

University of Southern California

Viterbi School of Engineering

**EE599 (to be EE595)**  
**Software Design and Optimization**

**Data Structures – CLLs, DLLs**

# Singly Linked List Review

- Used structures/classes and pointers to make '**linked**' data structures
- Singly-Linked Lists dynamically allocates each item when the user decides to add it.
- Each item includes a 'next' pointer holding the address of the following Item object
- **Traversal and iteration is only easily achieved in one direction**

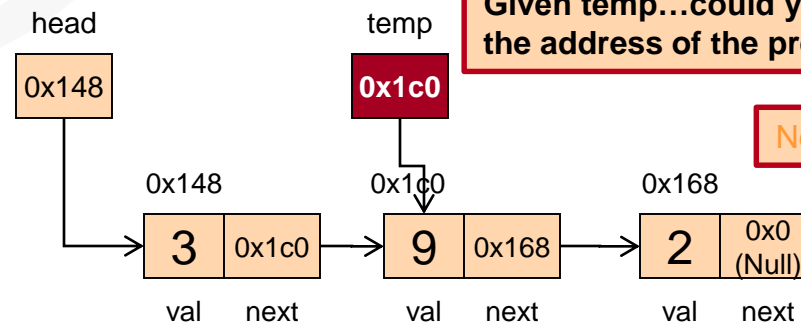
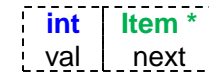
```
#include<iostream>

using namespace std;

struct Item {
    int val;
    Item* next;
};

class List
{
public:
    List();
    ~List();
    void push_back(int v); ...
private:
    Item* head;
};
```

struct Item blueprint:

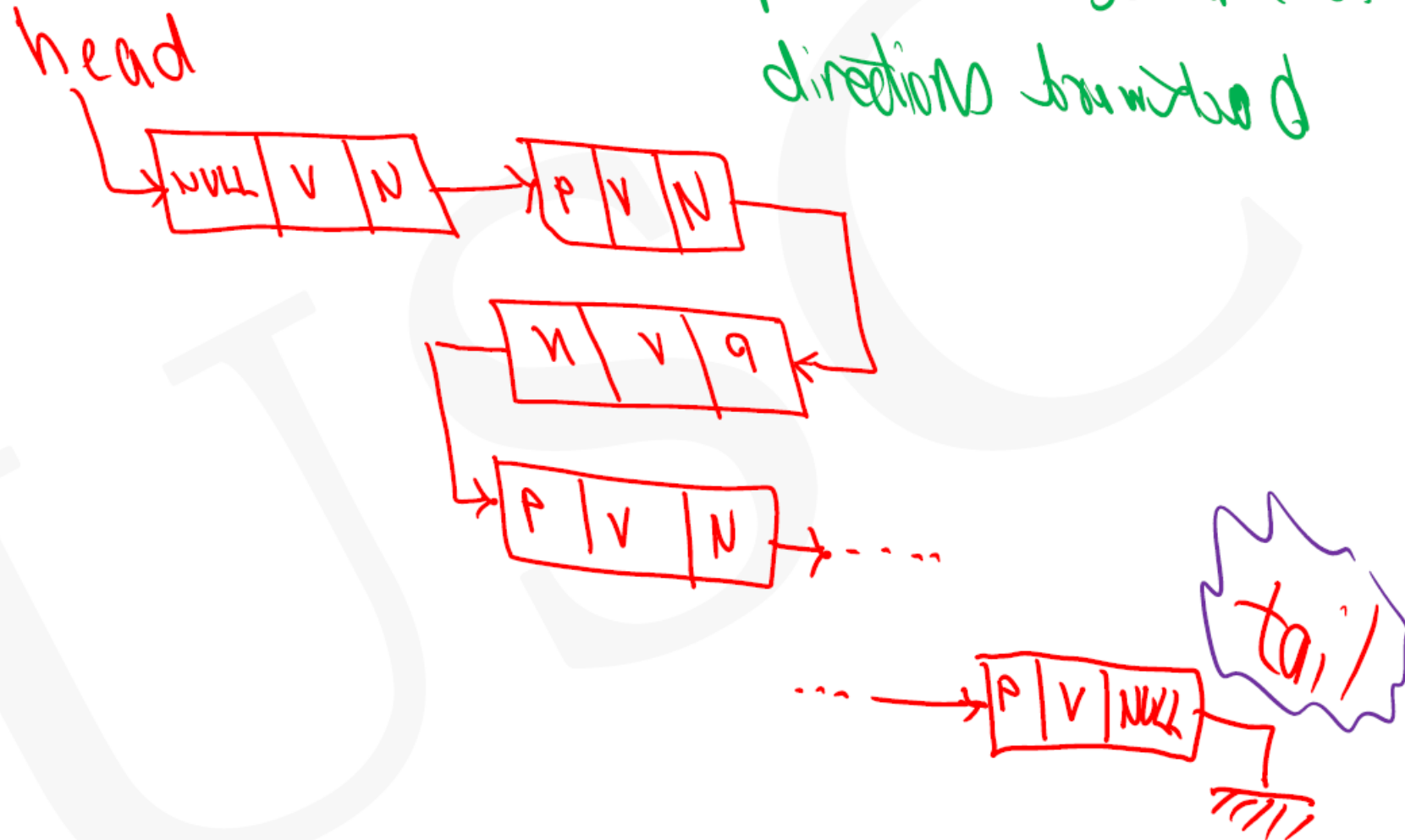


Given temp...could you ever recover the address of the previous item?

No!!!

# Motivation

Traversal possible in forward & directions bounded



# DLL

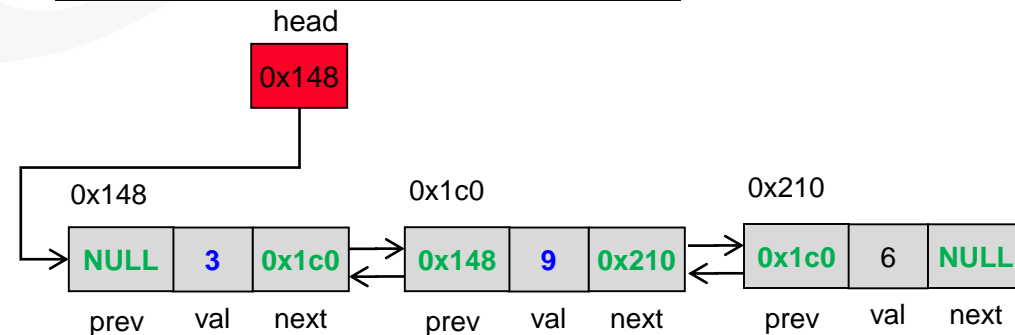
- Includes a previous pointer in each item so that we can traverse/iterate backwards or forward
- First item's previous field should be NULL
- Last item's next field should be NULL

```
#include<iostream>

using namespace std;
struct DLItem {
    int val;
    DLItem* prev;
    DLItem* next;
};

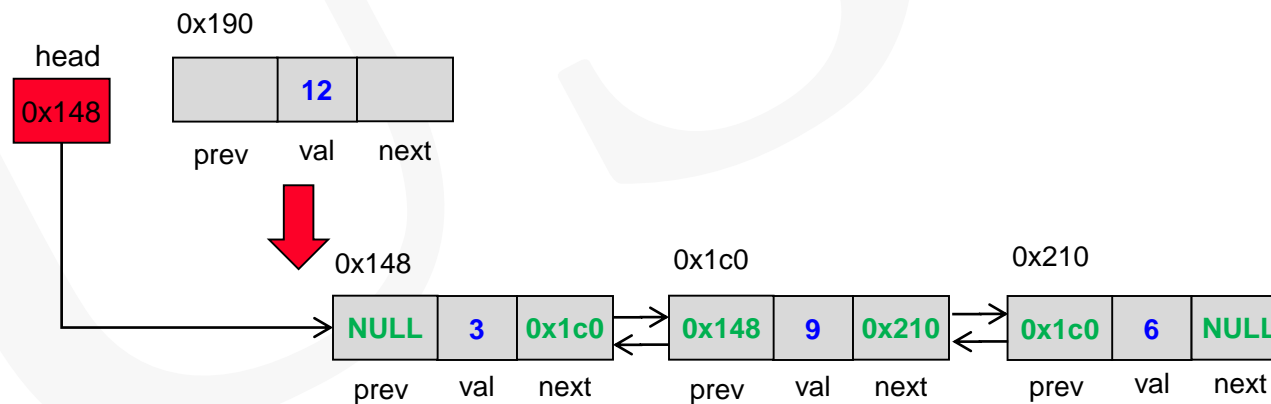
class DLLList
{
public:
    DLLList();
    ~DLLList();
    void push_back(int v); ...
private:
    DLItem* head;
};
```

struct Item blueprint:

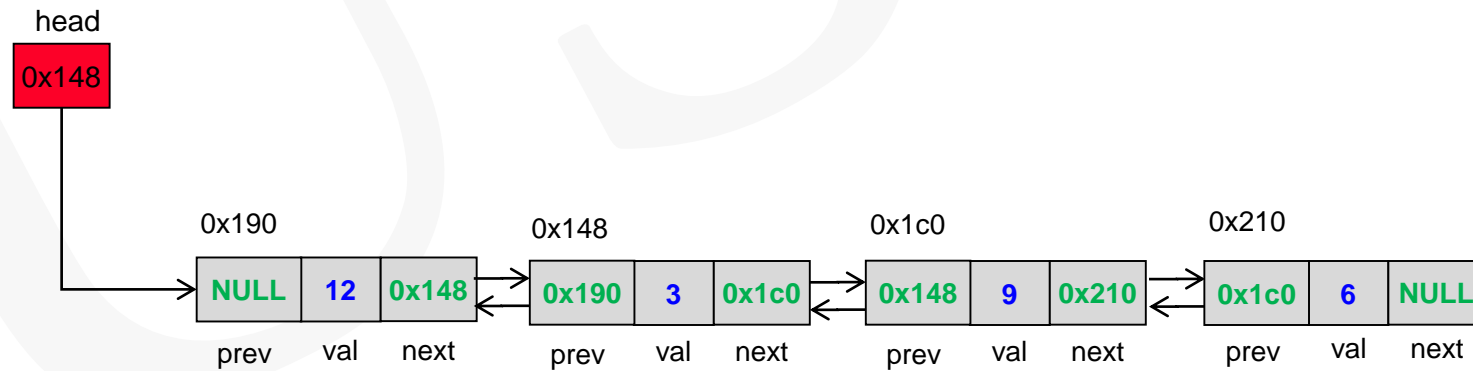


# DLL – Add Front

- Adding to the front requires you to update...
  - Head
  - New front's next & previous
  - Old front's previous

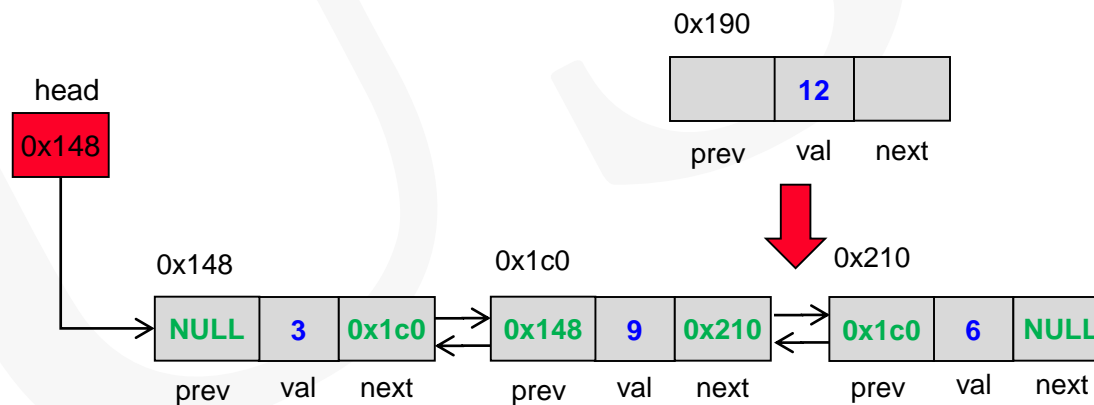


# DDL – Add Front (cont.)

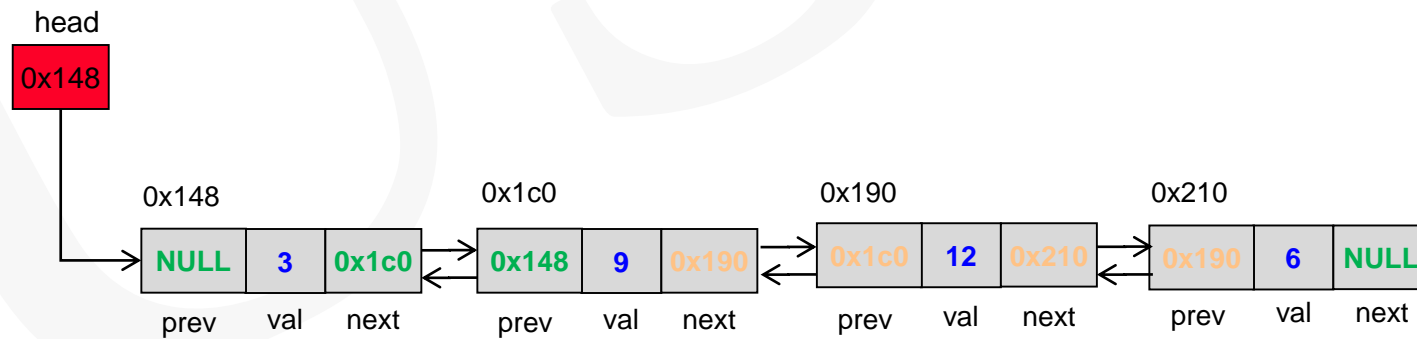


# DLL – Add Middle

- Adding to the middle requires you to update...
  - Previous item's next field
  - Next item's previous field
  - New item's next field
  - New item's previous field



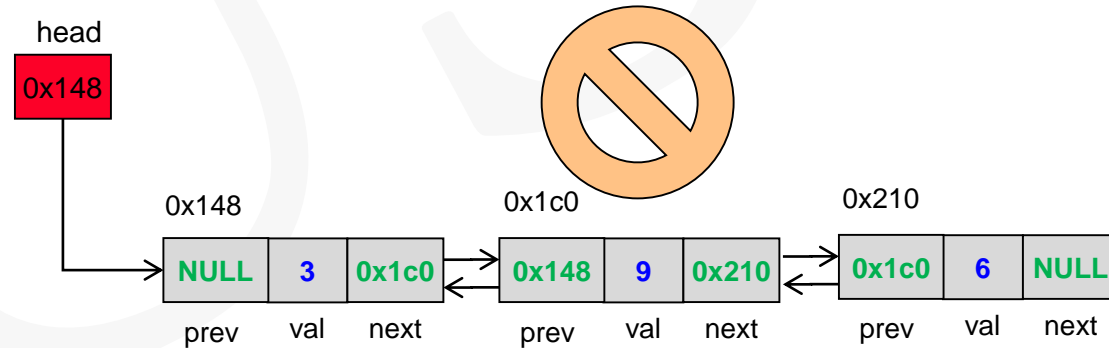
# DLL – Add Middle (cont.)



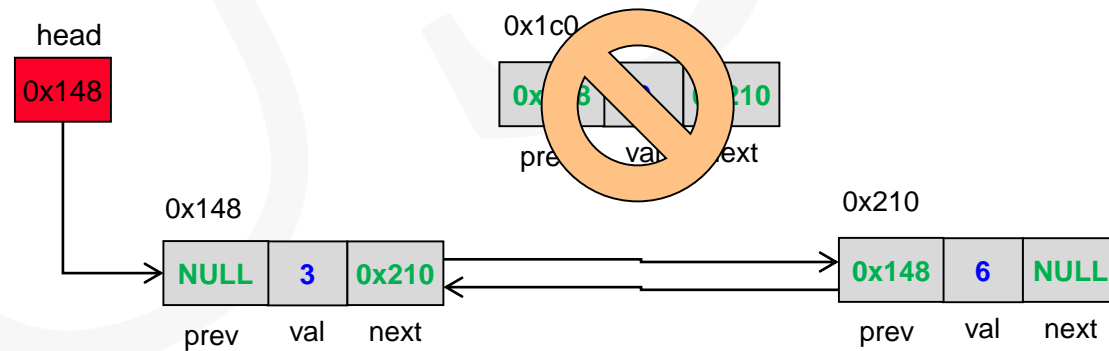


# DLL – Remove Middle

- Removing from the middle requires you to update...
  - Previous item's next field
  - Next item's previous field
  - Delete the item object



# DLL – Remove Middle (cont.)

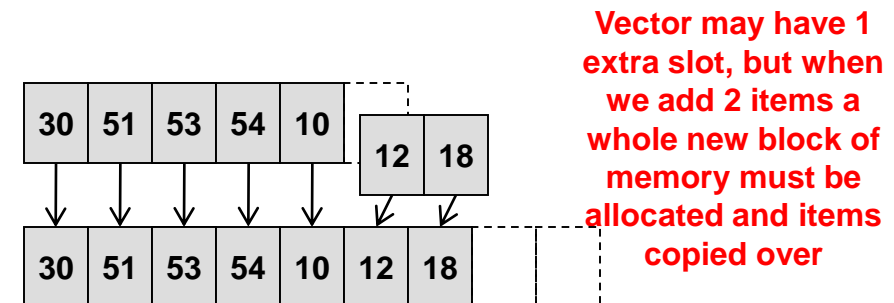
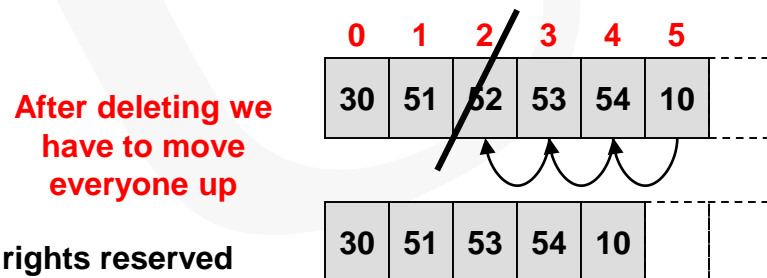


Using a Doubly-Linked List to Implement a Deque

# DEQUES AND THEIR IMPLEMENTATION

# Understanding Performance

- Recall vectors are good at some things and worse at others in terms of performance
- The Good:
  - Fast access for random access (i.e. indexed access such as `myvec[6]`)
  - Allows for 'fast' addition or removal of items at the back of the vector
- The Bad:
  - Erasing / removing item at the front or in the middle (it will have to copy all items behind the removed item to the previous slot)
  - Adding too many items (vector allocates more memory than needed to be used for additional `push_back()`'s...but when you exceed that size it will be forced to allocate a whole new block of memory and copy over every item)



# Deque Class

- Double-ended queues (like their name sounds) allow for efficient (fast) additions and removals from either 'end' (*front or back*) of the list/queue
- Performance:
  - Slightly slower at random access (i.e. array style indexing access such as: `data[3]`) than vector
  - Fast at adding or removing items at *front* or *back*

# Deque Class

- Similar to vector but allows for `push_front()` and `pop_front()` options
- Useful when we want to put things in one end of the list and take them out of the other



```
#include <iostream>
#include <deque>

using namespace std;

int main()
{
    deque<int> my_deq;
    for(int i=0; i < 5; i++){
        my_deq.push_back(i+50);
    }
    cout << "At index 2 is: " << my_deq[2] ;
    cout << endl;

    for(int i=0; i < 5; i++){
        int x = my_deq.front();
        my_deq.push_back(x+10);
        my_deq.pop_front();
    }
    while( ! my_deq.empty()){
        cout << my_deq.front() << " ";
        my_deq.pop_front();
    }
    cout << endl;
}
```

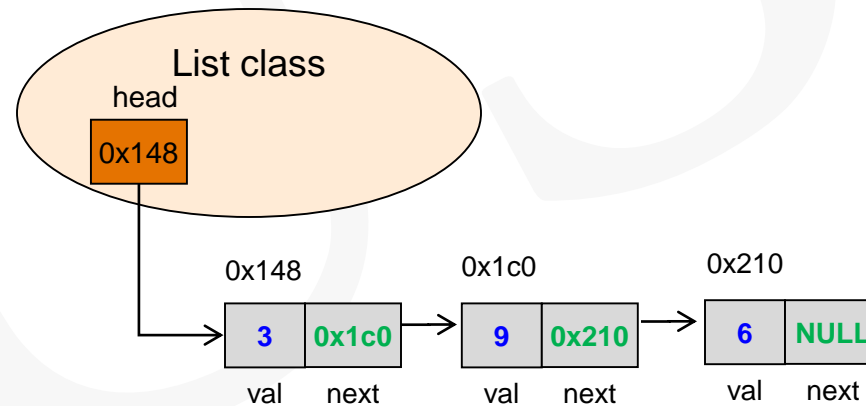
# Deque Implementation

- Let's consider how we can implement a deque
- Could we use a singly-linked list and still get fast (i.e.,  $O(1)$ ) insertion/removal from both front and back?

USC

# SLL Deque

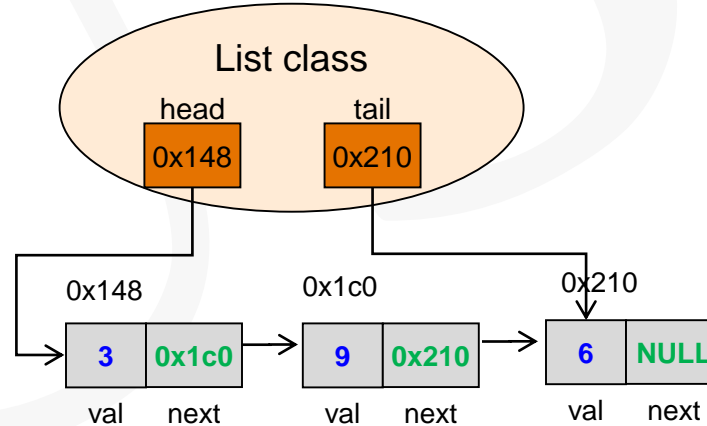
- Recall a deque should allow for fast (i.e.,  $O(1)$ ) addition and removal from front or back
- In our current singly-linked list we only know where the front is and would have to traverse the list to find the end (tail)





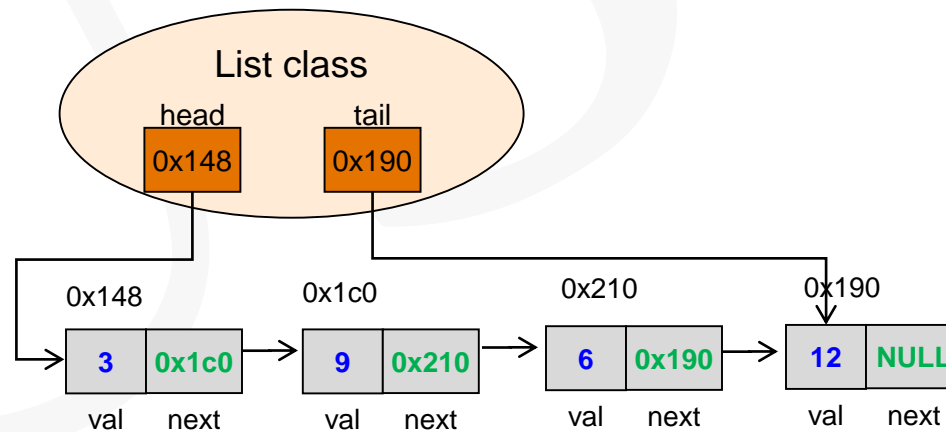
# Option 1: SLL + Tail Pointer

- We might think of adding a tail pointer data member to our list class
  - How fast could we add an item to the end?



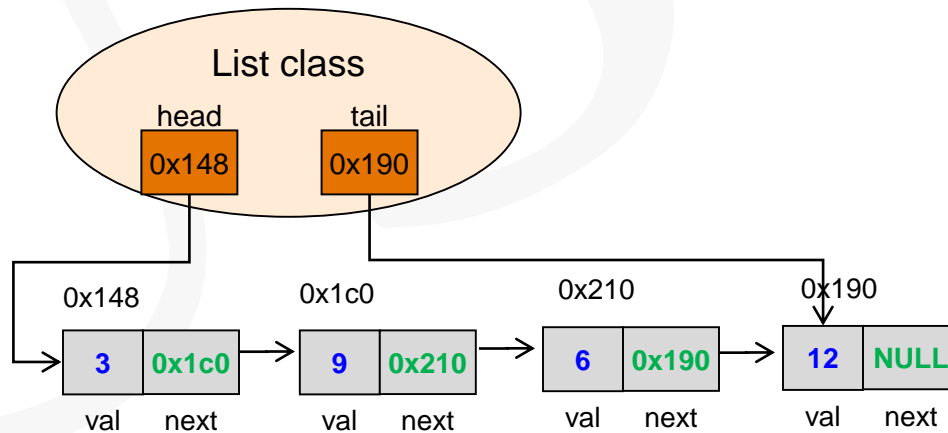
# Option 1: (cont.)

- How fast could we add an item to the end?  $O(1)$
- How fast could we remove the tail item?



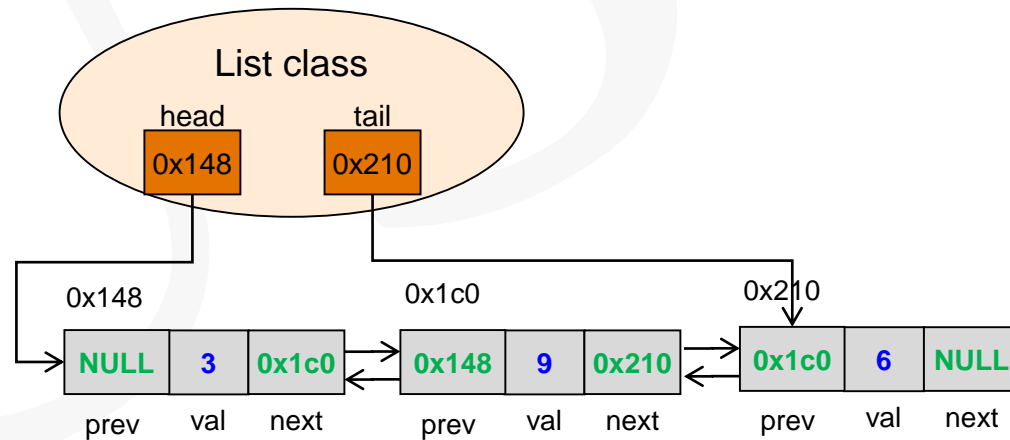
# Option 1 (cont.)

- How fast could we add an item to the end?  $O(1)$
- How fast could we remove the tail item?  $O(n)$ 
  - Would have to walk to the 2<sup>nd</sup> to last item



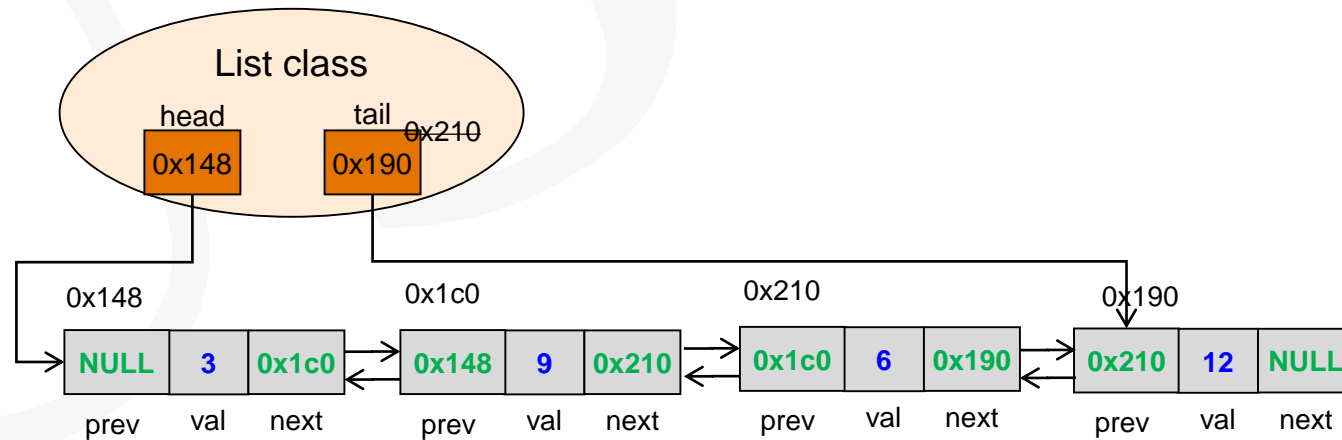
# Option 2: Tail Pointer + DLL

- We might think of adding a tail pointer data member to our list class
  - How fast could we add an item to the end?



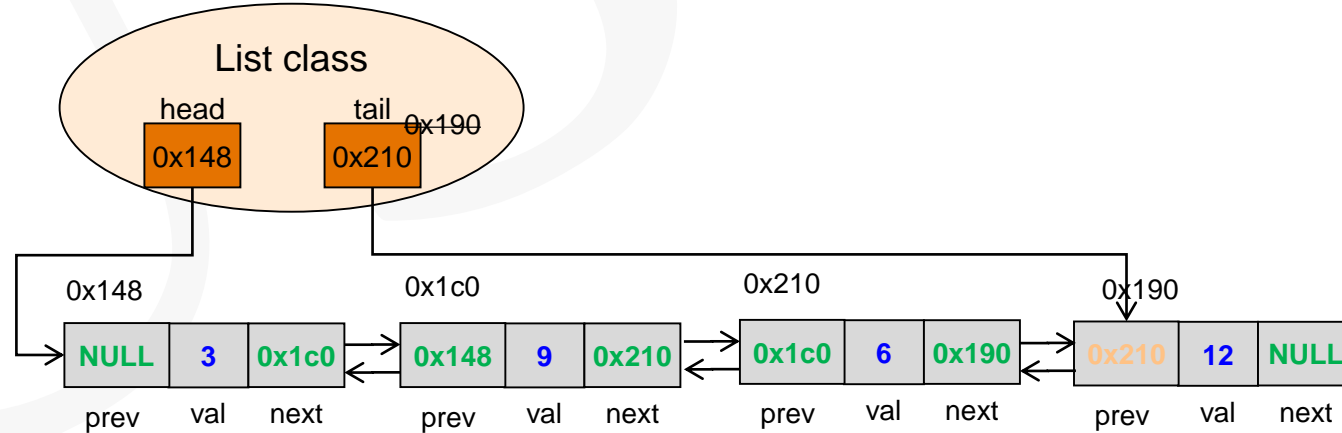
## Option 2 (cont.)

- How fast could we add an item to the end?  $O(1)$
- How fast could we remove the tail item?

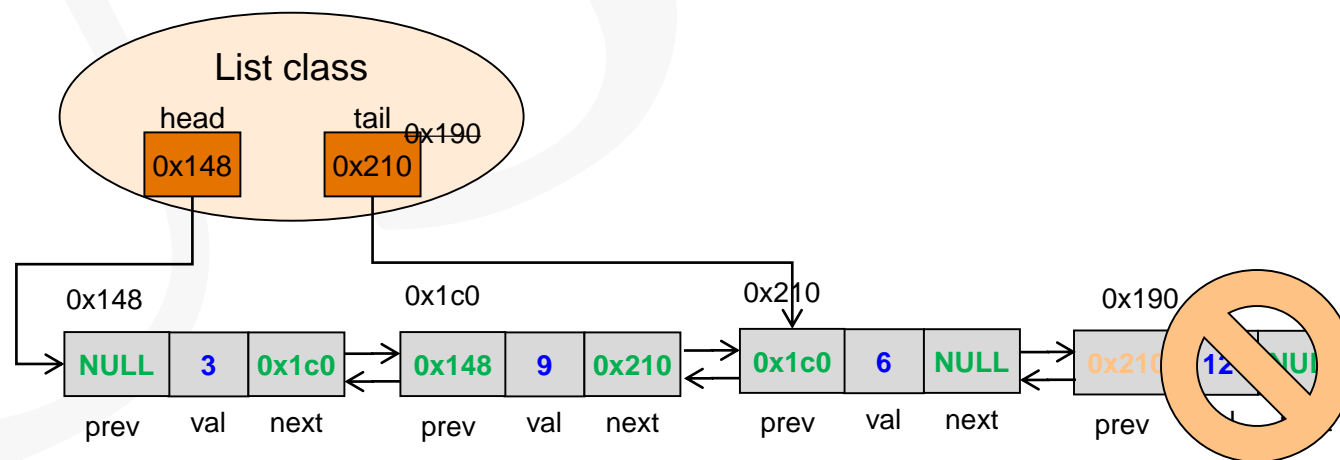


## Option 2 (cont.)

- How fast could we remove the tail item?  $O(1)$ 
  - We use the PREVIOUS pointer to update tail

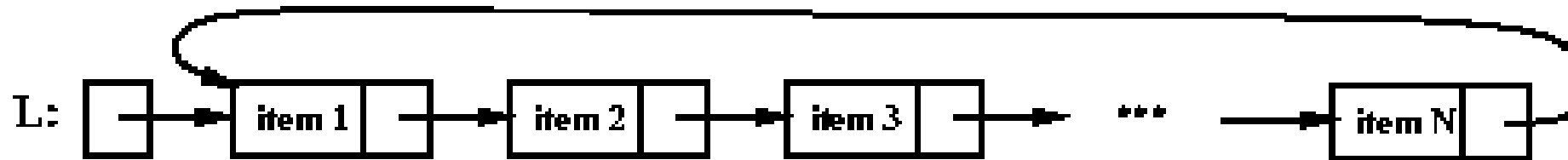


## Option 2 (cont.)

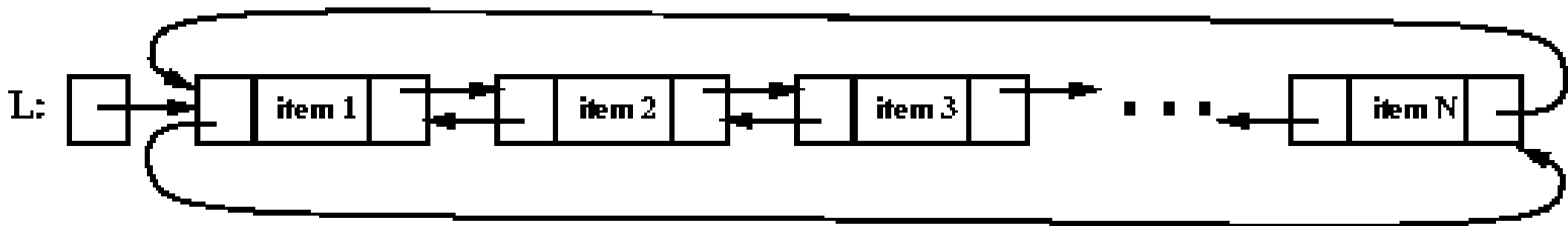


# Circular Lists

**Circular, singly linked list:**



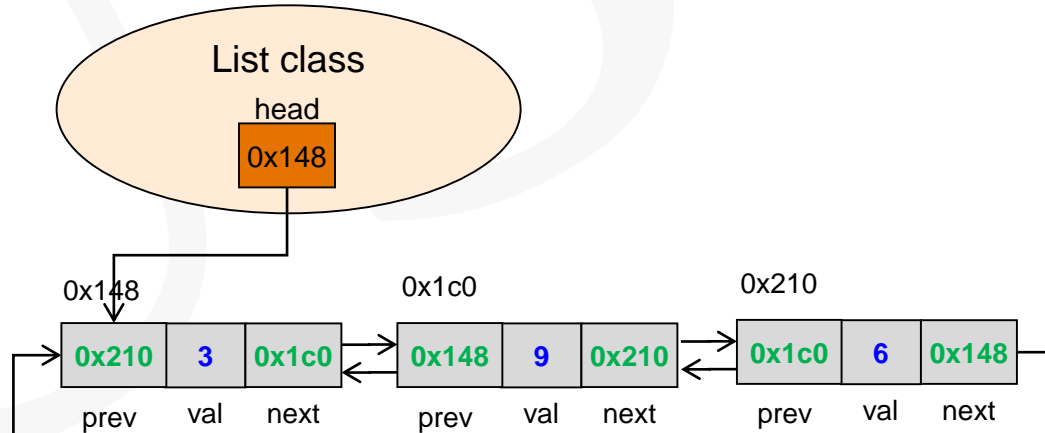
**Circular, doubly linked list:**





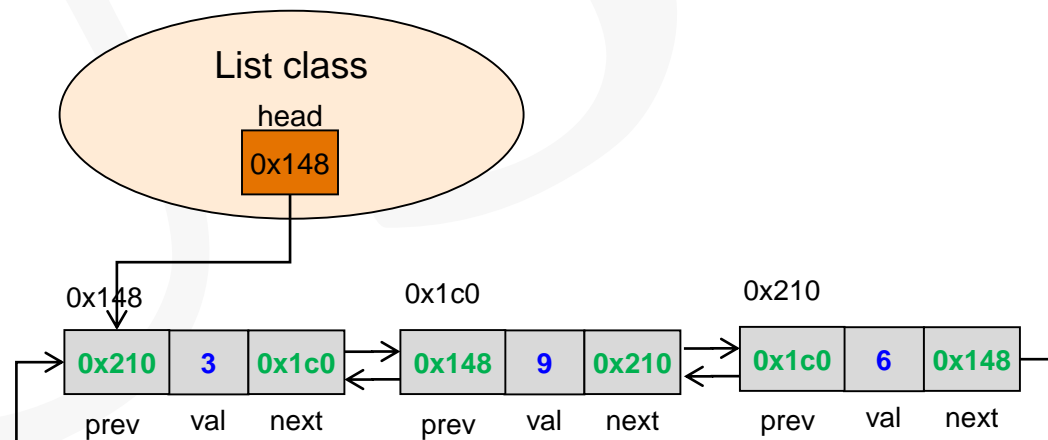
## Option 3: Circular DLL

- **Make first and last item point at each other to form a circular list**
  - We know which one is first via the 'head' pointer



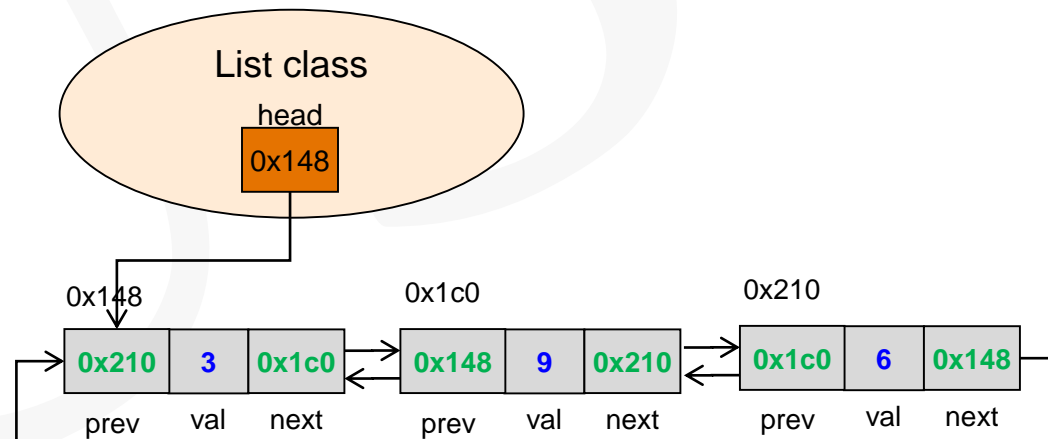
## Option 3 (cont.)

- What expression would yield the tail item?



## Option 3 (cont.)

- What expression would yield the tail item?
  - head->prev

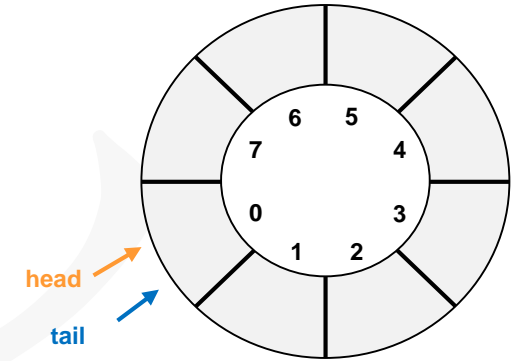
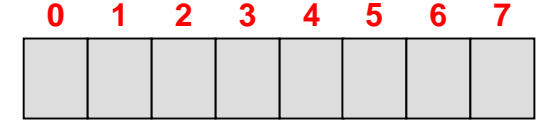


# One Last Point

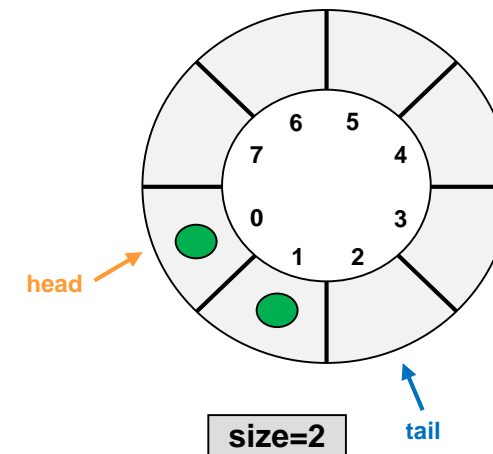
- Can this kind of deque implementation support  $O(1)$  access to element  $i$ ?, i.e., can you access `list[i]` quickly for any  $i$ ?
- No!!! Still need to traverse the list
- You can use a "circular" array based deque implementation to get fast random access
  - This is what the actual C++ `deque<T>` class does
  - Don't worry about this though...

# Exercise

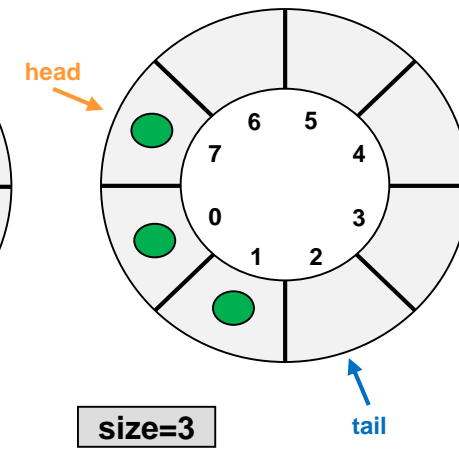
- Implement a circular buffer
- You should think about empty and full cases
- What is the best way to handle those cases?



1.) Push\_back()  
2.) Push\_back()

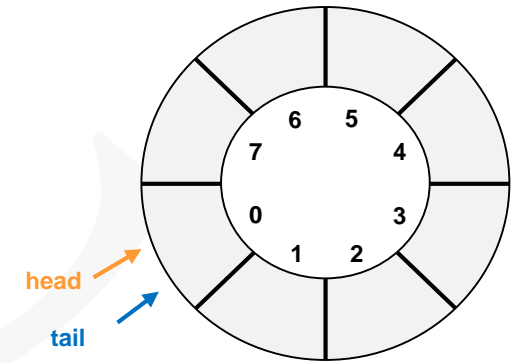
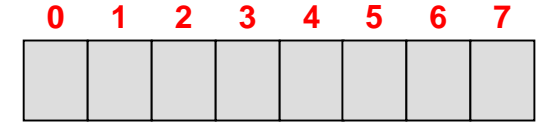


3.) Push\_front()

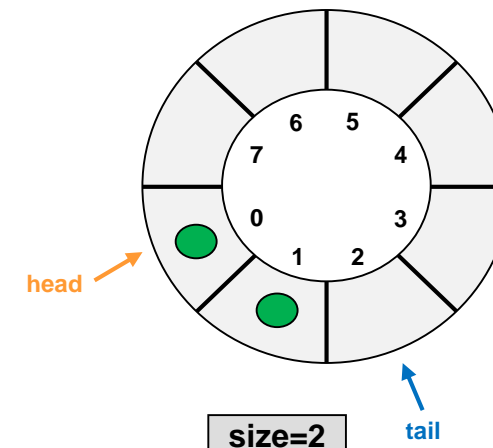


# Circular Buffers

- Take an array but imagine it wrapping into a circle to implement a deque
- Setup a head and tail pointer
  - Head points at first occupied item, tail at first free location
  - Push\_front() and pop\_front() update the head pointer
  - Push\_back() and pop\_back() update the tail pointer
- To overcome discontinuity from index 0 to MAX-1, use modulo operation
  - Index = 7; Index++ should cause index = 0
  - $\text{index} = (\text{index} + 1) \% \text{MAX}$
  - Index = 0; Index-- should cause index = 7
  - if(--index < 0) index = MAX-1;
- Get item at index i
  - It's relative to the head pointer
  - Return item at  $(\text{head} + i) \% \text{MAX}$



1.) Push\_back()  
2.) Push\_back()



3.) Push\_front()

