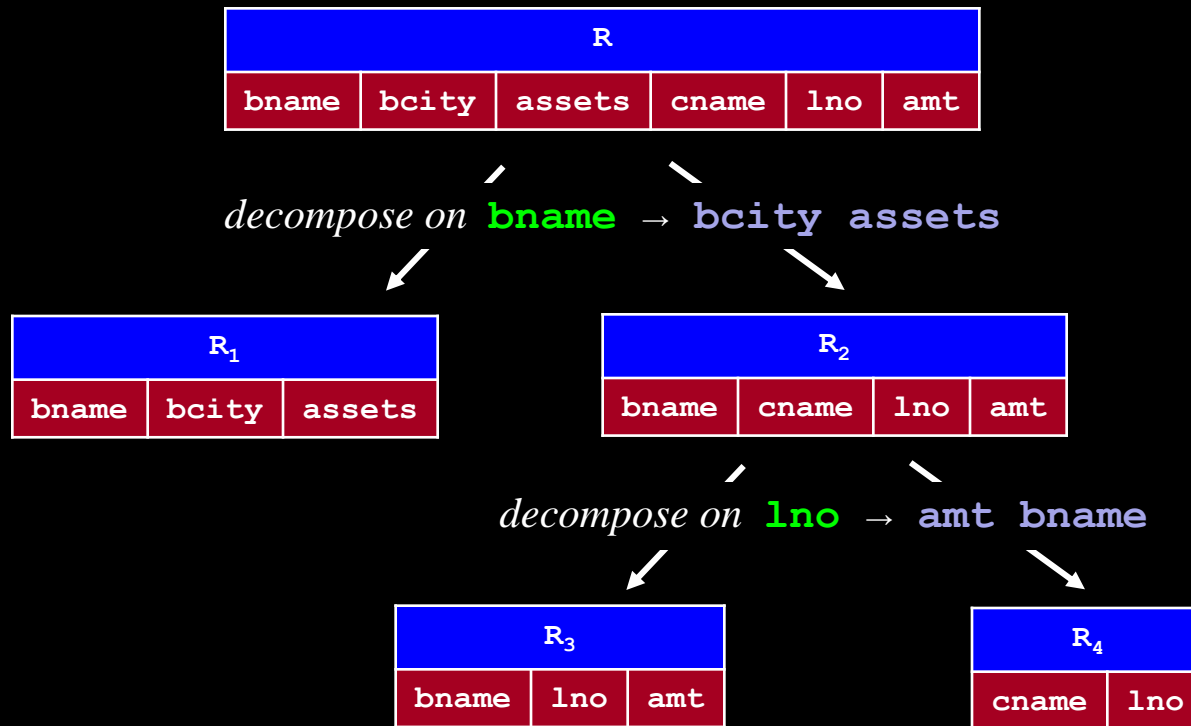
DP or not DP?

A: *Not DP*

Boyce-Codd Normal Form (BCNF)

Example 3:

$R = (\text{bname}, \text{bcity}, \text{assets}, \text{cname}, \text{lno}, \text{amt})$
 $F_c = \{ \text{lno} \rightarrow \text{amt bname}, \text{bname} \rightarrow \text{bcity assets} \}$



Boyce-Codd Normal Form (BCNF)

Example 3:

$R = (\text{bname}, \text{bcity}, \text{assets}, \text{cname}, \text{lno}, \text{amt})$
 $F_c = \{\text{lno} \rightarrow \text{amt bname},$
 $\quad \text{bname} \rightarrow \text{bcity assets}\}$

Result:

$$R = R_1 \cup R_3 \cup R_4$$

R ₁		
bname	bcity	assets

R ₃		
bname	lno	amt

R ₄	
cname	lno

covers $\text{bname} \rightarrow \text{bcity assets}$

\cup

covers $\text{lno} \rightarrow \text{amt bname}$

\cup

covers -

$\Rightarrow \text{covers } F_c \Rightarrow \text{covers } F^+$

DP or not DP?

A: *DP*

Boyce-Codd Normal Form (BCNF)

Ordering Decomposition Steps:

- Observe:

- 1) decompose on **lno** → amt bname
- 2) decompose on **bname** → bcity assets

but

- 1) decompose on **bname** → bcity assets
- 2) decompose on **lno** → amt bname

Not DP

DP

Why?

- 1) decompose on **lno** → amt bname
 $R_1 \leftarrow \{\text{lno}, \text{amt}, \text{bname}\}$
 $R_2 \leftarrow R - \{\text{amt}, \text{bname}\}$ (i.e., $\text{bname} \notin R_2$)
- 2) decompose on **bname** → bcity assets

cannot apply to R_1 or R_2 !!

Boyce-Codd Normal Form (BCNF)

Ordering Decomposition Steps:

When applying FD's to decomposition, for any FD,

$$\mathbf{x} \rightarrow \boxed{\mathbf{y}}$$

ensure that all FD's of the form,

$$\boxed{\mathbf{y}} \rightarrow \mathbf{z}$$

are applied before!

Boyce-Codd Normal Form (BCNF)

Example 4: $R = (\text{name}, \text{addr}, \text{fbeer}, \text{fmanf}, \text{lbeer}, \text{lmanf})$
 $F_c = \{ \text{name} \rightarrow \text{addr fbeer},$
 $\text{lbeer} \rightarrow \text{lmanf},$
 $\text{fbeer} \rightarrow \text{fmanf} \}$

Decompose R into BCNF, ensuring DP if possible

First...:



$R = (\text{name}, \text{addr}, \text{fbeer}, \text{fmanf}, \text{lbeer}, \text{lmanf})$
 $F_c = \{ \text{name} \rightarrow \text{addr fbeer},$
 $\text{lbeer} \rightarrow \text{lmanf},$
 $\text{fbeer} \rightarrow \text{fmanf} \}$

$R = (\text{name}, \text{addr}, \text{fbeer}, \text{fmanf}, \text{lbeer}, \text{lmanf})$
 $F_c = \{ \text{fbeer} \rightarrow \text{fmanf}$
 $\text{lbeer} \rightarrow \text{lmanf},$
 $\text{name} \rightarrow \text{addr fbeer} \}$

Boyce-Codd Normal Form (BCNF)

Example 4: $R = (\text{name}, \text{addr}, \text{fbeer}, \text{fmanf}, \text{lbeer}, \text{lmanf})$
 $F_c = \{ \text{fbeer} \rightarrow \text{fmanf}$
 $\text{lbeer} \rightarrow \text{lmanf},$
 $\text{name} \rightarrow \text{addr fbeer} \}$

R					
name	addr	fbeer	fmanf	lbeer	lmanf

decompose on $\text{fbeer} \rightarrow \text{fmanf}$

R ₁	
fbeer	fmanf

R ₂				
name	addr	fbeer	lbeer	lmanf

decompose on $\text{lbeer} \rightarrow \text{lmanf}$

R ₃	
lbeer	lmanf

R ₄			
name	addr	fbeer	lbeer

decompose on $\text{name} \rightarrow \text{addr fbeer}$

R ₅		
name	addr	fbeer

R ₆	
name	lbeer

Boyce-Codd Normal Form (BCNF)

Example 4: $R = (\text{name}, \text{addr}, \text{fbeer}, \text{fmanf}, \text{lbeer}, \text{lmanf})$
 $F_c = \{ \text{fbeer} \rightarrow \text{fmanf}, \text{lbeer} \rightarrow \text{lmanf}, \text{name} \rightarrow \text{addr fbeer} \}$

Result:

$$R = R_1 \cup R_3 \cup R_5 \cup R_6$$

R ₁	
fbeer	fmanf

R ₃	
lbeer	lmanf

R ₅		
name	addr	fbeer

R ₆	
name	lbeer

covers **fbeer** \rightarrow fmanf

\cup

covers **lbeer** \rightarrow lmanf

\cup

covers **name** \rightarrow addr fbeer

\cup

covers -

\Rightarrow covers $F_c \Rightarrow$ covers F^+

DP or not DP? **A:** DP

Normalization

BCNF

- can result in many decompositions (schemas) for same relation + FD Set
- all result schemas satisfy
 1. lossless joins
 2. redundancy avoidance
 3. dependency preservation (sometimes, but not always possible)

When is it impossible for BCNF to satisfy DP?

Normalization

BCNF

- can result in many decompositions (schemas) for same relation + FD Set
- all result schemas satisfy
 1. lossless joins
 2. redundancy avoidance
 3. dependency preservation (sometimes, but not always possible)

When is it impossible for BCNF to satisfy DP?

A: An example,

$$\begin{array}{l} R = (J, K, L) \\ F_c = \{ \mathbf{L} \rightarrow \mathbf{K}, \mathbf{JK} \rightarrow \mathbf{L} \} \end{array}$$

has no BCNF decomposition that is dependency preserving

Boyce-Codd Normal Form (BCNF)

Example 5:

$$\begin{aligned} R &= (J, K, L) \\ F_c &= \{ \mathbf{L} \rightarrow \mathbf{K}, \mathbf{JK} \rightarrow \mathbf{L} \} \end{aligned}$$

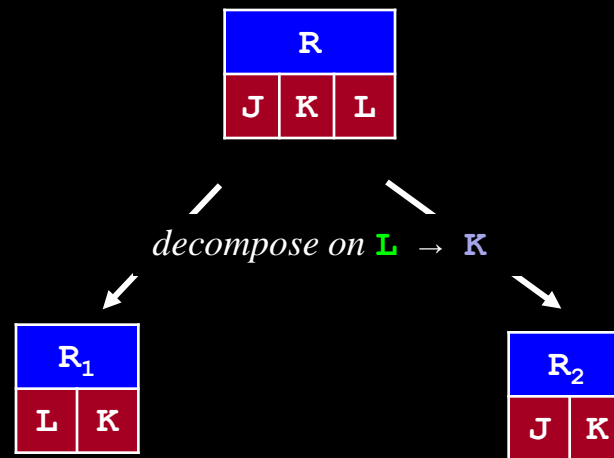
Decompose R into BCNF

Boyce-Codd Normal Form (BCNF)

Example 5:

$$\begin{aligned} R &= (J, K, L) \\ F_c &= \{ \mathbf{L} \rightarrow \mathbf{K}, \mathbf{JK} \rightarrow \mathbf{L} \} \end{aligned}$$

Decomposition #1



Boyce-Codd Normal Form (BCNF)

Example 5:

$$\begin{aligned} R &= (J, K, L) \\ F_c &= \{ \textcolor{red}{L} \rightarrow \textcolor{blue}{K}, \textcolor{red}{JK} \rightarrow \textcolor{blue}{L} \} \end{aligned}$$

Decomposition #1

$$R = R_1 \cup R_2$$

R_1	
$\textcolor{red}{L}$	$\textcolor{blue}{K}$

covers $\textcolor{red}{L} \rightarrow \textcolor{blue}{K}$

\cup

R_2	
$\textcolor{red}{J}$	$\textcolor{blue}{K}$

covers nothing

\Rightarrow *does not cover* $\textcolor{red}{JK} \rightarrow \textcolor{blue}{L}$

DP or not DP?

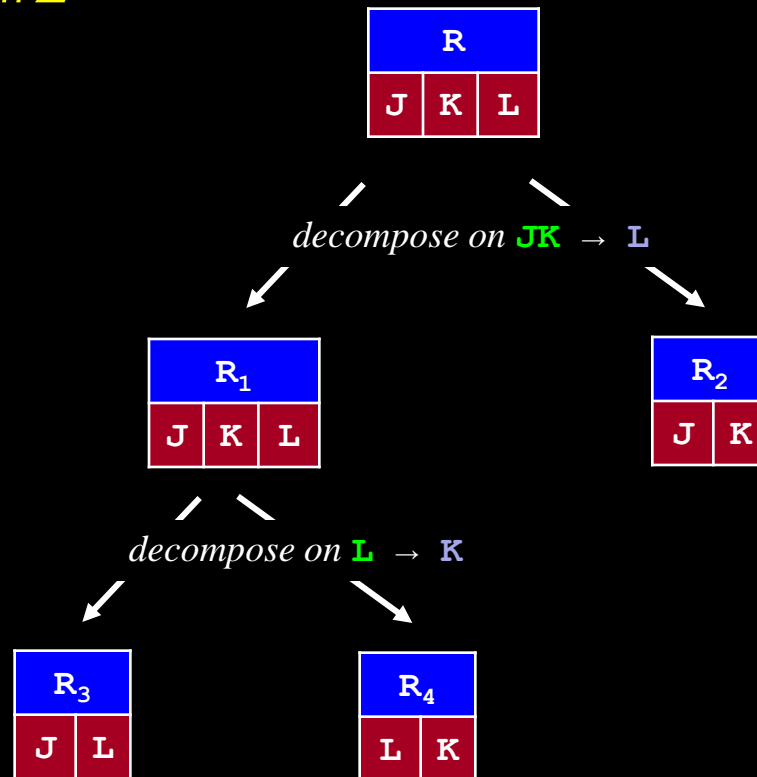
A: Not DP

Boyce-Codd Normal Form (BCNF)

Example 5:

$$\begin{aligned} R &= (J, K, L) \\ F_c &= \{ \mathbf{L} \rightarrow \mathbf{K}, \mathbf{JK} \rightarrow \mathbf{L} \} \end{aligned}$$

Decomposition #2



Boyce-Codd Normal Form (BCNF)

Example 5:

$$\begin{aligned} R &= (J, K, L) \\ F_c &= \{ \mathbf{L} \rightarrow \mathbf{K}, \mathbf{JK} \rightarrow \mathbf{L} \} \end{aligned}$$

Decomposition #2

$$R = R_2 \cup R_3 \cup R_4$$

R ₂	
J	K

R ₃	
J	L

R ₄	
L	K

covers -

\cup

covers -

\cup

covers $\mathbf{L} \rightarrow \mathbf{K}$

\Rightarrow *does not cover* $\mathbf{JK} \rightarrow \mathbf{L}$

DP or not DP?

A: *Not DP*

Boyce-Codd Normal Form (BCNF)

Ordering Decomposition Steps:

When applying FD's to decomposition, for any FD,

$$\mathbf{x} \rightarrow \boxed{\mathbf{y}}$$

ensure that all FD's of the form,

$$\boxed{\mathbf{y}} \rightarrow \mathbf{z}$$

are applied before!

Not Always Possible

$$\begin{aligned} R &= (J, K, L) \\ F_c &= \{ \mathbf{L} \rightarrow \mathbf{K}, \mathbf{JK} \rightarrow \mathbf{L} \} \end{aligned}$$


which goes first?

\Rightarrow *DP not possible with BCNF*

Boyce-Codd Normal Form (BCNF)

Is This a Realistic Example?

$$\begin{aligned} R &= (J, K, L) \\ F_c &= \{ \textcolor{red}{L} \rightarrow \textcolor{blue}{K}, \textcolor{red}{JK} \rightarrow \textcolor{blue}{L} \} \end{aligned}$$

A: Yes

$$\begin{aligned} R &= (\text{CustName}, \text{BranchName}, \text{BankerName}) \\ F_c &= \{ \textcolor{red}{BankerName} \rightarrow \textcolor{blue}{BranchName} \\ &\quad \textcolor{red}{CustName} \textcolor{red}{BranchName} \rightarrow \textcolor{blue}{BankerName} \} \end{aligned}$$

- *every banker works at one branch*
- *a customer works with the same banker at a given branch*

Normalization Summary

Theoretical Approach to DB Design based on FDs

- unlike ad hoc E/R approach, can know if designs are "good"
- good = satisfies some normal form

Approach

- decompose universal relation in steps
- decomposition goals:
 1. Lossless Joins (LJ): preserve semantics
 2. Redundancy Avoidance (RA): no update anomalies
 3. Dependency Preservation (DP): fewer GICs to enforce

Normal forms:

- BCNF: Guarantees LJ + RA
- 3NF: Guarantees LJ + DP (next class)