

Figure 20.11: Each step of the Markov chain associated with a trained denoising autoencoder, that generates the samples from the probabilistic model implicitly trained by the denoising log-likelihood criterion. Each step consists in (a) injecting noise via corruption process C in state \boldsymbol{x} , yielding $\tilde{\boldsymbol{x}}$, (b) encoding it with function f, yielding $\boldsymbol{h} = f(\tilde{\boldsymbol{x}})$, (c) decoding the result with function g, yielding parameters $\boldsymbol{\omega}$ for the reconstruction distribution, and (d) given $\boldsymbol{\omega}$, sampling a new state from the reconstruction distribution $p(\mathbf{x} \mid \boldsymbol{\omega} = g(f(\tilde{\boldsymbol{x}})))$. In the typical squared reconstruction error case, $g(\boldsymbol{h}) = \hat{\boldsymbol{x}}$, which estimates $\mathbb{E}[\boldsymbol{x} \mid \tilde{\boldsymbol{x}}]$, corruption consists in adding Gaussian noise and sampling from $p(\mathbf{x} \mid \boldsymbol{\omega})$ consists in adding Gaussian noise, a second time, to the reconstruction $\hat{\boldsymbol{x}}$. The latter noise level should correspond to the mean squared error of reconstructions, whereas the injected noise is a hyperparameter that controls the mixing speed as well as the extent to which the estimator smooths the empirical distribution (Vincent, 2011). In the example illustrated here, only the C and p conditionals are stochastic steps (f and g are deterministic computations), although noise can also be injected inside the autoencoder, as in generative stochastic networks (Bengio $et\ al.$, 2014).