solution.

So far we have discussed matrix inverses as being multiplied on the left. It is also possible to define an inverse that is multiplied on the right:

$$\mathbf{A}\mathbf{A}^{-1} = \mathbf{I}.\tag{2.29}$$

For square matrices, the left inverse and right inverse are equal.

2.5 Norms

Sometimes we need to measure the size of a vector. In machine learning, we usually measure the size of vectors using a function called a **norm**. Formally, the L^p norm is given by

$$||\boldsymbol{x}||_p = \left(\sum_i |x_i|^p\right)^{\frac{1}{p}}$$
 (2.30)

for $p \in \mathbb{R}, p \geq 1$.

Norms, including the L^p norm, are functions mapping vectors to non-negative values. On an intuitive level, the norm of a vector \boldsymbol{x} measures the distance from the origin to the point \boldsymbol{x} . More rigorously, a norm is any function f that satisfies the following properties:

- $\bullet \ f(\boldsymbol{x}) = 0 \Rightarrow \boldsymbol{x} = \boldsymbol{0}$
- $f(x + y) \le f(x) + f(y)$ (the triangle inequality)
- $\forall \alpha \in \mathbb{R}, f(\alpha \mathbf{x}) = |\alpha| f(\mathbf{x})$

The L^2 norm, with p=2, is known as the **Euclidean norm**. It is simply the Euclidean distance from the origin to the point identified by \boldsymbol{x} . The L^2 norm is used so frequently in machine learning that it is often denoted simply as $||\boldsymbol{x}||$, with the subscript 2 omitted. It is also common to measure the size of a vector using the squared L^2 norm, which can be calculated simply as $\boldsymbol{x}^{\top}\boldsymbol{x}$.

The squared L^2 norm is more convenient to work with mathematically and computationally than the L^2 norm itself. For example, the derivatives of the squared L^2 norm with respect to each element of \boldsymbol{x} each depend only on the corresponding element of \boldsymbol{x} , while all of the derivatives of the L^2 norm depend on the entire vector. In many contexts, the squared L^2 norm may be undesirable because it increases very slowly near the origin. In several machine learning