RBMs have been trained in this way, they can be combined to form a DBM. The DBM may then be trained with PCD. Typically PCD training will make only a small change in the model's parameters and its performance as measured by the log-likelihood it assigns to the data, or its ability to classify inputs. See figure 20.4 for an illustration of the training procedure.

This greedy layer-wise training procedure is not just coordinate ascent. It bears some passing resemblance to coordinate ascent because we optimize one subset of the parameters at each step. The two methods differ because the greedy layer-wise training procedure uses a different objective function at each step.

Greedy layer-wise pretraining of a DBM differs from greedy layer-wise pretraining of a DBN. The parameters of each individual RBM may be copied to the corresponding DBN directly. In the case of the DBM, the RBM parameters must be modified before inclusion in the DBM. A layer in the middle of the stack of RBMs is trained with only bottom-up input, but after the stack is combined to form the DBM, the layer will have both bottom-up and top-down input. To account for this effect, Salakhutdinov and Hinton (2009a) advocate dividing the weights of all but the top and bottom RBM in half before inserting them into the DBM. Additionally, the bottom RBM must be trained using two "copies" of each visible unit and the weights tied to be equal between the two copies. This means that the weights are effectively doubled during the upward pass. Similarly, the top RBM should be trained with two copies of the topmost layer.

Obtaining the state of the art results with the deep Boltzmann machine requires a modification of the standard SML algorithm, which is to use a small amount of mean field during the negative phase of the joint PCD training step (Salakhutdinov and Hinton, 2009a). Specifically, the expectation of the energy gradient should be computed with respect to the mean field distribution in which all of the units are independent from each other. The parameters of this mean field distribution should be obtained by running the mean field fixed point equations for just one step. See Goodfellow et al. (2013b) for a comparison of the performance of centered DBMs with and without the use of partial mean field in the negative phase.

## 20.4.5 Jointly Training Deep Boltzmann Machines

Classic DBMs require greedy unsupervised pretraining, and to perform classification well, require a separate MLP-based classifier on top of the hidden features they extract. This has some undesirable properties. It is hard to track performance during training because we cannot evaluate properties of the full DBM while training the first RBM. Thus, it is hard to tell how well our hyperparameters