Algorithms: Assignments

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1 Find a number in Sorted List

<u>Input</u>: A sorted list L of n numbers, and a number v. The list L can contain repeated values

 $\underline{\hbox{Output:}}$ Position of first occurrence of v in L, or raise a value error if v is not found in L

Solution:

```
def find_binary(L, v):
         left=0
         right = len(L)
         if (L[0] = v): return 0;
         while ((right-left) > 1):
                 m = (left + right)/2
                  \mathbf{if} \ (L[m] = v):
                           if (L[m-1] = v):
                                    right = m
                           {f else}:
                                    return m
                  if (L[m] < v):
                           left = m
                  else:
                           right = m
         raise ValueError('Value_is_not_in_list')
L = [0, 5, 9, 9, 10, 15, 20];
print (find_binary(L,20))
```

2 Recursive version of Find maximum number in List

 $\frac{\text{Input: A list L of n numbers. The list L can contain repeated values}}{\frac{\text{Output: }}{\text{Maximum value in L, or raise a value error if L is empty (like built-in function max())}}$

```
def Max(list):
    if len(list)==0:
        raise ValueError('Empty_list')
    elif len(list) == 1:
        return list[0]
    else:
        m = Max(list[1:])
        return m if m > list[0] else list[0]
L=[-5,-16,5,9,0];
print (Max(L))
```

3 Find a number in Sorted List, recursive version

 $\overline{\text{Input:}}$ A sorted list L of n numbers, and a number v. The list L can contain repeated values

<u>Output:</u> Position of first occurrence of v in L, or raise a value error if v is not found in L Solution:

```
def findB(L,V):
    N = len(L)
    if N == 0:
        raise ValueError ('Value_is_not_a_list')
    if N==1:
        if L[0]==V:
            return 0
        raise ValueError ('Value_is_not_in_the_list')
    m = N/2
    if V=L[m]:
        if V=L[m]:
        return findB(L[:m],V)
    return m
    if V<L[m]:
        return findB(L[:m],V)</pre>
```

```
return m+findB(L[m:],V)

L=[0,9,9,9,10,12]
print (findB(L,9))
```

4 Enumerating k-mers lexicographically

Input: A collection of at most 10 symbols defining an ordered alphabet, and a positive integer n.

Output: All strings of length n that can be formed from the alphabet, ordered lexicographically.

```
def alpha_combs(alphabet, n, acc='', res=[]):
    if n == 0:
        res.append(acc)
    else:
        for c in alphabet:
            alpha_combs(alphabet, n - 1, acc + c, res)
    return res

alphabet = ['A', 'T', 'C', 'G']
n=2
t= alpha_combs(alphabet, n)

for i in t:
        print i
#AA AT AC AG TA TT TC TG CA CT CC CG GA GT GC GG
```

5 Find k-mer in string with higher number of occurrences

6 Finding a Motif in DNA

Given two strings s and t, t is a substring of s if t is contained as a contiguous collection of symbols in s (as a result, t must be no longer than s). The position of a symbol in a string is the total number of symbols found to its left, including itself (e.g., the positions of all occurrences of 'U' in "AUGCUUCA-GAAAGGUCUUACG" are 1, 4, 5, 14, 16, and 17). The symbol at position i of s is denoted by s[i]. A substring of s can be represented as s[j:k], where j and k represent the starting and ending positions of the substring in s; for example, if s = "AUGCUUCAGAAAGGUCUUACG", then s[1:4] = "UGCU". The location of a substring s[j:k] is its beginning position j; note that t will have multiple locations in s if it occurs more than once as a substring of s (see the Sample below).

Input: Two DNA strings s and t (each of length at most 1 Kbp). Output: All locations of t as a substring of s.

```
seq = "GATATATGCATATACTT_"
subs ="ATAT"
# Start with this value.
location = -1

# Loop while true.
while True:
    # Advance location by 1.
    location = seq.find(subs, location + 1)

# Break if not found.
    if location == -1: break

# Display result.
    print(location)
#1
#3
#9
```

7 Find minimum length path between N cities

Input: N cities + distance between cities Output: a path traversing all cities with minimum length

```
import math
from itertools import permutations
def randList(N,a,b):
import random
 return [random.randint(a,b) for i in range(0,N)]
def randCities (N, SZ):
return zip(range(0,N), randList(N,0,SZ), randList(N,0,SZ))
def distance (x,y):
        return math. sqrt ((x[1] - y[1]) **2 + (x[2] - y[2]) **2)
def bruteForce (points):
        return min([perm for perm in permutations(points)],
    key=total_distance)
def total_distance(points):
         return sum([distance(point, points[index + 1])
     for index, point in enumerate (points [:-1])
lista=randCities (4,8)
print(lista)
print (total_distance(bruteForce(lista)))
print(bruteForce(lista))
```

8 Find minimum length path between N cities

Input: N cities + distance between cities Output: a path traversing all cities with minimum length

```
import math
from itertools import permutations

def randList(N,a,b):
   import random
   return [random.randint(a,b) for i in range(0,N)]

def randCities(N,SZ):
   return zip(range(0,N), randList(N,0,SZ), randList(N,0,SZ)))
```

```
\mathbf{def} distance (x,y):
        return math. sqrt ((x[1] - y[1])**2 + (x[2] - y[2])**2)
def heuristic (points):
        must_visit = points
        path = [points [0]]
        must_visit.remove(points[0])
        while must_visit:
                 nearest = min(must_visit, key=lambda x:
        distance(path[-1], x))
                path.append(nearest)
                must_visit.remove(nearest)
        print (path)
        return path
def total_distance(points):
         return sum([distance(point, points[index + 1])
     for index, point in enumerate(points [:-1])
lista=randCities (4,8)
print(lista)
print (total_distance(heuristic(lista)))
```