1 Sumário **Tabelas Tabelas** 1 precisao tipo bits min...max Codigos $\mathbf{2}$ char 8 0..1272 signed char 8 -128...1272 2.1 8 2 unsigned char 0...255short 16 -32.768 .. 32.767 4 2.3 $\operatorname{Grafos} \ \ldots \ \ldots \ \ldots \ \ldots \ \ldots \ \ldots \ \ldots$ $0 \dots 65.535$ 4 unsigned short 16 2.4 -2x10**9 .. 2 x 10**99 32 2.5 32 0 .. 4x10**9 9 unsigned int int64 t 64 -9 x 10**18 .. 9 x 10**18 18 Lista de Tabelas $uint64_t$ 64 0 .. 18 x 10**18 19 Limites de representação de dados Tabela 1: Limites de representação de dados 2 1 3 scanf() - %[*][width][modifiers]type1 2 0! = 14 $\operatorname{scanf}()\%[*][\operatorname{width}][\operatorname{modifiers}]$ type 1! = 15 2! = 2math (angulos em radianos) 3! = 64! = 24Lista de Listagens 5! = 1206! = 7201 7! = 5.0402 2 8! = 40.3203 .vimrc para a configuração do vim 2 9! = 362.8804 2 10! = 3.628.8005 3 11! = 39.916.8006 3 exemplo de set e multset 12! = 479.001.600 [limite do (unsigned) int] 7 3 13! = 6.227.020.8008 3 14! = 87.178.291.2009 15! = 1.307.674.368.00010 4 16! = 20.922.789.888.00011 4 17! = 355.687.428.096.00012 4 18! = 6.402.373.705.728.00013 5 19! = 121.645.100.408.832.00014 pesquisa binária......... 5 20! = 2.432.902.008.176.640.000 [limite do (u)int64_t] 15 Arredondamento e output em outras bases . . . 16 máximo divisor comum e mínimo multiplo co-Tabela 2: Fatorial 5 decide se um número é primo 17 6 18 Retorna a fatoração em números primos de abs(n)...... 6 19 20 Caminho minimo 1 para todos pesos positivos. 6 21 6 Floresta dijunta de arvores 22 Arvore geradora mínima kruskal 7 verifica se um grafo é bipartido 23 7 24 faz a ordenação topológica de um grafo acíclico 7 25 calcula fluxo máximo 8 26 27 Decide se q está sobre o segmento fechado pr. . 28 Decide se os segmentos fechados pq e rs têm 29 Calcula a distância do ponto r ao segmento pq. 9 30 Classifica o ponto p em relação ao polígono T. % Tipo Retorna 0, -1 ou 1 dependendo se p está no exterior, na fronteira ou no interior de T, reschar c 9 int d float e, E, f, g, G int (octal) o int (hexa) x, X uint u char* S

2 Codigos

2.1 Exemplos

```
#include <stdio.h>
modifiers
           tipo
                                                             #include <stdlib.h>
            short int (d, i, n), or unsigned short int (o, u, \hat{x})
h
           long int (d, i, n), or unsigned long int (o, u, x), winclude <string .h>
long int (d, i, n), or unsigned long int (o, u, x), or wind the extra sh .h>
1
L
            long double (e, f, g)
                                                             #include <inttypes.h>
                                                             #include <ctype.h>
       Tabela 4: scanf() %[*][width][modifiers]type
                                                             #include <algorithm>
                                                             #include <utility>
                                                         10
                                                             #include <iostream>
                                                         11
                                                             #include <map>
                                                         13
                                                             #include <set>
                                                         14
                                                             #include <vector>
                                                             #include <sstream>
                                                         16
                                                         17
                                                             using namespace std;
                                                         18
                                                         19
função
         descrição
                                                             #define abs(a) ((a) > 0 ? (a) : -(a))
                                                         20
atof
         Convert string to double
                                                         21
                                                             int main()
                                                         22
atoi
         Convert string to integer
                                                         23
atol
         Convert string to long integer
                                                                 int n;
                                                         24
         Convert string to double
strtod
                                                         25
                                                         26
                                                                 cin >> n;
strtol
         Convert string to long integer
                                                         27
strtoul
         Convert string to unsigned long integer
                                                                 for (int i = 0; i < n; i++)
                                                         29
                     Tabela 5: stdlib
                                                         30
                                                         32
                                                         33
                                                                 while (cin >> n)
                                                         34
                                                         35
                                                         36
                                                                 return 0;
                                                         37
                                                         38
                                                                                  Código 1: Modelo
função
         descrição
                                                             const double EPS = 1e-10;
                                                          1
cos
         Compute cosine
                                                          2
\sin
         Compute sine
                                                              * -1 se x < y
                                                                0 \ se \ x = y
                                                          4
tan
         Compute tangent
                                                          5
                                                              *
                                                                 1
                                                                   se x > y
         Compute arc cosine
acos
                                                          6
         Compute arc sine
asin
                                                             inline int cmp (double x, double y = 0, double tol =
                                                          7
         Compute arc tangent
atan
         Compute arc tangent with two parameters
atan2
                                                                 return (x \le y + tol) ? (x + tol < y) ? -1 : 0 :
                                                          9
         Compute hyperbolic cosine
\cosh
\sinh
         Compute hyperbolic sine
                                                             }
                                                         10
         Compute hyperbolic tangent
tanh
                                                                       Código 2: comparcao de ponto flutuante
         Compute exponential function
exp
frexp
         Get significand and exponent
                                                             set ai noet ts=4 sw=4 bs=2
ldexp
         Generate number from significand and exponent <sup>1</sup>
                                                             svn on
         Compute natural logarithm
log
                                                             mat Keyword "\<foreach\>"
                                                          3
log10
         Compute common logarithm
                                                                     Código 3: .vimrc para a configuração do vim
         Break into fractional and integral parts
modf
pow
         Raise to power
sqrt
         Compute square root
                                                              /* printf example */
                                                             #include <stdio.h>
                                                          2
         Round up value
ceil
                                                          3
fabs
         Compute absolute value
                                                             int main()
                                                          4
floor
         Round down value
fmod
         Compute remainder of division
                                                                 printf ("Characters: %c %c \n", 'a', 65);
                                                          6
                                                                 printf ("Decimals: %d %ld\n", 1977, 650000L);
                                                                         ("Preceding with blanks: %10d \n", 1977);
         Tabela 6: math (angulos em radianos)
                                                                 printf ("Preceding with zeros: %010d \n", 1977);
                                                          9
                                                                 printf ("Some different radixes: %d %x %o %#x %#o
                                                         10
                                                                       \n", 100, 100, 100, 100, 100);
                                                                 printf ("floats: %4.2f %+.0e %E %4.2f\n", 3.1416,
                                                         11
```

 $^{^{12}} 2$

3.1416, 3.1416, 3.1);

printf ("Width trick: %*d \n", 5, 10);

```
printf ("%s \n", "A string");
                                                                12
       return 0;
                                                                      cout << "size: " << (int) mymultiset.size() <<</pre>
14
                                                                13
                                                                      endl; cout << "count: " << (int) mymultiset.count(10) <<
15
   }
   /* \%[flags (-, +, etc)]/width]/.precision]/length (A)
16
                                                                            endl;
         , l, L) ] specifier
17
    Characters: a A
    Decimals: 1977 650000
                                                                       it=mymultiset.find(20);
18
                                                                16
    Preceding\ with\ blanks:
19
                                      1977
                                                                       mymultiset.erase (it);
                                                                17
    Preceding with zeros: 0000001977
                                                                18
    Some different radixes: 100 64 144 0x64 0144
                                                                       if (! mymultiset.empty)
21
                                                                19
    floats: 3.14 + 3e + 000 3.141600E + 000 3.10
                                                                        mymultiset.erase (mymultiset.find(40));
                                                                20
    Width trick:
                      10
                                                                21
   A string
                                                                       for (it=mymultiset.begin(); it!=mymultiset.end();
24
                                                                22
                                                                           it++)
    */
                                                                         cout << " " << *it;
                                                                23
                          Código 4: printf
                                                                24
                                                                      int myints [] = \{19,72,4,36,20,20\};
                                                                25
                                                                      multiset <int> first (myints, myints+3);
                                                                                                                          //
                                                                26
   #include <iostream>
                                                                           4.19.72
   #include <map>
                                                                       multiset <int> second (myints+3, myints+6);
    using namespace std;
                                                                           20,20,36
                                                                28
   int main ()
5
                                                                       29
6
   {
      map < char, int > mymap;
                                                                30
      map<char.int>::iterator it:
                                                                      return 0;
                                                                31
      pair < map < char , int > :: iterator , bool > ret;
                                                                32
10
      // first insert function version (single parameter
11
                                                                                 Código 6: exemplo de set e multset
      \label{eq:mymap.insert} \operatorname{mymap.insert} \ ( \ \operatorname{pair} <\! \operatorname{\mathbf{char}}, \operatorname{\mathbf{int}} >\! (\ '\ \! \operatorname{\mathbf{a'}}, 100) \ ) \ ;
12
      mymap.insert ( pair < char, int > ('z', 200) );
                                                                    #include <iostream>
13
                                                                    #include <list >
      ret=mymap.insert (pair < char, int > ('z', 500));
                                                                    using namespace std;
15
                                                                3
16
      if (ret.second=false)
17
                                                                    int main ()
                                                                5
        cout << "element 'z' already existed";</pre>
18
                                                                 6
        \mathrm{cout} << " with a value of " << ret.first -> second
19
                                                                       list \langle int \rangle mylist (2,100);
                                                                                                               // two ints with
              << endl;
                                                                            a value of 100
                                                                       mylist.push_front (200);
20
                                                                       mylist.push_back (300);
21
      // third insert function version (range insertions)
22
                                                                       it = mylist.begin():
      map<char, int> anothermap;
                                                                       mylist.insert (it,10);
23
                                                                12
      anothermap.insert(mymap.begin(),mymap.find('c'));13
                                                                      \label{eq:mylist.insert} \mbox{mylist.insert (it ,2 ,20); // two ints with a value}
24
                                                                           of 20
      // showing contents:
26
                                                                14
      cout << "mymap contains:\n";</pre>
                                                                       mylist.reverse(); // Reverses the order of the
27
                                                                           elements in the list.
      for (it=mymap.begin(); it != mymap.end(); it++)
        cout << (*it).first << " => " << (*it).second <
29
                                                                       cout << "mylist contains:";</pre>
              endl;
                                                                17
                                                                       for (list <int>::iterator it=mylist.begin(); it!=
30
                                                                18
                                                                           mylist.end(); ++it)
31
      map<char, string> mymap;
      mymap['a']="an element";
                                                                         cout << " " << *it;
32
                                                                19
      if (mymap.count('a') > 0)
                                                                20
33
           \mathrm{cout} << \mathrm{mymap} \left[ \text{'a'} \right] << \text{" is an element of mymaxp}
                                                                       \mathrm{cout} << "Popping out the elements in mylist:";
34
                .\n";
                                                                       while (!mylist.empty())
35
                                                                23
                                                                         cout << " " << mylist.front();
      while (!mymap.empty())
36
                                                                24
37
                                                                25
                                                                         mylist.pop_front();
          cout << mymap.begin()->first << " => ";
38
                                                                26
          cout << mymap.begin()->second << endl;</pre>
          map<char, int>::iterator erasedelement = mymaps
                                                                      while (!mylist.empty())
40
              erase (mymap.begin());
                                                                29
                                                                         cout << " " << mylist.back();
41
                                                                         mylist.pop_back();
42
                                                                31
43
      return 0:
                                                                32
    }
                                                                33
                                                                      \mathtt{cout} \, <\!< \, \mathtt{mylist.size} \, (\,) \, <\!< \, \mathtt{endl} \, ;
                                                                34
                     Código 5: exemplo de map
                                                                35
                                                                      return 0;
                                                                36
                                                                37
   #include <iostream>
   #include <set>
                                                                                      Código 7: exemplo de list
    using namespace std;
                                                                    #include <iostream>
   int main ()
5
                                                                 1
                                                                    #include <queue>
      multiset <int> mymultiset;
                                                                    using namespace std;
                                                                 3
      \verb|multiset| < \verb|int| > :: \verb|iterator| it;
                                                                 4
                                                                    int main ()
      // set some initial values:
10
      for (int i=1; i \le 5; i++) mymultiset.insert(i*10); 7
                                                                      queue<int> myqueue;
             // 10 20 30 40 50
                                                                      int sum (0);
```

```
vector < int > myvector (3,100);
      for (int i=1; i \le 10; i++) myqueue.push(i);
                                                                     vector<int>::iterator it;
10
11
      myqueue.back() -= myqueue.front();
                                                                     myvector.reserve(100);
12
                                                               10
13
                                                               11
      cout << "size: " << (int) myqueue.size() << endl;12
14
                                                                     for (i=0; i< myvector.size(); i++)
                                                                        myvector.at(i)=i; // = myvector[i] = i
15
                                                               13
      while (!myqueue.empty())
16
                                                               14
                                                                      it = myvector.begin();
17
                                                               15
         sum += myqueue.front();
                                                                      it = myvector.insert ( it , 200 );
18
                                                               16
                                                                     myvector.insert (it,2,300);
19
         myqueue.pop();
                                                               17
20
                                                               18
                                                                      vector <int> anothervector (2,400);
21
                                                               19
      \mathtt{cout} \;<<\; \texttt{"total:} \;\; \texttt{"} \;<<\; \mathtt{sum} \;<<\; \mathtt{endl} \; ;
                                                                     int myarray [] = \{ 501,502,503 \};
22
                                                               20
23
                                                               21
                                                                      myvector.insert (it+2, anothervector.begin(),
24
      return 0:
                                                                          anothervector.end());
   }
                                                                      myvector.insert (myvector.begin(), myarray,
                                                               22
                                                                          myarray+3);
                    Código 8: exemplo de queue
                                                               23
                                                                      cout << "myvector contains:";</pre>
                                                               24
                                                                      for (it=myvector.begin(); it<myvector.end(); it++)
                                                               25
   #include <iostream>
                                                                        cout << " " << *it;
                                                               26
   #include <queue>
                                                                      cout << endl;
                                                               27
   using namespace std;
                                                               28
                                                                     // erase the 6th element
                                                               29
   int main ()
                                                                     myvector.erase (myvector.begin()+5);
                                                               30
6
                                                                     int sum;
                                                               31
      priority_queue <int> mypq;
                                                               32
                                                                      while (!myvector.empty())
                                                               33
      mypq.push(30);
9
                                                               34
                                                                         sum += myvector.back();
      mypq.push(100);
                                                               35
                                                                         myvector.pop_back();
      mypq.push(25);
11
                                                               36
12
      mypq.push(40);
                                                                     return 0;
                                                               38
      cout << "size: " << (int) mypq.size() << endl;</pre>
14
                                                               39
15
16
      cout << "Popping out elements...";</pre>
                                                                                   Código 11: exemplo de vector
      \mathbf{while} \quad (\,!\,\mathrm{mypq}\,.\,\mathrm{empty}\,(\,)\,\,)
17
18
         cout << " " << mypq.top();</pre>
19
                                                                  #include <iostream>
                                                                1
20
         mypq.pop();
                                                                   #include <string>
21
                                                                   using namespace std;
      cout << endl;
22
23
                                                                5
                                                                   int main ()
24
      return 0;
                                                                6
   }
25
                                                                     string str ("There are two needles in this
                                                                7
                                                                         haystack with needles.");
                Código 9: exemplo de priority queue
                                                                      string str2 ("needle");
                                                                      size_t found;
                                                                9
                                                               10
   #include <iostream>
                                                                     // different member versions of find in the same
                                                               11
   #include <stack>
                                                                          order as above:
    using namespace std;
                                                               12
                                                                      found=str.find(str2);
                                                                      if (found!=string::npos)
                                                               13
5
   int main ()
                                                                        \mathrm{cout} << "first 'needle' found at: " << \mathrm{int}\,(\mathrm{found}
                                                               14
6
                                                                            ) << endl;
      stack<int> mystack;
                                                               15
      int sum = 0;
                                                                      found=str.find("needles are small", found+1,6);
                                                               16
                                                                      if (found!=string::npos)
                                                               17
      mystack.push(10);
10
                                                                        \mathrm{cout} << "second 'needle' found at: " << \mathrm{int}(
                                                               18
      mystack.push(20);
                                                                            found) << endl;
12
                                                               19
      mystack.top() -= 5;
13
                                                                      found=str.find("haystack");
                                                               20
14
                                                                      if (found!=string::npos)
                                                               21
      while (!mystack.empty())
15
                                                                        \mathrm{cout} << "'haystack' also found at: " << \mathrm{int}(
                                                               22
16
                                                                            found) << endl;
         sum += mystack.top();
                                                               23
         mystack.pop();
18
                                                                      found=str.find('.');
                                                               24
19
                                                                      if (found!=string::npos)
                                                               25
20
                                                                        \mathrm{cout} << "Period found at: " << \mathrm{int} \, (\mathrm{found}) <<
      cout \ll "size: " \ll (int) mystack.size() \ll endl;^{26}
21
                                                                            endl;
22
                                                               27
      return 0:
23
                                                                      // let's replace the first needle:
                                                               28
   }
^{24}
                                                               29
                                                                      str.replace(str.find(str2), str2.length(),"
                                                                          preposition");
                    Código 10: exemplo de stack
                                                                      cout << str << endl;
                                                               30
   #include <iostream>
                                                                      string str="We think in generalities, but we live
                                                               32
   #include <vector>
                                                                          in details.";
   using namespace std;
                                                                                                     // quoting Alfred N.
                                                               33
                                                                                                          Whitehead
   int main ()
                                                                      string str2, str3;
                                                               34
                                                               ^{35} 4
   {
                                                                      size_t pos;
```

```
str2 = str.substr (12,12); // "generalities"
37
38
      pos = str.find("live");
                                    // position of "live"
39
          in str
                                    // get from "live" to 9
      str3 = str.substr (pos);
40
          the end
41
      cout \ll str2 \ll ' ' \ll str3 \ll endl;
42
43
44
45
      return 0:
   }
46
47
   first 'needle' found at: 14
second 'needle' found at: 44
48
                                                              5
49
                                                              6
    `haystack' also found at: 30
    Period found at: 51
51
                                                              8
    There are two prepositions in this haystack with
                                                              9
        needles.
                                                             10
    generalities \ live \ in \ details \, .
53
54
                                                             11
                   Código 12: exemplo de string
                                                             12
   #include <iostream>
                                                             13
   #include <algorithm>
   #include <vector>
                                                             14
   using namespace std;
                                                             15
                                                             16
   bool myfunction (int i, int j) { return (i<j); }
                                                             17
                                                             18
   struct myclass {
                                                             19
      bool operator() (int i,int j) { return (i<j);}</pre>
                                                             20
10
   } mvobject:
                                                             21
11
                                                             22
12
    int compare (const void * a, const void * b)
                                                             23
13
14
      return (*(int*)a - *(int*)b);
                                                             24
15
16
                                                             25
                                                             26
   int main () {
18
      int myints [] = {32,71,12,45,26,80,53,33};
19
                                                             27
      vector <int> myvector (myints, myints+8);
                                                             28
                          // 32 71 12 45 26 80 53 33
                                                             29
21
                                                             30
      // using default comparison (operator <):
                                                             31
      sort (myvector.begin(), myvector.begin()+4);
23
                      //(12 32 45 71)26 80 53 33
                                                             33
      // using function as comp
                                                             34
      sort (myvector.begin()+4, myvector.end(),
25
                                                             35
          myfunction); // 12 32 45 71(26 33 53 80)
                                                             36
      // using object as comp
26
                                                             37
      \verb|sort| ( \verb|myvector.begin| () , \verb|myvector.end| () , \verb|myobject| )_{38}
27
                //(12 26 32 33 45 53 71 80)
                                                             39
28
                                                             40
      // if stable is need
29
                                                             41
      stable_sort (myvector.begin(), myvector.end(),
30
                                                             42
          myfunction);
                                                             43
                                                             44
      // Rearranges the elements in the range [first, _{45}
32
          last),\ in\ such\ a\ way\ that\ the\ subrange\ [first],
          middle)
      // contains the smallest elements of the entire
33
          range sorted in ascending order, and the
      // [middle,end) contains the remaining elements
34
          without\ any\ specific\ order.
      partial_sort (myvector.begin(), myvector.begin()
35
          +3, myvector.end());
                                                              3
      qsort (myints, 8, sizeof(int), compare);
37
                                                              4
38
                                                              5
      return 0;
39
                                                              6
   }
40
                 Código 13: exemplo de ordenação
```

```
int compareMyType (const void * a, const void * b)

if (*(MyType*)a > *(MyType*)b ) return 1;
```

```
if (*(MyType*)a == *(MyType*)b ) return 0;
if (*(MyType*)a < *(MyType*)b ) return -1;
}
int key = 40;
item = (int*) bsearch (&key, values, n, sizeof (int), compareMyType);</pre>
```

Código 14: pesquisa binária

```
#include <iostream>
\#include < iomanip > // setprecision()
using namespace std;
int main () {
  double a = 3.1415926534;
  double b = 2006.0;
  double c = 1.0e - 10;
  // setprecision (1) \Rightarrow 1 casa decimal apos a
      virgula
  cout << fixed << setprecision(1) << 9.09090901 <<
      endl;
  cout << fixed << setprecision(2) << 9.09090901 <<
      endl;
  cout << fixed << setprecision(3) << 9.09090901 <<
      endl;
  cout \ll fixed \ll setprecision(2) \ll 9.1 \ll endl;
  // anula o efeito de setprecision
  cout.unsetf(ios::floatfield);
  // 5 digitos no maximo
  cout.precision(5);
  cout << a << '\t' << b << '\t' << c << endl;
  cout << fixed << a << '\t' << b << '\t' << c <<
      endl:
  cout << scientific << a << '\t' << b << '\t' << c
      << endl;
  //\ Sets\ the\ basefield\ format\ flag\ for\ the\ str
      stream to dec, hex or oct.
  int n = 70:
  cout << dec << n << endl;
  cout << hex << n << endl;
  cout << oct << n << endl;
  return 0;
/* output
9.1
9.09
9.091
9.10
3.1416 2006
                 1e - 10
3.14159 2006.00000
                         0.00000
                2.00600e+03
3.14159e+00
                                 1.000000e-10
70
46
106
```

Código 15: Arredondamento e output em outras bases

2.2 Teoria dos números

Código 16: máximo divisor comum e mínimo multiplo comum

```
bool isPrime(int n)
                                                                  36
2
                                                                  37
                                                                          return true;
        if (n < 0) return isPrime(-n);
       if (n == 1) return true;
        if (n < 5 \mid \mid n \% 2 = 0 \mid \mid n \% 3 = 0) return (n = 0)
                                                                                 Código 19: Verifica se o grafo é aciclico.
            == 2 \mid \mid n == 3);
                                                                      #include <queue>
       int \max P = sqrt(n) + 2;
       for (int p = 5; p < maxP; p += 6)
                                                                      \label{eq:typedef} \textbf{typedef} \ \ \text{vector} < \!\! \text{map} < \!\! \textbf{int} \, , \ \ \textbf{int} > > \ \ \text{AdjList} \, ;
                                                                      typedef AdjList Grafo;
           if (n \% p == 0 \mid \mid n \% (p+2) == 0) return false
                                                                      int dist[MAX_VERTICES];
                                                                      int prev[MAX_VERTICES]; // para recuperar o caminho
                                                                   7
       return true;
12
                                                                           usando um dijoint forest set
13
    }
                                                                      void dijkstra(Grafo& grafo, int source)
              Código 17: decide se um número é primo
                                                                   9
                                                                  10
                                                                          for (int i = 0; i < grafo.size(); i++)
                                                                  11
    typedef map<int , int> prime_map;
                                                                  12
    void squeeze (prime_map& M, int& n, int p)
                                                                              dist[i] = INF;
2
                                                                  13
                                                                              \operatorname{prev}[i] = -1;
3
                                                                  14
       for (; n \% p == 0; n \neq p) M[p]++;
                                                                  15
                                                                  16
    void factor (int n, prime_map& M)
                                                                          dist[source] = 0;
                                                                  17
                                                                          \label{eq:continuous_prior} {\tt priority\_queue}\!<\!{\tt pair}\!<\!\!{\tt int}\;,\;\;{\tt int}\!>\;>\;{\tt heap}\;;
                                                                  18
        if (n < 0) return n = -n;
                                                                          heap.push(make_pair(0, source));
                                                                  19
       \quad \textbf{if} \ \ (n\,<\,2) \ \ \textbf{return}\,;
                                                                  20
                                                                          while (!heap.empty())
10
                                                                  21
       squeeze (M, n, 2);
11
                                                                  22
                                                                              \mathbf{int}\ u = \mathrm{heap.top}\left(\right).\mathrm{second}\,;
12
       squeeze (M, n, 3);
                                                                  23
                                                                              heap.pop();
       int \max P = sqrt(n) + 2;
14
                                                                  25
       for (int p = 5; p < maxP; p += 6)
15
                                                                  26
                                                                              // para cada vizinho de u
                                                                              for (map<int, int>::iterator i = grafo[u].begin
16
                                                                  27
           squeeze (M, n, p);
                                                                                  (); i != grafo[u].end(); i++)
17
18
           squeeze(M, n, p+2);
                                                                                 int totalDist = dist[u] + (*i).second;
19
                                                                  29
20
        if (n > 1) M[n]++;
                                                                  30
                                                                                 if (totalDist <= dist[(*i).first])</pre>
                                                                  31
                                                                                     dist[(*i).first] = totalDist;
    Código 18: Retorna a fatoração em números primos de abs(n)<sub>3</sub>
                                                                                     heap.push(make_pair(totalDist, (*i).
                                                                                          first));
                                                                                     prev[(*i).first] = u;
                                                                  34
                                                                  35
    2.3
           Grafos
                                                                              }
                                                                  36
                                                                          }
                                                                  37
   #define TAM 100
   #define BRANCO 0
                                                                       Código 20: Caminho minimo 1 para todos pesos positivos.
   #define CINZA 1
   #define PRETO 2
    bool grafo [TAM] [TAM];
                                                                      #define SIZE 100
   int pass [TAM];
                                                                   2
                                                                      struct dsf
                                                                   3
    bool dfs(int v)
                                                                   4
                                                                      1
                                                                           int element_count;
9
       pass[v] = CINZA;
                                                                           int parent[SIZE];
10
11
                                                                   7
                                                                           int rank [SIZE];
12
       for (int i = 0; i < TAM; i++)
                                                                   8
                                                                      typedef struct dsf * disjoint_set_forest_p;
13
           if (grafo[v][i])
14
                                                                  10
                                                                  11
                                                                      void dsf_init(disjoint_set_forest_p forest, int
15
               if (pass[i] == CINZA) return false;
                                                                           element_count)
16
               if (pass[i] = BRANCO && !dfs(i)) return
17
                                                                  12
                    false;
                                                                          forest -> element_count = element_count;
                                                                  13
           }
                                                                          memset(forest->parent, 0, element_count*sizeof(
18
                                                                  14
19
                                                                               int));
                                                                          memset(forest->rank, 0, element_count*sizeof(int)
20
                                                                  15
       pass[v] = PRETO;
21
22
       return true;
                                                                  16
23
   }
                                                                          for (int i = 0; i < element\_count; ++i)
                                                                  17
                                                                              forest \rightarrow parent[i] = i;
24
                                                                  18
25
    bool aciclico()
                                                                  19
26
    {
                                                                  20
       memset(pass, BRANCO, TAM*sizeof(int));
                                                                      int dsf_find_set(disjoint_set_forest_p forest, int i
27
                                                                  21
28
       for (int i = 0; i < TAM; i++)
29
                                                                  22
```

23

24

25

²⁶ 6

30

31

32

33

if (pass[i] == BRANCO)

if (!dfs(i)) return false;

if (i != forest->parent[i])

forest -> parent [i]);

forest -> parent [i] = dsf_find_set (forest,

```
// Obtain a list of edges and sort it by weight
29
                                                                58
    void dsf_union(disjoint_set_forest_p forest, int i
                                                                              in O(E lg E) time
30
                                                                         int edge_count = graph.edgeCnt;
                                                                59
                                                                         struct edge *edges = get_edge_list(graph);
31
                                                                60
         int x = dsf_find_set(forest, i);
                                                                         qsort(edges, edge_count, sizeof(struct edge),
32
                                                                61
         int y = dsf_find_set(forest, j);
33
                                                                              edge_compare);
34
                                                                62
         if (forest \rightarrow rank[x] > forest \rightarrow rank[y])
                                                                         disjoint_set_forest dsf;
35
                                                                63
                                                                64
                                                                        dsf_init(&dsf, edge_count);
36
37
             forest \rightarrow parent[y] = x;
                                                                65
         }
                                                                         for (int i = 0; i < edge\_count; ++i)
38
                                                                66
                                                                67
         else
39
                                                                              struct edge e = edges[i];
         {
40
                                                                68
                                                                              int uset = dsf_find_set(dsf, e.u);
             forest \rightarrow parent[x] = y;
41
                                                                69
             if (forest \rightarrow rank[x] = forest \rightarrow rank[y])
                                                                              int vset = dsf_find_set(dsf, e.v);
                                                                              if (uset != vset)
43
                                                                71
44
                  forest \rightarrow rank[y] + +;
                                                                72
                                                                73
                                                                                   mst.adj[e.u][e.v] = e.weight;
        }
                                                                               mst.edgeCnt++;
46
                                                                74
47
    }
                                                                75
                                                                                   dsf_union(dsf, uset, vset);
                                                                76
               Código 21: Floresta dijunta de arvores
                                                                77
                                                                         }
                                                                         free (edges);
                                                                79
   typedef vector <map<int, int> > AdjList;
                                                                80
    struct Grafo
2
                                                                             Código 22: Arvore geradora mínima kruskal
3
    {
4
       int edgeCnt:
       AdjList adj;
5
                                                                    #define TAM 200
   };
6
                                                                    bool grafo [TAM] [TAM];
                                                                 3
    struct edge
                                                                    int pass [TAM];
9
                                                                    int n:
10
         int u;
         int v;
11
                                                                    bool bipartido (int v, int color = 1)
12
         int weight;
    };
13
                                                                        pass[v] = color;
14
                                                                        int thisColor = color;
                                                                10
    int edge\_compare(const void * e1, const void * e2)
15
                                                                        bool ret = true:
                                                                11
16
    {
         struct edge * p1 = (struct edge *) e1;
17
                                                                        color = color == 1 ? 2 : 1;
                                                                13
18
         struct edge * p2 = (struct edge *) e2;
                                                                14
         int f = p1->weight - p2->weight;
19
                                                                        for (int i = 0; i < n; i++)
                                                                15
         if (f < 0)
20
                                                                16
21
                                                                            if (grafo[v][i])
                                                                17
            return -1;
22
                                                                18
23
                                                                               if (!pass[i]) ret = dfs(i, color);
                                                                19
         else if (f == 0)
24
                                                                20
                                                                               else if (pass[i] = thisColor) return false
25
             return edge_compare1(e1, e2);
26
                                                                21
27
                                                                               if (!ret) return false;
                                                                22
         else
28
                                                                            }
                                                                23
29
         {
                                                                        }
                                                                24
             return 1;
30
                                                                25
31
                                                                        return ret;
                                                                26
32
   }
                                                                27
33
    \mathbf{struct} \ \mathtt{edge} \ * \ \mathtt{get\_edge\_list} \ ( \ \mathsf{Grafo\&} \ \ \mathtt{graph} \, )
34
                                                                             Código 23: verifica se um grafo é bipartido
35
         int edge_count = graph.edgeCnt;
36
         struct edge *edges = (struct edge*) malloc(
                                                                    #define UNVISITED -1
37
             edge_count * sizeof(struct edge));
                                                                    int grafo[SIZE][SIZE];
38
                                                                 3
         int current_edge = 0;
                                                                    int prof[SIZE]
                                                                    int sorted [SIZE];
                                                                 5
40
         \mbox{ for } (\,\mbox{int}\ i \,=\, 0\,;\ i \,<\, \mbox{graph.adj.size}\,(\,)\,;\ +\!\!\!+\!\! i\,)
41
                                                                    int nordem;
42
             for (map<int, int>::iterator j = graph.adj[is
                                                                    void dfsTopsort(int no)
43
                  ]. begin(); j != graph.adj[i].end(); j++)
                                                                        for (int viz = 0; viz < SIZE; viz++)
                                                                10
44
45
                  struct edge e;
                                                                11
                  e.u = i < (*j).first ? i : (*j).first; 12
                                                                            if (grafo[no][viz])
                  e.v = i > (*j).first ? i : (*j).first; 13
47
                                                                               if (prof[viz] = UNVISITED)
48
                  e.weight = (*j).second;
                                                                14
                  edges[current\_edge++] = e;
                                                                15
             }
                                                                                   prof[viz] = prof[no] + 1;
50
                                                                16
51
                                                                17
                                                                                   dfsTopsort(viz);
52
                                                                18
        return edges;
53
                                                                19
                                                                            }
                                                                        }
54
                                                                20
                                                                <sup>21</sup> 7
55
```

56

57

void kruskal (Grafo& graph, Grafo& mst)

return forest -> parent [i];

28 }

```
sorted[nordem--] = no;
   }
23
                                                              63
24
                                                              64
   void topSort(int nvt)
25
26
   {
       memset(prof, UNVISITED, nvt*sizeof(int));
27
28
       nordem = nvt - 1;
29
       for (int i = 0; i < nvt; i++)
30
31
           if (prof[i] == UNVISITED)
32
33
              prof[i] = 0;
34
35
              dfsTopsort(i);
           }
36
       }
37
   }
```

Código 24: faz a ordenação topológica de um grafo acíclico

```
#define TAM 1000
   int grafo [TAM] [TAM];
   int pred [TAM]
   int f [TAM] [TAM]
    bool visitados [TAM];
    bool dfs(int s, int t, int size)
9
                                                              13
       visitados[s] = true;
10
                                                              14
       if(s == t) return true;
11
                                                              15
12
                                                              16
13
       for(int v = 0; v < size; v++)
14
           if(grafo[s][v] - f[s][v] > 0 & visitados[v]^{18}
15
16
              pred[v] = s;
17
                                                              20
              if(dfs(v, t, size)) return true;
19
                                                              21
20
21
       return false;
22
23
24
   bool findPath(int s, int t, int size)
25
                                                              25
26
                                                              26
       memset(visitados, false, sizeof(bool)*size);
27
                                                              27
28
       return dfs(s, t, size);
                                                              28
29
30
                                                              30
   int maxFlow(int size, int s, int t)
31
                                                              31
32
    {
       int delta;
33
                                                              33
34
                                                              34
       for(int i = 0; i < size; i++)
35
                                                              35
36
                                                              36
          memset(f[i], 0, sizeof(int)*size);
37
                                                              37
38
                                                              38
39
                                                              39
       pred[s] = s;
40
41
                                                              41
       while (findPath(s, t, size))
42
                                                              42
43
                                                              43
           delta = INT\_MAX;
44
                                                              44
           for(int c = t; pred[c] != c; c = pred[c])
45
                                                              45
46
47
              delta = min(delta, grafo[pred[c]][c] - f[
                  pred[c]][c]);
           }
48
49
           for(int c = t; pred[c] != c; c = pred[c])
50
51
              f [ pred [ c ] ] [ c ] += delta;
53
              f[c][pred[c]] -= delta;
54
55
56
       int soma = 0;
57
58
       for(int i = 0; i < size; i++)
59
60
          soma += f[i][t];
```

```
return soma;
```

Código 25: calcula fluxo máximo

Geometria 2.4

1

3

4

9

10

11

17

22

23

24

29

32

40

1

3

```
struct point
{
   double x, y;
   point (double x = 0, double y = 0): x(x), y(y) {}
   point operator +(point q) \{ return point(x + q.x,
        y + q.y); }
   point operator -(point q) \{ return point(x - q.x,
        y - q.y); 
   point operator *(double t) { return point(x * t,
       v * t): }
   point operator /(double t) { return point(x / t,
       y / t); }
   double operator *(point q) { return x * q.x + y *
         q.y; }
   double operator %(point q) { return x * q.y - y *
        q.x; }
   int cmp(point q) const
       \textbf{if} \ ( \, \textbf{int} \ t \, = \, :: cmp(x \, , \ q \, . \, x) \, ) \ \ \textbf{return} \ t \, ; 
      return :: cmp(y, q.y);
   bool operator ==(point q) const { return cmp(q)
         = 0; }
   bool operator !=(point q) const { return cmp(q)
       != 0;  }
   bool operator < (point q) const { return cmp(q) <
   friend ostream& operator <<(ostream& o, point p)
     return o << "(" << p.x << ", " << p.y << ")";
   static point pivot;
};
double abs(point p) { return hypot(p.x, p.y);
double arg(point p) { return atan2(p.y, p.x); }
point point :: pivot;
typedef vector<point> polygon;
int ccw(point p, point q, point r)
   return cmp((p - r) \% (q - r));
double angle (point p, point q, point r)
   point u = p - q, v = r - q;
   return atan2(u \% v, u * v);
               Código 26: ponto e poligono
bool between (point p, point q, point r)
   return ccw(p, q, r) == 0 \&\& cmp((p-q) * (r-q)
       ) <= 0;
```

Código 27: Decide se q está sobre o segmento fechado pr.

```
bool seg_intersect(point p, point q, point r, point
   s)
   point A = q - p;
```

```
point B = s - r;
                                                                                                                     15
              point C = r - p;
 5
                                                                                                                     16
              point D = s - q;
                                                                                                                     17
                                                                                                                     18
             \begin{array}{lll} \textbf{int} & a \, = \, \mathrm{cmp}(A \,\,\% \,\, C) \,\, + \,\, 2 \,\, * \,\, \mathrm{cmp}(A \,\,\% \,\, D) \,\, ; \\ \textbf{int} & b \, = \, \mathrm{cmp}(B \,\,\% \,\, C) \,\, + \,\, 2 \,\, * \,\, \mathrm{cmp}(B \,\,\% \,\, D) \,\, ; \end{array}
                                                                                                                     19
                                                                                                                     20
10
                                                                                                                     21
              if (a == 3 \mid \mid a == -3 \mid \mid b == 3 \mid \mid b == -3)
11
                                                                                                                     22
                      return false;
                  (a || b || p == r || p == s || q == r || q \Longrightarrow4
12
                      s) return true;
              \mathbf{int} \ t \ = \ (p \ < \ r \ ) \ + \ (p \ < \ s \ ) \ + \ (q \ < \ r \ ) \ + \ (q \ < \ s \ ) \, ;
14
              return t != 0 && t != 4;
15
       }
16
```

Código 28: Decide se os segmentos fechados pq e r
s têm pontos em comum.

```
double seg_distance(point p, point q, point r)

point A = r - q;
point B = r - p;
point C = q - p;

double a = A * A, b = B * B, c = C * C;

if (cmp(b, a + c) >= 0) return sqrt(a);
else if (cmp(a, b + c) >= 0) return sqrt(b);
else return fabs(A % B) / sqrt(c);
}
```

Código 29: Calcula a distância do ponto r ao segmento pq.

```
int in_poly(point p, polygon& T)

double a = 0;
int N = T. size();
for (int i = 0; i < N; i++)

if (between(T[i], p, T[(i+1) % N])) return -1;
    a += angle(T[i], p, T[(i+1) % N]);

return cmp(a) != 0;

}</pre>
```

Código 30: Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 dependendo se p está no exterior, na fronteira ou no interior de T, respectivamente.

2.5 Outros

```
The Josephus problem (or Josephus permutation) is a
        theoretical problem related to a certain
        counting-out\ game.\ There\ are\ people\ standing\ in
        a circle waiting to be executed. After the first
        man is executed, certain number of people are skipped and one man is executed. Then again,
        people are skipped and a man is executed. The
        elimination proceeds around the circle (which is
         becoming smaller and smaller as the executed
        people \ are \ removed) \,, \ until \ only \ the \ last \ man
        remains\,,\ who\ is\ given\ freedom\,.\ The\ task\ is\ to
        choose the place in the initial circle so that
        you are the last one remaining and so survive.
   using namespace std;
    int josephus (int n, int m)
8
       int res = 0;
       vector <int> people;
10
       int loc = 0;
11
12
       \label{eq:formula} \textbf{for (int } i = 0; \ i < n; \ i++) \ people.push_back(i+1)
13
```

```
while (people.size() > 1)
{
    if (loc >= people.size())
       loc %= people.size();

    people.erase(people.begin()+loc);
    loc += (m-1);
}
```

Código 31: josephus problem