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1 Codigos

1.1 Tricks e confs

Código 1: .vimrc para a configuração do vim

```
1 set ai noet ts=4 sw=4 bs=2
2 set cindent
```

Código 2: Speedup cin cout io. Caso usada não use printf

```
1 std::cout.sync_with_stdio(false);
```

Código 3: Arredondamento e output em outras bases

```
1 #include <iostream>
2 #include <iomanip> // setprecision()
3 using namespace std;
5 int main () {
    double a = 3.1415926534;
    double b = 2006.0;
    double c = 1.0e - 10;
    // setprecision(1) \Rightarrow 1 casa decimal apos a virgula
10
    cout << fixed << setprecision(1) << 9.09090901 << endl;
11
    cout << fixed << setprecision(2) << 9.09090901 << endl;
12
    cout << fixed << setprecision(3) << 9.09090901 << endl;
    cout << fixed << setprecision(2) << 9.1 << endl:
14
15
    // anula o efeito de setprecision
16
    cout.unsetf(ios::floatfield);
17
18
    // 5 digitos no maximo
19
    cout.precision(5);
20
21
    cout << a << '\t' << b << '\t' << c << endl;
^{22}
    cout << fixed << a << '\t' << b << '\t' << c << endl;
23
    cout << scientific << a << '\t' << b << '\t' << c << endl;
24
25
    // Sets the basefield format flag for the str stream to dec, hex or
         oct.
    int n = 70;
27
    cout \ll dec \ll n \ll endl;
28
    cout << hex << n << endl;
29
    cout << oct << n << endl;
30
31
32
    return 0;
33 }
34 /* output
35 9.1
36 9.09
37 9.091
38 9.10
```

1.2 Exemplos

Código 4: Modelo

```
1 #include <stdio.h>
2 #include <stdlib.h>
3 #include <string.h>
 4 #include <math.h>
6 #include <inttypes.h>
7 #include <ctvpe.h>
8 #include <limits.h>
10 #include <algorithm>
11 #include <utility>
12 #include <iostream>
14 #include <map>
15 #include <set>
16 #include <vector>
17 #include <list>
18 #include <queue>
19 #include <sstream>
21 using namespace std;
23 #define abs(a) ((a) > 0 ? (a) : -(a))
24
25 int main()
26
27
      int n;
28
29
      cin >> n;
30
      for (int i = 0; i < n; i++)
31
32
33
34
35
      while (cin \gg n)
36
37
38
39
      return 0;
40
41 }
```

Código 5: comparcao de ponto flutuante

```
1 /**
2 * -1 se x < y
3 * 0 se x = y
4 * 1 se x > y
5 */
6 const double EPS = 1e-10;
7 #define _inline(f...) f() _-attribute_-((always_inline)); f
8 _inline(int cmp)(double x, double y = 0, double tol = EPS)
9 {
10    return (x <= y + tol) ? (x + tol < y) ? -1 : 0 : 1;
11 }</pre>
```

1.3 Teoria dos números

Código 6: Máximo divisor comum e mínimo multiplo comum

```
int gcd(int x, int y)
2 {
3    return y ? gcd(y, x % y) : abs(x);
4 }
5  uint64_t lcm(int x, int y)
6 {
7    if (x && y) return abs(x) / gcd(x, y) * uint64_t(abs(y));
8    else return uint64_t(abs(x | y));
9 }
```

Código 7: Teste (ineficiente) de primalidade

```
1 bool isPrime(int n)
2 {
3      if (n < 0) return isPrime(-n);
4      if (n = 1) return true;
5      if (n < 5 || n % 2 = 0 || n % 3 = 0) return (n == 2 || n == 3);

6      7      int maxP = sqrt(n) + 2;
8      for (int p = 5; p < maxP; p += 6)
9      {
10          if (n % p == 0 || n % (p+2) == 0) return false;
11      }
12      return true;
13 }</pre>
```

Código 8: Fatoração em números primos.

```
1 typedef map<int, int> prime_map;
2 void squeeze(prime_map& M, int& n, int p)
3 {
4     for (; n % p == 0; n /= p) M[p]++;
5 }
6 void factor(int n, prime_map& M)
7 {
```

```
if (n < 0) { factor(-n, M); return; }
      if (n < 2) return;
10
      squeeze (M, n, 2);
11
      squeeze (M, n, 3);
12
13
      int maxP = sqrt(n) + 2:
      for (int p = 5; p < maxP; p += 6)
16
         squeeze (M, n, p);
17
         squeeze(M, n, p+2);
18
19
      if (n > 1) M[n]++;
20
21 }
```

Código 9: $a^b mod$ n de forma rápida.

```
1 int mpow(int a, int b, int n = 10)
2 {
3    if(b == 0)
4     return 1;
5    else {
6      long long res = mpow(a, b/2, n);
7     res = (res*res) % n;
8    if(b%2 == 1)
9     res = (res*a) % n;
10    return (int) res;
11   }
12 }
```

Código 10: (a*b) mod c rápido.

```
1 long long mulmod(long long a, long long b, long long c)
2 {
3      long long x = 0;
4      long long y = a % c;
5      while(b > 0)
6      {
7          if(b & 111) x = (x + y) % c;
8          y = (y << 1) % c;
9          b >>= 1;
10      }
11     return x % c;
12 }
```

Código 11: Computa x tal que a*x = b (mod c). Quando a equação não tem solução, retorna algum valor arbitrário errado, mas basta conferir o resultado.

```
1 long long axbmodc(long long a, long long b, long long c)
2 {
3     return a ? (axbmodc(c % a, (a - b % a) % a, a) * c + b) / a : 0;
4 }
```

Código 12: Baby-step Giant-step algorithm Calcula o menor valor de e para $b^e = n$ mod p. Retorna -1 se eh impossivel

```
1 #define inv_mult(a, n) axbmodc(a, 1, n)
3 long long discreteLlogarithm ( long long b, long long n, long long p )
4 {
     if (n == 1) return 0;
5
     map < long long, int > table;
     long long m = sqrt(p) + 1, pot = 1, pot2 = 1;
     for (int j = 0; j < m; j++)
10
11
        if (pot = n) return j;
12
        table [(n * inv_mult(pot, p)) \% p] = j;
13
        pot = (pot * b) \% p;
14
15
16
     for (int i = 0; i < m; i++)
17
18
        if (table.find(pot2)!= table.end()) return i * m + table[pot2]
19
        pot2 = (pot * pot2) \% p;
20
21
22
     return -1;
23
24
```

1.4 Estruturas de dados

Código 13: Números de precisão harbitrária (bigint).

```
1 const int DIG = 4;
2 const int BASE = 10000; // BASE**3 < 2**51
3 const int TAM = 1000:
5 struct BigInt
6 {
     int num[TAM], numDigits;
      BigInt(int x = 0): numDigits(1)
        memset(num, 0, sizeof(num));
10
        num[numDigits++] = x; fixInvariant();
11
12
      BigInt(char *s): numDigits(1)
13
14
         memset(num, 0, sizeof(num));
15
         int sign = 1;
16
17
         while (*s && !isdigit(*s))
18
19
           if (*s++= '-') sign *= -1;
20
21
```

```
char *t = strdup(s), *p = t + strlen(t);
   while (p > t)
      *p = 0; p = max(t, p - DIG);
      sscanf(p, "%d", &num[numDigits]);
      num[numDigits++] *= sign;
   free(t);
   fixInvariant();
BigInt& fixInvariant (int m = 0)
   numDigits = max(m, numDigits);
   int sign = 0;
   for (int i = 1, carry = 0; i <= numDigits || carry && (numDigits =
        i); i++)
      num[i] += carry;
      carry = num[i] / BASE;
      num[i] %= BASE;
      if (num[i]) sign = (num[i] > 0) ? 1 : -1;
   for (int i = 1; i < numDigits; i++)
      if (num[i] * sign < 0)
         num[i] += sign * BASE;
         num[i+1] -= sign;
   while (numDigits && !num[numDigits]) numDigits --;
   return *this:
//Comparacao
int cmp(const BigInt& x = 0) const
   int i = max(numDigits, x.numDigits), t = 0;
   while (1)
      if ((t = :: cmp(num[i], x.num[i])) | i = 0) return t;
bool operator <(const BigInt& x) const { return cmp(x) < 0; }
bool operator >(const BigInt& x) const { return cmp(x) > 0; }
bool operator \leq (const BigInt\&x) const \{ return cmp(x) <= 0; \}
bool operator >= (const BigInt&x) const { return cmp(x) >= 0;
bool operator ==(\mathbf{const} \ \mathrm{BigInt\&} \ \mathrm{x}) \ \mathbf{const} \ \{ \ \mathbf{return} \ \mathrm{cmp}(\mathrm{x}) == 0;
```

 24

25 26

27

28

29 30

31

32

33

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37

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47

48

49 50

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52

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54 55

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59 60

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62

63

64

65

66

67

68

69

70

71

72

73

```
77
      bool operator !=(const BigInt&x) const { return cmp(x) != 0; }
                                                                                    131
                                                                                           BigInt operator +(const BigInt&x) { return BigInt(*this) += x; }
                                                                                           BigInt operator -(const BigInt&x) { return BigInt(*this) -= x; }
78
                                                                                    132
      //operacoes fundamentais
                                                                                           BigInt operator -() { BigInt r = 0; return r -= *this; }
 79
                                                                                    133
      BigInt& operator +=(const BigInt& x)
                                                                                           BigInt& operator = (const BigInt&x) \{ return *this = div(x); \}
 80
                                                                                    134
                                                                                           BigInt& operator %=(const BigInt& x) { div(x); return *this; }
 81
                                                                                    135
                                                                                           BigInt operator /(const BigInt&x) { return BigInt(*this).div(x); }
          for (int i = 1; i \le x.numDigits; i++) num[i] += x.num[i];
 82
                                                                                    136
          return fixInvariant(x.numDigits);
                                                                                           BigInt operator %(const BigInt& x) { return BigInt(*this) %= x; }
 83
                                                                                    137
 84
                                                                                    138
       BigInt& operator -=(const BigInt& x)
                                                                                           // I/O
 85
                                                                                    139
                                                                                           operator string() const
 86
                                                                                    140
          for (int i = 1; i \le x.numDigits; i++) num[i] -= x.num[i];
 87
                                                                                    141
                                                                                              ostringstream s; s << num[numDigits];
          return fixInvariant(x.numDigits);
 88
                                                                                    142
                                                                                              for (int i = numDigits - 1; i > 0; i--)
 89
                                                                                    143
 90
                                                                                    144
      void multiAndAcumWithShift(const BigInt& x. int m. int b)
                                                                                                 s.width(DIG):
 91
                                                                                    145
      \{ // *this += (x * m) << b; \}
                                                                                                 s.fill('0');
 92
                                                                                    146
          for (int i = 1, carry = 0; (i <= x.numDigits || carry) && (
                                                                                                 s \ll abs(num[i]);
 93
                                                                                    147
              numDigits = i + b); i++)
                                                                                    148
                                                                                    149
 94
             num[i+b] += x.num[i] * m + carry;
                                                                                              return s.str();
 95
                                                                                    150
             carry = num[i+b] / BASE;
 96
                                                                                    151
             num [i+b] %= BASE;
 97
                                                                                    152
                                                                                           friend ostream& operator <<(ostream& o, const BigInt& x)
                                                                                    153
 98
 99
                                                                                    154
                                                                                              return o << (string) x;
100
                                                                                    155
       BigInt operator *(const BigInt& x) const
101
                                                                                    156
102
                                                                                    157
                                                                                           friend istream& operator >>(istream& in, BigInt& x)
103
          BigInt r;
                                                                                    158
          for (int i = 1; i <= numDigits; i++) r.multiAndAcumWithShift(x,
104
                                                                                    159
             num [i], i-1;
                                                                                              string num;
                                                                                    160
          return r;
                                                                                              in >> num:
105
                                                                                    161
                                                                                              x = BigInt((char*) num.c_str());
                                                                                    162
106
                                                                                              return in:
107
                                                                                    163
      BigInt div(const BigInt& x)
108
                                                                                    164
109
                                                                                    165
          if (x = 0) return 0;
                                                                                           // potencia e raiz
110
                                                                                    166
111
                                                                                    167
                                                                                           BigInt pow(int x)
          BigInt a:
112
                                                                                    168
          q.numDigits = max(numDigits - x.numDigits + 1, 0):
                                                                                              if (x < 0) return (*this = 1 | | *this = -1)? pow(-x) : 0;
113
                                                                                    169
          int d = x.num[x.numDigits] * BASE + x.num[x.numDigits - 1];
                                                                                              BigInt r = 1:
114
                                                                                    170
115
                                                                                    171
                                                                                              for (int i = 0; i < x; i++) r *= *this;
          for (int i = q.numDigits; i > 0; i--)
                                                                                              return r:
116
                                                                                    172
                                                                                    173
117
             int j = x.numDigits + i - 1;
118
                                                                                    174
             q.num[i] = int((num[j] * double(BASE) + num[j-1]) / d);
                                                                                           BigInt root(int x)
119
                                                                                    175
             multiAndAcumWithShift(x, -q.num[i], i-1);
                                                                                    176
120
             if (i = 1 | | j = 1) break;
                                                                                              if (cmp() = 0 \mid | cmp() < 0 \&\& x \% 2 = 0) return 0;
                                                                                    177
121
             num[i-1] += BASE * num[i];
                                                                                              if (*this = 1 \mid | x = 1) return *this;
122
                                                                                    178
             num[j] = 0;
                                                                                              if (cmp() < 0) return -(-*this).root(x);
123
                                                                                    179
                                                                                              BigInt a = 1, d = *this;
124
                                                                                    180
                                                                                              while (d != 1)
125
                                                                                    181
          fixInvariant(x.numDigits);
126
                                                                                    182
          return q. fixInvariant();
                                                                                                 BigInt b = a + (d /= 2);
127
                                                                                    183
                                                                                                 if (cmp(b.pow(x)) >= 0) \{ d += 1; a = b; \}
128
                                                                                    184
129
                                                                                    185
      BigInt& operator *=(const BigInt& x) { return *this = (*this) * x; }
130
                                                                                    186
```

1.5 Programação Dinâmica

Código 14: **Sub Set Sum**: Verifica se há um sobconjunto dos elementos do vetor cuja soma seja igual a soma pedida.

```
1 //soma maxima dos elementos do vetor
2 #define MAX.SUM 10000
з int n:
4 int vet [TAM];
5 bool m[MAX.SUM];
7 //M->soma maxima dos elementos do vetor c->soma procurada
s bool subSetSum(int M, int c)
9 {
      for (int i = 0; i \leftarrow M; i++) m[i] = false;
10
     m[0] = true;
11
12
      for (int i = 0; i < n; i++)
13
14
         for (int j = M; j >= vet[i]; j--)
15
16
            m[j] = m[j - vet[i]];
17
18
19
20
     return m[c];
^{21}
22 }
```

Código 15: Lis: longest increasing (decreasing) subsequence $O(n^2)$

```
1 #define TAM 10000
2 int c [TAM];
з int A[TAM];
4 int H[TAM];
5
6 void ssctf(int n)
      for (int m = 1; m \le n; m++)
         c[m] = H[m];
10
         for (int i = m -1; i > 0; i --)
11
12
            if (A[i] < A[m] \&\& c[i] + H[m] > c[m])
13
               c[m] = c[i] + H[m];
15
16
17
18
19 }
```

```
20
21 void ssdtf(int n)
^{22}
      for (int m = 1; m \le n; m++)
^{24}
          c[m] = H[m];
25
          for (int i = m - 1; i > 0; i - -)
26
27
             if (A[i] > A[m] \&\& c[i] + H[m] > c[m])
                 c[m] = c[i] + H[m];
30
31
32
33
34
36 int lis1d(int n, bool inc = true)
37
      if (inc) ssctf(n);
38
      else ssdtf(n);
      int max = 0:
41
42
      for (int i = 1; i \le n; i++)
43
          \mathbf{if} \pmod{\mathbf{c}[i]}
44
             \max = c[i];
45
46
47
      return max;
48 }
```

Código 16: Lis: longest increasing subsequence O(n*logn)

```
1 // Longest Increasing Subsequence - LIS O(n log n)
2 #define fori(i, n) for (int i = 0; i < (n); ++i)
 3 void lis (const vector < int > & v, vector < int > & asw)
     vector < int > pd(v.size(),0), pd_index(v.size()), pred(v.size());
     int maxi = 0, x, j, ind;
     fori(i, v. size())
        x = v[i];
10
        j = lower_bound( pd.begin(), pd.begin() + maxi, x ) - pd.begin();
11
        //j = upper\_bound(pd.begin(), pd.begin() + maxi, x) - pd.begin()
12
             ; para lds
        pd[j] = x;
13
        pd_index[j] = i;
14
        if(j = maxi) \{ maxi++; ind = i; \}
15
        pred[i] = j ? pd_index[j-1] : -1;
16
17
     // return maxi; se a sequencia nao precisa ser refeita
18
19
     int pos = maxi-1, k = v[ind];
20
21
     asw.resize( maxi );
22
     while (pos >= 0)
```

Código 17: Problema da Mochila O(n*W)

```
1 #include <stdio.h>
з #define MAXWEIGHT 100
5 int n = 3; /* The number of objects */
6 int c[10] = \{8, 6, 4\}; /* c[i] is the *COST* of the ith object; i.e.
      what
                       YOU PAY to take the object */
s int v[10] = \{16, 10, 7\}; /* v[i] is the *VALUE* of the ith object; i.e.
                        what YOU GET for taking the object */
int W = 10; /* The maximum weight you can take */
11
12 void fill_sack()
     int a [MAXWEIGHT]; /* a i l holds the maximum value that can be
13
          obtained
                      using at most i weight */
14
     int last_added [MAXWEIGHT]; /* I use this to calculate which object
15
         were
                             added */
16
17
     int i, j;
     int aux;
18
19
     for (i = 0; i \le W; ++i)
20
21
        a[i] = 0;
        last\_added[i] = -1;
^{22}
23
24
     a[0] = 0;
25
     for (i = 1; i \le W; ++i)
26
         for (j = 0; j < n; ++j)
27
            if ((c[j] \le i) \&\& (a[i] < a[i - c[j]] + v[j]))
28
              a[i] = a[i - c[j]] + v[j];
29
               last_added[i] = j;
30
31
32
     for (i = 0; i \le W; ++i)
33
         if (last\_added[i] != -1)
34
            printf("Weight %d; Benefit: %d; To reach this weight I added
35
                object %d (%d$ %dKg) to weight %d.\n", i, a[i], last_added[i
                + 1, v[last_added[i]], c[last_added[i]], i - c[last_added[
                i ]]);
         else
            printf("Weight %d; Benefit: 0; Can't reach this exact weight.\n
37
                ", i);
     printf("---\n");
39
40
```

```
41
      aux = W:
      while ((aux > 0) \&\& (last\_added[aux] != -1)) {
42
         printf("Added object %d (%d$ %dKg). Space left: %d\n", last_added[
43
             aux] + 1, v[last_added[aux]], c[last_added[aux]], aux - c[
             last_added [aux]]);
         aux -= c[last_added[aux]];
44
45
46
      printf("Total value added: %d$\n", a[W]);
47
48
49
50 int main(int argc, char *argv[]) {
      fill_sack();
51
52
      return 0;
53
54 }
```

1.6 Grafos

Código 18: Verifica se o grafo é aciclico.

```
1 #define TAM 100
2 #define BRANCO 0
з #define CINZA 1
_4 #define PRETO _2
5 bool grafo [TAM] [TAM];
6 int pass [TAM];
s bool dfs(int v)
10
      pass[v] = CINZA;
11
      for (int i = 0; i < TAM; i++)
12
13
         if (grafo[v][i])
14
15
            if (pass[i] == CINZA) return false;
16
            if (pass[i] = BRANCO && !dfs(i)) return false;
17
18
19
20
      pass[v] = PRETO;
21
      return true;
22
23 }
24
25 bool aciclico()
26
      memset(pass, BRANCO, TAM*sizeof(int));
27
28
      for (int i = 0; i < TAM; i++)
29
30
31
         if (pass[i] == BRANCO)
32
            if (!dfs(i)) return false;
```

Código 19: Caminho minimo Dijkstra.

```
1 #include <queue>
3 typedef vector <map <int, int> > AdjList;
4 typedef AdjList Grafo;
6 int dist[MAX_VERTICES];
7 int prev[MAX_VERTICES]; // para recuperar o caminho usando um dijoint
       forest set
9 void dijkstra (Grafo& grafo, int source)
10 {
     for (int i = 0; i < grafo.size(); i++)
11
12
         dist[i] = INF;
13
         prev[i] = -1;
14
15
16
      dist[source] = 0;
17
      priority_queue < pair < int , int > > heap;
18
     heap.push(make_pair(0, source));
19
20
      while (!heap.empty())
21
22
         int u = heap.top().second;
23
         heap.pop();
24
25
         // para cada vizinho de u
26
         for (map<int,int>::iterator i = grafo[u].begin(); i != grafo[u].
27
             end(): i++)
28
            int totalDist = dist[u] + (*i).second;
29
            if (totalDist <= dist[(*i).first])</pre>
30
31
               dist[(*i).first] = totalDist;
32
               heap.push(make_pair(totalDist, (*i).first));
33
               prev[(*i).first] = u;
34
35
36
37
38
```

Código 20: Floresta dijunta de arvores

```
1 #define SIZE 100
2
3 struct dsf
4 {
```

```
int element_count;
       int parent[SIZE];
       int rank[SIZE];
9 typedef struct dsf * disjoint_set_forest_p;
10 typedef struct dsf disjoint_set_forest;
12 void dsf_init(disjoint_set_forest_p forest, int element_count)
13
      forest -> element_count = element_count;
14
      memset(forest -> parent, 0, element_count*sizeof(int));
15
      memset(forest -> rank, 0, element_count * size of (int));
17
      for (int i = 0; i < element\_count; ++i)
18
          forest -> parent [i] = i;
19
20 }
21
22 int dsf_find_set(disjoint_set_forest_p forest, int i)
23
24
       if (i != forest ->parent[i])
25
            forest -> parent [i] = dsf_find_set (forest, forest -> parent [i]);
26
27
       return forest -> parent [i];
28
29 }
30
  void dsf_union(disjoint_set_forest_p forest, int i, int j)
31
32
       int x = dsf_find_set(forest, i);
33
       int y = dsf_find_set(forest, j);
34
35
       if (forest ->rank[x] > forest ->rank[v])
36
37
            forest \rightarrow parent[y] = x;
38
39
       else
40
41
            forest \rightarrow parent[x] = y;
42
            if (forest \rightarrow rank[x] = forest \rightarrow rank[y])
43
44
45
                 forest \rightarrow rank[y]++;
46
47
48 }
```

Código 21: Arvore geradora mínima Kruskal

```
1 typedef vector < map < int , int > > AdjList;
2 struct Grafo
3 {
4    int edgeCnt;
5    AdjList adj;
6 };
7    s struct edge
8
```

```
10
      int u:
       int v;
11
       int weight;
^{12}
13 };
14
int edge_compare(const void * e1, const void * e2)
16 {
       struct edge * p1 = (struct edge *) e1;
17
       struct edge * p2 = (struct edge *) e2;
18
       int f = p1->weight - p2->weight;
19
      if (f < 0)
20
21
          return -1;
^{22}
23
       else if (f = 0)
24
25
           return edge_compare1 (e1, e2);
26
27
       else
28
29
           return 1;
30
31
32
33
34 struct edge * get_edge_list(Grafo& graph)
35 {
       int edge_count = graph.edgeCnt;
36
       struct edge *edges = (struct edge*) malloc(edge_count * sizeof(
37
           struct edge));
38
      int current_edge = 0;
39
40
       for (int i = 0; i < graph.adj.size(); ++i)
41
42
           for (map<int, int>::iterator j = graph.adj[i].begin(); j !=
43
               graph.adj[i].end(); j++)
44
               struct edge e;
45
               e.u = i < (*j).first ? i : (*j).first;
46
               e.v = i > (*j).first ? i : (*j).first;
47
48
               e.weight = (*j).second;
               edges[current\_edge++] = e;
49
50
51
52
53
       return edges;
54 }
55
56 void kruskal (Grafo& graph, Grafo& mst)
57 {
       // Obtain a list of edges and sort it by weight in O(E lg E) time
58
      int edge_count = graph.edgeCnt;
59
       struct edge *edges = get_edge_list(graph);
60
       qsort(edges, edge_count, sizeof(struct edge), edge_compare);
61
62
63
       disjoint_set_forest dsf;
```

```
64
      dsf_init(&dsf, edge_count);
65
       for (int i = 0; i < edge\_count; ++i)
66
67
           struct edge e = edges[i];
68
           int uset = dsf_find_set(\&dsf, e.u);
69
           int vset = dsf_find_set(\&dsf, e.v);
70
           if (uset != vset)
71
72
                mst.adj[e.u][e.v] = e.weight;
73
            mst.edgeCnt++;
74
                dsf_union(&dsf, uset, vset);
75
76
77
78
       free (edges);
79
80 }
```

Código 22: Verifica se um grafo é bipartido

```
1 #define TAM 200
з bool grafo [TAM] [TAM];
4 int pass [TAM];
5 int n:
7 bool bipartido (int v, int color = 1)
      pass[v] = color;
      int thisColor = color;
10
      bool ret = true;
11
12
      color = color == 1 ? 2 : 1:
13
14
      for (int i = 0; i < n; i++)
15
16
         if (grafo[v][i])
17
18
            if (!pass[i]) ret = bipartido(i, color);
19
            else if (pass[i] = thisColor) return false;
20
21
22
            if (!ret) return false;
23
24
25
26
      return ret;
27
```

Código 23: Ordenação topológica de um grafo acíclico

```
1 #define UNVISITED -1
2
3 int grafo[SIZE][SIZE];
4 int prof[SIZE];
5 int sorted[SIZE];
```

```
6 int nordem;
s void dfsTopsort(int no)
9 {
      for (int viz = 0; viz < SIZE; viz++)
10
11
         if (grafo[no][viz])
12
13
            if (prof[viz] == UNVISITED)
14
15
                prof[viz] = prof[no] + 1;
16
                dfsTopsort(viz);
17
18
19
20
^{21}
      sorted[nordem--] = no;
22
23
24
25 void topSort(int nvt)
26
     memset(prof, UNVISITED, nvt*sizeof(int));
27
     nordem = nvt - 1;
28
29
      for (int i = 0; i < nvt; i++)
30
31
         if (prof[i] == UNVISITED)
32
33
            prof[i] = 0;
34
            dfsTopsort(i);
35
36
37
38 }
```

Código 24: Ordenação topológica de um grafo acíclico

```
1 bool topologicalSort(vector< vector< int >> &g, vector< int > &r)
2 {
     vector < int > deg(g.size());
     FOREACH(node, g) {
         FOREACH(ngb, *node) {
            deg[*ngb]++;
6
     priority_queue< int, vector< int >, greater< int >> q;
10
     FORN(i, 0, g.size())
11
         \mathbf{if}(0 = \deg[i]) \neq \mathrm{push}(i);
12
13
      while (not q.empty()) {
14
         int node = q.top();
15
         q.pop();
16
         r.push_back(node);
17
18
         FOREACH(ngb, g[node]) {
            if(--deg[*ngb] == 0) q.push(*ngb);
19
20
```

```
21     }
22
23     return r.size() == g.size();
24 }
```

Código 25: Fluxo máximo, Ford-Fulkerson

```
1 #define TAM 1000
 2 #define MAX_INT 1000000
 4 int grafo [TAM] [TAM];
 5 int pred[TAM];
 6 int f [TAM] [TAM];
 7 bool visitados [TAM];
 s int fila [TAM];
   bool bfs (int n, int ini, int fim)
11
      int no. s = 0. e = 0:
12
       fila[e++] = ini;
13
14
       while (s != e)
15
16
          no = fila[s++];
17
18
          if (visitados [no] == 2) continue;
19
          visitados[no] = 2;
20
21
          for (int i = 0; i < n; i++)
22
23
              if (visitados[i] < 2)
24
25
26
                  \mathbf{if}(\operatorname{grafo}[\operatorname{no}][i] - \operatorname{f}[\operatorname{no}][i] > 0)
27
                     pred[i] = no;
28
                     if (i == fim) return true;
                     if (visitados [i] == 0)
30
31
                         fila[e++] = i;
32
                         visitados[i] = 1;
33
34
35
36
37
38
39
      return false;
40
41
42
   bool dfs(int s, int t, int size)
43
44
       visitados[s] = true;
^{45}
       if(s == t) return true;
46
47
      for (int v = 0; v < size; v++)
48
```

```
50
          if (! visitados[v] \&\& grafo[s][v] - f[s][v] > 0)
51
             pred[v] = s;
52
             if (dfs(v, t, size)) return true;
53
54
55
56
      return false;
57
58 }
59
60 bool findPath(int s, int t, int size)
61
      memset(visitados, false, sizeof(bool)*size);
62
      pred[s] = s;
63
      // Aqui pode ser usado tanto busca em larqura quanto em profundidade.
64
      // busca em largura geralmente apresenta tempos de execucao bem
65
           menores.
      return bfs(size, s, t);
66
       //return\ dfs(s, t, size);
67
68 }
69
70 int maxFlow(int size, int s, int t)
71
      int delta:
72
73
      for (int i = 0; i < size; i++)
74
75
          memset(f[i], 0, sizeof(int)*size);
76
77
78
      \mathbf{while}(1)
79
80
          bool path = findPath(s, t, size);
81
          if (!path) break;
82
83
          delta = MAX_{INT}:
84
          for(int c = t; pred[c] != c; c = pred[c])
85
86
             delta = min(delta, grafo[pred[c]][c] - f[pred[c]][c]);
87
88
89
          for(int c = t; pred[c] != c; c = pred[c])
90
91
             f[pred[c]][c] += delta;
92
             f[c][pred[c]] -= delta;
93
         }
94
95
96
      int soma = 0;
97
98
      for(int i = 0; i < size; i++)
99
100
         soma += f[i][t];
101
102
103
104
      return soma;
```

Código 26: Fluxo máximo (mais eficiente)

105 }

```
1 const int VT = 100;
2 const int AR = VT * VT:
4 struct grafo
     // lista de adjacencias representada na forma de vetor
     int nvt, nar;
     int dest[2 * AR];
     int adj [VT] [2 * VT];
10
     int nadj[VT];
11
     int cap[AR]; // capacidade do arco
12
     int fluxo [AR];
13
     int ent[VT];
14
15
     int padj [VT], lim [VT], nivel [VT], qtd [VT];
16
17
     int inv(int a) { return a ^ 0x1; }
18
     int orig(int a) { return dest[inv(a)]; }
19
     int capres(int a) { return cap[a] - fluxo[a]; }
20
21
     void inic (int n = 0)
22
23
        nvt = n;
24
25
        nar = 0;
        memset(nadj, 0, sizeof(nadj));
26
27
28
29
     // Adiciona uma aresta ao grafo.
30
31
     // "int u" apenas para Fluxos;
32
33
     int aresta (int i, int j, int u = 0)
34
35
        int ar = nar;
36
        cap[nar] = u;
37
        dest[nar] = i;
38
        adj[i][nadj[i]] = nar++;
39
        nadj[i]++;
40
41
        cap[nar] = 0;
42
        dest[nar] = i;
43
        adj[j][nadj[j]] = nar++;
44
        nadj[j]++;
45
46
        return ar;
47
48
     void revbfs(int ini, int fim)
49
50
        int i, no, viz, ar;
51
        queue < int > fila;
```

```
53
                                                                                       108
          memset(nivel, NULO, sizeof(nivel));
                                                                                                 return ((ent[no] = NULO) ? no : orig(ent[no]));
54
                                                                                       109
          memset(qtd, 0, sizeof(qtd));
55
                                                                                       110
56
                                                                                       111
          nivel[fim] = 0;
                                                                                             int avanca (int no, int ar)
57
                                                                                       112
          fila.push(fim);
58
                                                                                       113
                                                                                                 int viz = dest[ar];
59
                                                                                       114
          while (!fila.empty())
                                                                                                 ent[viz] = ar;
60
                                                                                       115
                                                                                                 \lim [viz] = \min(\lim [no], capres(ar));
61
                                                                                       116
             no = fila.front();
                                                                                                 return viz;
62
                                                                                       117
             fila.pop();
63
                                                                                       118
             qtd[nivel[no]]++;
64
                                                                                       119
                                                                                             int aumenta(int ini, int fim)
65
                                                                                       120
             for (i = 0; i < nadj[no]; i++)
66
                                                                                       121
                                                                                                 int ar, no = fim, fmax = lim [fim];
67
                                                                                       122
                ar = adj[no][i];
68
                                                                                       123
                viz = dest[ar];
                                                                                                 while (no != ini)
69
                                                                                       124
                                                                                       125
70
                if (cap[ar] = 0 \&\& nivel[viz] = NULO)
                                                                                                    fluxo[ar = ent[no]] += fmax;
71
                                                                                       126
                                                                                       127
                                                                                                    fluxo[inv(ar)] = fmax;
72
                    nivel[viz] = nivel[no] + 1;
                                                                                                    no = orig(ar);
73
                                                                                       128
                    fila.push(viz);
74
                                                                                       129
75
                                                                                       130
                                                                                                 return fmax;
76
                                                                                       131
77
                                                                                       132
78
                                                                                       133
                                                                                             int maxflow(int ini, int fim)
79
                                                                                       134
      int admissivel(int no)
80
                                                                                       135
                                                                                                 int ar, no = ini, fmax = 0;
81
                                                                                       136
          while (padj[no] < nadj[no])
82
                                                                                       137
                                                                                                 memset(fluxo, 0, sizeof(fluxo));
83
                                                                                       138
                                                                                                 memset(padj, 0, sizeof(padj));
             int ar = adj[no][padj[no]];
84
                                                                                       139
             if (nivel[no] = nivel[dest[ar]] + 1 && capres(ar) > 0) return
85
                                                                                       140
                                                                                                 revbfs(ini, fim);
                                                                                       141
             padj[no]++;
86
                                                                                       142
                                                                                                 \lim [ini] = INF;
87
                                                                                       143
                                                                                                 ent[ini] = NULO;
88
                                                                                       144
          padj[no] = 0;
89
                                                                                       145
                                                                                                 while (nivel[ini] < nvt && no != NULO)
          return NULO:
90
                                                                                       146
91
                                                                                       147
                                                                                                    if ((ar = admissivel(no)) == NULO)
92
                                                                                       148
       int retrocede (int no)
93
                                                                                       149
                                                                                                       no = retrocede(no);
94
                                                                                       150
          int i, ar, viz, menor = NULO;
95
                                                                                       151
                                                                                                    else if ((no = avanca(no, ar)) == fim)
96
                                                                                       152
          if (--qtd[nivel[no]] == 0) return NULO;
97
                                                                                       153
                                                                                                       fmax += aumenta(ini, fim);
98
                                                                                       154
          for (i = 0; i < nadj[no]; i++)
                                                                                                       no = ini;
99
                                                                                       155
                                                                                       156
100
             ar = adi[no][i]; viz = dest[ar];
101
                                                                                       157
             if (capres (ar) <= 0) continue;
                                                                                                 return fmax;
102
                                                                                       158
             if (menor == NULO | | nivel[viz] < nivel[menor]) menor = viz;
103
                                                                                       159
                                                                                       160 };
104
105
          if (menor != NULO) nivel[no] = nivel[menor];
106
```

qtd[++nivel[no]]++;

Código 27: Ponto e poligono

```
1 struct point
     double x, y;
     double z; // para pontos no espaco
     point (double x = 0, double y = 0, double z = 0): x(x), y(y), z(z) {}
     point operator +(point q) { return point (x + q.x, y + q.y, z + q.z);
7
     point operator -(point q) { return point (x - q.x, y - q.y, z - q.z);
     point operator *(double t) { return point(x * t, y * t, z * t); }
     point operator /(double t) { return point(x / t, y / t, z / t); }
10
     double operator *(point q) { return x * q.x + y * q.y + z * q.z; }
11
     point vec(point q) { return point(y * q.z - z * q.y, z * q.x - x * q.y)
12
         z, x * q.y - y * q.x); }
     double operator \%(point q) { return x * q.y - y * q.x; }
13
14
     int cmp(point q) const
15
16
        if (int t = ::cmp(x, q.x)) return t;
17
        else if (int t = ::cmp(y, q.y)) return t;
18
        return :: cmp(z, q.z);
19
20
^{21}
     bool operator ==(point q) const { return cmp(q) == 0; }
22
     bool operator !=(point q) const { return cmp(q) != 0; }
23
     bool operator < (point q) const \{ return cmp(q) < 0; \}
24
25
     friend ostream& operator <<(ostream& o, point p) {
26
       return o << "(" << p.x << ", " << p.y << ", " << p.z << ")";
27
28
     static point pivot;
29
30
31
     para pontos 2D
33 double abs(point p) { return hypot(p.x, p.y); }
34 double arg(point p) { return atan2(p.y, p.x); }
35
36 point point :: pivot;
37
38 typedef vector<point> polygon;
40 int ccw(point p, point q, point r)
41 {
     return cmp((p - r) \% (q - r));
42
43 }
45 double angle (point p, point q, point r)
     point u = p - q, v = r - q;
     return atan2(u \% v, u * v);
49 }
```

```
1 bool between(point p, point q, point r)
2 {
3    return ccw(p, q, r) == 0 && cmp((p - q) * (r - q)) <= 0;
4 }</pre>
```

Código 29: Decide se os segmentos fechados pq e rs têm pontos em comum.

```
1 bool seg_intersect(point p, point q, point r, point s)
2 {
     point A = q - p;
     point B = s - r;
     point C = r - p;
     point D = s - q;
     int a = cmp(A \% C) + 2 * cmp(A \% D);
     int b = cmp(B % C) + 2 * cmp(B % D);
10
      if (a = 3 \mid | a = -3 \mid | b = 3 \mid | b = -3) return false;
11
      if (a || b || p == r || p == s || q == r || q == s) return true;
12
13
     int t = (p < r) + (p < s) + (q < r) + (q < s);
14
     return t != 0 && t != 4:
15
16 }
```

Código 30: Calcula a distância do ponto r ao segmento pq.

```
1 double seg_distance(point p, point q, point r)
2 {
3     point A = r - q;
4     point B = r - p;
5     point C = q - p;
6     double a = A * A, b = B * B, c = C * C;
8     if (cmp(b, a + c) >= 0) return sqrt(a);
10     else if (cmp(a, b + c) >= 0) return sqrt(b);
11     else return fabs(A % B) / sqrt(c);
12 }
```

Código 31: Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 dependendo se p está no exterior, na fronteira ou no interior de T, respectivamente.

```
int in_poly(point p, polygon& T)

2 {
3     double a = 0;
4     int N = T.size();
5     for (int i = 0; i < N; i++)
6     {
7         if (between(T[i], p, T[(i+1) % N])) return -1;
8         a += angle(T[i], p, T[(i+1) % N]);
9     }
10     return cmp(a) != 0;</pre>
```

Código 32: Convex Hull **graham scan**.

```
1 #define INF 1e9
2 #define EPS 1e-9
3
4 int cmp(double a, double b = 0.0) {
     return a+EPS < b ? -1 : a-EPS > b;
6 }
7
s struct Point {
     double x, v;
     Point (double a=0.0, double b=0.0) {x=a, v=b;}
10
     Point operator+(const Point &P) const {return Point(x+P.x,v+P.v);}
11
     Point operator - (const Point &P) const {return Point (x-P.x,y-P.y);}
12
     Point operator*(double c) const {return Point(x*c,y*c);}
13
     Point operator/(double c) const {return Point(x/c,y/c);}
14
     double operator!() const {return sqrt(x*x+y*y);}
15
     bool operator == (const Point &p) const {return !cmp(x,p.x) && !cmp(y,p
16
     bool operator < (const Point &p) const {if (cmp(x,p.x)) return cmp(x,p.x)
17
         (x) < 0; return cmp(v,p.v) < 0;
     void print (string prefix = "") const {printf("%s%.3lf %.3lf\n", prefix
18
          .c_str(),x,y);
19 };
20
21 typedef vector < Point > Polygon;
22
23 double cross (Point A, Point B) {
     return A.x*B.y - B.x*A.y;
^{24}
25 }
26
27 Point pmin;
28
  bool lessThan (Point A, Point B) {
29
      if (cmp(cross(A-pmin,B-pmin))) return cmp(cross(A-pmin,B-pmin)) > 0;
30
     return cmp(!(pmin-A),!(pmin-B)) < 0;
31
32
33
34 int sort (Polygon &p) {
     int imin = 0, i, j, n = p.size();
35
36
     for (i=1; i < p.size(); i++) {
37
         if (p[i] < p[imin]) imin = i;
38
39
40
     swap(p[0], p[imin]);
41
     pmin = p[0];
42
43
     sort(p.begin()+1,p.end(),lessThan);
44
45
     for (i=n-1; i > 0 & (ross(p[i]-p[0], p[i-1]-p[0])); i--);
46
47
     if (i = 0) return 1:
     for (j=0; j < (n-i)/2; j++) swap(p[i+j], p[n-j-1]);
48
49
     return 0:
```

```
50 }
51
52 Polygon convex_hull(Polygon &p) { // tirar o & para nao alterar o
       poliaono oriainal
      int hs = 2, n = p.size();
      Polygon hull;
54
55
      if (p.size() < 3) return p;
56
57
      int isline = sort(p);
58
      hull.push_back(p[0]), hull.push_back(p[1]);
59
60
      for (int i=2; i \le n-isline; i++) {
61
         while (hull.size) > 1 \&\& cmp(cross(p[i\%n]-hull[hs-1],hull[hs-2]-
62
             [hull[hs-1]] = 0 \{ // trocar o \leq para \leq para manter pontos \}
             intermediarios
            hull.pop_back(), hs--;
63
64
         if (i < n) hull.push_back(p[i]), hs++;
65
67
68
      return hull:
69 }
70
71 int main() {
72
      Polygon p;
73
      while (...) {
74
         double x = \dots;
75
         double y = \dots;
76
         p.push_back(Point(x,y));
77
78
79
      Polygon hull = convex_hull(p);
80
81
      for (int i=0; i < hull.size(); i++) {
82
83
84
85
      return 0;
86 }
```

1.8 Algebra Linear

Código 33: Simplex

```
1 #include <iostream>
2 #include <vector>
3 #include <algorithm>
4
5 using namespace std;
6
7 #define fori(i,n) for(int i=0; i < (n); ++i)
8 #define forr(i,a,b) for(int i=(a); i <= (b); ++i)
9 #define ford(i,a,b) for(int i=(a); i >= (b); --i)
```

```
10 #define sz size()
13
14 #define all(x) (x).begin(),(x).end()
15
int cmpD(double x, double y=0, double tol=EPS) {
     return (x \le y+tol)? (x+tol \le y)? -1: 0: 1;
17
18 }
19
20 struct simplex {
     // \max c * x, s.t: A * x <= b; x >= 0
     simplex (const vector < vector < double > > & A., const vector < double
         > \& b_{-},
           const vector < double > \& c_-) : A(A<sub>-</sub>), b(b<sub>-</sub>), c(c<sub>-</sub>) \{\}
23
     vector< vector< double > > A; vector< double > b, c, sol;
^{24}
     vector< bool > N; vector< int > kt; int m, n;
25
     void pivot( int k, int l, int e ) {
26
        int x = kt[l]; double p = A[l][e];
27
        fori(i,k) A[l][i] \neq p;
28
        b[l] /= p; N[e] = false;
29
        fori(i,m) if (i != 1) \{b[i] -= A[i][e]*b[1]; A[i][x] = -A[i][e]*A[i][x]
30
            1 ] [x]; }
        fori(j,k) if (N[j])
31
           c[j] -= c[e] * A[l][j];
32
           fori(i,m) if ( i != l ) A[i][j] == A[i][e] * A[l][j];
33
34
        kt[1] = e; N[x] = true; c[x] = -c[e] * A[1][x];
35
36
     vector < double > go( int k ) {
37
        vector< double > res;
38
        while (1) {
39
           int e = -1, l = -1;
           fori(i,k) if (N[i] \&\& cmpD(c[i]) > 0) { e = i; break; }
41
           if (e = -1) break:
^{42}
           for i(i,m) if (cmpD(A[i][e]) > 0 && (l = -1 || cmpD(b[i] / A)
43
                | i | e | ,
                        b[1] / A[1][e], 1e-20 ) < 0 ) ] 1 = i;
44
           if (l = -1) return vector< double >(); // unbounded
45
           pivot(k, l, e);
46
47
        res.resize(k, 0);
48
        fori(i,m) res[kt[i]] = b[i];
49
        return res:
50
51
     vector < double > solve() {
52
        m = A.sz; n = A[0].sz; int k = m+n+1;
53
        N = vector < bool > (k, true); vector < double > c_copy = c;
54
        c.resize(n+m); kt.resize(m);
55
        fori(i,m) {
56
           A[i]. resize(k); A[i][n+i] = 1; A[i][k-1] = -1;
57
           kt[i] = n+i; N[kt[i]] = false;
58
59
        int l = min_element(all(b)) - b.begin();
60
        if(cmpD(b[1]) < 0)
61
           c = vector < double > (k, 0);
62
```

```
63
             c[k-1] = -1; pivot(k, 1, k-1); sol=go(k);
             if (\text{cmpD}(\text{sol}[k-1])>0) return vector<double>(); // infeasible
64
             fori(i,m) if(kt[i] = k-1) {
65
                fori(j,k-1) if(N[j] && cmpD(A[i][j]) != 0) {
                    pivot(k, i, j); break;
67
68
             c=c\_copy; c.resize(k,0);
             fori(i,m) fori(j,k) if(N[j]) c[j] = c[kt[i]]*A[i][j];
71
72
          sol = go(k-1);
73
          if (!sol.empty()) sol.resize(n);
74
          return sol:
75
76
77 };
78
79 // Como usar
80 int main() {
      /* Exemplo: Maximize cx Subject to Ax \le b */
      vector < vector < double > A(9);
      double Av[][3] = {{1,1,0}, {0,0,-1}, {-1,-1,0},
                       \{0,0,1\}, \{1,0,0\}, \{0,1,0\},
84
                       \{0,0,1\}, \{1,0,1\}, \{0,1,0\}\};
85
86
      for (int i=0; i < 9; i++) {
87
         A[i].insert(A[i].begin(), &(Av[i][0]), &(Av[i][3])); // Sim, [3]!
88
              Ou seja, idx-final+1
89
      vector <double > c(3, 1); // c = [1 \ 1 \ 1]
91
      double by [] = \{2, -1, -2, 1, 2, 1, 1, 2, 1\};
92
      vector < double > b(bv, bv+sizeof(bv)/sizeof(double));
93
      simplex sim(A,b,c);
      vector < double > s = sim.solve();
      if (!s.size()) cout << "Impossivel\n";</pre>
97
98
      for (int i=0; i < s. size(); i++) {
99
          cout \ll s[i] \ll endl;
100
101
102 }
```

1.9 Casamento de strings

Código 34: String matching - Algoritmo \mathbf{KMP} - $\mathbf{O}(n+m)$

```
F[0] = -1;
     for (int i = 0; i < m; i++)
10
        F[i+1] = F[i] + 1;
11
         while (F[i+1] > 0 \&\& pattern[i] != pattern[F[i+1]-1])
^{12}
           F[i+1] = F[F[i+1]-1] + 1;
13
14
15
16
     retorna a posicao inicial de cada ocorrencia de pattern em text
17 //
     ctor < int > KMP( const string & text, const string & pattern )
18
19
     build_failure_function( pattern );
20
     vector < int > start_positions;
21
     int i = 0, m = pattern.size(), n = text.size();
22
23
     for (int i = 0; i < n; i++)
24
25
         while (true)
26
27
            if ( text[i] == pattern[j] )
28
29
               if (++j = m)
30
31
                  start_positions.push_back(i-m+1);
32
                  j = F[j];
33
34
35
               break;
36
37
            if (j = 0) break;
38
           j = F[j];
39
41
42
     return start_positions;
43
44 }
```

Outros 1.10

Código 35: Encontra o elemento mais comum no vetor.

```
int findMajority(int vec[], int n)
2 {
     int cnt = 0;
     int major:
     for (int i = 0; i < n; i++)
6
        if (cnt == 0) {maior = v; cnt = 1;}
        else if (v = maior) cnt++;
        else cnt --:
10
11
12
     return maior;
```

13 }

Código 36: Josephus problem

```
1 /**
2 The Josephus problem (or Josephus permutation) is a theoretical problem
      related to a certain counting-out game. There are people standing in
      a circle waiting to be executed. After the first man is executed,
      certain number of people are skipped and one man is executed. Then
      again, people are skipped and a man is executed. The elimination
      proceeds around the circle (which is becoming smaller and smaller as
      the executed people are removed), until only the last man remains,
      who is given freedom. The task is to choose the place in the initial
      circle so that you are the last one remaining and so survive.
3 */
5 using namespace std:
7 int josephus (int n, int m)
8 {
     int res = 0;
      vector <int> people;
     int loc = 0;
11
12
13
      for (int i = 0; i < n; i++) people.push_back(i+1);
14
     while (people.size() > 1)
15
16
         if (loc >= people.size())
17
            loc %= people.size();
18
19
         people.erase(people.begin()+loc);
20
         loc += (m-1):
21
22
23
     return people [0];
^{24}
25 }
```

Código 37: Gera as permutações dos elementos da string

```
1 bool nextPermutation(string& number)
   2 {
             bool is Bigger = true;
             int i, j;
             for (i = number. size() - 1; i >= 0; i--)
                      if (number[i] < number[i+1]) break;</pre>
   10
             if (i != -1)
   11
   12
   13
                      isBigger = false:
   14
                      for (j = number. size() - 1; j >= i+1; j--)
16
```

```
16
                              if (number[j] > number[i])
17
18
                                       break;
19
20
21
22
                    int tmp = number[i];
23
                    number [i] = number [j];
24
                    number[j] = tmp;
25
26
                    j = number.size() -1;
27
                    i++;
28
29
                    \mathbf{while} \ (i < j)
30
31
                             tmp = number [i];
32
                             number[i] = number[j];
33
                             number[j] = tmp;
34
35
                              i++;
                             j --;
36
37
38
39
           return is Bigger;
41 }
```

Código 38: Permutações dos elementos da string, usando backtracking

```
1 #define TAM 10
2 int cnt = 0;
3 int total; //numero de elementos de elem
4 int elem [TAM];
5 bool usados [TAM]; //ZERE ME
7 void enumera(int num)
8 {
      if (num == total)
10
11
         for (int i = 0; i < total; i++) cout << elem[i];
12
         cout << endl;
13
         return;
15
16
      for (int i = 0; i < total; i++)
17
18
         if (!usados[i])
19
20
            elem[num] = i;
^{21}
            usados[i] = true;
            enumera (num + 1);
23
            usados[i] = false;
^{24}
25
26
27 }
```

Complexidade	Tamanho máximo da entrada
1	α
log(n)	10^{9}
n	10^{6}
n * log(n)	10^{4}
n^2	10^{3}
$n^{2*} log(n)$	10^{3}
n^3	10^{2}
2^n	20
n!	10

Tabela 1: Complexidade máxima da solução em fução do tamanho da entrada

2 Tabelas

tipo	bits	minmax	precisao
char	8	0127	2
signed char	8	-128127	2
unsigned char	8	0255	2
short	16	-32.768 32.767	4
unsigned short	16	0 65.535	4
int	32	-2x10**9 2 x 10**9	9
unsigned int	32	0 4x10**9	9
$int64_t$	64	-9 x 10**18 9 x 10**18	18
$uint64_t$	64	0 18 x 10**18	19

Tabela 2: Limites de representação de dados

```
%
Tipo
char
            \mathbf{c}
int
            d
                                                                                          função
                                                                                                   descrição
float
            e, E, f, g, G
                                                                                          atof
                                                                                                   Convert string to double
                                                                                                    Convert string to integer
int (octal)
            O
                                                                                          atoi
                                                                                                   Convert string to long integer
            x, X
int (hexa)
                                                                                          atol
                                                                                                   Convert string to double
uint
            u
                                                                                          strtod
char*
            \mathbf{S}
                                                                                          strtol
                                                                                                   Convert string to long integer
                                                                                                   Convert string to unsigned long integer
                                                                                          strtoul
                    Tabela 3: scanf() - %[*][width][modifiers]type
                                                                                                                             Tabela 6: stdlib
modifiers
           tipo
           short int (d, i, n), or unsigned short int (o, u, x)
           long int (d, i, n), or unsigned long int (o, u, x), or double (e, f, g)
           long long int (d, i, n), or unsigned long long int (o, u, x)
11
L
           long double (e, f, g)
                                                                                          função
                                                                                                   descrição
                    Tabela 4: scanf() %[*][width][modifiers]type
                                                                                                   Compute cosine
                                                                                          \cos
                                                                                                   Compute sine
                                                                                          \sin
                                                                                                   Compute tangent
                                                                                          \tan
                                                                                                   Compute arc cosine
                                                                                           acos
0! = 1
                                                                                          asin
                                                                                                   Compute arc sine
1! = 1
                                                                                                   Compute arc tangent
                                                                                          atan
2! = 2
                                                                                                   Compute arc tangent with two parameters
                                                                                          atan2
3! = 6
                                                                                                   Compute hyperbolic cosine
                                                                                          \cosh
4! = 24
                                                                                                   Compute hyperbolic sine
                                                                                          \sinh
5! = 120
                                                                                                   Compute hyperbolic tangent
                                                                                          tanh
6! = 720
                                                                                                   Compute exponential function
                                                                                          exp
7! = 5.040
                                                                                                   Get significand and exponent
                                                                                          frexp
8! = 40.320
                                                                                                   Generate number from significand and exponent
                                                                                          ldexp
9! = 362.880
                                                                                                   Compute natural logarithm
                                                                                          log
10! = 3.628.800
                                                                                          log10
                                                                                                   Compute common logarithm
11! = 39.916.800
                                                                                          modf
                                                                                                   Break into fractional and integral parts
12! = 479.001.600 [limite do (unsigned) int]
                                                                                                   Raise to power
                                                                                          pow
13! = 6.227.020.800
                                                                                                   Compute square root
                                                                                          sqrt
14! = 87.178.291.200
                                                                                                   Round up value
                                                                                          ceil
15! = 1.307.674.368.000
                                                                                          fabs
                                                                                                   Compute absolute value
16! = 20.922.789.888.000
                                                                                          floor
                                                                                                   Round down value
17! = 355.687.428.096.000
                                                                                                   Compute remainder of division
                                                                                          fmod
18! = 6.402.373.705.728.000
19! = 121.645.100.408.832.000
                                                                                                                  Tabela 7: math (angulos em radianos)
20! = 2.432.902.008.176.640.000 [limite do (u)int64_t]
```

Tabela 5: Fatorial