Símplex

Investigación de operaciones

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Algoritmo Símplex

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Problema original

Fábrica de carros

Maximizar

• Z = -300 Camiones -200 Carros

Restricciones

- 1. 0,0*Camiones* + 0,0*Carros* ≤ 1
- 2. 0,0 Camiones +0,0 Carros ≤ 1
- 3. 1 *Camiones* + 0 *Carros* ≥ 30
- **4**. 0*Camiones* + 1*Carros* ≥ 20

Tabla inicial

Tabla inicial

| Z | Camiones | Carros | S ₁ | S ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|--------|----------------|-----------------------|----------------|-----------------------|-----------------------|-----------------------|----|
| 1 | -300 | -200 | 0 | 0 | 0 | 0 | 1M | 1M | 0 |
| 0 | 0,0 | 0,0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 0,0 | 0,0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 0 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 1: Tabla inicial.

| Z | Camiones | Carros | S ₁ | s ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|---------|----------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-------|
| 1 | -300-1M | -200-1M | 0 | 0 | 1M | 1M | 0 | 0 | 0-50M |
| 0 | 0,0 | 0,0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 0,0 | 0,0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 0 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 2: Tabla intermedia 1, con las columnas a_i canonizadas.

Tablas intermedias

| Z | Camiones | Carros | S ₁ | s ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|---------|----------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-------|
| 1 | -300-1M | -200-1M | 0 | 0 | 1M | 1M | 0 | 0 | 0-50M |
| 0 | 0,0 | 0,0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 0,0 | 0,0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 0 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 3: Tabla intermedia 1, durante el pivoteo.

Cálculos: 1/0,0 = 62,5 | 1/0,0 = 50 | **30/1 = 30** |

| Z | Camiones | Carros | S ₁ | s ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|---------|----------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|----------|
| 1 | 0 | -200-1M | 0 | 0 | -300 | 1M | 300+1M | 0 | 9000-20M |
| 0 | 0 | 0,0 | 1 | 0 | 0,0 | 0 | -0,0 | 0 | 0,5 |
| 0 | 0 | 0,0 | 0 | 1 | 0,0 | 0 | -0,0 | 0 | 0,4 |
| 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 0 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 4: Tabla intermedia 2, con la columna de 2 canonizada.

| Z | Camiones | Carros | S ₁ | s ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|---------|----------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|----------|
| 1 | 0 | -200-1M | 0 | 0 | -300 | 1M | 300+1M | 0 | 9000-20M |
| 0 | 0 | 0,0 | 1 | 0 | 0,0 | 0 | -0,0 | 0 | 0,5 |
| 0 | 0 | 0,0 | 0 | 1 | 0,0 | 0 | -0,0 | 0 | 0,4 |
| 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 0 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 5: Tabla intermedia 2, durante el pivoteo.

Cálculos: $0.5/0.0 = 20.8 \mid 0.4/0.0 = 20 \mid 20/1 = 20$

| Z | Camiones | Carros | S ₁ | s ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|--------|----------------|-----------------------|-----------------------|-----------------------|----------------|-----------------------|-------|
| 1 | 0 | 0 | 0 | 0 | -300 | -200 | 300+1M | 200+1M | 13000 |
| 0 | 0 | 0 | 1 | 0 | 0,0 | 0,0 | -0,0 | -0,0 | 0,0 |
| 0 | 0 | 0 | 0 | 1 | 0,0 | 0,0 | -0,0 | -0,0 | 0 |
| 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 0 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 6: Tabla intermedia 3, con la columna de 3 canonizada.

| Z | Camiones | Carros | S ₁ | S ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|--------|----------------|-----------------------|----------------|-----------------------|-----------------------|-----------------------|-------|
| 1 | 0 | 0 | 0 | 0 | -300 | -200 | 300+1M | 200+1M | 13000 |
| 0 | 0 | 0 | 1 | 0 | 0,0 | 0,0 | -0,0 | -0,0 | 0,0 |
| 0 | 0 | 0 | 0 | 1 | 0,0 | 0,0 | -0,0 | -0,0 | 0 |
| 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 0 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 7: Tabla intermedia 3, durante el pivoteo.

Cálculos: 0,0/0,0 = 1,2 | **0/0,0 = 0** |

| Z | Camiones | Carros | S ₁ | s ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|--------|----------------|-----------------------|----------------|-----------------------|----------------|-----------------------|---------|
| 1 | 0 | 0 | 0 | 15000 | 0 | 100 | 1M | -100+1M | 13000,0 |
| 0 | 0 | 0 | 1 | -0,8 | 0 | 0,0 | 0 | -0,0 | 0,0 |
| 0 | 0 | 0 | 0 | 50 | 1 | 1 | -1 | -1 | 0 |
| 0 | 1 | 0 | 0 | 50 | 0 | 1 | 0 | -1 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 8: Tabla intermedia 4, con la columna de 6 canonizada.

Tabla final

Tabla final

| Z | Camiones | Carros | S ₁ | s ₂ | e ₁ | e ₂ | a ₁ | a ₂ | • |
|---|----------|--------|----------------|-----------------------|----------------|-----------------------|-----------------------|-----------------------|---------|
| 1 | 0 | 0 | 0 | 15000 | 0 | 100 | 1M | -100+1M | 13000,0 |
| 0 | 0 | 0 | 1 | -0,8 | 0 | 0,0 | 0 | -0,0 | 0,0 |
| 0 | 0 | 0 | 0 | 50 | 1 | 1 | -1 | -1 | 0 |
| 0 | 1 | 0 | 0 | 50 | 0 | 1 | 0 | -1 | 30 |
| 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 1 | 20 |

Cuadro 9: Tabla final.

Solución

Solución

Solución óptima

Fábrica de carros

- Z = 13000, 0
- $x_1 = 30$
- $x_2 = 20$

Casos especiales

El problema no presentó ningún caso especial

- slide final -