

Clase 5

03/11/2020.

Resolver los siguientes ejercicios.

$$\int \frac{ue^{3x}}{1+e^{2x}} = \int \frac{ue^{2x}}{1+e^{2x}} \cdot e^x$$

$$u = e^x \quad u = (e^x)$$

$$u^2 = e^{2x}$$

$$du = e^x dx$$

$$\int \frac{ue^{2x}}{1+u^2} \cdot du$$

$$\int \frac{uv^2}{1+u^2} du = \int \frac{u^2}{1+u^2}$$

$$u \int -\frac{1}{1+u^2} + 1 \cdot du$$

$$u (\arctan(u) + u) + C$$

$$u (1 - \arctan(e^x) + e^x) + C$$

$$\int \frac{x^3}{\sqrt{x^2+1}} dx$$

$$u^2 = x^2 + 1 \cdot x = \sqrt{u^2 - 1}$$

$$dx = \frac{x}{\sqrt{u^2 - 1}} du$$

$$\int \frac{(\sqrt{u^2-1})^3}{u} \cdot \frac{u}{\sqrt{u^2-1}} du$$

$$\int \frac{(u^2-1)^{3/2}}{u} \cdot \frac{u}{(u^2-1)^{1/2}} du$$

$$\int \frac{(u^2-1)^{3/2}}{(u^2-1)^{1/2}} du$$

$$\int (u^2-1)^{3/2-1/2} du$$

$$\int (u^2-1) du = (x^2+1)^2 - 1 + C$$

$$\left(\int \frac{u e^{3x}}{1+29x} \right) \int 2 \sqrt{1+x} dx$$

$$u = 1+x \quad x = u-1 \quad dx = du$$

$$\int (u-1) (\sqrt{u}) du$$

$$\int u(\sqrt{u}) - \sqrt{u} du$$

$$\int u(u)^{1/2} - u^{1/2} du$$

$$\int u^{3/2} - u^{1/2} du$$

$$\frac{u^{5/2}}{5/2} - \frac{u^{3/2}}{3/2} du = \frac{2}{5} u^{5/2} - \frac{2}{3} u^{3/2}$$

$$\frac{2}{5} (1+x)^{5/2} - \frac{2}{3} (1+x)^{3/2}$$