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	27 28 29	porém muito maior em tempo de codificação . 9 ponto e poligono	1		
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	32	pectivamente			

33	Gera as permutações dos elementos da string . 11
34	Ignora os dois floats do meio. Retornará 2 no
	sucesso
35	Referencias map

1	Tabelas					
uns sho uns int uns inte	r ned char signed char	bits 8 8 8 16 16 32 32 64 64	minmax 0127 -128127 0255 -32.768 32.767 0 65.535 -2x10**9 2 x 10**9 0 4x10**9 -9 x 10**18 9 x 10**18 0 18 x 10**18	precisao 2 2 2 2 4 4 9 9 18 19	modifiers h l L	s tipo short int (d, i, n), or unsigned short int (o, u, x) long int (d, i, n), or unsigned long int (o, u, x), or dou long double (e, f, g) abela 4: scanf() %[*][width][modifiers]type
	Tabela 1:	Limit	es de representação de dado	s		
4! : 5! : 6! : 7! : 8! : 10! 11! 12! 13! 14! 15! 16! 17! 18! 19!	= 1 $= 2$ $= 6$ $= 24$ $= 120$ $= 720$ $= 5.040$ $= 40.320$ $= 362.880$ $= 3628.800$ $= 39.916.800$ $= 479.001.60$ $= 6.227.020$ $= 87.178.29$ $= 1.307.674$ $= 20.922.789$ $= 355.687.49$ $= 6.402.373$ $= 121.645.10$	00 [lim 800 1.200 368.00 9.888.0 28.096 705.72	00 000 08.000 832.000		função atof atoi atol strtod strtol strtoul	descrição Convert string to double Convert string to integer Convert string to long integer Convert string to double Convert string to long integer Convert string to unsigned long integer Tabela 5: stdlib
20!	= 2.432.902.		6.640.000 [limite do (u)int64bela 2: Fatorial	*_b]	função cos sin tan acos asin atan atan2 cosh sinh	descrição Compute cosine Compute sine Compute tangent Compute arc cosine Compute arc sine Compute arc tangent Compute arc tangent Compute arc tangent with two parameters Compute hyperbolic cosine Compute hyperbolic sine

acos	Compute arc cosine
asin	Compute arc sine
atan	Compute arc tangent
atan2	Compute arc tangent with two parameters
\cosh	Compute hyperbolic cosine
\sinh	Compute hyperbolic sine
anh	Compute hyperbolic tangent
\exp	Compute exponential function
frexp	Get significand and exponent
ldexp	Generate number from significand and exponent
log	Compute natural logarithm
$\log 10$	Compute common logarithm
modf	Break into fractional and integral parts
pow	Raise to power
sqrt	Compute square root
ceil	Round up value
fabs	Compute absolute value
floor	Round down value
fmod	Compute remainder of division
	Tabela 6: math (angulos em radianos)

Tabela 6: math (angulos em radianos)

```
%
{\rm Tipo}
\operatorname{char}
                     \mathbf{c}
                     \mathrm{d}
int
                     e, E, f, g, G
float
int (octal)
                     О
int (hexa)
                    x, X
uint
                     u
\mathrm{char}^*
                     \mathbf{S}
```

2 Codigos

2.1Exemplos

```
15
                                                           16
   #include <stdio.h>
   #include <stdlib.h>
                                                           17
   #include <string.h>
                                                           18
   #include <math.h>
                                                           20
   #include <inttypes.h>
   #include <ctype.h>
   #include <limits.h>
                                                           23
   #include <algorithm>
10
   #include <utility>
11
   #include <iostream>
13
   #include <map>
14
   #include <set>
   #include <vector>
16
   #include <sstream>
17
18
   using namespace std;
19
21
   #define abs(a) ((a) > 0 ? (a) : -(a))
22
23
   int main()
24
   {
25
       int n;
26
       cin >> n;
27
       for (int i = 0; i < n; i++)
29
30
32
33
34
       while (cin >> n)
35
36
37
38
       return 0;
                        Código 1: Modelo
   const double EPS = 1e-10;
    * -1 se x < y
    * 0 se x = y
    * 1 \ se \ x > y
   inline int cmp (double x, double y = 0, double tol \frac{1}{32}
       return (x \le y + tol) ? (x + tol < y) ? -1 : 0 :
           1:
   }
             Código 2: comparcao de ponto flutuante
   set ai noet ts=4 sw=4 bs=2
   syn on
   mat Keyword "\<foreach\>"
           Código 3: .vimrc para a configuração do vim
```

```
24
   A string
25
   */
                         Código 4: printf
   #include <iostream>
   #include <map>
   using namespace std;
   int main ()
5
6
     map<char,int> mymap;
     map<char, int >:: iterator it;
8
9
      pair < map < char , int > :: iterator , bool > ret ;
10
      //\ first\ insert\ function\ version\ (single\ parameter
11
          ):
      12
     mymap.insert ( pair < char, int > ('z', 200) );
13
14
      ret=mymap.insert (pair < char, int > ('z', 500));
15
      if (ret.second=false)
16
17
        \mathrm{cout} << "element 'z' already existed";
18
        {\rm cout} \,<<\, " with a value of " <<\,{\rm ret.first}\,-\!\!>\!\!{\rm second}
19
             << endl;
20
21
      // third insert function version (range insertion)
22
      map<char, int> anothermap;
23
      anothermap.insert(mymap.begin(),mymap.find('c'));
24
25
      // showing contents:
26
27
      cout << "mymap contains:\n";</pre>
      for ( it=mymap.begin() ; it != mymap.end(); it++ )
28
        cout << (*it).first << " => " << (*it).second <<
29
             endl;
30
      map\!\!<\!\!\mathbf{char}\,,\,s\,t\,r\,i\,n\,g\!>\,mymap\,;
      mymap['a']="an element":
      if (mymap.count('a') > 0)
33
          cout << mymap['a'] << " is an element of mymap
35
      while (!mymap.empty())
36
37
         cout << mymap.begin()->first << " => ";
38
         cout << mymap.begin()->second << endl;</pre>
39
         map<char, int>::iterator erasedelement = mymap.
40
              erase (mymap.begin());
      }
42
43
      return 0;
44
   #include <iostream>
   #include <set>
   using namespace std;
   int main ()
      multiset <int> mymultiset;
      multiset < int > :: iterator it;
```

printf ("Width trick: $%*d \n"$, 5, 10);

Some different radixes: 100 64 144 0x64 0144

floats: 3.14 +3e+000 3.141600E+000 3.10

printf ("%s \n", "A string");

Preceding with zeros: 0000001977

return 0:

Characters: a A

Width trick:

, l, L) / specifier

 $Decimals:\ 1977\ 650000$

 $Preceding\ with\ blanks:$

12

Código 5: exemplo de map

```
/* printf example */
   #include <stdio.h>
   int main()
       printf ("Characters: %c %c \n", 'a', 65);
       printf ("Decimals: %d %ld\n", 1977, 650000L);
       printf ("Preceding with blanks: %10d \n", 1977); 5 printf ("Preceding with zeros: %010d \n", 1977); 6
       printf ("Some different radixes: %d %x %o %#x %#\sigma
10
             \n", 100, 100, 100, 100, 100);
       printf ("floats: %4.2f %+.0e %E %4.2f\n", 3.14169
             3.1416, 3.1416, 3.1);
```

```
// set some initial values:
```

```
for (int i=1; i \le 5; i++) mymultiset.insert(i*10); 7
                                                                    queue<int> myqueue;
            // 10 20 30 40 50
                                                                    int sum (0);
      cout << "size: " << (int) mymultiset.size() <<
                                                                    for (int i=1; i <=10; i++) myqueue.push(i);
13
                                                              10
          endl;
                                                              11
      cout << "count: " << (int) mymultiset.count(10) <<
                                                                    myqueue.back() -= myqueue.front();
            endl;
                                                              13
                                                                    cout << "size: " << (int) myqueue.size() << endl;</pre>
15
                                                              14
      it=mymultiset.find(20);
16
                                                              15
                                                                    while (!myqueue.empty())
      mymultiset.erase (it);
17
                                                              16
                                                              17
18
      if (! mymultiset.empty)
                                                                        sum += myqueue.front();
19
                                                              18
       mymultiset.erase (mymultiset.find(40));
                                                                        myqueue.pop();
20
                                                              19
21
                                                                    }
          (it=mymultiset.begin(); it!=mymultiset.end();21
22
                                                                    \operatorname{cout} << \operatorname{"total:} \operatorname{"} << \operatorname{sum} << \operatorname{endl};
          it++
                                                              22
        cout << " " << *it;
23
                                                                    return 0;
                                                              ^{24}
24
      int myints [] = {19,72,4,36,20,20};
25
                                                              25
      multiset <int> first (myints, myints+3);
26
                                                                                  Código 8: exemplo de queue
          4.19.72
      multiset < int > second (myints + 3, myints + 6);
          20,20,36
                                                                 #include <iostream>
28
                                                                  #include <queue>
      using namespace std;
30
                                                                  int main ()
31
      return 0;
                                                               6
                                                                  {
   }
32
                                                                    Código 6: exemplo de set e multset
                                                                    mvpq.push(30):
                                                               9
                                                                    mypq.push(100);
                                                              10
   #include <iostream>
                                                                    mypq.push(25);
                                                              11
   #include <list>
                                                              12
                                                                    mypq.push(40);
    using namespace std;
                                                              13
                                                                    cout << "size: " << (int) mypq.size() << endl;</pre>
                                                              14
   int main ()
                                                              15
6
                                                                    cout << "Popping out elements...";</pre>
      list \langle int \rangle mylist (2,100);
                                             // two ints with
                                                                    \mathbf{while} \quad (\,!\,\mathrm{mypq}\,.\,\mathrm{empty}\,(\,)\,)
           a value of 100
                                                              18
      mylist.push_front (200);
                                                                        cout << " " << mypq.top();
                                                              19
      mylist.push_back (300);
                                                              20
                                                                        mypq.pop();
10
                                                              ^{21}
      it = mylist.begin();
11
                                                                    cout << endl;
                                                              22
      mylist.insert (it,10)
                                                              23
      mylist.insert (it,2,20); // two ints with a value24
13
                                                                    return 0:
           of 20
                                                              25
      mylist.reverse(); // Reverses the order of the
                                                                              Código 9: exemplo de priority queue
15
          elements in the list.
                                                                  #include <iostream>
      cout << "mylist contains:";</pre>
17
                                                                  #include <stack>
      for (list <int>::iterator it=mylist.begin(); it!= 2
18
                                                                  using namespace std;
          mylist.end(); ++it)
        cout << " " << *it;
19
                                                                  int main ()
20
      \mathrm{cout} << "Popping out the elements in mylist:";
21
                                                                    stack<int> mystack;
      while (!mylist.empty())
22
                                                                    int sum = 0:
                                                               8
23
        cout << " " << mylist.front();</pre>
24
                                                                    mystack.push(10);
                                                              10
        mylist.pop_front();
25
                                                                    mystack.push(20);
                                                              11
26
                                                              12
27
                                                                    mystack.top() -= 5;
      while (!mylist.empty())
                                                              13
                                                              14
29
        cout << " " << mylist.back();
                                                                    while (!mystack.empty())
                                                              15
30
                                                              16
31
        mylist.pop_back();
                                                                        sum += mystack.top();
                                                              17
32
                                                                        \operatorname{mystack}.\operatorname{pop}\left(\right);
                                                              18
33
      cout << mylist.size() << endl;</pre>
                                                              19
34
                                                              20
35
                                                                    cout << "size: " << (int) mystack.size() << endl;</pre>
      return 0;
                                                              21
36
                                                              22
   }
37
                                                              23
                                                                    return 0;
                     Código 7: exemplo de list
                                                              24
                                                                                  Código 10: exemplo de stack
   #include <iostream>
   #include <queue>
   using namespace std;
                                                                 #include <iostream>
```

#include <vector>

using namespace std;

2

3

int main ()

{

```
5 int main ()
                                                               34
                                                                      string str2, str3;
                                                                     size_t pos;
6
                                                               35
   ₹
      vector < int > myvector (3,100);
                                                               36
      vector < int > :: iterator it;
                                                                      str2 = str.substr (12,12); // "generalities"
9
                                                               38
                                                                                                     // position of "live"
                                                                      pos = str.find("live");
10
      myvector.reserve(100);
                                                               39
                                                                          in str
11
                                                                      str3 = str.substr (pos);
      for (i=0; i< myvector.size(); i++)
                                                                                                     // get from "live" to
12
                                                               40
        myvector.at(i)=i; // = myvector[i] = i
                                                                          the end
13
14
                                                               41
      \begin{array}{lll} \mbox{it} &= \mbox{myvector.begin();} \\ \mbox{it} &= \mbox{myvector.insert ( it , 200 );} \end{array}
                                                                     cout << str2 << , , << str3 << endl;  
15
                                                               42
16
                                                               43
      myvector.insert (it,2,300);
17
                                                               44
                                                               45
                                                                     return 0;
18
      vector <int> anothervector (2,400);
19
                                                               46
      int myarray [] = \{ 501,502,503 \};
20
                                                               47
                                                                  first 'needle' found at: 14
second 'needle' found at: 44
'haystack' also found at: 30
      myvector.insert (it+2, anothervector.begin(),
                                                               48
           anothervector.end());
                                                               49
      myvector.insert (myvector.begin(), myarray,
                                                               50
22
          myarray+3);
                                                                   Period found at: 51
                                                                   There are two prepositions in this haystack with
23
      cout << "myvector contains:";</pre>
24
                                                                       needles.
      for (it=myvector.begin(); it < myvector.end(); it++3
                                                                   generalities live in details.
25
        cout << " " << *it;
26
27
      cout << endl;
                                                                                   Código 12: exemplo de string
28
      // erase the 6th element
29
30
      myvector.erase (myvector.begin()+5);
                                                                   #include <iostream>
      int sum;
31
                                                                   #include <algorithm>
32
      while (!myvector.empty())
                                                                   #include <vector>
                                                                3
33
                                                                4
                                                                   using namespace std;
         sum += mvvector.back();
34
         myvector.pop_back();
35
                                                                   bool myfunction (int i, int j) { return (i<j); }
                                                                6
36
37
                                                                   struct myclass {
      return 0;
                                                                     bool operator() (int i, int j) { return (i<j);}</pre>
                                                                9
39
   }
                                                                   } myobject;
                                                               10
                                                               11
                   Código 11: exemplo de vector
                                                               12
                                                                   int compare (const void * a, const void * b)
                                                               13
                                                                     return (*(int*)a - *(int*)b);
                                                               14
   #include <iostream>
                                                                   }
                                                               15
   #include <string>
                                                               16
   using namespace std;
                                                               17
                                                                   int main () {
                                                               18
   int main ()
5
                                                                     \mathbf{int} \ \ \mathbf{myints} \ \tilde{[} \ ] \ = \ \{32\,, 71\,, 12\,, 45\,, 26\,, 80\,, 53\,, 33\,\};
                                                               19
6
                                                                      vector <int> myvector (myints, myints+8);
                                                               20
      string str ("There are two needles in this
                                                                                          // 32 71 12 45 26 80 53 33
          haystack with needles.");
                                                               21
      string str2 ("needle");
                                                                      // using default comparison (operator <):
                                                               22
      size_t found;
                                                                      sort (myvector.begin(), myvector.begin()+4);
                                                               23
10
                                                                                      //(12 32 45 71)26 80 53 33
      // different member versions of find in the same _{24}
11
                                                                      // using function as comp
          order as above:
                                                                     sort (myvector.begin()+4, myvector.end(),
                                                               25
      found=str.find(str2);
12
                                                                          myfunction); // 12 32 45 71(26 33 53 80)
      if (found!=string::npos)
13
                                                                      // using object as comp
        \mathrm{cout} << "first 'needle' found at: " << \mathrm{int} ( \mathrm{found}^{26}
14
                                                                     sort (myvector.begin(), myvector.end(), myobject);
//(12 26 32 33 45 53 71 80)
             ) << endl;
15
      found = str. find ("needles are small", found + 1, 6);
                                                               28
16
                                                                     // if stable is need
                                                               29
      if (found!=string::npos)
17
                                                                      stable_sort (myvector.begin(), myvector.end(),
        cout << "second 'needle' found at: " << int(</pre>
18
                                                                          myfunction);
             found\,) \;<<\; endl\;;
                                                               31
19
                                                                     // Rearranges the elements in the range [first,
      found=str.find("haystack");
20
                                                                          last), in such a way that the subrange [first,
      if (found!=string::npos)
21
                                                                          middle)
        \mathrm{cout} << "'haystack' also found at: " << \mathrm{int}(
22
                                                                     // contains the smallest elements of the entire
             found) << endl;
                                                                          range sorted in ascending order, and the
23
                                                                          subrange
      found=str.find('.');
24
                                                                     // [middle, end) contains the remaining elements
                                                               34
      if (found!=string::npos)
25
                                                                          without\ any\ specific\ order.
        cout << "Period found at: " << int(found) <<</pre>
26
                                                                      partial_sort (myvector.begin(), myvector.begin()
                                                               35
             endl:
                                                                          +3, myvector.end());
27
                                                               36
      // let's replace the first needle:
28
                                                                      qsort (myints, 8, sizeof(int), compare);
      str.replace(str.find(str2),str2.length(),"
29
                                                               38
          preposition");
                                                               39
                                                                     return 0;
      cout << str << endl;
30
                                                               40
31
      \operatorname{string} \operatorname{str}="We think in generalities, but we live
32
                                                                                 Código 13: exemplo de ordenação
          in details.";
```

// quoting Alfred N.

Whitehead

1 5 int compareMyType (const void * a, const void * b)

```
1
      if (*(MyType*)a > *(MyType*)b) return 1;
                                                             2
      i f
         (*(MyType*)a == *(MyType*)b) return 0;
      if (*(MyType*)a < *(MyType*)b) return -1;
                                                             4
   int key = 40;
   item = (int*) bsearch (&key, values, n, sizeof (int)
        , compareMyType);
                   Código 14: pesquisa binária
                                                             9
                                                            10
   #include <iostream>
   #include <iomanip> // setprecision()
                                                            12
   using namespace std;
                                                            13
   int main () {
     double \vec{a} = 3.1415926534;
      double b = 2006.0;
      double c = 1.0e - 10;
                                                             2
      // setprecision(1) \Rightarrow 1 casa decimal apos a
                                                            3
          virgula
      cout << fixed << setprecision(1) << 9.09090901 << \frac{1}{5}
          endl;
      cout \ll fixed \ll setprecision(2) \ll 9.09090901 \ll
12
      cout << fixed << setprecision(3) << 9.09090901 << 9
13
          endl;
      cout << fixed << setprecision (2) << 9.1 << endl; _{11}
15
                                                            12
      // anula o efeito de setprecision
16
      cout.unsetf(ios::floatfield);
17
                                                            14
18
                                                            15
19
      // 5 digitos no maximo
                                                            16
      cout.precision(5);
20
                                                            17
21
      cout << a << '\t' << b << '\t' << c << endl;
22
                                                            19
      cout << fixed << a << '\t' << b << '\t' << c <<
23
          endl:
      cout << scientific << a << '\t' << b << '\t' << c^{21}
          \ll endl:
      // Sets the basefield format flag for the str
26
          stream to dec, hex or oct.
      int n = 70;
      cout << dec << n << endl;
28
29
      cout \ll hex \ll n \ll endl;
      cout << oct << n << endl;
30
31
32
      return 0;
   }
33
34
   /* output
35
   9.1
   9.09
36
   9.091
                                                             8
37
                                                             9
38
                                                            10
   3.1416 2006
                     1e - 10
39
                                                            11
   3.14159 2006.00000
                              0.00000
                                                            12
   3.14159e+00
                     2.00600e+03
                                       1.000000e\!-\!10
41
                                                            13
42
   70
   46
                                                            14
43
                                                            15
   106
44
                                                            16
45
   */
```

Código 15: Arredondamento e output em outras bases

2.2Teoria dos números

```
22
   int gcd(int x, int y)
                                                               23
                                                               24
      return y ? gcd(y, x \% y) : abs(x);
   }
                                                               26
   uint64_t lcm(int x, int y)
                                                               27
6
       if (x \&\& y) return abs(x) / gcd(x, y) * uint 64 - t<sub>2</sub>(y)
           abs(y));
       else return uint64_t(abs(x | y));
                                                               31
                                                               32
```

Código 16: máximo divisor comum e mínimo multiplo comum

```
bool isPrime(int n)
    if (n < 0) return isPrime(-n);
   if (n == 1) return true;
    if (n < 5 \mid \mid n \% 2 = 0 \mid \mid n \% 3 = 0) return (n = 0)
        = 2 \mid \mid n = 3);
   int \max P = sqrt(n) + 2;
   for (int p = 5; p < maxP; p += 6)
       if (n \% p = 0 \mid \mid n \% (p+2) = 0) return false
   return true;
```

Código 17: decide se um número é primo

```
typedef map<int , int> prime_map;
void squeeze (prime_map& M, int& n, int p)
   for (; n \% p == 0; n \neq p) M[p]++;
void factor (int n, prime_map& M)
    if (n < 0) return n = -n;
   if (n < 2) return;
   squeeze (M, n, 2);
   squeeze(M, n, 3);
   int \max P = sqrt(n) + 2;
   \mathbf{for} \ (\mathbf{int} \ p = 5; \ p < maxP; \ p +\!\!= 6)
       squeeze\left( M,\ n\,,\ p\right) ;
       squeeze(M, n, p+2);
   if (n > 1) M[n]++;
```

Código 18: Retorna a fatoração em números primos de abs(n).

Grafos 2.3

18 19 20

```
#define TAM 100
#define BRANCO 0
#define CINZA 1
#define PRETO 2
bool grafo [TAM] [TAM];
int pass [TAM];
bool dfs(int v)
   pass[v] = CINZA;
   for (int i = 0; i < TAM; i++)
      if (grafo[v][i])
          if (pass[i] == CINZA) return false;
          if (pass[i] == BRANCO && !dfs(i)) return
              false;
      }
   pass[v] = PRETO;
   return true;
}
bool aciclico()
   memset(pass, BRANCO, TAM*sizeof(int));
   for (int i = 0; i < TAM; i++)
      if (pass[i] == BRANCO)
          if (!dfs(i)) return false;
```

```
27
                                                                          return forest -> parent [i];
                                                                     }
36
                                                                 28
       return true;
                                                                 29
37
                                                                     void dsf_union(disjoint_set_forest_p forest, int i,
    }
                                                                 30
                                                                          int i)
              Código 19: Verifica se o grafo é aciclico.
                                                                 31
                                                                          int x = dsf_find_set(forest, i);
                                                                 32
                                                                          int y = dsf_find_set(forest, j);
                                                                 33
   #include <queue>
                                                                          if (forest -> rank[x] > forest -> rank[y])
                                                                 35
    \label{eq:typedef} \textbf{typedef} \ \ \text{vector} < \!\! \text{map} < \!\! \textbf{int} \, , \ \ \textbf{int} > > \ \ \text{AdjList} \, ;
                                                                 36
    typedef AdjList Grafo;
                                                                               forest \rightarrow parent[y] = x;
                                                                          }
                                                                 38
    int dist[MAX_VERTICES];
                                                                          else
    \mathbf{int} \  \, \mathbf{prev} \, \big[ \mathbf{MAX.VERTICES} \, \big] \, ; \  \, // \  \, \mathit{para} \  \, \mathit{recuperar} \  \, \mathit{o} \  \, \mathit{caminho}^{39} \,
                                                                 40
                                                                          {
         usando um dijoint forest set
                                                                               forest \rightarrow parent[x] = y;
                                                                 41
                                                                               if (forest -> rank[x] == forest -> rank[y])
                                                                 42
    void dijkstra(Grafo& grafo, int source)
9
                                                                 43
10
                                                                 44
                                                                                    forest \rightarrow rank[y]++;
       for (int i = 0; i < grafo.size(); i++)
11
                                                                 45
12
                                                                          }
                                                                 46
           dist[i] = INF;
13
                                                                 47
           prev[i] = -1;
14
15
                                                                                Código 21: Floresta dijunta de arvores
16
        dist[source] = 0;
17
        priority_queue<pair<int, int>> heap;
                                                                     typedef vector <map<int, int> > AdjList;
                                                                 1
       heap.push(make_pair(0, source));
19
                                                                     struct Grafo
                                                                 2
20
                                                                 3
                                                                     {
        while (!heap.empty())
21
                                                                         int edgeCnt;
                                                                 4
22
                                                                         AdjList adj;
                                                                 5
           int u = heap.top().second;
23
                                                                     };
                                                                 6
           heap.pop();
25
                                                                     struct edge
26
           // para cada vizinho de u
           for (map<int, int>::iterator i = grafo[u].begin
                                                                          int u;
                (); i != grafo[u].end(); i++)
                                                                 11
                                                                          int v;
                                                                 12
                                                                          int weight;
              int totalDist = dist[u] + (*i).second;
29
                                                                     };
                                                                 13
              if (totalDist <= dist[(*i).first])</pre>
30
                                                                 14
                                                                     int edge_compare(const void * e1, const void * e2)
                                                                 15
                  dist[(*i).first] = totalDist;
32
                                                                 16
                                                                     {
                  heap.push(make_pair(totalDist, (*i).
                                                                          struct edge * p1 = (struct edge *) e1;
                                                                 17
                       first));
                                                                 18
                                                                          struct edge * p2 = (struct edge *) e2;
                  prev[(*i).first] = u;
34
                                                                          int f = p1->weight - p2->weight;
                                                                 19
                                                                          if (f < 0)
                                                                 20
           }
36
                                                                 21
       }
37
                                                                             return -1;
                                                                 22
                                                                 23
                                                                          else if (f == 0)
     Código 20: Caminho minimo 1 para todos pesos positivos.<sup>24</sup>
                                                                               return edge_compare1(e1, e2);
                                                                 26
   #define SIZE 100
                                                                 27
                                                                          else
                                                                 28
    struct dsf
                                                                 29
                                                                               return 1;
4
                                                                 30
         int element_count;
                                                                 31
         int parent[SIZE];
                                                                 32
         int rank[SIZE];
                                                                 33
                                                                     struct edge * get_edge_list(Grafo& graph)
                                                                 34
    typedef struct dsf * disjoint_set_forest_p;
                                                                 35
                                                                          int edge_count = graph.edgeCnt;
10
                                                                 36
                                                                          struct edge *edges = (struct edge*) malloc(
    void dsf_init(disjoint_set_forest_p forest, int
                                                                 37
11
        element_count)
                                                                               edge_count * sizeof(struct edge));
12
                                                                 38
        forest -> element_count = element_count;
                                                                          int current_edge = 0;
13
       memset(forest->parent, 0, element_count*sizeof(40
14
            int));
                                                                          for (int i = 0; i < graph.adj.size(); ++i)
       memset (forest -> rank, 0, element_count * size of (int4)
15
                                                                               for (map<int, int>::iterator j = graph.adj[i
                                                                 43
                                                                                    ]. begin(); j != graph.adj[i].end(); j++)
16
17
        for (int i = 0; i < element\_count; ++i)
                                                                               {
                                                                 44
           forest->parent[i] = i;
18
                                                                 45
                                                                                   struct edge e;
19
   }
                                                                 46
                                                                                    e.u = i < (*j).first ? i : (*j).first;
                                                                                   e.v = i > (*j).first ? i : (*j).first;
20
                                                                 47
    int dsf_find_set(disjoint_set_forest_p forest, int 48
21
                                                                                   e.weight = (*j).second;
                                                                                    edges[current_edge++] = e;
    {
                                                                               }
22
                                                                 50
23
         if (i != forest ->parent[i])
                                                                 51
24
                                                                 52
             forest -> parent [i] = dsf_find_set (forest,
                                                                          return edges;
25
                                                                 53
                  forest -> parent [i]);
                                                                 54
```

⁵⁵ 7

```
void kruskal (Grafo& graph, Grafo& mst)
                                                             22
                                                                     sorted[nordem--] = no;
                                                                 }
57
   1
                                                             23
        // Obtain a list of edges and sort it by weight24
58
             in O(E lg E) time
                                                                 void topSort(int nvt)
                                                             25
        int edge_count = graph.edgeCnt;
59
                                                             26
                                                                 {
                                                                     memset(prof, UNVISITED, nvt*sizeof(int));
        struct edge *edges = get_edge_list(graph);
60
                                                             27
        qsort(edges, edge_count, sizeof(struct edge),
                                                                     nordem = nvt - 1;
61
                                                             28
             edge_compare);
                                                             29
                                                                     for (int i = 0; i < nvt; i++)
                                                              30
        disjoint_set_forest dsf;
63
                                                             31
64
                                                                        if (prof[i] == UNVISITED)
       dsf_init(&dsf, edge_count);
                                                             32
65
                                                             33
        for (int i = 0; i < edge\_count; ++i)
                                                                            prof[i] = 0;
66
                                                             34
                                                             35
                                                                            dfsTopsort(i);
67
             struct edge e = edges[i];
                                                             36
68
             int uset = dsf_find_set(dsf, e.u);
                                                                     }
69
                                                             37
             int vset = dsf_find_set(dsf, e.v);
             if (uset != vset)
71
                                                                  Código 24: faz a ordenação topológica de um grafo acíclico
72
                 mst.adj[e.u][e.v] = e.weight;
73
              mst.edgeCnt++;
74
                                                                 #define TAM 1000
75
                 dsf_union(dsf, uset, vset);
                                                                 #define MAX_INT 1000000
76
        }
77
                                                                 int grafo [TAM] [TAM];
                                                              4
78
                                                                 int pred [TAM];
        free (edges);
79
                                                                 int f [TAM] [TAM]
                                                              6
   }
80
                                                                 bool visitados [TAM];
            Código 22: Arvore geradora mínima kruskal
                                                                 int fila [TAM];
                                                              9
                                                                 bool bfs(int n, int ini, int fim)
                                                              10
   #define TAM 200
                                                             11
                                                                     int no, s = 0, e = 0;
                                                              12
   bool grafo [TAM] [TAM];
                                                              13
                                                                     fila[e++] = ini;
   int pass [TAM];
                                                             14
   int n:
                                                              15
                                                                     while (s != e)
6
                                                             16
    bool bipartido (int v, int color = 1)
                                                                        no = fila[s++];
                                                             17
                                                              18
9
       pass[v] = color;
                                                                        if (visitados [no]) continue;
                                                             19
       int thisColor = color;
                                                                        visitados [no] = true;
                                                             20
       bool ret = true:
11
                                                             21
                                                                        for (int i = 0; i < n; i++)
                                                             22
       color = color == 1 ? 2 : 1;
13
                                                             23
14
                                                                            if (!visitados[i])
                                                             24
       for (int i = 0; i < n; i++)
                                                             25
16
                                                                               if (grafo [no][i] - f[no][i] > 0)
                                                             26
          if (grafo[v][i])
17
                                                             27
                                                             28
                                                                                   pred[i] = no;
              if \ (!\,pass\,[\,i\,]) \ ret \, = \, dfs\,(i\;,\; color\,)\,;
19
                                                                                   if (i == fim) return true;
              else if (pass[i] = thisColor) return false
20
                                                                                   fila[e++] = i;
                                                             31
21
                                                                            }
                                                             32
              if (!ret) return false;
22
                                                                        }
                                                             33
          }
23
                                                             34
                                                                     }
       }
24
                                                             35
25
                                                                     return false;
                                                             36
       return ret;
26
                                                                 }
                                                             37
                                                             38
                                                             39
                                                                 bool dfs(int s, int t, int size)
            Código 23: verifica se um grafo é bipartido
                                                              40
                                                                     visitados[s] = true;
                                                              41
   #define UNVISITED -1
                                                              42
                                                                     if(s == t) return true;
                                                             43
   int grafo[SIZE][SIZE];
                                                                     for(int v = 0; v < size; v++)
                                                             44
   int prof[SIZE]
                                                              45
   int sorted[SIZE];
                                                                        if(!visitados[v] && grafo[s][v] - f[s][v] > 0)
                                                             46
   int nordem;
                                                             47
                                                                            pred[v] = s;
                                                              48
   void dfsTopsort(int no)
                                                                            if(dfs(v, t, size)) return true;
                                                             49
9
                                                             50
       for (int viz = 0; viz < SIZE; viz++)
10
                                                                     }
                                                             51
11
                                                             52
          if (grafo [no][viz])
                                                             53
                                                                     return false;
13
                                                             54
                                                                 }
              i\,f\ (\,\mathrm{prof}\,[\,\mathrm{viz}\,]\,=\!\!\!-\,\mathrm{UNVISITED})
14
                                                             55
                                                                 bool findPath(int s, int t, int size)
                                                             56
                 prof[viz] = prof[no] + 1;
16
                                                             57
                 dfsTopsort(viz);
                                                                     memset(visitados, false, sizeof(bool)*size);
17
                                                             58
                                                                     pred[s] = s;
                                                             59
18
                                                                     // Aqui pode ser usado tanto busca em largura
19
          }
                                                             60
       }
                                                                          quanto\ em\ profundidade .
20
```

⁶¹ 8

21

// busca em largura geralmente apresenta tempos

```
de execucao bem menores.
                                                            35
       \textbf{return} \hspace{0.1in} \text{bfs(size, s, t);} \\
                                                                       int ar = nar;
62
                                                            36
63
        //return dfs(s, t, size);
                                                            37
                                                                       cap[nar] = u;
64
                                                                       dest[nar] = j
                                                            38
                                                                       adj[i][nadj[i]] = nar++;
65
                                                            39
66
    int maxFlow(int size, int s, int t)
                                                            40
                                                                       nadj[i]++;
67
    {
                                                            41
       int delta;
68
                                                            42
                                                                       cap[nar] = 0;
                                                                       dest[nar] = i
69
                                                            43
       for (int i = 0; i < size; i++)
                                                                       adj[j][nadj[j]] = nar++;
70
                                                            44
71
                                                            45
                                                                       nadj[j]++;
           memset(f[i], 0, sizeof(int)*size);
72
                                                            46
                                                                       return ar:
73
                                                            47
74
                                                            48
75
       \mathbf{while}(1)
                                                                   void revbfs (int ini, int fim)
                                                            49
76
                                                            50
           bool path = findPath(s, t, size);
                                                                       int i, no, viz, ar;
77
           if (!path) break;
                                                                       queue<int> fila;
78
                                                            52
79
                                                            53
           delta = MAXJNT;
                                                                       memset(nivel, NULO, sizeof(nivel));
80
           for(int c = t; pred[c] != c; c = pred[c])
                                                                       memset(qtd, 0, sizeof(qtd));
81
                                                            55
82
                                                            56
              delta = min(delta, grafo[pred[c]][c] - f[ 57
                                                                       nivel[fim] = 0;
83
                                                                       fila.push(fim);
                  pred[c]][c]);
                                                            58
                                                            59
                                                                       while (!fila.empty())
85
                                                            60
           for(int c = t; pred[c] != c; c = pred[c])
                                                            61
86
87
                                                                          no = fila.front();
              f[pred[c]][c] += delta;
                                                                          fila.pop();
88
                                                            63
              f[c][pred[c]] -= delta;
                                                            64
                                                                          qtd[nivel[no]]++;
89
90
                                                            65
                                                                          for (i = 0; i < nadj[no]; i++)
91
                                                            66
       int soma = 0;
                                                                             ar = adj[no][i];
93
                                                            68
94
                                                            69
                                                                             viz = dest[ar];
       for(int i = 0; i < size; i++)
                                                                             if (cap[ar] = 0 \&\& nivel[viz] = NULO)
96
                                                            71
97
           soma += f[i][t];
                                                            72
98
                                                                                 nivel[viz] = nivel[no] + 1;
                                                            73
                                                                                 fila.push(viz);
99
                                                            74
100
       return soma;
                                                            75
                                                                          }
    }
101
                                                            76
                                                            77
                                                                       }
         Código 25: calcula fluxo máximo, Ford-Fulkerson
                                                            78
                                                            79
                                                                   int admissivel (int no)
                                                            80
    const int VT = 100;
                                                            81
    const int AR = VT * VT;
                                                                       while (padj[no] < nadj[no])
 2
                                                            82
 3
                                                            83
    struct grafo
                                                                          int ar = adj[no][padj[no]];
                                                            84
 5
    {
                                                                          if (nivel[no] == nivel[dest[ar]] + 1 &&
       // lista de adjacencias representada na forma de
                                                                              capres(ar) > 0) return ar;
            vetor
                                                                          padj[no]++;
                                                            86
       int nvt. nar:
                                                            87
       int dest[2 * AR];
                                                            88
       int adj [VT] [2 * VT];
 9
                                                                       padj[no] = 0;
                                                            89
       int nadj [VT];
10
                                                            90
                                                                       return NULO;
                                                            91
       int cap[AR]; // capacidade do arco
12
                                                            92
13
       int fluxo [AR];
                                                                   int retrocede (int no)
                                                            93
       int ent[VT];
14
                                                            94
15
                                                            95
                                                                       int i, ar, viz, menor = NULO;
       int padj[VT], lim[VT], nivel[VT], qtd[VT];
16
                                                            96
                                                                       if (--qtd[nivel[no]] == 0) return NULO;
17
                                                            97
       int inv(int a) { return a ^{\circ} 0x1; }
18
                                                            98
       int orig(int a) { return dest[inv(a)]; }
                                                                       for (i = 0; i < nadj[no]; i++)
19
                                                            99
       int capres(int a) { return cap[a] - fluxo[a]; }<sub>100</sub>
20
21
                                                                          ar = adj[no][i]; viz = dest[ar];
       void inic(int n = 0)
                                                                          if (capres(ar) <= 0) continue;
if (menor == NULO || nivel[viz] < nivel[</pre>
22
                                                           102
23
                                                           103
24
           nvt = n;
                                                                              menor]) menor = viz;
25
           nar = 0;
                                                           104
           memset(nadj, 0, sizeof(nadj));
26
                                                           105
27
                                                                       if (menor != NULO) nivel[no] = nivel[menor];
                                                           106
28
                                                                       qtd[++nivel[no]]++;
                                                           107
29
            // Adiciona uma aresta ao grafo.
30
                                                           110
31
                                                           111
           "int u" apenas para Fluxos;
32
                                                           112
                                                                   int avanca (int no, int ar)
33
                                                           113
                                                                   {
       int aresta(int i, int j, int u = 0)
```

```
int viz = dest[ar];
       ent[viz] = ar;
      \lim [\operatorname{viz}] = \min(\lim [\operatorname{no}], \operatorname{capres}(\operatorname{ar}));
      return viz:
   int aumenta(int ini, int fim)
      int ar, no = fim, fmax = lim [fim];
       while (no != ini)
          fluxo[ar = ent[no]] += fmax;
          fluxo[inv(ar)] = fmax;
          no = orig(ar);
      return fmax;
   int maxflow(int ini, int fim)
       int ar, no = ini, fmax = 0;
       memset(fluxo, 0, sizeof(fluxo));
      memset(padj, 0, sizeof(padj));
       revbfs(ini, fim);
      \lim [ini] = INF;
      ent[ini] = NULO;
       while (nivel[ini] < nvt && no != NULO)
          if ((ar = admissivel(no)) == NULO)
          {
             no = retrocede(no);
          else if ((no = avanca(no, ar)) = fim)
             fmax += aumenta(ini, fim);
             no = ini;
      return fmax;
   }
};
```

20

21

22

23

24

26

28

29

30

32

33

34

35

36

37

38

39

40

42

43

44

45

46

47

48

49

2

3

4

4

6

7

Código 26: calcula fluxo máximo, algoritmo mais eficiente porém muito maior em tempo de codificação

2.4 Geometria

115

116

117

118

119

120

121

122

123

124

125

126

127

128

129

131

132

133

134

135

136

137

138

139

 $\frac{140}{141}$

142

143

144 145

147

148

149

150 151

152

153

154

155

156

157

158

159

```
1
    struct point
                                                                       9
2
    {
                                                                      10
        double x, y;
3
        double z; // para pontos no espa o
        point (double x = 0, double y = 0, double z = 0):<sub>12</sub>
             x\,(\,x\,)\;,\;\;y\,(\,y\,)\;,\;\;z\,(\,z\,)\;\;\{\,\}
        point operator +(point q) \{ return point(x + q.x_{14}) \}
             y + q.y, z + q.z); 
        point operator -(point q) { return point(x - q.x_{16})
             y - q.y, z - q.z); 
        point operator *(double t) { return point(x * t,
             y * t, z * t); }
        point operator /(double t) { return point(x / t,
10
             y / t, z / t); }
        double operator *(point q) { return x * q.x + y *
11
              q.y + z * q.z; }
        point vec(point q) { return point(y * q.z - z * q)
             .y, z * q.x - x * q.z, x * q.y - y * q.x); }
        double operator %(point q) { return x * q.y - y *
13
              q.x; }
14
15
        int cmp(point q) const
                                                                       9
16
            if (int t = ::cmp(x, q.x)) return t;
17
                                                                      10
            \label{eq:else} \begin{array}{lll} \textbf{else} & \textbf{if} & (\textbf{int} & t \ = \ :: cmp(\texttt{y}\,, \ \texttt{q}\,.\,\texttt{y}\,)\,) & \textbf{return} & t\,; \end{array}
                                                                      11
            return :: cmp(z, q.z);
                                                                      ^{12}10^{}
```

```
}
   bool operator ==(point q) const { return cmp(q)
       == 0:  }
   bool operator !=(point q) const { return cmp(q)
      != 0; }
   bool operator < (point q) const { return cmp(q) <
   friend ostream& operator <<(ostream& o, point p)
     return o << "(" << p.x << ", " << p.y << ", "
        << p.z << ")";
   static point pivot;
};
// para pontos 2D
double abs(point p) { return hypot(p.x, p.y);
double arg(point p) { return atan2(p.y, p.x);
point point :: pivot;
typedef vector<point> polygon;
int ccw(point p, point q, point r)
   return cmp((p - r) \% (q - r));
double angle (point p, point q, point r)
   point u = p - q, v = r - q;
   return atan2(u \% v, u * v);
              Código 27: ponto e poligono
```

Código 28: Decide se q está sobre o segmento fechado pr.

```
bool seg_intersect(point p, point q, point r, point s)

{
    point A = q - p;
    point B = s - r;
    point C = r - p;
    point D = s - q;

    int a = cmp(A % C) + 2 * cmp(A % D);
    int b = cmp(B % C) + 2 * cmp(B % D);

    if (a == 3 || a == -3 || b == 3 || b == -3)
        return false;
    if (a || b || p == r || p == s || q == r || q == s) return true;

    int t = (p < r) + (p < s) + (q < r) + (q < s);
    return t != 0 && t != 4;
```

Código 29: Decide se os segmentos fechados p
q ${\bf e}$ rs têm pontos em comum.

```
double seg_distance(point p, point q, point r)
{
    point A = r - q;
    point B = r - p;
    point C = q - p;

    double a = A * A, b = B * B, c = C * C;

    if (cmp(b, a + c) >= 0) return sqrt(a);
    else if (cmp(a, b + c) >= 0) return sqrt(b);
    else return fabs(A % B) / sqrt(c);
}
```

```
Código 30: Calcula a distância do ponto r<br/> ao segmento p\mathbf{q}_{i_8}^{"}
                                                            20
   int in-poly (point p, polygon& T)
                                                            21
                                                            22
       double a = 0:
                                                            23
       int N = T. size();
       for (int i = 0; i < N; i++)
                                                            25
          if (between(T[i], p, T[(i+1) \% N])) return
          a \leftarrow angle(T[i], p, T[(i+1)\% N]);
                                                            28
                                                            29
       return cmp(a) != 0;
10
                                                            30
   }
11
                                                            31
   Código 31: Classifica o ponto p em relação ao polígono T<sup>2</sup>:
   Retorna 0, -1 ou 1 dependendo se p está no exterior, nã
   fronteira ou no interior de T, respectivamente.
                                                            36
                                                            37
                                                            38
   2.5
          Outros
                                                            39
                                                            40
                                                            41
   The Josephus problem (or Josephus permutation) is a
        theoretical\ problem\ related\ to\ a\ certain
        counting-out game. There are people standing in
        a circle waiting to be executed. After the first
        man is executed, certain number of people are
        skipped and one man is executed. Then again,
        people are skipped and a man is executed. The
        elimination proceeds around the circle (which is
         becoming smaller and smaller as the executed
        people are removed), until only the last man
        remains, who is given freedom. The task is to
        choose\ the\ place\ in\ the\ initial\ circle\ so\ that
        you are the last one remaining and so survive.
   using namespace std;
   int josephus (int n, int m)
       int res = 0:
       vector <int> people;
       int loc = 0;
11
12
       for (int i = 0; i < n; i++) people.push_back(i+1)
       while (people.size() > 1)
15
16
          if (loc >= people.size())
             loc %= people.size();
18
                                                            10
19
          people.erase(people.begin()+loc);
20
                                                            12
          loc += (m-1);
21
                                                            13
22
                                                            14
23
                                                            15
       return people [0];
24
                                                            16
                                                            17
                   Código 32: josephus problem
                                                            18
                                                            19
   bool nextPermutation(string& number)
                                                            20
   {
                                                            21
           bool is Bigger = true;
                                                            22
           int i, j;
                                                            23
                                                            24
           for (i = number.size() - 1; i >= 0; i--)
                                                            25
                    if (number [i] < number [i+1]) break; 26
           if (i != -1)
11
                                                            29
12
```

isBigger = false;

for $(j = number.size() - 1; j >= i+k_2$

13 14

Código 33: Gera as permutações dos elementos da string

3 Biblioteca C/C++

3.1 I/O

Ignorando entradas na família scanf:

```
scanf("%f %*f %*f %d", &a, &b);
```

Código 34: Ignora os dois floats do meio. Retornará 2 no sucesso.

3.2 Map

30

```
#include <map>
#include <string>
#include <cstdio>
using namespace std; // USE ISTO!!!
class Comparadora:
class Pessoa {
   int idade:
   string nome;
   friend class Comparadora;
public:
   Pessoa (string nome, int idade) {
      this->idade = idade;
      this->nome = nome;
   void print() const {
       printf("Nome: %s Idade: %d\n", nome.c_str(),
          idade);
};
class Comparadora { // Ordena crescentemente
public: // <- IMPORTANTE</pre>
   bool operator() (const Pessoa &a, const Pessoa &b
      int idDif = a.idade-b.idade;
       if(idDif < 0) return true;</pre>
      else if (idDif==0) return a.nome.compare(b.nome
          ) < 0 ? true : false;
      else return false;
};
```

```
int main() {
             Pessoa r("Rangelz", 86);
35
             Pessoa r2("Rangelzao", 86);
36
37
             \label{eq:pessoa} \begin{array}{l} \text{map}{<} \text{Pessoa} \;, \; \; \text{string} \;, \; \; \text{Comparadora}{>} \; \; \text{alunos} \; ; \\ \text{alunos} \; [\; r\; ] = \text{"UFMG"} \; ; \end{array}
38
39
             alunos[r2]="PUC";
40
             // Iterator
for (map<Pessoa, string, Comparadora>::iterator it
=alunos.begin(); it != alunos.end(); it++) {
41
42
                    it -> first.print();
printf("\t%s\n\n", it -> second.c_str());
43
44
45
              // Find
46
             if(alunos.find(Pessoa("Rangelz", 86)) != alunos.
  end()) { // Achou!
  printf("Achei Rangel!\n");
47
48
49
             \textbf{return} \quad 0\,;
50
       }
```

Código 35: Referencias map