

## 6-th Exercise Sheet in „Computer Algebra“

Deadline: Thursday, 01 December 2011, 10.00 h

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**Exercise 1.** Let  $A \subset B$  be rings. Show that  $C := \{b \in B \mid b \text{ is integral over } A\}$ , is a subring of  $B$ .

HINT: Consider  $A[b_1, b_2]$  to show that  $b_1 - b_2, b_1 b_2 \in C$ .

**Exercise 2.** Let  $B = A[b_1, \dots, b_n]$  be a finite extension and  $A \subset K$  where  $K$  is an algebraically closed field. Prove that there exists an extension  $\lambda : B \rightarrow K$ .

**Exercise 3.** Let  $x_1(t), \dots, x_n(t) \in K[t]$  such that  $A = K[x_1(t), \dots, x_n(t)] \subset K[t]$  is finite and  $K(x_1(t), \dots, x_n(t)) = K(t)$ . Prove that  $K[t]$  is the normalization of  $A$ .

**Exercise 4.** Add the Product Criterion (see Exercise 3 on Sheet 2) to your SINGULAR procedure `standard` such that your algorithm takes an optional parameter with which you can switch this criterion on and off.