

Sumário

1	Tabelas	1	23	ponto e poligono	9
2	Codigos	1	24	Decide se q está sobre o segmento fechado pr.	10
2.1	Exemplos	1	25	Decide se os segmentos fechados pq e rs têm pontos em comum.	10
2.2	Teoria dos números	6	26	Calcula a distância do ponto r ao segmento pq.	10
2.3	Grafos	7	27	Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 dependendo se p está no exterior, na fronteira ou no interior de T, respectivamente.	10
2.4	Geometria	9	28	josephus problem	10
2.5	Outros	10			

Lista de Tabelas

1	Limites de representação de dados	1	tipo	bits	min...max	precisao
2	Fatorial	2	char	8	0..127	2
3	scanf() - %[*][width][modifiers]type	2	signed char	8	-128..127	2
4	scanf() %[*][width][modifiers]type	2	unsigned char	8	0..255	2
5	stdlib	2	short	16	-32.768 .. 32.767	4
6	math (angulos em radianos)	2	unsigned short	16	0 .. 65.535	4
			int	32	-2x10**9 .. 2 x 10**9	9
			unsigned int	32	0 .. 4x10**9	9
			int64_t	64	-9 x 10**18 .. 9 x 10**18	18
			uint64_t	64	0 .. 18 x 10**18	19

Lista de Listagens

1	Modelo	1			
2	comparcao de ponto flutuante	3			
3	.vimrc para a configuração do vim	3			
4	printf	3			
5	exemplo de map	3			
6	exemplo de set e multiset	4			
7	exemplo de list	4			
8	exemplo de queue	4			
9	exemplo de priority queue	4			
10	exemplo de stack	5			
11	exemplo de vector	5			
12	exemplo de ordenação	5			
13	pesquisa binária	6			
14	Arredondamento e output em outras bases	6			
15	máximo divisor comum e mínimo multiplo comum	6			
16	decide se um número é primo	6			
17	Retorna a fatoração em números primos de abs(n).	7			
18	Caminho minimo 1 para todos pesos positivos.	7			
19	Floresta dijunta de arvores	7			
20	Arvore geradora mínima kruskal	8			
21	verifica se um grafo é bipartido	8			
22	faz a ordenação topológica de um grafo acíclico	9			

1

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <math.h>

#include <inttypes.h>
#include <ctype.h>

#include <algorithm>
#include <utility>
#include <iostream>

#include <map>
#include <set>
#include <vector>
#include <sstream>

using namespace std;
```

Tabela 1: Limites de representação de dados

2 Codigos

2.1 Exemplos

$0! = 1$
 $1! = 1$
 $2! = 2$
 $3! = 6$
 $4! = 24$
 $5! = 120$
 $6! = 720$
 $7! = 5.040$
 $8! = 40.320$
 $9! = 362.880$
 $10! = 3.628.800$
 $11! = 39.916.800$
 $12! = 479.001.600$ [limite do (unsigned) int]
 $13! = 6.227.020.800$
 $14! = 87.178.291.200$
 $15! = 1.307.674.368.000$
 $16! = 20.922.789.888.000$
 $17! = 355.687.428.096.000$
 $18! = 6.402.373.705.728.000$
 $19! = 121.645.100.408.832.000$
 $20! = 2.432.902.008.176.640.000$ [limite do (u)int64_t]

Tabela 2: Fatorial

Tipo	%
char	c
int	d
float	e, E, f, g, G
int (octal)	o
int (hexa)	x, X
uint	u
char*	s

Tabela 3: scanf() - %[*][width][modifiers]type

modifiers	tipo
h	short int (d, i, n), or unsigned short int (o, u, x)
l	long int (d, i, n), or unsigned long int (o, u, x), or double (e, f, g)
L	long double (e, f, g)

Tabela 4: scanf() %[*][width][modifiers]type

função	descrição
atof	Convert string to double
atoi	Convert string to integer
atol	Convert string to long integer
strtod	Convert string to double
strtol	Convert string to long integer
strtoul	Convert string to unsigned long integer

Tabela 5: stdlib

função	descrição
cos	Compute cosine
sin	Compute sine
tan	Compute tangent
acos	Compute arc cosine
asin	Compute arc sine
atan	Compute arc tangent
atan2	Compute arc tangent with two parameters
cosh	Compute hyperbolic cosine
sinh	Compute hyperbolic sine
tanh	Compute hyperbolic tangent
exp	Compute exponential function
frexp	Get significand and exponent
ldexp	Generate number from significand and exponent
log	Compute natural logarithm
log10	Compute common logarithm
modf	Break into fractional and integral parts
pow	Raise to power
sqrt	Compute square root
ceil	Round up value
fabs	Compute absolute value
floor	Round down value
fmod	Compute remainder of division

Tabela 6: math (angulos em radianos)

```

20 #define abs(a) ((a) > 0 ? (a) : -(a))
21
22 int main()
23 {
24     int n;
25
26     cin >> n;
27
28     for (int i = 0; i < n; i++)
29     {
30
31     }
32
33     while (cin >> n)
34     {
35
36     }
37     return 0;
38 }

```

Código 1: Modelo

```

1 const double EPS = 1e-10;
2 /**
3  * -1 se x < y
4  * 0 se x = y
5  * 1 se x > y
6  */
7 inline int cmp (double x, double y = 0, double tol = EPS)
8 {
9     return (x <= y + tol) ? (x + tol < y) ? -1 : 0 : 1;
10 }

```

Código 2: comparcao de ponto flutuante

```

1 set ai noet ts=4 sw=4 bs=2
2 syn on
3 mat Keyword "\<foreach\>"

```

Código 3: .vimrc para a configuração do vim

```

1 /* printf example */
2 #include <stdio.h>
3
4 int main()
5 {
6     printf ("Characters: %c %c \n", 'a', 65);
7     printf ("Decimals: %d %ld\n", 1977, 650000L);
8     printf ("Preceding with blanks: %10d \n", 1977);
9     printf ("Preceding with zeros: %010d \n", 1977);
10    printf ("Some different radixes: %d %x %o %#x %#o \n", 100, 100, 100,
        100, 100);
11    printf ("floats: %4.2f %+0e %E %4.2f\n", 3.1416, 3.1416, 3.1416, 3.1);
12    printf ("Width trick: %*d \n", 5, 10);
13    printf ("%s \n", "A string");

```

```

14     return 0;
15 }
16 /* %[flags (-, +, etc)][width][.precision][length (h,l,L)]specifier
17 Characters: a A
18 Decimals: 1977 650000
19 Preceding with blanks:      1977
20 Preceding with zeros: 0000001977
21 Some different radixes: 100 64 144 0x64 0144
22 floats: 3.14 +3e+000 3.141600E+000 3.10
23 Width trick:      10
24 A string
25 */

```

Código 4: printf

```

1 #include <iostream>
2 #include <map>
3 using namespace std;
4
5 int main ()
6 {
7     map<char,int> mymap;
8     map<char,int>::iterator it;
9     pair<map<char,int>::iterator,bool> ret;
10
11     // first insert function version (single parameter):
12     mymap.insert ( pair<char,int>('a',100) );
13     mymap.insert ( pair<char,int>('z',200) );
14
15     ret=mymap.insert (pair<char,int>('z',500) );
16     if (ret.second==false)
17     {
18         cout << "element 'z' already existed";
19         cout << " with a value of " << ret.first->second << endl;
20     }
21
22     // third insert function version (range insertion):
23     map<char,int> anothermap;
24     anothermap.insert(mymap.begin(),mymap.find('c'));
25
26     // showing contents:
27     cout << "mymap contains:\n";
28     for ( it=mymap.begin(); it != mymap.end(); it++ )
29         cout << (*it).first << " => " << (*it).second << endl;
30
31     map<char,string> mymap;
32     mymap['a']="an element";
33     if (mymap.count('a') > 0)
34         cout << mymap['a'] << " is an element of mymap.\n";
35
36     while (!mymap.empty())
37     {
38         cout << mymap.begin()->first << " => ";
39         cout << mymap.begin()->second << endl;
40         map<char, int>::iterator erasedelement = mymap.erase(mymap.begin());
41     }

```

```
42
43     return 0;
44 }
```

Código 5: exemplo de map

```
1 #include <iostream>
2 #include <set>
3 using namespace std;
4
5 int main ()
6 {
7     multiset<int> mymultiset;
8     multiset<int>::iterator it;
9
10    // set some initial values:
11    for (int i=1; i<=5; i++) mymultiset.insert(i*10);    // 10 20 30 40 50
12
13    cout << "size: " << (int) mymultiset.size() << endl;
14    cout << "count: " << (int) mymultiset.count(10) << endl;
15
16    it=mymultiset.find(20);
17    mymultiset.erase (it);
18
19    if (! mymultiset.empty)
20        mymultiset.erase (mymultiset.find(40));
21
22    for (it=mymultiset.begin(); it!=mymultiset.end(); it++)
23        cout << " " << *it;
24
25    int myints[]={19,72,4,36,20,20};
26    multiset<int> first (myints,myints+3);    // 4,19,72
27    multiset<int> second (myints+3,myints+6);    // 20,20,36
28
29    first.swap(second); // troca conteudo. o primeiro fica [20,20,36] e o
30                        // segundo [4,19,72]
31
32    return 0;
33 }
```

Código 6: exemplo de set e multiset

```
1 #include <iostream>
2 #include <list>
3 using namespace std;
4
5 int main ()
6 {
7     list<int> mylist (2,100);    // two ints with a value of 100
8     mylist.push_front (200);
9     mylist.push_back (300);
10
11    it = mylist.begin();
12    mylist.insert (it,10);
13    mylist.insert (it,2,20); // two ints with a value of 20
14 }
```

```
15     mylist.reverse(); // Reverses the order of the elements in the list.
16
17     cout << "mylist contains:";
18     for (list<int>::iterator it=mylist.begin(); it!=mylist.end(); ++it)
19         cout << " " << *it;
20
21     cout << "Popping out the elements in mylist:";
22     while (!mylist.empty())
23     {
24         cout << " " << mylist.front();
25         mylist.pop_front();
26     }
27
28     while (!mylist.empty())
29     {
30         cout << " " << mylist.back();
31         mylist.pop_back();
32     }
33
34     cout << mylist.size() << endl;
35
36     return 0;
37 }
```

Código 7: exemplo de list

```
1 #include <iostream>
2 #include <queue>
3 using namespace std;
4
5 int main ()
6 {
7     queue<int> myqueue;
8     int sum (0);
9
10    for (int i=1;i<=10;i++) myqueue.push(i);
11
12    myqueue.back() -= myqueue.front();
13
14    cout << "size: " << (int) myqueue.size() << endl;
15
16    while (!myqueue.empty())
17    {
18        sum += myqueue.front();
19        myqueue.pop();
20    }
21
22    cout << "total: " << sum << endl;
23
24    return 0;
25 }
```

Código 8: exemplo de queue

```
1 #include <iostream>
2 #include <queue>
3
4
```

```

3  using namespace std;
4
5  int main ()
6  {
7      priority_queue<int> mypq;
8
9      mypq.push(30);
10     mypq.push(100);
11     mypq.push(25);
12     mypq.push(40);
13
14     cout << "size: " << (int) mypq.size() << endl;
15
16     cout << "Popping out elements...";
17     while (!mypq.empty())
18     {
19         cout << " " << mypq.top();
20         mypq.pop();
21     }
22     cout << endl;
23
24     return 0;
25 }

```

Código 9: exemplo de priority queue

```

1  #include <iostream>
2  #include <stack>
3  using namespace std;
4
5  int main ()
6  {
7      stack<int> mystack;
8      int sum = 0;
9
10     mystack.push(10);
11     mystack.push(20);
12
13     mystack.top() -= 5;
14
15     while (!mystack.empty())
16     {
17         sum += mystack.top();
18         mystack.pop();
19     }
20
21     cout << "size: " << (int) mystack.size() << endl;
22
23     return 0;
24 }

```

Código 10: exemplo de stack

```

1  #include <iostream>
2  #include <vector>
3  using namespace std;

```

```

4
5  int main ()
6  {
7      vector<int> myvector (3,100);
8      vector<int>::iterator it;
9
10     myvector.reserve(100);
11
12     for (i=0; i<myvector.size(); i++)
13         myvector.at(i)=i; // = myvector[i] = i
14
15     it = myvector.begin();
16     it = myvector.insert ( it , 200 );
17     myvector.insert ( it,2,300);
18
19     vector<int> anothervector (2,400);
20     int myarray [] = { 501,502,503 };
21     myvector.insert ( it+2,anothervector.begin(),anothervector.end());
22     myvector.insert (myvector.begin(), myarray, myarray+3);
23
24     cout << "myvector contains:";
25     for ( it=myvector.begin(); it<myvector.end(); it++)
26         cout << " " << *it;
27     cout << endl;
28
29     // erase the 6th element
30     myvector.erase (myvector.begin()+5);
31     int sum;
32     while (!myvector.empty())
33     {
34         sum += myvector.back();
35         myvector.pop_back();
36     }
37
38     return 0;
39 }

```

Código 11: exemplo de vector

```

1  #include <iostream>
2  #include <algorithm>
3  #include <vector>
4  using namespace std;
5
6  bool myfunction (int i,int j) { return (i<j); }
7
8  struct myclass {
9      bool operator() (int i,int j) { return (i<j);}
10 } myobject;
11
12 int compare (const void * a, const void * b)
13 {
14     return ( *(int*)a - *(int*)b );
15 }
16
17

```

```

18 int main () {
19     int myints[] = {32,71,12,45,26,80,53,33};
20     vector<int> myvector (myints, myints+8);           // 32 71 12 45 26
        80 53 33
21
22     // using default comparison (operator <):
23     sort (myvector.begin(), myvector.begin()+4);      //(12 32 45 71)26
        80 53 33
24     // using function as comp
25     sort (myvector.begin()+4, myvector.end(), myfunction); // 12 32 45 71(26
        33 53 80)
26     // using object as comp
27     sort (myvector.begin(), myvector.end(), myobject); // (12 26 32 33 45
        53 71 80)
28
29     // if stable is need
30     stable_sort (myvector.begin(), myvector.end(), myfunction);
31
32     // Rearranges the elements in the range [first,last), in such a way that
        the subrange [first,middle)
33     // contains the smallest elements of the entire range sorted in ascending
        order, and the subrange
34     // [middle,end) contains the remaining elements without any specific order
        .
35     partial_sort (myvector.begin(), myvector.begin()+3, myvector.end());
36
37     qsort (myints, 8, sizeof(int), compare);
38
39     return 0;
40 }

```

Código 12: exemplo de ordenação

```

1 int compareMyType (const void * a, const void * b)
2 {
3     if ( *(MyType*)a > *(MyType*)b ) return 1;
4     if ( *(MyType*)a == *(MyType*)b ) return 0;
5     if ( *(MyType*)a < *(MyType*)b ) return -1;
6 }
7
8 int key = 40;
9 item = (int*) bsearch (&key, values, n, sizeof (int), compareMyType);

```

Código 13: pesquisa binária

```

1 #include <iostream>
2 #include <iomanip> // setprecision()
3 using namespace std;
4
5 int main () {
6     double a = 3.1415926534;
7     double b = 2006.0;
8     double c = 1.0e-10;
9
10    // setprecision(1) => 1 casa decimal apos a virgula
11    cout << fixed << setprecision(1) << 9.09090901 << endl;

```

```

12    cout << fixed << setprecision(2) << 9.09090901 << endl;
13    cout << fixed << setprecision(3) << 9.09090901 << endl;
14    cout << fixed << setprecision(2) << 9.1 << endl;
15
16    // anula o efeito de setprecision
17    cout.unsetf(ios::floatfield);
18
19    // 5 digitos no maximo
20    cout.precision(5);
21
22    cout << a << '\t' << b << '\t' << c << endl;
23    cout << fixed << a << '\t' << b << '\t' << c << endl;
24    cout << scientific << a << '\t' << b << '\t' << c << endl;
25
26    // Sets the basefield format flag for the str stream to dec, hex or oct.
27    int n =70;
28    cout << dec << n << endl;
29    cout << hex << n << endl;
30    cout << oct << n << endl;
31
32    return 0;
33 }
34 /* output
35 9.1
36 9.09
37 9.091
38 9.10
39 3.1416 2006 1e-10
40 3.14159 2006.00000 0.00000
41 3.14159e+00 2.00600e+03 1.00000e-10
42 70
43 46
44 106
45 */

```

Código 14: Arredondamento e output em outras bases

2.2 Teoria dos números

```

1 int gcd(int x, int y)
2 {
3     return y ? gcd(y, x % y) : abs(x);
4 }
5 uint64_t lcm(int x, int y)
6 {
7     if (x && y) return abs(x) / gcd(x, y) * uint64_t(abs(y));
8     else return uint64_t(abs(x | y));
9 }

```

Código 15: máximo divisor comum e mínimo múltiplo comum

```

1 bool isPrime(int n)
2 {
3     if (n < 0) return isPrime(-n);

```

```

4     if (n == 1) return true;
5     if (n < 5 || n % 2 == 0 || n % 3 == 0) return (n == 2 || n == 3);
6
7     int maxP = sqrt(n) + 2;
8     for (int p = 5; p < maxP; p += 6)
9     {
10         if (n % p == 0 || n % (p+2) == 0) return false;
11     }
12     return true;
13 }

```

Código 16: decide se um número é primo

```

1 typedef map<int, int> prime_map;
2 void squeeze(prime_map& M, int& n, int p)
3 {
4     for (; n % p == 0; n /= p) M[p]++;
5 }
6 void factor(int n, prime_map& M)
7 {
8     if (n < 0) return n = -n;
9     if (n < 2) return;
10
11     squeeze(M, n, 2);
12     squeeze(M, n, 3);
13
14     int maxP = sqrt(n) + 2;
15     for (int p = 5; p < maxP; p += 6)
16     {
17         squeeze(M, n, p);
18         squeeze(M, n, p+2);
19     }
20     if (n > 1) M[n]++;
21 }

```

Código 17: Retorna a fatoração em números primos de abs(n).

2.3 Grafos

```

1 #include <queue>
2
3 typedef vector<map<int, int> > AdjList;
4 typedef AdjList Grafo;
5
6 int dist[MAX_VERTICES];
7 int prev[MAX_VERTICES]; // para recuperar o caminho usando um disjoint forest
8
9 void dijkstra(Grafo& grafo, int source)
10 {
11     for (int i = 0; i < grafo.size(); i++)
12     {
13         dist[i] = INF;
14         prev[i] = -1;

```

```

15     }
16
17     dist[source] = 0;
18     priority_queue<pair<int, int> > heap;
19     heap.push(make_pair(0, source));
20
21     while (!heap.empty())
22     {
23         int u = heap.top().second;
24         heap.pop();
25
26         // para cada vizinho de u
27         for (map<int, int>::iterator i = grafo[u].begin(); i != grafo[u].end(); i++)
28         {
29             int totalDist = dist[u] + (*i).second;
30             if (totalDist <= dist[(*i).first])
31             {
32                 dist[(*i).first] = totalDist;
33                 heap.push(make_pair(totalDist, (*i).first));
34                 prev[(*i).first] = u;
35             }
36         }
37     }
38 }

```

Código 18: Caminho minimo 1 para todos pesos positivos.

```

1 #define SIZE 100
2
3 struct dsf
4 {
5     int element_count;
6     int parent[SIZE];
7     int rank[SIZE];
8 };
9 typedef struct dsf * disjoint_set_forest_p;
10
11 void dsf_init(disjoint_set_forest_p forest, int element_count)
12 {
13     forest->element_count = element_count;
14     memset(forest->parent, 0, element_count*sizeof(int));
15     memset(forest->rank, 0, element_count*sizeof(int));
16
17     for (int i = 0; i < element_count; ++i)
18         forest->parent[i] = i;
19 }
20
21 int dsf_find_set(disjoint_set_forest_p forest, int i)
22 {
23     if (i != forest->parent[i])
24     {
25         forest->parent[i] = dsf_find_set(forest, forest->parent[i]);
26     }
27     return forest->parent[i];
28 }

```

```

29
30 void dsf_union(disjoint_set_forest_p forest, int i, int j)
31 {
32     int x = dsf_find_set(forest, i);
33     int y = dsf_find_set(forest, j);
34
35     if (forest->rank[x] > forest->rank[y])
36     {
37         forest->parent[y] = x;
38     }
39     else
40     {
41         forest->parent[x] = y;
42         if (forest->rank[x] == forest->rank[y])
43         {
44             forest->rank[y]++;
45         }
46     }
47 }

```

Código 19: Floresta disjunta de arvores

```

1 typedef vector<map<int, int> > AdjList;
2 struct Grafo
3 {
4     int edgeCnt;
5     AdjList adj;
6 };
7
8 struct edge
9 {
10     int u;
11     int v;
12     int weight;
13 };
14
15 int edge_compare(const void * e1, const void * e2)
16 {
17     struct edge * p1 = (struct edge *) e1;
18     struct edge * p2 = (struct edge *) e2;
19     int f = p1->weight - p2->weight;
20     if (f < 0)
21     {
22         return -1;
23     }
24     else if (f == 0)
25     {
26         return edge_compare1(e1, e2);
27     }
28     else
29     {
30         return 1;
31     }
32 }
33
34 struct edge * get_edge_list(Grafo& graph)

```

```

35 {
36     int edge_count = graph.edgeCnt;
37     struct edge *edges = (struct edge*) malloc(edge_count * sizeof(struct
38         edge));
39
40     int current_edge = 0;
41
42     for (int i = 0; i < graph.adj.size(); ++i)
43     {
44         for (map<int, int>::iterator j = graph.adj[i].begin(); j != graph.
45             adj[i].end(); j++)
46         {
47             struct edge e;
48             e.u = i < (*j).first ? i : (*j).first;
49             e.v = i > (*j).first ? i : (*j).first;
50             e.weight = (*j).second;
51             edges[current_edge++] = e;
52         }
53     }
54
55     return edges;
56 }
57
58 void kruskal(Grafo& graph, Grafo& mst)
59 {
60     // Obtain a list of edges and sort it by weight in O(E lg E) time
61     int edge_count = graph.edgeCnt;
62     struct edge *edges = get_edge_list(graph);
63     qsort(edges, edge_count, sizeof(struct edge), edge_compare);
64
65     disjoint_set_forest dsf;
66     dsf_init(&dsf, edge_count);
67
68     for (int i = 0; i < edge_count; ++i)
69     {
70         struct edge e = edges[i];
71         int uset = dsf_find_set(dsf, e.u);
72         int vset = dsf_find_set(dsf, e.v);
73         if (uset != vset)
74         {
75             mst.adj[e.u][e.v] = e.weight;
76             mst.edgeCnt++;
77             dsf_union(dsf, uset, vset);
78         }
79     }
80
81     free(edges);
82 }

```

Código 20: Arvore geradora mínima kruskal

```

1 #define TAM 200
2
3 bool grafo[TAM][TAM];
4 int pass[TAM];
5 int n;
6

```



```

6
7 bool bipartido(int v, int color = 1)
8 {
9     pass[v] = color;
10    int thisColor = color;
11    bool ret = true;
12
13    color = color == 1 ? 2 : 1;
14
15    for (int i = 0; i < n; i++)
16    {
17        if (grafo[v][i])
18        {
19            if (!pass[i]) ret = dfs(i, color);
20            else if (pass[i] == thisColor) return false;
21
22            if (!ret) return false;
23        }
24    }
25
26    return ret;
27 }

```

Código 21: verifica se um grafo é bipartido

```

1 #define UNVISITED -1
2
3 int grafo[SIZE][SIZE];
4 int prof[SIZE];
5 int sorted[SIZE];
6 int nordem;
7
8 void dfsTopsort(int no)
9 {
10    for (int viz = 0; viz < SIZE; viz++)
11    {
12        if (grafo[no][viz])
13        {
14            if (prof[viz] == UNVISITED)
15            {
16                prof[viz] = prof[no] + 1;
17                dfsTopsort(viz);
18            }
19        }
20    }
21
22    sorted[nordem--] = no;
23 }
24
25 void topSort(int nvt)
26 {
27     memset(prof, UNVISITED, nvt*sizeof(int));
28     nordem = nvt - 1;
29
30     for (int i = 0; i < nvt; i++)
31     {

```

```

32         if (prof[i] == UNVISITED)
33         {
34             prof[i] = 0;
35             dfsTopsort(i);
36         }
37     }
38 }

```

Código 22: faz a ordenação topológica de um grafo acíclico

2.4 Geometria

```

1 struct point
2 {
3     double x, y;
4     point(double x = 0, double y = 0): x(x), y(y) {}
5
6     point operator +(point q) { return point(x + q.x, y + q.y); }
7     point operator -(point q) { return point(x - q.x, y - q.y); }
8     point operator *(double t) { return point(x * t, y * t); }
9     point operator /(double t) { return point(x / t, y / t); }
10    double operator *(point q) { return x * q.x + y * q.y; }
11    double operator %(point q) { return x * q.y - y * q.x; }
12
13    int cmp(point q) const
14    {
15        if (int t = ::cmp(x, q.x)) return t;
16        return ::cmp(y, q.y);
17    }
18
19    bool operator ==(point q) const { return cmp(q) == 0; }
20    bool operator !=(point q) const { return cmp(q) != 0; }
21    bool operator < (point q) const { return cmp(q) < 0; }
22
23    friend ostream& operator <<(ostream& o, point p) {
24        return o << "(" << p.x << ", " << p.y << ")";
25    }
26    static point pivot;
27 };
28
29 double abs(point p) { return hypot(p.x, p.y); }
30 double arg(point p) { return atan2(p.y, p.x); }
31
32 point point::pivot;
33
34 typedef vector<point> polygon;
35
36 int ccw(point p, point q, point r)
37 {
38     return cmp((p - r) % (q - r));
39 }
40
41 double angle(point p, point q, point r)
42 {

```

```

43     point u = p - q, v = r - q;
44     return atan2(u % v, u * v);
45 }

```

Código 23: ponto e poligono

```

1 bool between(point p, point q, point r)
2 {
3     return ccw(p, q, r) == 0 && cmp((p - q) * (r - q)) <= 0;
4 }

```

Código 24: Decide se q está sobre o segmento fechado pr.

```

1 bool seg_intersect(point p, point q, point r, point s)
2 {
3     point A = q - p;
4     point B = s - r;
5     point C = r - p;
6     point D = s - q;
7
8     int a = cmp(A % C) + 2 * cmp(A % D);
9     int b = cmp(B % C) + 2 * cmp(B % D);
10
11     if (a == 3 || a == -3 || b == 3 || b == -3) return false;
12     if (a || b || p == r || p == s || q == r || q == s) return true;
13
14     int t = (p < r) + (p < s) + (q < r) + (q < s);
15     return t != 0 && t != 4;
16 }

```

Código 25: Decide se os segmentos fechados pq e rs têm pontos em comum.

```

1 double seg_distance(point p, point q, point r)
2 {
3     point A = r - q;
4     point B = r - p;
5     point C = q - p;
6
7     double a = A * A, b = B * B, c = C * C;
8
9     if (cmp(b, a + c) >= 0) return sqrt(a);
10    else if (cmp(a, b + c) >= 0) return sqrt(b);
11    else return fabs(A % B) / sqrt(c);
12 }

```

Código 26: Calcula a distância do ponto r ao segmento pq.

```

1 int in_poly(point p, polygon& T)
2 {
3     double a = 0;
4     int N = T.size();
5     for (int i = 0; i < N; i++)
6     {
7         if (between(T[i], p, T[(i+1) % N])) return -1;

```

```

8         a += angle(T[i], p, T[(i+1) % N]);
9     }
10    return cmp(a) != 0;
11 }

```

Código 27: Classifica o ponto p em relação ao polígono T. Retorna 0, -1 ou 1 dependendo se p está no exterior, na fronteira ou no interior de T, respectivamente.

2.5 Outros

```

1 /**
2  * The Josephus problem (or Josephus permutation) is a theoretical problem
3  * related to a certain counting-out game. There are people standing in a
4  * circle waiting to be executed. After the first man is executed, certain
5  * number of people are skipped and one man is executed. Then again, people
6  * are skipped and a man is executed. The elimination proceeds around the
7  * circle (which is becoming smaller and smaller as the executed people are
8  * removed), until only the last man remains, who is given freedom. The
9  * task is to choose the place in the initial circle so that you are the
10  * last one remaining and so survive.
11  */
12
13 using namespace std;
14
15 int josephus(int n, int m)
16 {
17     int res = 0;
18     vector<int> people;
19     int loc = 0;
20
21     for (int i = 0; i < n; i++) people.push_back(i+1);
22
23     while (people.size() > 1)
24     {
25         if (loc >= people.size())
26             loc %= people.size();
27
28         people.erase(people.begin()+loc);
29         loc += (m-1);
30     }
31
32     return people[0];
33 }

```

Código 28: josephus problem