Sumário			14	exemplo de stringstream
1 To	halaa	2	15	exemplo de ordenação
1 Ta	Detas	2	16	pesquisa binária
2 Cc	ndigos	2	17	Arredondamento e output em outras bases
2 1	Exemplos	2	18	máximo divisor comum e mínimo multiplo comum
2.1	Teoria dos números		19	decide se um número é primo
2.3			20	Retorna a fatoração em números primos de abs(n)
$\frac{2.3}{2.4}$			21	Calcula Valor de $a^b mod$ n de forma rápida
	0 3		22	Calcula (a*b)%c de forma rápida
2.5			23	Computa $x$ tal que $a^*x = b \pmod{c}$ . Quando a equação não tem solução,
2.6				retorna algum valor arbitrário errado, mas basta conferir o resultado
2.7	Algebra Linear		24	<b>Baby-step Giant-step algorithm</b> Calcula o menor valor de e para $b^e = n$
2.8	8			mod p. Retorna -1 se eh impossivel
2.9	Outros	21	25	Números de precisão harbitrária
o D:	h!:	00	26	Sub Set Sum: Verifica se há um sobconjunto dos elementos do vetor cuja
	blioteca $C/C++$	23		soma seja igual a soma pedida
	I/O		27	Lis: longest increasing (decreasing) subsequence $O(n^2)$
3.2	Map	23	28	Lis: longest increasing subsequence O(n*logn)
			29	Problema da Mochila $O(n^*W)$
List	a de Tabelas		30	Verifica se o grafo é aciclico
List	a de Tabelas		31	Dijkstra Caminho minimo 1 para todos pesos positivos
1	Complexidade máxima da solução em fução do tamanho da entrada	2	32	Floresta dijunta de arvores
2	Limites de representação de dados		33	Kruskal Arvore geradora mínima kruskal
2	Fatorial		34	verifica se um grafo é bipartido
3 4	scanf() - %[*][width][modifiers]type		35	faz a ordenação topológica de um grafo acíclico
4			36	outro metodo para fazer a ordenação topológica de um grafo acíclico 1
3 c	$\operatorname{scanf}()\%[*][\operatorname{width}][\operatorname{modifiers}]$ type		37	calcula fluxo máximo, Ford-Fulkerson
0	stdlib		38	calcula fluxo máximo, algoritmo mais eficiente porém muito maior em
1	math (angulos em radianos)	3		tempo de codificação
			39	ponto e poligono
$\Delta \log a$	oritmos		40	Decide se q está sobre o segmento fechado pr
Aig	51101105		41	Decide se os segmentos fechados pq e rs têm pontos em comum
1	Modelo	2	42	Calcula a distância do ponto r ao segmento pq
2	comparcao de ponto flutuante		43	Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 depen-
3	.vimrc para a configuração do vim		10	dendo se p está no exterior, na fronteira ou no interior de T, respectivamente. 1
<i>J</i>	função que acelara o cin. Não deve ser usada com printf		44	Convex Hull <b>graham scan</b>
5	printf		45	Simplex
6	exemplo de map		46	String matching - Algoritmo $\mathbf{KMP}$ - O( n + m)
7			47	josephus problem
0	exemplo de set e multset		48	Gera as permutações dos elementos da string
8	exemplo de list		49	Exemplo de geração de permutações dos elementos da string, usando back-
9	exemplo de queue		-10	tracking
10	exemplo de priority queue		50	Ignora os dois floats do meio. Retornará 2 no sucesso
11	exemplo de stack		50 51	Referencias map
12	exemplo de etring	6	91	Referencias map
13	ovemble de string	6		

Complexidade	Tamanho máximo da entrada
1	$\alpha$
log(n)	$10^{9}$
n	$10^{6}$
n * log(n)	$10^{4}$
$n^2$	$10^{3}$
$n^{2*} log(n)$	$10^{3}$
$n^3$	$10^{2}$
$2^n$	20
n!	10

Tabela 1: Complexidade máxima da solução em fução do tamanho da entrada

## 1 Tabelas

tipo	bits	minmax	precisao
char	8	0127	2
signed char	8	-128127	2
unsigned char	8	0255	2
short	16	-32.768 32.767	4
unsigned short	16	$0 \dots 65.535$	4
int	32	-2x10**9 2 x 10**9	9
unsigned int	32	0 4x10**9	9
$int64_{-}t$	64	-9 x 10**18 9 x 10**18	18
$uint64_t$	64	0 18 x 10**18	19

Tabela 2: Limites de representação de dados

```
0! = 1
1! = 1
2! = 2
3! = 6
4! = 24
5! = 120
6! = 720
7! = 5.040
8! = 40.320
9! = 362.880
10! = 3.628.800
11! = 39.916.800
12! = 479.001.600 [limite do (unsigned) int]
13! = 6.227.020.800
14! = 87.178.291.200
15! = 1.307.674.368.000
16! = 20.922.789.888.000
17! = 355.687.428.096.000
18! = 6.402.373.705.728.000
19! = 121.645.100.408.832.000
20! = 2.432.902.008.176.640.000 [limite do (u)int64_t]
```

Tabela 3: Fatorial

# 2 Codigos

## 2.1 Exemplos

Código 1: Modelo

```
1 #include <stdio.h>
2 #include <stdlib.h>
з #include <string.h>
4 #include <math.h>
6 #include <inttypes.h>
7 #include <ctype.h>
8 #include <limits.h>
10 #include <algorithm>
11 #include <utility>
12 #include <iostream>
13
14 #include <map>
15 #include <set>
16 #include <vector>
17 #include <list >
18 #include <queue>
19 #include <sstream>
```

```
\begin{array}{lll} \mbox{Tipo} & \% \\ \mbox{char} & c \\ \mbox{int} & d \\ \mbox{float} & e, \, E, \, f, \, g, \, G \\ \mbox{int (octal)} & o \\ \mbox{int (hexa)} & x, \, X \\ \mbox{uint} & u \\ \mbox{char*} & s \end{array}
```

Tabela 4: scanf() - %[\*][width][modifiers]type

```
\begin{array}{ll} modifiers & tipo \\ h & short int \ (d, \, i, \, n), \, or \, unsigned \, short \, int \, (o, \, u, \, x) \\ l & long \, int \, (d, \, i, \, n), \, or \, unsigned \, long \, int \, (o, \, u, \, x), \, or \, double \, (e, \, f, \, g) \\ ll & long \, long \, int \, (d, \, i, \, n), \, or \, unsigned \, long \, long \, int \, (o, \, u, \, x) \\ L & long \, double \, (e, \, f, \, g) \end{array}
```

Tabela 5: scanf() %[\*][width][modifiers]type

função	descrição
atof	Convert string to double
atoi	Convert string to integer
atol	Convert string to long integer
strtod	Convert string to double
strtol	Convert string to long integer
strtoul	Convert string to unsigned long integer

Tabela 6: stdlib

função	descrição
cos	Compute cosine
$\sin$	Compute sine
an	Compute tangent
acos	Compute arc cosine
asin	Compute arc sine
atan	Compute arc tangent
atan2	Compute arc tangent with two parameters
$\cosh$	Compute hyperbolic cosine
$\sinh$	Compute hyperbolic sine
anh	Compute hyperbolic tangent
$\exp$	Compute exponential function
frexp	Get significand and exponent
ldexp	Generate number from significand and exponent
$\log$	Compute natural logarithm
$\log 10$	Compute common logarithm
$\operatorname{modf}$	Break into fractional and integral parts
pow	Raise to power
$\operatorname{sqrt}$	Compute square root
ceil	Round up value
fabs	Compute absolute value
floor	Round down value
$\operatorname{fmod}$	Compute remainder of division

Tabela 7: math (angulos em radianos)

```
20
21 using namespace std;
23 #define abs(a) ((a) > 0 ? (a) : -(a))
25 int main()
26
      int n;
27
28
      cin >> n;
29
30
      for (int i = 0; i < n; i++)
31
32
33
34
35
      while (cin >> n)
36
37
38
39
      return 0;
40
41 }
```

### Código 2: comparcao de ponto flutuante

```
1 /**
2 * -1 se x < y
3 * 0 se x = y
4 * 1 se x > y
5 */
6 const double EPS = 1e-10;
7 #define _inline(f...) f() __attribute__((always_inline)); f
8 _inline(int cmp)(double x, double y = 0, double tol = EPS)
9 {
10     return (x <= y + tol) ? (x + tol < y) ? -1 : 0 : 1;
11 }</pre>
```

## Código 3: .vimrc para a configuração do vim

```
1 set ai noet ts=4 sw=4 bs=2
2 set cindent
```

## Código 4: função que acelara o cin. Não deve ser usada com printf

```
std::cout.sync_with_stdio(false);
```

## Código 5: printf

```
1 /* printf example */
2 #include <stdio.h>
3
4 int main()
5 {
```

```
printf ("Characters: %c %c \n", 'a', 65);
     printf ("Decimals: %d %ld\n", 1977, 650000L);
     printf ("Preceding with blanks: %10d \n", 1977);
     printf ("Preceding with zeros: %010d \n", 1977);
     printf ("Some different radixes: %d %x %o %#x %#o \n", 100, 100, 100,
          100, 100);
     printf ("floats: %4.2f %+.0e %E %4.2f\n", 3.1416, 3.1416, 3.1416,
         3.1);
     printf ("Width trick: %*d \n", 5, 10);
12
     printf ("%s \n", "A string");
13
     return 0:
14
  /* \%[flags (-, +, etc)]/width]/.precision][length (h, l, L)]specifier
17 Characters: a A
18 Decimals: 1977 650000
19 Preceding with blanks:
                                1977
20 Preceding with zeros: 0000001977
21 Some different radixes: 100 64 144 0x64 0144
22 floats: 3.14 +3e+000 3.141600E+000 3.10
23 Width trick: 10
24 A string
25 */
```

#### Código 6: exemplo de map

```
1 #include <iostream>
2 #include <map>
3 using namespace std;
5 int main ()
6 {
    map<char.int> mymap:
    map<char, int >:: iterator it;
     pair < map < char , int > :: iterator , bool > ret ;
1.0
    // first insert function version (single parameter):
11
    mymap.insert (pair < char, int > ('a', 100));
12
    mymap.insert ( pair < char, int > ('z', 200));
14
     ret=mymap.insert (pair < char, int > ('z', 500));
15
     if (ret.second=false)
16
17
       cout << "element 'z' already existed";</pre>
       cout << " with a value of " << ret.first->second << endl;
19
20
21
     // third insert function version (range insertion):
22
    map<char, int> anothermap;
     anothermap.insert(mymap.begin().mymap.find('c')):
24
25
     // showing contents:
     cout << "mymap contains:\n";</pre>
27
     for ( it=mymap.begin(); it != mymap.end(); it++)
28
      cout << (*it).first << " => " << (*it).second << endl;
29
    map < char, string > mymap;
```

```
32
    mymap['a']="an element";
    if (mymap.count('a') > 0)
33
         cout << mymap['a'] << " is an element of mymap.\n";</pre>
34
35
    while (!mymap.empty())
36
37
       cout << mymap.begin()->first << " => ";
38
       cout << mymap.begin()->second << endl;
39
       map<char, int>::iterator erasedelement = mymap.erase(mymap.begin())
40
41
42
    return 0;
43
44 }
```

### Código 7: exemplo de set e multset

```
1 #include <iostream>
2 #include <set>
3 using namespace std;
4
5 int main ()
    multiset < int > mvmultiset:
     multiset <int>::iterator it;
     // set some initial values:
    for (int i=1; i <=5; i++) mymultiset.insert(i*10); // 10 20 30 40 50
11
12
    cout << "size: " << (int) mymultiset.size() << endl;</pre>
13
    cout << "count: " << (int) mymultiset.count(10) << endl;</pre>
14
15
     it=mvmultiset.find(20):
16
     mymultiset.erase (it);
17
18
     if (! mymultiset.empty)
19
     mymultiset.erase (mymultiset.find(40));
20
21
     for (it=mymultiset.begin(); it!=mymultiset.end(); it++)
22
      cout << " " << *it;
23
24
     int myints [] = {19,72,4,36,20,20};
25
     multiset <int> first (myints, myints+3);
                                                    // 4,19,72
26
     multiset \langle int \rangle second (myints +3, myints +6); // 20.20.36
27
28
     first.swap(second); // troca conteudo. o primeiro fica [20.20.36] e o
29
         segundo [4,19,72]
30
    return 0;
31
32 }
```

## Código 8: exemplo de list

```
1 #include <iostream>
2 #include <list>
```

```
3 using namespace std;
5 int main ()
     list \langle int \rangle mylist (2,100);
                                           // two ints with a value of 100
     mylist.push_front (200);
     mylist.push_back (300);
    it = mylist.begin():
11
     mylist.insert (it,10);
12
     mylist.insert (it,2,20); // two ints with a value of 20
13
14
     mylist.reverse(); // Reverses the order of the elements in the list.
15
16
     cout << "mvlist contains:":</pre>
17
     for (list <int>::iterator it=mylist.begin(); it!=mylist.end(); ++it)
18
       cout << " " << *it;
19
20
     cout << "Popping out the elements in mylist:";</pre>
21
22
     while (!mylist.empty())
23
       cout << " " << mylist.front();</pre>
24
       mylist.pop_front();
25
26
27
     while (!mylist.empty())
28
29
       cout << " " << mylist.back();
30
       mylist.pop_back();
31
32
33
     cout << mylist.size() << endl;</pre>
34
35
    return 0;
36
37 }
```

#### Código 9: exemplo de queue

```
1 #include <iostream>
2 #include <queue>
3 using namespace std;
5 int main ()
6 {
    queue < int > myqueue;
    int sum (0);
    for (int i=1; i \le 10; i++) myqueue.push(i);
10
11
    myqueue.back() -= myqueue.front();
12
13
    cout << "size: " << (int) myqueue.size() << endl;
14
15
16
    while (!myqueue.empty())
17
        sum += myqueue.front();
```

5

```
19          myqueue.pop();
20     }
21
22     cout << "total: " << sum << endl;
23
24     return 0;
25 }</pre>
```

### Código 10: exemplo de priority queue

```
1 #include <iostream>
2 #include <queue>
3 using namespace std;
5 int main ()
6 {
     priority_queue < int > mypq;
    mypq.push(30);
    mypq. push (100);
10
    mypq.push(25);
11
    mypq.push(40);
12
     cout << "size: " << (int) mypq.size() << endl;</pre>
14
15
     cout << "Popping out elements...";</pre>
16
     while (!mypq.empty())
17
18
        cout << " " << mypq.top();
19
20
        mypq.pop();
^{21}
     cout << endl;
22
23
    return 0;
24
25
```

## Código 11: exemplo de stack

```
1 #include <iostream>
2 #include <stack>
3 using namespace std;
4
5 int main ()
6 {
    stack<int> mystack;
    int sum = 0;
    mystack.push(10);
10
    mystack.push(20);
11
12
    mystack.top() -= 5;
13
14
    while (!mystack.empty())
15
16
       sum += mystack.top();
17
```

### Código 12: exemplo de vector

```
1 #include <iostream>
2 #include <vector>
3 using namespace std;
5 int main ()
6 {
     vector <int> myvector (3,100); // (100 100 100)
     vector < int > :: iterator it;
     myvector.reserve(100);
10
11
     for (int i=0; i < myvector.size(); i++)
12
       myvector.at(i)=i; // = myvector[i] = i
13
14
     it = myvector.begin();
15
     it = myvector.insert ( it , 200 );
16
     myvector.insert (it,2,300);
18
     vector <int> anothervector (2,400);
19
     int myarray [] = \{ 501,502,503 \};
20
     vector < int > initializer (myarray /* Pointer Inicio*/, myarray + sizeof (
21
         myarray)/sizeof(int)/*PointerFim*/);
     myvector.insert (it +2, anothervector.begin(), anothervector.end());
22
     myvector.insert (myvector.begin(), myarray, myarray+3);
23
24
     cout << "myvector contains:";</pre>
25
     for (it=myvector.begin(); it < myvector.end(); it++)</pre>
26
       cout << " " << *it;
27
     cout << endl;
28
     // erase the 6th element
30
31
     myvector.erase (myvector.begin()+5);
32
     while (!myvector.empty())
33
34
        sum += myvector.back();
35
        myvector.pop_back();
36
37
38
    return 0:
39
40 }
```

Código 13: exemplo de string

```
2 #include <string>
3 using namespace std;
5 int main ()
6 {
    string str ("There are two needles in this haystack with needles.");
    string str2 ("needle"):
    size_t found;
10
    // different member versions of find in the same order as above:
11
    found=str.find(str2);
12
    if (found!=string::npos)
      cout << "first 'needle' found at: " << int(found) << endl;</pre>
14
15
    found=str.find("needles are small".found+1.6):
16
     if (found!=string::npos)
17
       cout << "second 'needle' found at: " << int(found) << endl;</pre>
18
19
     found=str.find("haystack");
20
     if (found!=string::npos)
21
       cout << "'haystack' also found at: " << int(found) << endl;</pre>
^{22}
23
    found=str.find(','):
24
     if (found!=string::npos)
25
      cout << "Period found at: " << int(found) << endl;</pre>
26
27
    // let's replace the first needle:
28
     str.replace(str.find(str2),str2.length(),"preposition");
29
    cout << str << endl;
30
31
     string str="We think in generalities, but we live in details.";
32
                                 // quoting Alfred N. Whitehead
33
     string str2, str3;
     size_t pos;
35
36
    str2 = str.substr (12,12); // "generalities"
37
38
                              // position of "live" in str
    pos = str.find("live");
39
    str3 = str.substr (pos); // get from "live" to the end
40
41
    cout \ll str2 \ll ' ' \ll str3 \ll endl;
42
43
44
    return 0:
45
46 }
48 first 'needle' found at: 14
49 second 'needle' found at: 44
  'haustack' also found at: 30
51 Period found at: 51
52 There are two prepositions in this haystack with needles.
53 generalities live in details.
54 */
```

Código 14: exemplo de stringstream

```
1 #include <string>
2 #include <sstream>
3 #include <iostream>
6 using namespace std;
9 int main() {
      string linha="Olah mundo";
     stringstream separador(linha); // Tokenizador
11
      string word:
     separador >> word: // word=Olah
13
     char mu[4]:
14
     separador.readsome(mu, 3); // Le " mu" (inclui espaco)
15
     cout << separador.tellg() << endl; // 7 (posicao de leitura)</pre>
16
      cout << separador.tellp() << endl; // 0, posicao de escrita
17
18
      separador.seekp(separador.str().size());
19
     separador << " cruel"; // separador = "Olah mundo cruel"
20
21
22
      separador.seekp(5):
      separador << "doido"; // separador = "Olah doido cruel" (sobrescrito)
23
     return 0;
24
```

#### Código 15: exemplo de ordenação

```
1 #include <iostream>
2 #include <algorithm>
з #include <vector>
4 using namespace std:
6 bool myfunction (int i, int j) { return (i<j); }
s struct myclass {
    bool operator() (int i, int j) { return (i<j);}
    mvobject:
11
12 int compare (const void * a, const void * b)
13 {
    return (*(int*)a - *(int*)b);
14
15 }
16
17
18 int main () {
    int myints [] = \{32,71,12,45,26,80,53,33\};
                                                              // 32 71 12 45
    vector <int> myvector (myints, myints+8);
        26 80 53 33
21
    // using default comparison (operator <):
    sort (myvector.begin(), myvector.begin()+4);
                                                             //(12 32 45 71)
        26 80 53 33
    // using function as comp
    sort (myvector.begin()+4, myvector.end(), myfunction); // 12 32 45
         71(26 33 53 80)
```

```
// using object as comp
    sort (myvector.begin(), myvector.end(), myobject);
                                                            //(12 26 32 33
        45 53 71 80)
28
    // if stable is need
29
    stable_sort (myvector.begin(), myvector.end(), myfunction);
30
31
    // Rearranges the elements in the range [first, last], in such a way
        that the subrange [first, middle]
    // contains the smallest elements of the entire range sorted in
        ascending order, and the subrange
    // [middle,end) contains the remaining elements without any specific
        order.
    partial_sort (myvector.begin(), myvector.begin()+3, myvector.end());
35
    qsort (myints, 8, sizeof(int), compare);
37
38
    return 0;
39
40 }
```

### Código 16: pesquisa binária

```
int compareMyType (const void * a, const void * b)

{
    if ( *(MyType*)a > *(MyType*)b ) return 1;
    if ( *(MyType*)a == *(MyType*)b ) return 0;
    if ( *(MyType*)a < *(MyType*)b ) return -1;
}

int key = 40;
int key = 40;
item = (int*) bsearch (&key, values, n, sizeof (int), compareMyType);</pre>
```

## Código 17: Arredondamento e output em outras bases

```
1 #include <iostream>
2 #include <iomanip> // setprecision()
3 using namespace std;
5 int main () {
    double a = 3.1415926534:
    double b = 2006.0;
    double c = 1.0e - 10;
    // setprecision(1) \Rightarrow 1 casa decimal apos a virgula
10
    cout \ll fixed \ll setprecision(1) \ll 9.09090901 \ll endl;
11
    cout \ll fixed \ll setprecision(2) \ll 9.09090901 \ll endl;
12
    cout << fixed << setprecision(3) << 9.09090901 << endl;
13
    cout << fixed << setprecision(2) << 9.1 << endl:
14
15
     // anula o efeito de setprecision
16
    cout.unsetf(ios::floatfield);
17
18
    // 5 digitos no maximo
19
    cout.precision(5);
20
21
```

```
cout << a << '\t' << b << '\t' << c << endl;
     cout \ll fixed \ll a \ll '\t' \ll b \ll '\t' \ll c \ll endl;
    cout \ll scientific \ll a \ll '\t' \ll b \ll '\t' \ll c \ll endl;
25
    // Sets the basefield format flag for the str stream to dec, hex or
26
         oct.
    int n = 70:
     cout << dec << n << endl;
    cout \ll hex \ll n \ll endl:
     cout << oct << n << endl;
30
31
32
    return 0;
33 }
34 /* output
35 9.1
36 9.09
37 9.091
38 9.10
39 3.1416 2006
                    1e - 10
40 3.14159 2006.00000
                             0.00000
41 3.14159e+00
                    2.00600e+03
                                      1.000000e-10
42 70
43 46
44 106
45 */
```

#### 2.2 Teoria dos números

Código 18: máximo divisor comum e mínimo multiplo comum

```
int gcd(int x, int y)
2 {
3    return y ? gcd(y, x % y) : abs(x);
4 }
5  uint64_t lcm(int x, int y)
6 {
7    if (x && y) return abs(x) / gcd(x, y) * uint64_t(abs(y));
8    else return uint64_t(abs(x | y));
9 }
```

Código 19: decide se um número é primo

```
1 bool isPrime(int n)
2 {
3     if (n < 0) return isPrime(-n);
4     if (n = 1) return true;
5     if (n < 5 || n % 2 = 0 || n % 3 = 0) return (n == 2 || n == 3);
6
7     int maxP = sqrt(n) + 2;
8     for (int p = 5; p < maxP; p += 6)
9     {
10         if (n % p == 0 || n % (p+2) == 0) return false;
11     }</pre>
```

```
12     return true;
13 }
```

### Código 20: Retorna a fatoração em números primos de abs(n).

```
1 typedef map<int, int> prime_map;
2 void squeeze (prime_map& M, int& n, int p)
3 {
      for (; n % p == 0; n /= p) M[p]++;
6 void factor (int n, prime_map& M)
      if (n < 0) { factor(-n, M); return; }
     if (n < 2) return;
10
     squeeze(M, n, 2);
11
     squeeze (M, n, 3);
12
13
     int \max P = sqrt(n) + 2;
14
     for (int p = 5; p < maxP; p += 6)
15
16
         squeeze (M, n, p);
17
         squeeze(M, n, p+2);
18
19
20
     if (n > 1) M[n]++;
21
```

## Código 21: Calcula Valor de $a^b mod$ n de forma rápida.

```
int mpow(int a, int b, int n = 10)

if (b = 0)

return 1;

else {

long long res = mpow(a, b/2, n);

res = (res*res) % n;

if (b%2 = 1)

res = (res*a) % n;

return (int) res;

}
```

## Código 22: Calcula (a\*b)%c de forma rápida.

```
1 long long mulmod(long long a, long long b, long long c)
2 {
3     long long x = 0;
4     long long y = a % c;
5     while(b > 0)
6     {
7         if(b & 111) x = (x + y) % c;
8         y = (y << 1) % c;
9         b >>= 1;
10     }
```

```
return x % c;
```

Código 23: Computa x tal que a\*x = b (mod c). Quando a equação não tem solução, retorna algum valor arbitrário errado, mas basta conferir o resultado.

```
long long axbmodc(long long a, long long b, long long c)
[2 {
    return a ? (axbmodc(c % a, (a - b % a) % a, a) * c + b) / a : 0;
    4 }
```

Código 24: Baby-step Giant-step algorithm Calcula o menor valor de e para  $b^e = n$  mod p. Retorna -1 se eh impossivel

```
1 #define inv_mult(a, n) axbmodc(a, 1, n)
3 long long discreteLlogarithm ( long long b, long long n, long long p )
      if (n == 1) return 0:
     map < long long, int > table;
     long long m = \operatorname{sqrt}(p) + 1, pot = 1, pot2 = 1;
10
     for (int j = 0; j < m; j++)
11
12
        if (pot = n) return j;
        table [(n * inv_mult(pot, p)) \% p] = j;
13
        pot = (pot * b) \% p;
14
15
16
     for (int i = 0; i < m; i++)
17
18
        if (table.find(pot2)!= table.end()) return i * m + table[pot2]
19
        pot2 = (pot * pot2) \% p;
20
21
22
     return -1;
23
24 }
```

## 2.3 Estruturas de dados

Código 25: Números de precisão harbitrária.

```
1 const int DIG = 4;
2 const int BASE = 10000; // BASE**3 < 2**51
3 const int TAM = 1000;
4
5 struct BigInt
6 {
7    int num[TAM], numDigits;
8    BigInt(int x = 0): numDigits(1)</pre>
```

```
9
                                                                                    64
         memset(num, 0, sizeof(num));
                                                                                             int i = max(numDigits, x.numDigits), t = 0;
                                                                                    65
10
        num[numDigits++] = x; fixInvariant();
                                                                                             while (1)
11
                                                                                    66
12
                                                                                    67
      BigInt(char *s): numDigits(1)
                                                                                                 if ((t = :: cmp(num[i], x.num[i])) \mid i = 0) return t;
13
                                                                                    68
                                                                                    69
14
         memset(num, 0, sizeof(num));
15
                                                                                    70
         int sign = 1;
16
                                                                                    71
                                                                                          bool operator <(const BigInt& x) const { return cmp(x) < 0: }
17
                                                                                    72
         while (*s && !isdigit(*s))
                                                                                          bool operator >(const BigInt& x) const { return cmp(x) > 0; }
18
                                                                                    73
                                                                                          bool operator \leq (const BigInt\&x) const \{ return cmp(x) \leq 0 \}
19
                                                                                    74
            if (*s++= '-') sign *= -1;
                                                                                          bool operator >=(const BigInt& x) const {
                                                                                                                                       return cmp(x) >= 0;
20
                                                                                          bool operator ==(const BigInt& x) const {
                                                                                                                                       return cmp(x) == 0;
^{21}
                                                                                    76
                                                                                          bool operator !=(const BigInt& x) const { return cmp(x) != 0;
22
                                                                                    77
         char *t = strdup(s), *p = t + strlen(t):
23
                                                                                    78
                                                                                          //operacoes fundamentais
^{24}
                                                                                    79
         while (p > t)
                                                                                          BigInt& operator +=(const BigInt& x)
                                                                                    80
25
                                                                                    81
26
            *p = 0; p = max(t, p - DIG);
                                                                                             for (int i = 1; i \le x.numDigits; i++) num[i] += x.num[i];
27
                                                                                    82
            sscanf(p, "%d", &num[numDigits]);
                                                                                             return fixInvariant (x.numDigits);
28
                                                                                    83
            num[numDigits++] *= sign;
29
                                                                                    84
                                                                                    85
                                                                                          BigInt& operator -=(const BigInt& x)
30
31
                                                                                    86
         free(t);
                                                                                             for (int i = 1; i \le x.numDigits; i++) num[i] -= x.num[i];
32
                                                                                    87
         fixInvariant();
                                                                                             return fixInvariant (x.numDigits);
33
                                                                                    88
34
                                                                                    89
35
                                                                                    90
      BigInt& fixInvariant (int m = 0)
                                                                                          void multiAndAcumWithShift(const BigInt& x, int m, int b)
36
                                                                                    91
                                                                                          \{ // *this += (x * m) << b : 
37
                                                                                    92
         numDigits = max(m, numDigits);
                                                                                             for (int i = 1, carry = 0; (i <= x.numDigits || carry) && (
38
                                                                                    93
         int sign = 0:
                                                                                                 numDigits = i + b): i++)
39
40
                                                                                    94
         for (int i = 1, carry = 0; i <= numDigits || carry && (numDigits =
                                                                                                num[i+b] += x.num[i] * m + carry;
41
              i); i++)
                                                                                                 carry = num[i+b] / BASE;
                                                                                    96
                                                                                                num[i+b] \% = BASE;
42
                                                                                    97
            num[i] += carry;
43
                                                                                    98
            carry = num[i] / BASE;
44
                                                                                    99
            num[i] %= BASE;
45
                                                                                   100
            if (num[i]) sign = (num[i] > 0) ? 1 : -1;
                                                                                          BigInt operator *(const BigInt& x) const
46
                                                                                   101
47
                                                                                   102
48
                                                                                   103
                                                                                             BigInt r;
         for (int i = 1; i < numDigits; i++)
                                                                                             for (int i = 1; i <= numDigits; i++) r.multiAndAcumWithShift(x,
49
                                                                                   104
                                                                                                 num [i], i-1);
50
            if (num[i] * sign < 0)
                                                                                             return r:
51
                                                                                   105
52
                                                                                   106
               num[i] += sign * BASE;
53
                                                                                   107
               num[i+1] = sign;
                                                                                          BigInt div(const BigInt& x)
54
                                                                                   108
55
                                                                                   109
                                                                                             if (x = 0) return 0;
                                                                                   110
56
57
                                                                                   111
         while (numDigits && !num[numDigits]) numDigits --;
                                                                                             BigInt q;
58
                                                                                   112
                                                                                             q.numDigits = max(numDigits - x.numDigits + 1, 0);
         return *this;
59
                                                                                   113
                                                                                             int d = x.num[x.numDigits] * BASE + x.num[x.numDigits - 1];
                                                                                   114
60
61
                                                                                   115
      //Comparacao
                                                                                             for (int i = q.numDigits; i > 0; i--)
62
                                                                                   116
     int cmp(const BigInt\& x = 0) const
                                                                                   117
```

```
int j = x.numDigits + i - 1;
118
            q.num[i] = int((num[i]) * double(BASE) + num[i-1]) / d);
119
            multiAndAcumWithShift(x, -q.num[i], i-1);
120
            if (i = 1 | | j = 1) break;
121
            num[j-1] += BASE * num[j];
122
            num[j] = 0;
123
124
125
         fixInvariant (x.numDigits):
126
         return q.fixInvariant();
127
128
129
      BigInt& operator *=(const BigInt& x) { return *this = (*this) * x; }
130
      BigInt operator +(const BigInt& x) { return BigInt(*this) += x;
131
      BigInt operator -(const BigInt& x) { return BigInt(*this) -= x: }
132
      BigInt operator -() { BigInt r = 0; return r -= *this; }
133
      BigInt& operator = (const BigInt&x) \{ return *this = div(x); \}
134
      BigInt& operator %=(const BigInt& x) { div(x); return *this; }
135
      BigInt operator /(const BigInt&x) { return BigInt(*this).div(x); }
136
      BigInt operator %(const BigInt&x) { return BigInt(*this) %= x; }
137
138
      // I/O
139
      operator string() const
140
141
         ostringstream s; s << num[numDigits];
142
         for (int i = numDigits - 1; i > 0; i--)
143
144
            s.width(DIG);
145
            s. fill('0');
146
            s \ll abs(num[i]);
147
148
149
         return s.str();
150
151
152
      friend ostream& operator <<(ostream& o, const BigInt& x)
153
154
         return o << (string) x;
155
156
157
      friend istream& operator >>(istream& in, BigInt& x)
158
159
         string num;
160
         in >> num:
161
         x = BigInt((char*) num.c_str());
162
         return in:
163
164
165
      // potencia e raiz
166
      BigInt pow(int x)
167
168
         if (x < 0) return (*this = 1 || *this = -1) ? pow(-x) : 0;
169
         BigInt r = 1:
170
         for (int i = 0; i < x; i++) r *= *this;
171
         return r;
172
173
```

```
174
       BigInt root(int x)
175
176
          if (cmp() = 0 \mid | cmp() < 0 \&\& x \% 2 = 0) return 0;
177
          if (*this = 1 \mid | x = 1) return *this;
178
          if (cmp() < 0) return -(-*this).root(x);
179
          BigInt a = 1, d = *this;
180
          while (d != 1)
181
182
             BigInt b = a + (d /= 2);
183
             if (cmp(b.pow(x)) >= 0) \{ d += 1; a = b; \}
184
185
186
187
          return a;
188
189 };
```

## 2.4 Programação Dinâmica

Código 26: **Sub Set Sum**: Verifica se há um sobconjunto dos elementos do vetor cuja soma seja igual a soma pedida.

```
1 //soma maxima dos elementos do vetor
2 #define MAX.SUM 10000
з int n;
4 int vet [TAM];
5 bool m[MAX_SUM];
 7 //M->soma maxima dos elementos do vetor c->soma procurada
 8 bool subSetSum(int M, int c)
      for (int i = 0; i \ll M; i++) m[i] = false;
10
     m[0] = true;
11
12
      for (int i = 0; i < n; i++)
13
14
         for (int j = M; j >= vet[i]; j--)
15
16
            m[j] = m[j - vet[i]];
17
18
19
20
      return m[c];
21
22 }
```

Código 27: Lis: longest increasing (decreasing) subsequence  $O(n^2)$ 

```
1 #define TAM 10000

2 int c [TAM];

3 int A [TAM];

4 int H [TAM];

5

6 void ssctf(int n)
```

```
7 {
      for (int m = 1; m \le n; m++)
8
9
          c[m] = H[m];
10
          for (int i = m -1; i > 0; i --)
11
12
             if (A[i] < A[m] \&\& c[i] + H[m] > c[m])
13
14
                c[m] = c[i] + H[m];
15
16
17
18
19
20
21 void ssdtf(int n)
22 {
      for (int m = 1; m \le n; m++)
23
^{24}
          c[m] = H[m];
25
          for (int i = m -1; i > 0; i --)
26
27
             if (A[i] > A[m] \&\& c[i] + H[m] > c[m])
28
29
                c[m] = c[i] + H[m];
30
31
32
33
34
35
36 int lis1d(int n, bool inc = true)
37
      if (inc) ssctf(n);
38
      else ssdtf(n);
39
40
      int max = 0;
41
42
43
      for (int i = 1; i \le n; i++)
          \mathbf{if} \pmod{\mathbf{c}[i]}
44
             \max = c[i];
45
46
47
      return max;
48
```

## Código 28: Lis: longest increasing subsequence O(n\*logn)

```
12
        //j = upper\_bound(pd.beqin(), pd.beqin() + maxi, x) - pd.beqin()
             ; para lds
        pd[j] = x;
13
         pd_index[j] = i;
14
         if(j = maxi) \{ maxi++; ind = i; \}
15
         pred[i] = j? pd_index[j-1] : -1;
16
17
      // return maxi; se a sequencia nao precisa ser refeita
18
19
     int pos = maxi-1, k = v[ind];
20
     asw.resize( maxi );
21
22
     while (pos >= 0)
23
24
         asw[pos--] = k;
25
        ind = pred[ind];
26
        k = v [ind];
27
28
29 }
```

### Código 29: Problema da Mochila O(n\*W)

```
1 #include <stdio.h>
3 #define MAXWEIGHT 100
5 int n = 3; /* The number of objects */
6 int c[10] = \{8, 6, 4\}; /* c[i] is the *COST* of the ith object; i.e.
       what
                       YOU PAY to take the object */
s int v[10] = \{16, 10, 7\}; /* v[i] is the *VALUE* of the ith object; i.e.
                        what YOU GET for taking the object */
int W = 10; /* The maximum weight you can take */
12 void fill_sack()
     int a [MAXWEIGHT]; /* a [i] holds the maximum value that can be
13
          obtained
                      using at most i weight */
14
     int last_added [MAXWEIGHT]; /* I use this to calculate which object
15
          were
                              added */
16
     int i, j;
17
     int aux;
18
19
      for (i = 0; i \le W; ++i) {
20
21
        a[i] = 0;
        last\_added[i] = -1;
22
23
24
25
     a[0] = 0;
      for (i = 1; i \le W; ++i)
26
         for (j = 0; j < n; ++j)
27
            if ((c[j] \le i) \&\& (a[i] < a[i - c[j]] + v[j])) 
28
29
               a[i] = a[i - c[j]] + v[j];
               last_added[i] = j;
```

```
32
      for (i = 0; i \le W; ++i)
33
         if (last\_added[i] != -1)
34
            printf("Weight %d; Benefit: %d; To reach this weight I added
35
                object %d (%d$ %dKg) to weight %d.\n", i, a[i], last_added[i
                + 1, v[last_added[i]], c[last_added[i]], i - c[last_added[
                i ]]);
         else
36
            printf("Weight %d; Benefit: 0; Can't reach this exact weight.\n
37
38
      printf("---\n");
39
40
     aux = W:
41
      while ((aux > 0) \&\& (last\_added[aux] != -1)) {
42
         printf("Added object %d (%d$ %dKg). Space left: %d\n", last_added[
43
             aux] + 1, v[last_added[aux]], c[last_added[aux]], aux - c[
             last_added[aux]]);
         aux -= c[last_added[aux]];
44
45
46
47
      printf("Total value added: %d$\n", a[W]);
48 }
49
50 int main(int argc, char *argv[]) {
     fill_sack();
51
52
     return 0;
53
54 }
```

#### 2.5 Grafos

Código 30: Verifica se o grafo é aciclico.

```
1 #define TAM 100
2 #define BRANCO 0
з #define CINZA 1
4 #define PRETO 2
5 bool grafo [TAM] [TAM];
6 int pass [TAM];
7
s bool dfs(int v)
9 {
     pass[v] = CINZA;
10
11
     for (int i = 0; i < TAM; i++)
12
13
        if (grafo[v][i])
14
15
            if (pass[i] == CINZA) return false;
16
            if (pass[i] == BRANCO && !dfs(i)) return false;
17
18
19
20
```

```
21
      pass[v] = PRETO;
22
      return true;
23 }
24
25 bool aciclico()
26
      memset(pass, BRANCO, TAM*sizeof(int));
27
28
      for (int i = 0: i < TAM: i++)
29
30
         if (pass[i] == BRANCO)
31
32
             if (!dfs(i)) return false;
33
34
35
36
      return true;
37
38 }
```

Código 31: Dijkstra Caminho minimo 1 para todos pesos positivos.

```
1 #include <queue>
3 typedef vector<map<int, int>> AdjList;
4 typedef AdjList Grafo;
6 int dist[MAX_VERTICES];
7 int prev[MAX_VERTICES]; // para recuperar o caminho usando um dijoint
       forest set
9 void dijkstra (Grafo& grafo, int source)
10
      for (int i = 0; i < grafo.size(); i++)
11
12
13
         dist[i] = INF;
         prev[i] = -1;
14
15
16
      dist[source] = 0;
17
      priority_queue < pair < int , int > > heap;
18
      heap.push(make_pair(0, source));
19
20
      while (!heap.empty())
21
22
         int u = heap.top().second;
23
         heap.pop();
24
25
         // para cada vizinho de u
26
         for (map<int, int>::iterator i = grafo[u].begin(); i != grafo[u].
27
             end(); i++)
28
            int totalDist = dist[u] + (*i).second;
29
            if (totalDist <= dist[(*i).first])</pre>
30
31
               dist[(*i).first] = totalDist;
32
               heap.push(make_pair(totalDist, (*i).first));
```

Código 32: Floresta dijunta de arvores

```
1 #define SIZE 100
2
3 struct dsf
4 {
       int element_count;
       int parent[SIZE];
       int rank [SIZE];
8 };
9 typedef struct dsf * disjoint_set_forest_p;
11 void dsf_init(disjoint_set_forest_p forest, int element_count)
12 {
      forest -> element_count = element_count:
13
      memset(forest -> parent, 0, element_count*sizeof(int));
14
      memset(forest -> rank, 0, element_count * size of (int));
15
16
      for (int i = 0; i < element\_count; ++i)
17
          forest -> parent [i] = i;
18
19
20
21 int dsf_find_set(disjoint_set_forest_p forest, int i)
22 {
       if (i != forest -> parent[i])
23
^{24}
            forest->parent[i] = dsf_find_set(forest, forest->parent[i]);
25
26
       return forest -> parent [i];
27
28 }
29
30 void dsf_union(disjoint_set_forest_p forest, int i, int j)
31 {
       int x = dsf_find_set(forest, i);
32
       int y = dsf_find_set(forest, j);
33
34
       if (forest \rightarrow rank[x] > forest \rightarrow rank[y])
35
36
            forest \rightarrow parent[y] = x;
37
38
39
       else
40
            forest \rightarrow parent[x] = y;
41
            if (forest \rightarrow rank[x] = forest \rightarrow rank[y])
42
43
                 forest \rightarrow rank[y]++;
47 }
```

```
1 typedef vector <map<int, int> > AdjList;
2 struct Grafo
      int edgeCnt;
      AdjList adj;
6 };
s struct edge
9 {
       int u;
10
11
       int v;
       int weight;
12
13 };
int edge_compare(const void * e1, const void * e2)
16
       struct edge * p1 = (struct edge *) e1;
17
       struct edge * p2 = (struct edge *) e2;
18
       int f = p1->weight - p2->weight;
19
       if (f < 0)
20
21
          return -1;
22
23
       else if (f = 0)
24
25
           return edge_compare1 (e1, e2);
26
27
28
       else
29
30
           return 1;
31
32
34 struct edge * get_edge_list(Grafo& graph)
35 {
       int edge_count = graph.edgeCnt;
36
       struct edge *edges = (struct edge*) malloc(edge_count * sizeof(
37
           struct edge));
38
       int current_edge = 0;
39
40
       for (int i = 0; i < graph.adj.size(); ++i)
41
42
           for (map<int, int>::iterator j = graph.adj[i].begin(); j !=
43
               graph.adj[i].end(); j++)
44
               struct edge e;
45
               e.u = i < (*j).first ? i : (*j).first;
46
               e.v = i > (*j).first ? i : (*j).first;
47
               e.weight = (*j).second;
48
               edges[current_edge++] = e;
49
50
51
52
       return edges;
```

```
54 }
55
56 void kruskal (Grafo& graph, Grafo& mst)
57 {
       // Obtain a list of edges and sort it by weight in O(E lg E) time
58
      int edge_count = graph.edgeCnt;
59
      struct edge *edges = get_edge_list(graph);
60
      qsort(edges, edge_count, sizeof(struct edge), edge_compare);
62
       disjoint_set_forest dsf;
63
      dsf_init(&dsf, edge_count);
64
65
      for (int i = 0; i < edge\_count; ++i)
66
67
           struct edge e = edges[i];
68
           int uset = dsf_find_set(dsf, e.u);
69
           int vset = dsf_find_set(dsf, e.v);
70
           if (uset != vset)
71
72
               mst.adj[e.u][e.v] = e.weight;
73
           mst.edgeCnt++;
74
               dsf_union(dsf, uset, vset);
75
76
77
78
       free (edges);
79
80 }
```

Código 34: verifica se um grafo é bipartido

```
1 #define TAM 200
з bool grafo [TAM] [TAM];
4 int pass [TAM];
5 int n;
7 bool bipartido (int v, int color = 1)
8 {
      pass[v] = color;
     int thisColor = color;
10
     bool ret = true:
11
12
     color = color == 1 ? 2 : 1;
13
14
     for (int i = 0; i < n; i++)
15
16
         if (grafo[v][i])
17
18
            if (!pass[i]) ret = dfs(i, color);
19
            else if (pass[i] == thisColor) return false;
20
21
            if (!ret) return false;
^{22}
23
24
25
     return ret;
```

27 }

Código 35: faz a ordenação topológica de um grafo acíclico

```
₁ #define UNVISITED -1
3 int grafo [SIZE] [SIZE];
4 int prof[SIZE];
5 int sorted[SIZE];
6 int nordem:
s void dfsTopsort(int no)
      for (int viz = 0; viz < SIZE; viz++)
11
         if (grafo [no] [viz])
12
13
            if (prof[viz] == UNVISITED)
14
15
                prof[viz] = prof[no] + 1;
16
17
                dfsTopsort(viz);
18
19
20
21
      sorted[nordem--] = no;
22
23
24
  void topSort(int nvt)
25
26
      memset(prof, UNVISITED, nvt*sizeof(int));
27
      nordem = nvt - 1;
28
29
      for (int i = 0; i < nvt; i++)
30
31
         if (prof[i] == UNVISITED)
32
33
            prof[i] = 0;
34
            dfsTopsort(i);
35
36
37
38
```

Código 36: outro metodo para fazer a ordenação topológica de um grafo acíclico

```
11
       FORN(i, 0, g.size())
            if(0 = deg[i]) q.push(i);
12
13
        while (not q.empty()) {
14
            int node = q.top();
15
16
           q.pop();
            r.push_back(node);
17
           FOREACH(ngb, g[node]) {
18
                \mathbf{if}(--\operatorname{deg}[*\operatorname{ngb}] = 0) \operatorname{q.push}(*\operatorname{ngb});
19
20
21
22
       return r.size() == g.size();
23
24 }
```

Código 37: calcula fluxo máximo, Ford-Fulkerson

```
1 #define TAM 1000
2 #define MAX_INT 1000000
4 int grafo [TAM] [TAM];
5 int pred [TAM];
6 int f [TAM] [TAM];
7 bool visitados [TAM];
s int fila [TAM];
10 bool bfs (int n, int ini, int fim)
11
      int no, s = 0, e = 0;
12
      fila[e++] = ini;
13
14
      while (s != e)
15
16
         no = fila[s++];
17
18
         if (visitados [no] == 2) continue;
19
         visitados[no] = 2;
20
21
         for (int i = 0; i < n; i++)
22
23
            if (visitados[i] < 2)
24
25
               if (grafo [no][i] - f[no][i] > 0)
26
27
                   pred[i] = no;
28
                   if (i == fim) return true;
29
                   if(visitados[i] == 0)
30
31
                      fila[e++] = i;
32
                      visitados[i] = 1;
33
34
35
36
37
38
39
```

```
40
      return false;
41
42
  bool dfs(int s. int t. int size)
43
44
      visitados[s] = true;
45
      if (s == t) return true;
46
47
      for (int v = 0; v < size; v++)
48
49
         if(!visitados[v] \&\& grafo[s][v] - f[s][v] > 0)
50
51
            pred[v] = s;
52
            if (dfs(v, t, size)) return true;
53
54
55
56
57
      return false;
58
  bool findPath(int s, int t, int size)
61
      memset(visitados, false, sizeof(bool)*size);
62
      pred[s] = s;
63
      //\ \textit{Aqui pode ser usado tanto busca em largura quanto em profundidade}\,.
      // busca em largura geralmente apresenta tempos de execucao bem
65
          menores.
      return bfs(size, s, t);
66
      //return\ dfs(s, t, size);
67
68
70 int maxFlow(int size, int s, int t)
71
      int delta;
72
73
      for (int i = 0; i < size; i++)
74
75
         memset(f[i], 0, sizeof(int)*size);
76
77
78
79
      \mathbf{while}(1)
80
         bool path = findPath(s, t, size);
81
         if (!path) break;
82
83
         delta = MAXINT:
         for(int c = t; pred[c]!= c; c = pred[c])
85
86
            delta = min(delta, grafo[pred[c]][c] - f[pred[c]][c]);
87
88
89
         for(int c = t; pred[c] != c; c = pred[c])
90
91
            f[pred[c]][c] += delta;
92
            f[c][pred[c]] -= delta;
93
94
```

Código 38: calcula fluxo máximo, algoritmo mais eficiente porém muito maior em tempo de codificação

```
1 const int VT = 100;
2 const int AR = VT * VT;
4 struct grafo
5 {
     // lista de adjacencias representada na forma de vetor
     int nvt, nar;
     int dest[2 * AR];
     int adj [VT] [2 * VT];
     int nadj[VT];
10
11
     int cap[AR]; // capacidade do arco
12
     int fluxo [AR];
13
     int ent[VT];
14
15
     int padj [VT], lim [VT], nivel [VT], qtd [VT];
16
17
     int inv(int a) { return a ^ 0x1; }
18
     int orig(int a) { return dest[inv(a)]; }
19
     int capres(int a) { return cap[a] - fluxo[a]; }
20
21
     void inic (int n = 0)
22
23
        nvt = n;
^{24}
        nar = 0;
25
        memset(nadj, 0, sizeof(nadj));
26
27
28
     29
     // Adiciona uma aresta ao grafo.
30
31
     // "int u" apenas para Fluxos;
32
33
     int aresta (int i, int j, int u = 0)
34
35
36
        int ar = nar;
        cap[nar] = u;
37
        dest[nar] = i;
38
        adj[i][nadj[i]] = nar++;
39
        nadj[i]++;
40
41
```

```
cap[nar] = 0;
   dest[nar] = i;
   adj[j][nadj[j]] = nar++;
  nadj[j]++;
  return ar;
void revbfs(int ini, int fim)
   int i, no, viz, ar;
  queue < int > fila;
  memset(nivel, NULO, sizeof(nivel));
  memset(qtd, 0, sizeof(qtd));
   nivel[fim] = 0;
   fila.push(fim);
   while (! fila.empty())
      no = fila.front();
      fila.pop();
      qtd[nivel[no]]++;
      for (i = 0; i < nadj[no]; i++)
         ar = adj[no][i];
         viz = dest[ar];
         if (cap[ar] = 0 \&\& nivel[viz] = NULO)
            nivel[viz] = nivel[no] + 1;
            fila.push(viz);
int admissivel(int no)
   while (padj[no] < nadj[no])
      int ar = adj[no][padj[no]];
      if (nivel[no] = nivel[dest[ar]] + 1 && capres(ar) > 0) return
      padj[no]++;
   padj[no] = 0;
  return NULO:
int retrocede (int no)
   int i, ar, viz, menor = NULO;
```

42 43

44

45

46

47

48

49

50

51

52 53

54

55 56

57

58

59

60

61

62

63

64

65

66

67

68

69

70

71

72

73

74

75

76

77

78

79

80

81

82

83

84

85

87

88

89

90

91

92

93

94

95

96

```
97
          if (--qtd[nivel[no]] == 0) return NULO;
 98
          for (i = 0; i < nadj[no]; i++)
 99
100
             ar = adj[no][i]; viz = dest[ar];
101
             if (capres (ar) <= 0) continue;
102
             if (menor == NULO | | nivel[viz] < nivel[menor]) menor = viz;</pre>
103
104
105
          if (menor != NULO) nivel[no] = nivel[menor];
106
          atd[++nivel[no]]++
107
108
          return ((ent[no] == NULO) ? no : orig(ent[no]));
109
110
111
112
       int avanca (int no, int ar)
113
          int viz = dest[ar];
114
          ent[viz] = ar;
115
          \lim [viz] = \min(\lim [no], capres(ar));
116
          return viz;
117
118
119
       int aumenta(int ini, int fim)
120
121
          int ar, no = fim, fmax = lim[fim];
122
123
          while (no != ini)
124
125
             fluxo[ar = ent[no]] += fmax;
126
             fluxo[inv(ar)] = fmax:
127
             no = orig(ar);
128
129
130
          return fmax;
131
132
133
      int maxflow(int ini, int fim)
134
135
          int ar, no = ini, fmax = 0;
136
137
          memset(fluxo, 0, sizeof(fluxo));
138
          memset(padj, 0, sizeof(padj));
139
140
          revbfs(ini, fim);
141
142
          \lim [ini] = INF;
143
          ent[ini] = NULO;
144
145
          while (nivel[ini] < nvt && no != NULO)
146
147
             if ((ar = admissivel(no)) == NULO)
148
149
                no = retrocede(no);
150
151
152
             else if ((no = avanca(no, ar)) = fim)
```

### 2.6 Geometria

Código 39: ponto e poligono

```
1 struct point
2 {
     double x, y;
     double z; // para pontos no espaco
      point (double x = 0, double y = 0, double z = 0): x(x), y(y), z(z) {}
     point operator +(point q) { return point (x + q.x, y + q.y, z + q.z);
     point operator -(point q) { return point (x - q.x, y - q.y, z - q.z);
     point operator *(double t) { return point(x * t, y * t, z * t); }
     point operator /(double t) { return point(x / t, y / t, z / t); }
10
     double operator *(point q) { return x * q.x + y * q.y + z * q.z; }
11
      point vec(point q) { return point(y * q.z - z * q.y, z * q.x - x * q.
12
         z, x * q.y - y * q.x); }
     double operator \%(point q) { return x * q.y - y * q.x; }
13
14
15
     int cmp(point q) const
16
        if (int t = ::cmp(x, q.x)) return t;
17
         else if (int t = ::cmp(y, q.y)) return t;
18
        return :: cmp(z, q.z);
19
20
21
     bool operator == (point q) const { return cmp(q) == 0; }
22
     bool operator !=(point q) const { return cmp(q) != 0; }
23
     bool operator < (point q) const \{ return cmp(q) < 0; \}
24
25
     friend ostream& operator <<(ostream& o, point p) {
26
       return o << "(" << p.x << ", " << p.y << ", " << p.z << ")";
27
28
      static point pivot;
29
30 };
     para pontos 2D
33 double abs(point p) { return hypot(p.x, p.y); }
34 double arg(point p) { return atan2(p.y, p.x); }
35
36 point point::pivot;
38 typedef vector<point> polygon;
```

```
39
40 int ccw(point p, point q, point r)
41 {
42     return cmp((p - r) % (q - r));
43 }
44     double angle(point p, point q, point r)
46 {
47          point u = p - q, v = r - q;
48          return atan2(u % v, u * v);
49 }
```

### Código 40: Decide se q está sobre o segmento fechado pr.

```
1 bool between(point p, point q, point r)
2 {
3     return ccw(p, q, r) == 0 \&\& cmp((p - q) * (r - q)) <= 0;
4 }
```

### Código 41: Decide se os segmentos fechados pq e rs têm pontos em comum.

```
1 bool seg_intersect(point p, point q, point r, point s)
2 {
     point A = q - p;
3
     point B = s - r;
     point C = r - p;
     point D = s - q:
     int a = cmp(A \% C) + 2 * cmp(A \% D);
     int b = cmp(B \% C) + 2 * cmp(B \% D);
9
10
      if (a = 3 \mid | a = -3 \mid | b = 3 \mid | b = -3) return false;
11
      if (a \mid |b| \mid p = r \mid |p = s| \mid q = r \mid |q = s|) return true;
^{12}
13
     int t = (p < r) + (p < s) + (q < r) + (q < s);
14
      return t != 0 && t != 4;
15
16 }
```

## Código 42: Calcula a distância do ponto r ao segmento pq.

```
double seg_distance(point p, point q, point r)

{
    point A = r - q;
    point B = r - p;
    point C = q - p;

    double a = A * A, b = B * B, c = C * C;

if (cmp(b, a + c) >= 0) return sqrt(a);
    else if (cmp(a, b + c) >= 0) return sqrt(b);
    else return fabs(A % B) / sqrt(c);
}
```

Código 43: Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 dependendo se p está no exterior, na fronteira ou no interior de T, respectivamente.

```
int in-poly(point p, polygon& T)

double a = 0;

int N = T.size();

for (int i = 0; i < N; i++)

{
    if (between(T[i], p, T[(i+1) % N])) return -1;
    a += angle(T[i], p, T[(i+1) % N]);

}

return cmp(a) != 0;</pre>
```

### Código 44: Convex Hull **graham scan**.

```
1 #define INF 1e9
2 #define EPS 1e-9
 4 int cmp(double a, double b = 0.0) {
      return a+EPS < b ? -1 : a-EPS > b;
6 }
s struct Point {
     double x, y;
     Point (double a=0.0, double b=0.0) {x=a, y=b;}
10
     Point operator+(const Point &P) const {return Point(x+P.x,v+P.v);}
11
     Point operator - (const Point &P) const {return Point (x-P.x,y-P.y);}
12
     Point operator * (double c) const {return Point(x*c,y*c);}
13
     Point operator/(double c) const {return Point(x/c,y/c);}
14
     double operator!() const {return sqrt(x*x+y*y);}
15
      bool operator == (const Point &p) const {return !cmp(x,p.x) && !cmp(y,p.x)
16
     bool operator < (const Point &p) const { if (cmp(x,p.x)) return cmp(x,p.x)
17
          x) < 0; return cmp(v,p.v) < 0;}
      void print(string prefix = "") const {printf("%s%.31f %.31f\n", prefix
18
          .c_str(),x,y);
19
20
21 typedef vector < Point > Polygon;
22
23 double cross (Point A, Point B) {
      return A.x*B.y - B.x*A.y;
24
25 }
26
27 Point pmin;
28
29 bool lessThan(Point A. Point B) {
      if (cmp(cross(A-pmin,B-pmin))) return cmp(cross(A-pmin,B-pmin)) > 0;
30
      return cmp(!(pmin-A),!(pmin-B)) < 0;
31
32 }
33
34 int sort (Polygon &p) {
     int imin = 0, i, j, n = p.size();
```

```
37
      for (i=1; i < p.size(); i++) {
         if (p[i] < p[imin]) imin = i;
38
39
40
     swap(p[0], p[imin]);
41
42
     pmin = p[0];
43
      sort(p.begin()+1,p.end(),lessThan);
44
45
      for (i=n-1; i > 0 \&\& !cmp(cross(p[i]-p[0],p[i-1]-p[0])); i--);
46
      if (i = 0) return 1;
47
      for (j=0; j < (n-i)/2; j++) swap(p[i+j], p[n-j-1]);
48
     return 0:
49
50 }
51
52 Polygon convex_hull(Polygon &p) { // tirar o & para nao alterar o
       poligono original
      int hs = 2, n = p.size();
53
     Polygon hull;
54
55
      if (p.size() < 3) return p;
56
57
     int isline = sort(p);
58
      hull.push_back(p[0]), hull.push_back(p[1]);
59
60
     for (int i=2; i \le n-isline; i++) {
61
         while (hull.size() > 1 \&\& cmp(cross(p[i\%n]-hull[hs-1],hull[hs-2]-
62
             hull[hs-1]) \le 0 { // trocar o <= para < para manter pontos
             intermediarios
            hull.pop_back(), hs--;
63
64
         if (i < n) hull.push_back(p[i]), hs++;
65
66
67
     return hull;
68
69 }
70
71 int main() {
     Polygon p;
72
73
74
      while (...) {
         double x = \dots;
75
         double v = \dots;
76
         p. push_back(Point(x,y));
77
78
79
     Polygon hull = convex_hull(p);
80
81
     for (int i=0; i < hull.size(); i++) {
82
83
84
85
     return 0;
86 }
```

## 2.7 Algebra Linear

Código 45: Simplex

```
1 #include <iostream>
2 #include <vector>
з #include <algorithm>
5 using namespace std;
7 #define fori(i,n) for(int i=0; i < (n); ++i)
s \# define forr(i,a,b) for(int i=(a); i <= (b); ++i)
9 #define ford(i,a,b) for(int i=(a); i >= (b); —i)
10 #define sz size()
11
const double EPS=1e-9; const int INF = 0 \times 3f3f3f3f3f;
13
14 #define all(x) (x).begin(),(x).end()
15
int cmpD(double x, double y=0, double tol=EPS) {
      return (x \le y+tol)? (x+tol \le y)? -1:0:1;
17
18 }
19
20 struct simplex {
      // \max c * x, s.t: A * x <= b; x >= 0
     simplex (const vector < vector < double > > & A_, const vector < double
22
         > \& b_{-},
            const vector < double > \& c_-) : A(A_-), b(b_-), c(c_-) \{ \}
23
      vector < vector < double > > A; vector < double > b, c, sol;
24
      vector< bool > N; vector< int > kt; int m, n;
25
     void pivot( int k, int l, int e ) {
26
         int x = kt[1]; double p = A[1][e];
27
28
        fori(i,k) A[l][i] \neq p;
        b[l] /= p; N[e] = false;
29
        for i(i,m) if (i != 1) {b[i] -= A[i][e]*b[1]; A[i][x] = -A[i][e]*A[
30
            1][x];}
         fori(j,k) if (N[j])
31
            c[j] = c[e] * A[l][j];
32
            fori(i,m) if ( i != 1 ) A[i][j] = A[i][e] * A[1][j];
33
34
        kt[1] = e; N[x] = true; c[x] = -c[e] * A[1][x];
35
36
     vector < double > go( int k ) {
37
        vector< double > res;
38
         while (1) {
39
            int e = -1, l = -1;
40
            fori(i,k) if (N[i] \&\& cmpD(c[i]) > 0) { e = i; break; }
41
            if (e = -1) break;
42
            for i(i,m) if (cmpD(A[i][e]) > 0 && (l = -1 | cmpD(b[i] / A)
43
                [i][e],
                        b[1] / A[1][e], 1e-20 ) < 0 ) ] 1 = i;
44
            if (l = -1) return vector< double >(); // unbounded
45
            pivot(k, l, e);
46
47
         res.resize(k, 0);
48
         fori(i,m) res[kt[i]] = b[i];
```

```
50
          return res:
51
      vector < double > solve() {
52
         m = A.sz; n = A[0].sz; int k = m+n+1;
53
         N = vector < bool > (k, true); vector < double > c_copy = c;
54
          c.resize(n+m); kt.resize(m);
55
          fori(i,m) {
56
             A[i]. resize(k); A[i][n+i] = 1; A[i][k-1] = -1;
57
             kt[i] = n+i; N[kt[i]] = false;
58
59
          int l = min_element(all(b)) - b.begin();
60
          if(cmpD(b[1]) < 0)
61
             c = vector < double > (k, 0);
62
             c[k-1] = -1; pivot(k, 1, k-1); sol=go(k);
63
             if (\text{cmpD}(\text{sol}[k-1])>0) return vector <double >(): // in feasible
64
             fori(i,m) if(kt[i] == k-1) {
65
                fori(j,k-1) if(N[j] && cmpD(A[i][j]) != 0) {
66
                    pivot(k, i, j); break;
67
68
69
             c=c\_copy; c.resize(k,0);
70
             fori(i,m) fori(j,k) if(N[j]) c[j] = c[kt[i]]*A[i][j];
71
72
          sol = go(k-1);
73
          if (!sol.empty()) sol.resize(n);
74
          return sol;
75
76
77 };
78
      Como\ usar
79 //
80 int main() {
       /* Exemplo: Maximize cx Subject to Ax \le b */
81
      vector < vector < double > A(9);
82
      double Av[][3] = {{1,1,0}, {0,0,-1}, {-1,-1,0},
83
                       \{0,0,1\}, \{1,0,0\}, \{0,1,0\},
84
                       \{0,0,1\}, \{1,0,1\}, \{0,1,0\}\};
85
86
      for (int i=0; i < 9; i++) {
87
         A[i]. insert (A[i]. begin (), &(Av[i][0]), &(Av[i][3])); // Sim, [3]!
88
              Ou seja, idx-final+1
89
      vector <double > c(3, 1); // c=[1 \ 1 \ 1]
91
      double by [] = \{2, -1, -2, 1, 2, 1, 1, 2, 1\};
92
       vector < double > b(bv, bv+sizeof(bv)/sizeof(double));
93
       simplex sim(A,b,c);
95
       vector < double > s = sim.solve();
96
      if (!s.size()) cout << "Impossivel\n";</pre>
97
98
       for(int i=0; i < s.size(); i++) {
          cout << s[i] << endl;
100
101
102 }
```

## 2.8 Casamento de strings

Código 46: String matching - Algoritmo **KMP** - O( n + m)

```
1 // F[i] - size of the largest prefix of pattern [0...i] that is also a
2 // suffix of pattern [1...i]. Ex: pattern = {a,b,a,c,a,b}. F =
      {0,0,1,0,1,2}
3 #define MAX_PATTERN_SIZE 10010
4 int F[MAX_PATTERN_SIZE];
 5 void build_failure_function ( const string & pattern )
     int m = pattern.size();
     F[0] = -1:
     for (int i = 0; i < m; i++)
10
        F[i+1] = F[i] + 1;
11
        while (F[i+1] > 0 \&\& pattern[i] != pattern[F[i+1]-1])
12
           F[i+1] = F[F[i+1]-1] + 1;
13
14
15 }
     retorna a posicao inicial de cada ocorrencia de pattern em text
17
  vector<int> KMP( const string & text, const string & pattern )
19
      build_failure_function( pattern );
20
     vector < int > start_positions:
21
     int j = 0, m = pattern.size(), n = text.size();
22
23
     for (int i = 0; i < n; i++)
24
25
        while (true)
26
27
            if ( text[i] == pattern[j] )
28
29
               if ( ++j == m )
30
31
                  start_positions.push_back(i-m+1);
                  j = F[j];
33
34
35
               break;
36
37
            if (j == 0) break;
38
            j = F[j];
39
40
41
42
     return start_positions;
43
44 }
```

### 2.9 Outros

```
1 /**
2 The Josephus problem (or Josephus permutation) is a theoretical problem
      related to a certain counting-out game. There are people standing in
      a circle waiting to be executed. After the first man is executed,
      certain number of people are skipped and one man is executed. Then
      again, people are skipped and a man is executed. The elimination
      proceeds around the circle (which is becoming smaller and smaller as
      the executed people are removed), until only the last man remains,
      who is given freedom. The task is to choose the place in the initial
      circle so that you are the last one remaining and so survive.
3 */
5 using namespace std;
7 int josephus (int n, int m)
8 {
     int res = 0;
9
     vector <int> people;
10
     int loc = 0;
11
12
     for (int i = 0; i < n; i++) people.push_back(i+1);
13
14
     while (people.size() > 1)
15
16
        if (loc >= people.size())
17
           loc %= people.size();
18
19
        people . erase (people . begin ()+loc);
20
        loc += (m-1);
^{21}
22
23
     return people [0];
^{24}
```

Código 48: Gera as permutações dos elementos da string

```
1 bool nextPermutation(string& number)
2 {
          bool is Bigger = true;
          int i, j;
          for (i = number. size() - 1; i >= 0; i--)
                   if (number[i] < number[i+1]) break;</pre>
10
          if (i != -1)
11
12
                   isBigger = false:
13
14
                   for (j = number. size() - 1; j >= i+1; j--)
16
                            if (number[j] > number[i])
17
18
                                    break;
19
20
```

```
21
22
                    int tmp = number[i];
23
                    number [i] = number [j];
24
                    number[j] = tmp;
25
26
                   j = number.size() -1;
27
                    i++;
28
29
                    while (i < j)
30
31
                             tmp = number[i];
32
                             number[i] = number[j];
33
                             number[j] = tmp;
34
                             i++;
35
36
                             j --;
37
38
39
          return is Bigger;
40
41 }
```

Código 49: Exemplo de geração de permutações dos elementos da string, usando backtracking

```
1 #define TAM 10
2 int cnt = 0;
3 int total; //numero de elementos de elem
4 int elem [TAM];
5 bool usados [TAM]; //ZERE ME
7 void enumera(int num)
      if (num = total)
10
11
         for (int i = 0; i < total; i++) cout << elem[i];
12
         cout << endl;
13
         return;
14
15
16
      for (int i = 0; i < total; i++)
17
18
         if (!usados[i])
19
20
            elem[num] = i;
21
            usados[i] = true;
22
            enumera (num + 1);
23
24
            usados[i] = false;
25
26
27 }
```

# 3 Biblioteca C/C++

## 3.1 I/O

Ignorando entradas na família scanf:

Código 50: Ignora os dois floats do meio. Retornará 2 no sucesso.

```
scanf("%f %*f %*f %d", &a, &b);
```

## 3.2 Map

Código 51: Referencias map

```
1 #include <map>
2 #include <string>
з #include <cstdio>
5 using namespace std; // USE ISTO!!!
7 class Comparadora;
  class Pessoa {
     int idade;
10
     string nome;
11
     friend class Comparadora;
^{12}
13 public:
     Pessoa (string nome, int idade) {
         this->idade = idade;
15
         this->nome = nome:
16
17
     void print() const {
18
         printf("Nome: %s Idade: %d\n", nome.c_str(), idade);
19
20
21 };
23 class Comparadora { // Ordena crescentemente
24 public: // <- IMPORTANTE
     bool operator() (const Pessoa &a, const Pessoa &b)
25
26
         int idDif = a.idade-b.idade;
27
         if(idDif < 0) return true;</pre>
28
         else if(idDif==0) return a.nome.compare(b.nome) < 0 ? true : false
29
         else return false;
31
32 };
33
34 int main() {
     Pessoa r("Rangelz", 86);
35
     Pessoa r2("Rangelzao", 86);
36
37
     map<Pessoa, string, Comparadora> alunos;
38
     alunos[r] = "UFMG";
39
```

```
alunos [r2]="PUC";
40
41
      // Iterator
      for (map < Pessoa, string, Comparadora > :: iterator it=alunos.begin(); it
          != alunos.end(); it++) {
         it -> first . print();
43
         printf("\t%s\n\n", it->second.c_str());
44
45
      // Find
46
      if (alunos.find(Pessoa("Rangelz", 86)) != alunos.end()) { // Achou!
47
         printf("Achei Rangel!\n");
48
49
      return 0;
50
51 }
```