Sumário									
1	Tab	elas	2						
${f L}_{f j}$	2.1 2.2 2.3 2.4 2.5		3 8 8 11 12						
L i	1 2 3 4 5 6	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2 2 2 2 2 3						
	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22	Modelo comparcao de ponto flutuante .vimrc para a configuração do vim printf exemplo de map exemplo de set e multset exemplo de list exemplo de queue exemplo de priority queue exemplo de stack exemplo de stack exemplo de vector exemplo de ordenação pesquisa binária Arredondamento e output em outras bases máximo divisor comum e mínimo multiplo comum decide se um número é primo Retorna a fatoração em números primos de abs(n). Verifica se o grafo é aciclico. Caminho minimo 1 para todos pesos positivos. Floresta dijunta de arvores Arvore geradora mínima kruskal	3 3 4 4 4 4 5 5 5 5 6 6 7 7 7 8 8 8 8 9 9 9						

23	verifica se um grafo é bipartido	10
24	faz a ordenação topológica de um grafo acíclico	10
25	calcula fluxo máximo	11
26	ponto e poligono	11
27	Decide se q está sobre o segmento fechado pr	12
28	Decide se os segmentos fechados pq e rs têm pontos em comum	12
29	Calcula a distância do ponto r ao segmento pq	12
30	Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 depen-	
	dendo se p está no exterior, na fronteira ou no interior de T, respectivamente.	12
31	josephus problem	12

1 Tabelas

tipo	bits	minmax	precisao
char	8	0127	2
signed char	8	-128127	2
unsigned char	8	0255	2
short	16	-32.768 32.767	4
unsigned short	16	$0 \dots 65.535$	4
int	32	-2x10**9 2 x 10**9	9
unsigned int	32	0 4x10**9	9
$int64_t$	64	-9 x 10**18 9 x 10**18	18
$\mathrm{uint}64_\mathrm{t}$	64	0 18 x 10**18	19

Tabela 1: Limites de representação de dados

```
0! = 1
1! = 1
2! = 2
3! = 6
4! = 24
5! = 120
6! = 720
7! = 5.040
8! = 40.320
9! = 362.880
10! = 3.628.800
11! = 39.916.800
12! = 479.001.600 [limite do (unsigned) int]
13! = 6.227.020.800
14! = 87.178.291.200
15! = 1.307.674.368.000
16! = 20.922.789.888.000
17! = 355.687.428.096.000
18! = 6.402.373.705.728.000
19! = 121.645.100.408.832.000
20! = 2.432.902.008.176.640.000 [limite do (u)int64_t]
```

Tabela 2: Fatorial

```
\begin{array}{lll} \mbox{Tipo} & \% \\ \mbox{char} & c \\ \mbox{int} & d \\ \mbox{float} & e, E, f, g, G \\ \mbox{int (octal)} & o \\ \mbox{int (hexa)} & x, X \\ \mbox{uint} & u \\ \mbox{char*} & s \end{array}
```

Tabela 3: scanf() - %[*][width][modifiers]type

```
modifiers tipo
h short int (d, i, n), or unsigned short int (o, u, x)
l long int (d, i, n), or unsigned long int (o, u, x), or double (e, f, g)
L long double (e, f, g)
```

Tabela 4: scanf() %[*][width][modifiers]type

```
função descrição
atof Convert string to double
atoi Convert string to integer
atol Convert string to long integer
strtod Convert string to double
strtol Convert string to long integer
strtoul Convert string to unsigned long integer
```

Tabela 5: stdlib

```
Compute cosine
\cos
        Compute sine
\sin
        Compute tangent
\tan
        Compute arc cosine
acos
        Compute arc sine
asin
        Compute arc tangent
atan
        Compute arc tangent with two parameters
atan2
        Compute hyperbolic cosine
\cosh
        Compute hyperbolic sine
\sinh
        Compute hyperbolic tangent
tanh
        Compute exponential function
exp
        Get significand and exponent
frexp
        Generate number from significand and exponent
ldexp
        Compute natural logarithm
\log
        Compute common logarithm
log10
        Break into fractional and integral parts
modf
        Raise to power
pow
sqrt
        Compute square root
        Round up value
ceil
fabs
        Compute absolute value
        Round down value
floor
        Compute remainder of division
fmod
```

função

descrição

Tabela 6: math (angulos em radianos)

2 Codigos

2.1 Exemplos

```
#include <stdio.h>
   #include <stdlib.h>
   #include <string.h>
   #include <math.h>
   #include <inttypes.h>
   #include <ctype.h>
   #include <algorithm>
   #include <utility>
   #include <iostream>
11
12
   #include <map>
   #include <set>
   #include <vector>
   #include <sstream>
17
    using namespace std;
18
19
   #define abs(a) ((a) > 0 ? (a) : -(a))
20
21
   int main()
22
23
24
      int n:
25
26
       cin >> n;
27
28
       for (int i = 0; i < n; i++)
29
30
31
32
       while (cin \gg n)
33
34
35
36
       return 0;
37
38
```

Código 1: Modelo

```
const double EPS = 1e-10;

/**

* * -1 se x < y

* * 0 se x = y

* * 1 se x > y

* inline int cmp (double x, double y = 0, double tol = EPS)

* {

* return (x <= y + tol) ? (x + tol < y) ? -1 : 0 : 1;

* 3}</pre>
```

```
17
                                                                                   18
                                                                                           cout << "element 'z' already existed";</pre>
                         Código 2: comparcao de ponto flutuante
                                                                                           cout << " with a value of " << ret.first ->second << endl;</pre>
                                                                                   19
                                                                                   20
                                                                                   21
   set ai noet ts=4 sw=4 bs=2
                                                                                         // third insert function version (range insertion):
                                                                                   22
                                                                                         map<char, int> anothermap;
                                                                                   23
   mat Keyword "\<foreach\>"
                                                                                         anothermap.insert(mymap.begin(),mymap.find('c'));
                                                                                   24
                                                                                   25
                       Código 3: .vimrc para a configuração do vim
                                                                                         // showing contents:
                                                                                   26
                                                                                         cout << "mymap contains:\n";</pre>
                                                                                   27
                                                                                         for ( it=mymap.begin(); it != mymap.end(); it++ )
   /* printf example */
                                                                                   28
                                                                                           cout << (*it).first << " => " << (*it).second << endl;
   #include <stdio.h>
                                                                                   29
                                                                                   30
                                                                                         map<char.string> mymap:
   int main()
                                                                                   31
                                                                                         mymap['a']="an element";
                                                                                   32
                                                                                         if (mymap.count('a') > 0)
       printf ("Characters: %c %c \n", 'a', 65);
                                                                                   33
       printf ("Decimals: %d %ld\n", 1977, 650000L);
                                                                                   34
                                                                                             cout << mymap['a'] << " is an element of mymap.\n";
       printf ("Preceding with blanks: %10d \n", 1977);
                                                                                   35
       printf ("Preceding with zeros: %010d \n", 1977);
                                                                                         while (!mymap.empty())
       printf ("Some different radixes: %d %x %o %#x %#o \n", 100, 100, 100,
                                                                                            cout << mymap.begin()->first << " => ";
          100, 100):
                                                                                            cout << mymap.begin()->second << endl;</pre>
       printf ("floats: %4.2f %+.0e %E %4.2f\n", 3.1416, 3.1416, 3.1416, 3.1); 39
       printf ("Width trick: %*d \n", 5, 10);
                                                                                            map<char, int>::iterator erasedelement = mymap.erase(mymap.begin());
                                                                                   40
13
       printf ("%s \n", "A string");
                                                                                   41
                                                                                   42
      return 0:
14
                                                                                         return 0;
                                                                                   43
   /* %[flags (-, +, etc)]/width]/.precision]/length (h,l,L)]specifier
                                                                                   44
   Characters: a A
                                                                                                                   Código 5: exemplo de map
   Decimals: 1977 650000
   Preceding with blanks:
                                  1977
   Preceding with zeros: 0000001977
                                                                                    1 #include <iostream>
   Some different radixes: 100 64 144 0x64 0144
                                                                                    2 #include <set>
   floats: 3.14 +3e+000 3.141600E+000 3.10
                                                                                       using namespace std;
   Width trick: 10
A string
                                                                                       int main ()
   */
                                    Código 4: printf
                                                                                         multiset < int > mvmultiset:
                                                                                         multiset < int > :: iterator it;
   #include <iostream>
                                                                                         // set some initial values:
                                                                                   10
   #include <map>
                                                                                         for (int i=1; i <=5; i++) mymultiset.insert(i*10); // 10 20 30 40 50
                                                                                   11
   using namespace std;
                                                                                   12
                                                                                         cout << "size: " << (int) mymultiset.size() << endl;</pre>
                                                                                   13
                                                                                         cout << "count: " << (int) mymultiset.count(10) << endl;</pre>
   int main ()
                                                                                   14
                                                                                   1.5
     map<char, int> mymap;
                                                                                         it=mymultiset.find(20);
                                                                                   16
     map<char, int>::iterator it;
                                                                                         mymultiset.erase (it);
                                                                                   17
     pair < map < char . int > :: iterator . bool > ret :
                                                                                   18
                                                                                         if (! mymultiset.empty)
10
                                                                                   19
     // first insert function version (single parameter):
                                                                                          mymultiset.erase (mymultiset.find(40));
11
                                                                                   20
     mymap.insert ( pair < char, int > ('a', 100));
^{12}
                                                                                   21
     mymap.insert (pair < char, int > ('z', 200));
                                                                                         for (it=mymultiset.begin(); it!=mymultiset.end(); it++)
                                                                                   22
13
                                                                                           cout << " " << *it:
14
                                                                                   23
      ret=mymap.insert (pair < char, int > ('z', 500));
                                                                                   24
     if (ret.second=false)
                                                                                   25
                                                                                         int myints [] = \{19,72,4,36,20,20\};
```

```
26
      multiset <int> first (myints, myints+3);
                                                     // 4,19,72
      multiset <int> second (myints+3, myints+6); // 20,20,36
                                                                                            queue<int> myqueue;
27
                                                                                            int sum (0);
28
      first.swap(second); // troca conteudo. o primeiro fica [20,20,36] e o
29
          segundo [4,19,72]
                                                                                      10
                                                                                            for (int i=1; i \le 10; i++) myqueue.push(i);
30
                                                                                      11
     return 0;
                                                                                            myqueue.back() -= myqueue.front();
31
                                                                                      12
32
                                                                                      13
                                                                                      14
                                                                                            cout << "size: " << (int) myqueue.size() << endl;</pre>
                            Código 6: exemplo de set e multset
                                                                                      15
                                                                                            while (!myqueue.empty())
                                                                                      16
                                                                                      17
   #include <iostream>
                                                                                               sum += myqueue.front();
                                                                                      18
   #include <list >
                                                                                               myqueue.pop();
                                                                                      19
   using namespace std;
                                                                                      20
                                                                                      21
   int main ()
                                                                                            cout << "total: " << sum << endl;
                                                                                      22
                                                                                      23
      list \langle int \rangle mylist (2.100):
                                           // two ints with a value of 100
                                                                                            return 0;
                                                                                      24
      mylist.push_front (200);
                                                                                      25
      mylist.push_back (300);
                                                                                                                      Código 8: exemplo de queue
11
      it = mylist.begin();
      mylist.insert (it,10);
12
      mylist.insert (it,2,20); // two ints with a value of 20
                                                                                       1 #include <iostream>
13
                                                                                         #include <queue>
      mylist.reverse(); // Reverses the order of the elements in the list.
                                                                                          using namespace std;
15
16
      cout << "mylist contains:";</pre>
                                                                                         int main ()
17
      for (list <int>::iterator it=mylist.begin(); it!=mylist.end(); ++it)
18
       cout << " " << *it;
                                                                                            priority_queue <int> mypq;
19
20
      cout << "Popping out the elements in mylist:";</pre>
                                                                                            mypq.push(30);
21
      while (!mylist.empty())
                                                                                            mypg.push(100);
22
                                                                                      10
                                                                                            mypq.push(25);
23
                                                                                      11
       cout << " " << mylist.front();
                                                                                            mypq.push(40);
24
                                                                                      12
        mylist.pop_front();
                                                                                      13
25
                                                                                            cout << "size: " << (int) mypq.size() << endl;</pre>
26
                                                                                      14
27
                                                                                      15
28
      while (! mylist.empty())
                                                                                      16
                                                                                            cout << "Popping out elements...";</pre>
                                                                                            while (!mypq.empty())
                                                                                      17
29
       cout << " " << mylist.back();
30
                                                                                      18
        mylist.pop_back();
                                                                                               cout << " " << mypq.top();
31
                                                                                      19
                                                                                               mypq.pop();
32
                                                                                      20
33
                                                                                      21
      cout << mylist.size() << endl;</pre>
                                                                                            cout << endl;
34
                                                                                      22
                                                                                      23
35
     return 0;
                                                                                            return 0;
36
                                                                                      24
37
                                                                                      25
                                                                                                                  Código 9: exemplo de priority queue
```

Código 7: exemplo de list

```
#include <iostream>
                                                                             1 #include <iostream>
  #include <queue>
                                                                             2 #include <stack>
  using namespace std;
                                                                                using namespace std;
                                                                             5 int main ()
5 int main ()
```

```
stack<int> mystack;
     int sum = 0;
      mystack.push(10);
10
      mystack.push(20);
11
     mvstack.top() = 5;
13
14
      while (!mystack.empty())
15
16
         sum += mystack.top();
17
         mystack.pop();
18
19
20
     cout << "size: " << (int) mystack.size() << endl;</pre>
^{21}
22
23
     return 0:
24
                                Código 10: exemplo de stack
```

```
#include <iostream>
   #include <vector>
   using namespace std;
   int main ()
5
6
     vector < int > mvvector (3,100);
     vector < int > :: iterator it;
     mvvector.reserve(100):
10
11
     for (i=0; i < mvvector.size(); i++)
12
13
       myvector.at(i)=i; // = myvector[i] = i
14
      it = mvvector.begin();
15
      it = myvector.insert ( it , 200 );
     myvector.insert (it,2,300);
17
18
      vector < int > another vector (2.400):
19
      int myarray [] = \{ 501,502,503 \};
20
     myvector.insert (it+2, anothervector.begin(), anothervector.end());
21
     myvector.insert (myvector.begin(), myarray, myarray+3);
^{22}
23
      cout << "myvector contains:";</pre>
24
      for (it=myvector.begin(); it < myvector.end(); it++)</pre>
25
       cout << " " << *it;
26
     cout << endl:
27
28
     // erase the 6th element
29
     myvector.erase (myvector.begin()+5);
30
31
32
     while (!myvector.empty())
33
         sum += myvector.back();
```

```
35
          myvector.pop_back();
36
37
      return 0:
38
39
```

14

15

16

19

22 23

27

28

34

36

38

Código 11: exemplo de vector

```
#include <iostream>
   #include <string>
   using namespace std;
   int main ()
      string str ("There are two needles in this haystack with needles.");
     string str2 ("needle");
     size_t found:
10
     // different member versions of find in the same order as above:
     found=str.find(str2);
12
     if (found!=string::npos)
13
       cout << "first 'needle' found at: " << int(found) << endl;</pre>
     found=str.find("needles are small", found+1,6);
      if (found!=string::npos)
17
       cout << "second 'needle' found at: " << int(found) << endl;</pre>
18
     found=str.find("haystack");
20
     if (found!=string::npos)
21
       cout << "'haystack' also found at: " << int(found) << endl;</pre>
     found=str.find(','):
24
      if (found!=string::npos)
       cout << "Period found at: " << int(found) << endl;</pre>
     // let's replace the first needle:
     str.replace(str.find(str2), str2.length(), "preposition");
29
     cout << str << endl;
30
31
      string str="We think in generalities, but we live in details.";
32
                                  // quoting Alfred N. Whitehead
33
     string str2, str3;
      size_t pos;
35
      str2 = str.substr (12,12); // "generalities"
37
     pos = str.find("live"); // position of "live" in str
39
      str3 = str.substr (pos); // get from "live" to the end
40
     cout \ll str2 \ll ' ' \ll str3 \ll endl;
42
43
44
45
     return 0:
46
48 first 'needle' found at: 14
```

```
second 'needle' found at: 44
    'haystack' also found at: 30
                                                                                                               Código 13: exemplo de ordenação
   Period found at: 51
   There are two prepositions in this haustack with needles.
   generalities live in details.
                                                                                   int compareMvTvpe (const void * a. const void * b)
  */
                                                                                   2
                                                                                         if (*(MyType*)a > *(MyType*)b) return 1;
                              Código 12: exemplo de string
                                                                                        if (*(MyType*)a = *(MyType*)b) return 0;
                                                                                         if (*(MyType*)a < *(MyType*)b) return -1;
  #include <iostream>
  #include <algorithm>
                                                                                      int key = 40;
  #include <vector>
                                                                                      item = (int*) bsearch (&key, values, n, sizeof (int), compareMyType);
   using namespace std;
                                                                                                                  Código 14: pesquisa binária
   bool myfunction (int i, int j) { return (i<j); }
   struct myclass {
                                                                                    1 #include <iostream>
     bool operator() (int i, int j) { return (i<j);}
                                                                                      #include <iomanip> // setprecision()
   } mvobject:
                                                                                      using namespace std:
   int compare (const void * a, const void * b)
                                                                                      int main () {
                                                                                        double a = 3.1415926534;
13
     return ( *(int*)a - *(int*)b );
                                                                                        double b = 2006.0;
14
                                                                                        double c = 1.0e - 10;
15
                                                                                        // setprecision (1) \Rightarrow 1 casa decimal apos a virgula
                                                                                   10
   int main () {
                                                                                        cout \ll fixed \ll setprecision(1) \ll 9.09090901 \ll endl;
                                                                                   11
     int myints [] = \{32,71,12,45,26,80,53,33\};
                                                                                        \operatorname{cout} \ll \operatorname{fixed} \ll \operatorname{setprecision}(2) \ll 9.09090901 \ll \operatorname{endl};
19
     vector <int> myvector (myints, myints+8);
                                                                // 32 71 12 45 26 13
                                                                                        cout \ll fixed \ll setprecision(3) \ll 9.09090901 \ll endl;
                                                                                        cout << fixed << setprecision(2) << 9.1 << endl;
         80 53 33
21
                                                                                        // anula o efeito de setprecision
     // using default comparison (operator <):
22
                                                                                  16
     sort (myvector.begin(), myvector.begin()+4);
                                                                                        cout.unsetf(ios::floatfield);
23
                                                                //(12 32 45 71)26 17
         80 53 33
     // using function as comp
                                                                                        // 5 digitos no maximo
24
     sort (myvector.begin()+4, myvector.end(), myfunction); // 12 32 45 71(26 20
                                                                                        cout.precision(5);
          33 53 80)
     // using object as comp
                                                                                        cout << a << '\t' << b << '\t' << c << endl;
     sort (myvector.begin(), myvector.end(), myobject);
                                                                //(12 26 32 33 45 23
                                                                                        cout << fixed << a << '\t' << b << '\t' << c << endl:
27
         53 71 80)
                                                                                        cout << scientific << a << '\t' << b << '\t' << c << endl;
     // if stable is need
                                                                                        // Sets the basefield format flag for the str stream to dec. hex or oct.
29
     stable_sort (myvector.begin(), myvector.end(), myfunction);
                                                                                  27
                                                                                        int n = 70:
30
                                                                                        cout << dec << n << endl;
31
     // Rearranges the elements in the range [first, last], in such a way that 29
                                                                                        cout << hex << n << endl;
32
         the subrange [first, middle]
                                                                                        cout \ll oct \ll n \ll endl;
     // contains the smallest elements of the entire range sorted in ascending31
          order, and the subrange
                                                                                        return 0:
     // [middle,end) contains the remaining elements without any specific orders
                                                                                      /* output
     partial_sort (myvector.begin(), myvector.begin()+3, myvector.end());
                                                                                      9.1
                                                                                      9.09
     gsort (myints, 8, sizeof(int), compare);
                                                                                      9.091
37
                                                                                      9.10
                                                                                      3.1416 2006
                                                                                                       1e - 10
     return 0;
                                                                                   40 7 3.14159 2006.00000
                                                                                                                0.00000
```

```
3.14159e+00
                  2.00600e + 03
                                   1.00000e-10
106
```

Código 15: Arredondamento e output em outras bases

Teoria dos números

int gcd(int x, int y)

```
return y ? gcd(y, x \% y) : abs(x);
uint64_t lcm(int x, int y)
   if (x &  y) return abs(x) / gcd(x, y) * uint64_t(abs(y));
   else return uint64_t(abs(x | y));
            Código 16: máximo divisor comum e mínimo multiplo comum
                                                                                 10
                                                                                 11
bool isPrime(int n)
                                                                                 13
                                                                                 14
   if (n < 0) return isPrime(-n);
   if (n == 1) return true;
   if (n < 5 \mid | n \% 2 = 0 \mid | n \% 3 = 0) return (n = 2 \mid | n = 3);
   int \max P = sqrt(n) + 2;
   for (int p = 5; p < maxP; p += 6)
                                                                                 21
      if (n \% p == 0 \mid \mid n \% (p+2) == 0) return false;
                                                                                 23
   return true;
                                                                                 24
                                                                                 25
                                                                                 27
```

Código 17: decide se um número é primo

```
typedef map<int, int> prime_map;
   void squeeze (prime_map& M, int& n, int p)
      for (; n \% p == 0; n \neq p) M[p]++;
   void factor (int n, prime_map& M)
      if (n < 0) return n = -n;
      if (n < 2) return;
      squeeze (M, n, 2);
11
      squeeze (M, n, 3);
12
13
      int \max P = sqrt(n) + 2;
14
      for (int p = 5; p < maxP; p += 6)
```

```
squeeze(M, n, p);
  squeeze (M, n, p+2);
if (n > 1) M[n]++;
```

Código 18: Retorna a fatoração em números primos de abs(n).

2.3Grafos

16

17

18

19 20

21

15

17 18

19

20

22

26

28

31 32

33 34

35 36

37

```
#define TAM 100
#define BRANCO 0
#define CINZA 1
#define PRETO 2
bool grafo [TAM] [TAM];
int pass [TAM];
bool dfs(int v)
   pass[v] = CINZA;
   for (int i = 0; i < TAM; i++)
      if (grafo[v][i])
         if (pass[i] == CINZA) return false;
         if (pass[i] == BRANCO && !dfs(i)) return false;
   pass[v] = PRETO;
   return true;
bool aciclico()
   memset(pass, BRANCO, TAM*sizeof(int));
   for (int i = 0; i < TAM; i++)
      if (pass[i] == BRANCO)
         if (!dfs(i)) return false;
   return true;
```

Código 19: Verifica se o grafo é aciclico.

```
1 #include <queue>
```

```
typedef AdjList Grafo;
                                                                                              for (int i = 0; i < element\_count; ++i)
                                                                                       17
                                                                                                 forest->parent[i] = i;
                                                                                       18
   int dist[MAX_VERTICES]:
                                                                                       19
   int prev[MAX_VERTICES]; // para recuperar o caminho usando um dijoint foresto
                                                                                           int dsf_find_set(disjoint_set_forest_p forest, int i)
                                                                                       21
                                                                                       22
   void dijkstra(Grafo& grafo, int source)
                                                                                               if (i != forest -> parent[i])
                                                                                       23
10
                                                                                       24
       for (int i = 0; i < grafo.size(); i++)
                                                                                                    forest -> parent [i] = dsf_find_set (forest, forest -> parent [i]);
11
                                                                                       25
                                                                                       26
12
          dist[i] = INF;
                                                                                               return forest -> parent [i];
                                                                                       27
          prev[i] = -1;
                                                                                       28
14
15
                                                                                       29
                                                                                           void dsf_union(disjoint_set_forest_p forest. int i. int i)
16
                                                                                       30
       dist[source] = 0;
17
                                                                                       31
                                                                                               int x = dsf_find_set(forest, i);
       priority_queue < pair < int , int > > heap;
                                                                                       32
18
                                                                                               int y = dsf_find_set(forest, j);
       heap.push(make_pair(0, source));
                                                                                       33
19
20
                                                                                       34
       while (!heap.empty())
                                                                                               if (forest -> rank[x] > forest -> rank[y])
21
                                                                                       35
22
                                                                                       36
          int u = heap.top().second;
                                                                                       37
                                                                                                   forest \rightarrow parent[y] = x;
23
          heap.pop();
24
                                                                                       38
                                                                                               else
                                                                                       39
25
          // para cada vizinho de u
          for (map<int,int>::iterator i = grafo[u].begin(); i != grafo[u].end()41
                                                                                                   forest \rightarrow parent[x] = v;
27
               i++)
                                                                                                   if (forest \rightarrow rank[x] = forest \rightarrow rank[y])
                                                                                       43
             int totalDist = dist[u] + (*i).second;
                                                                                                        forest \rightarrow rank[y]++;
                                                                                       44
             if (totalDist <= dist[(*i).first])</pre>
                                                                                       45
                                                                                       46
                 dist[(*i).first] = totalDist;
                                                                                       47
32
                 heap.push(make_pair(totalDist, (*i).first));
                                                                                                                   Código 21: Floresta dijunta de arvores
                 prev[(*i).first] = u;
36
                                                                                          typedef vector <map<int, int> > AdjList;
37
                                                                                           struct Grafo
                  Código 20: Caminho minimo 1 para todos pesos positivos.
                                                                                              int edgeCnt;
                                                                                              AdjList adj;
   #define SIZE 100
                                                                                           struct edge
   struct dsf
                                                                                               int u:
                                                                                       10
        int element_count;
                                                                                       11
                                                                                               int v;
        int parent[SIZE];
                                                                                               int weight:
        int rank [SIZE];
                                                                                       13
                                                                                       14
   typedef struct dsf * disjoint_set_forest_p;
                                                                                           int edge_compare(const void * e1, const void * e2)
                                                                                       15
                                                                                       16
   void dsf_init(disjoint_set_forest_p forest, int element_count)
                                                                                               struct edge * p1 = (struct edge *) e1;
11
                                                                                       17
                                                                                               struct edge * p2 = (struct edge *) e2;
                                                                                       18
12
       forest -> element_count = element_count:
                                                                                       19
                                                                                               int f = p1->weight - p2->weight;
13
       memset(forest->parent, 0, element_count*sizeof(int));
                                                                                               if (f < 0)
14
                                                                                       20
       memset(forest -> rank, 0, element_count*sizeof(int));
```

16

typedef vector <map <int, int> > AdjList;

```
return -1:
       else if (f == 0)
^{24}
                                                                                    79
            return edge_compare1(e1, e2);
                                                                                    80
26
27
       else
           return 1;
30
31
32
   struct edge * get_edge_list(Grafo& graph)
34
35
       int edge_count = graph.edgeCnt:
36
       struct edge *edges = (struct edge*) malloc(edge_count * sizeof(struct
37
            edge));
                                                                                    10
       int current_edge = 0;
39
                                                                                    11
                                                                                    12
       for (int i = 0; i < graph.adj.size(); ++i)
41
                                                                                    13
42
            for (map<int, int>::iterator j = graph.adj[i].begin(); j != graph.
43
                adj[i].end(); j++)
                                                                                    16
                                                                                    17
                struct edge e;
                                                                                    18
                e.u = i < (*j).first ? i : (*j).first;
                                                                                    19
                e.v = i > (*j).first ? i : (*j).first;
                                                                                    20
                e.weight = (*j).second;
                                                                                    21
                edges[current_edge++] = e;
                                                                                    22
                                                                                    23
51
                                                                                    24
52
                                                                                    25
       return edges;
53
                                                                                    26
54
                                                                                    27
   void kruskal (Grafo& graph, Grafo& mst)
56
57
        // Obtain a list of edges and sort it by weight in O(E lq E) time
58
       int edge_count = graph.edgeCnt;
       struct edge *edges = get_edge_list(graph);
       qsort(edges, edge_count, sizeof(struct edge), edge_compare);
61
       disjoint_set_forest dsf:
63
       dsf_init(&dsf, edge_count);
64
       for (int i = 0; i < edge\_count; ++i)
            struct edge e = edges[i];
                                                                                    10
            int uset = dsf_find_set(dsf, e.u);
                                                                                    11
            int vset = dsf_find_set(dsf, e.v);
                                                                                    12
                                                                                    13
            if (uset != vset)
71
                                                                                    14
72
                mst.adj[e.u][e.v] = e.weight;
                                                                                    15
                                                                                    16
             mst.edgeCnt++;
74
                dsf_union(dsf, uset, vset);
                                                                                    17
```

```
}
free(edges);
}
```

Código 22: Arvore geradora mínima kruskal

Código 23: verifica se um grafo é bipartido

```
#define UNVISITED -1

int grafo[SIZE][SIZE];
int prof[SIZE];
int sorted[SIZE];
int nordem;

void dfsTopsort(int no)

for (int viz = 0; viz < SIZE; viz++)

if (grafo[no][viz])

if (prof[viz] = UNVISITED)

prof[viz] = prof[no] + 1;
dfsTopsort(viz);

laddefine UNVISITED -1

int prof[viz] = prof[no] + 1;
dfsTopsort(viz);

laddefine UNVISITED -1

int prof[SIZE];

int prof[SIZE];

int prof[Viz] = UNVISITED -1

dfsTopsort(viz);

laddefine UNVISITED -1

int prof[SIZE];

int prof[SIZE]
```

```
^{21}
       sorted[nordem --] = no;
22
23
24
   void topSort(int nvt)
25
26
       memset(prof, UNVISITED, nvt*sizeof(int));
27
       nordem = nvt - 1;
28
29
       for (int i = 0; i < nvt; i++)
31
          if (prof[i] == UNVISITED)
32
33
             prof[i] = 0;
34
             dfsTopsort(i);
37
```

Código 24: faz a ordenação topológica de um grafo acíclico

#define TAM 1000

```
int grafo [TAM] [TAM];
   int pred [TAM];
    int f [TAM] [TAM];
    bool visitados [TAM];
    bool dfs(int s, int t, int size)
9
10
       visitados[s] = true;
       if(s == t) return true;
11
12
       for (int v = 0; v < size; v++)
13
14
           \mathbf{if}(\operatorname{grafo}[s][v] - f[s][v] > 0 \&\& ! \operatorname{visitados}[v])
16
17
              pred[v] = s;
              if (dfs(v, t, size)) return true;
18
19
20
^{21}
       return false;
^{22}
23
^{24}
    bool findPath(int s, int t, int size)
25
26
       memset(visitados, false, sizeof(bool)*size);
27
       return dfs(s, t, size);
28
29
   int maxFlow(int size, int s, int t)
31
32
       int delta:
```

```
for (int i = 0; i < size; i++)
   memset(f[i], 0, sizeof(int)*size);
pred[s] = s;
while (findPath(s, t, size))
   delta = INT\_MAX;
   for(int c = t; pred[c] != c; c = pred[c])
      delta = min(delta, grafo[pred[c]][c] - f[pred[c]][c]);
   for (int c = t; pred [c] != c; c = pred [c])
      f [pred [c]] [c] += delta;
      f[c][pred[c]] -= delta;
int soma = 0;
for (int i = 0; i < size; i++)
   soma += f[i][t];
return soma;
```

Código 25: calcula fluxo máximo

2.4 Geometria

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53 54

55 56

57

58

59

60

61

62

63

64

```
struct point
2
      double x, v;
       point (double x = 0, double y = 0): x(x), y(y) {}
      point operator +(point q) \{ return point(x + q.x, y + q.y); \}
       point operator -(point q) { return point(x - q.x, y - q.y); }
      point operator *(double t) { return point(x * t, y * t); }
      point operator /(double t) { return point(x / t, y / t); }
      double operator *(point q) { return x * q.x + y * q.y; }
10
      double operator \%(point q) { return x * q.y - y * q.x; }
11
12
      int cmp(point q) const
13
14
15
          if (int t = ::cmp(x, q.x)) return t;
          return :: cmp(y, q.y);
16
<sup>17</sup>11
```

```
bool operator ==(point q) const { return cmp(q) == 0; }
19
       bool operator !=(point q) const { return cmp(q) != 0; }
20
       bool operator < (point q) const \{ return cmp(q) < 0; \}
21
22
       friend ostream& operator <<(ostream& o, point p) {
23
        return o << "(" << p.x << ", " << p.y << ")";
24
25
      static point pivot:
26
27
28
   double abs(point p) { return hypot(p.x, p.y); }
   double arg(point p) { return atan2(p.v, p.x); }
31
   point point :: pivot :
32
33
   typedef vector<point> polygon;
   int ccw(point p, point q, point r)
36
37
      return cmp((p - r) \% (q - r));
39
   double angle (point p, point q, point r)
41
      point u = p - q, v = r - q;
43
      return atan2(u \% v, u * v);
44
```

Código 26: ponto e poligono

```
bool between(point p, point q, point r)
{
   return ccw(p, q, r) == 0 && cmp((p - q) * (r - q)) <= 0;
}</pre>
```

Código 27: Decide se q está sobre o segmento fechado pr.

```
bool seg_intersect(point p, point q, point r, point s)
      point A = q - p;
      point B = s - r:
      point C = r - p;
      point D = s - q;
      int a = cmp(A \% C) + 2 * cmp(A \% D);
      int b = cmp(B % C) + 2 * cmp(B % D);
10
      if (a = 3 \mid | a = -3 \mid | b = 3 \mid | b = -3) return false;
11
       if (a \mid |b| \mid p = r \mid |p = s| \mid q = r \mid |q = s|) return true;
12
13
      int t = (p < r) + (p < s) + (q < r) + (q < s);
14
      return t != 0 && t != 4;
15
```

Código 28: Decide se os segmentos fechados pq e rs têm pontos em comum.

```
double seg_distance(point p, point q, point r)

{
    point A = r - q;
    point B = r - p;
    point C = q - p;

    double a = A * A, b = B * B, c = C * C;

    if (cmp(b, a + c) >= 0) return sqrt(a);
    else if (cmp(a, b + c) >= 0) return sqrt(b);
    else return fabs(A % B) / sqrt(c);
}
```

Código 29: Calcula a distância do ponto r ao segmento pq.

```
int in_poly(point p, polygon& T)
{
    double a = 0;
    int N = T.size();
    for (int i = 0; i < N; i++)
    {
        if (between(T[i], p, T[(i+1) % N])) return -1;
        a += angle(T[i], p, T[(i+1) % N]);
    }
    return cmp(a) != 0;
}</pre>
```

Código 30: Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 dependendo se p está no exterior, na fronteira ou no interior de T, respectivamente.

2.5 Outros

10

```
1 /**
   The Josephus problem (or Josephus permutation) is a theoretical problem
       related to a certain counting-out game. There are people standing in a
       circle waiting to be executed. After the first man is executed, certain
       number of people are skipped and one man is executed. Then again, people
        are skipped and a man is executed. The elimination proceeds around the
       circle (which is becoming smaller and smaller as the executed people are
        removed), until only the last man remains, who is given freedom. The
       task is to choose the place in the initial circle so that you are the
       last one remaining and so survive.
    */
   using namespace std;
   int josephus (int n, int m)
9
      int res = 0;
      vector <int> people;
10
11
      int loc = 0:
12
      for (int i = 0; i < n; i++) people.push_back(i+1);
```

```
14
       while (people.size() > 1)
15
16
           if (loc >= people.size())
  loc %= people.size();
17
18
19
           people.erase(people.begin()+loc);
20
           loc += (m-1);
^{21}
22
23
       return people[0];
^{24}
25 }
```

Código 31: josephus problem