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1 Basic

1.1 vimrc

```
syn on
se ai nu ru mouse=a
se cin et ts=4 sw=4 sts=4
so $VIMRUNTIME/mswin.vim
colo desert
se gfn=Monospace\ 15
execute pathogen#infect()
```

1.2 Fast Integer Input

```
#define getchar gtx
inline int gtx() {
   const int N = 1048576;
   static char buffer[N];
   static char *p = buffer, *end = buffer;
   if (p == end) {
      if ((end = buffer + fread(buffer, 1, N, stdin)) ==
      buffer) return EOF;
      p = buffer;
   return *p++;
}
template <typename T>
inline bool rit(T& x) {
  char __c = 0; bool flag = false;
while (__c = getchar(), (__c < '0' && __c != '-') ||
    __c > '9') if (__c == -1) return false;
    _c == '-' ? (flag = true, x = 0) : (x = __c - '0');
while (__c = getchar(), __c >= '0' && __c <= '9') x =
    x * 10 + __c - '0';
if (flaa) x = -x'
  if (flag) x = -x;
   return true;
}
template <typename T, typename ...Args>
inline bool rit(T& x, Args& ...args) { return rit(x) &&
        rit(args...); }
```

1.3 Big Integer

```
#include <bits/stdc++.h>
struct Int {
  std::vector<int> dig;
  bool sgn;
  Int() {
    dig.push_back(0);
    sgn = true;
  Int(int n) {
    sgn = n >= 0;
    while (n) {
      dig.push_back(n % 10);
      n = 10;
    if (dig.size() == 0) dig.push_back(0);
  Int(std::string s) {
    int i = 0; sgn = true;
if (s[i] == '-') sgn = false, ++i;
    for (;i < s.length(); ++i) dig.push_back(s[i] - '0'</pre>
    reverse(dig.begin(), dig.end());
    if (dig.size() == 1 && dig[0] == '0') sgn = true;
  Int(const std::vector<int>& d, const bool& s = true)
    dig = std::vector<int>(d.begin(), d.end());
    sgn = s;
```

```
Int(const Int& n) {
  sgn = n.sgn;
  dig = n.dig;
bool operator<(const Int& rhs) const {</pre>
  if (sgn && !rhs.sgn) return true;
  if (!sgn && rhs.sgn) return false
  if (!sgn && !rhs.sgn) return Int(dig) > Int(rhs.dig
  if (dig.size() < rhs.dig.size()) return true;</pre>
  if (dig.size() > rhs.dig.size()) return false;
  for (int i = dig.size() - 1; i >= 0; --i) {
    if (dig[i] != rhs.dig[i]) return dig[i] < rhs.dig</pre>
  [i];
  return false;
bool operator==(const Int& rhs) const {
  if (sgn != rhs.sgn) return false;
  return dig == rhs.dig;
bool operator>(const Int& rhs) const {
  return !(*this < rhs) && !(*this == rhs);</pre>
bool operator<(const int& n) const {</pre>
  return *this < Int(n);</pre>
bool operator>(const int& n) const {
  return *this > Int(n);
bool operator==(const int& n) const {
  return *this == Int(n);
Int operator-() const {
  return Int(dig, !sgn);
Int operator+(const Int& rhs) const {
  bool res = true;
  if (!sgn && !rhs.sgn) res = false;
  else if (!sgn && rhs.sgn) return rhs - (-*this);
  else if (sgn && !rhs.sgn) return *this - -rhs;
  std::vector<int> v1 = dig, v2 = rhs.dig;
  if (v2.size() > v1.size()) swap(v1, v2);
  int car = 0;
  std::vector<int> nvec;
  for (int i = 0; i < v2.size(); ++i) {
  int k = v1[i] + v2[i] + car;</pre>
    nvec.push_back(k \% 10);
    car = k / 10;
  for (int i = v2.size(); i < v1.size(); ++i) {</pre>
    int k = v1[i] + car;
    nvec.push_back(k % 10);
    car = k / 10;
  return Int(nvec, res);
Int operator-(const Int& rhs) const {
  if (*this < rhs) {</pre>
    std::vector<int> nvec = (rhs - *this).dig;
    return Int(nvec, false);
  if (*this == rhs) return Int(0);
  std::vector<int> v1 = dig, v2 = rhs.dig;
  std::vector<int> nvec;
  for (int i = 0; i < v2.size(); ++i) {</pre>
    int k = v1[i] - v2[i];
    if (k < 0) {
      for (int j = i + 1; j < v1.size(); ++j) if (v1[</pre>
         -v1[j]; k += 10;
        break;
      }
    nvec.push_back(k);
  int rind = v1.size() - 1;
  while (rind >= v2.size() && v1[rind] == 0) --rind;
  for (int i = v2.size(); i <= rind; ++i) {</pre>
    nvec.push_back(v1[i]);
  return Int(nvec);
```

```
Int operator*(const Int& rhs) const {
  if (sgn && !rhs.sgn || !sgn && rhs.sgn) return -(
  Int(dig, true) * Int(rhs.dig, true));
  if (*this == 0) return Int();
  if (rhs == 0) return Int();
  std::vector<int> v1 = dig, v2 = rhs.dig;
if (v1.size() < v2.size()) swap(v1, v2);</pre>
  std::vector<int> res(v1.size() * v2.size(), 0);
  for (int i = 0; i < v2.size(); ++i) {
    int car = 0;
    for (int j = 0; j < v1.size(); ++j) {</pre>
      int k = car + v1[j] * v2[i];
      res[j + i] += k \% 10;
      car = k / 10;
    }
  int car = 0;
  for (int i = 0; i < res.size(); ++i) {</pre>
    int k = car + res[i];
    res[i] = k % 10;
    car = k / 10;
  while (car) {
    res.push_back(car % 10);
    car \neq 10;
  int ind = res.size() - 1;
  while (ind >= 0 && res[ind] == 0) --ind;
  std::vector<int> nvec;
  for (int i = 0; i <= ind; ++i) nvec.push_back(res[i</pre>
  ]);
  return Int(nvec);
Int operator+(const int& n) const {
  return *this + Int(n);
Int operator-(const int& n) const {
  return *this - Int(n);
Int& operator+=(const Int& n) {
  *this = (*this + n);
  return *this;
Int& operator-=(const Int& n) {
  *this = (*this - n);
  return *this;
Int& operator+=(const int& n) {
  *this += Int(n);
  return *this;
Int& operator-=(const int& n) {
  *this -= Int(n);
  return *this:
Int& operator*=(const Int& n) {
  *this = *this * n;
  return *this;
Int& operator*=(const int& n) {
  *this *= Int(n);
  return *this;
Int& operator++(int) {
  *this += 1;
  return *this;
Int& operator--(int) {
  *this -= 1;
  return *this;
friend std::istream& operator>>(std::istream& in, Int
  & n) {
std::string s; in >> s;
  n = Int(s);
  return in;
friend std::ostream& operator<<(std::ostream& out,</pre>
  const Int& n) {
  if (!n.sgn) out << "-";</pre>
```

```
for (int i = n.dig.size() - 1; i >= 0; --i) out <<
    n.dig[i];
    return out;
}
</pre>
```

2 Flow

2.1 Dinic's algorithm

```
struct Dinic {
  int n, s, t;
  vector<int> level;
  struct Edge {
    int to, rev, cap;
    Edge() {}
    Edge(int a, int b, int c): to(a), cap(b), rev(c) {}
  vector<Edge> G[maxn];
  bool bfs() {
    level.assign(n, -1);
    level[s] = 0;
    queue<int> que; que.push(s);
    while (que.size()) {
      int tmp = que.front(); que.pop();
      for (auto e : G[tmp]) {
        if (e.cap > 0 && level[e.to] == -1) {
          level[e.to] = level[tmp] + 1;
          que.push(e.to);
        }
      }
    return level[t] != -1;
  int flow(int now, int low) {
    if (now == t) return low;
    int ret = 0;
    for (auto &e : G[now]) {
      if (e.cap > 0 \& level[e.to] == level[now] + 1) {
        int tmp = flow(e.to, min(e.cap, low - ret));
        e.cap -= tmp; G[e.to][e.rev].cap += tmp;
        ret += tmp;
      }
    if (ret == 0) level[now] = -1;
    return ret;
  Dinic(int _n, int _s, int _t): n(_n), s(_s), t(_t) {
    fill(G, G + maxn, vector<Edge>());
  void add_edge(int a, int b, int c) {
    G[a].push_back(Edge(b, c, G[b].size()));
G[b].push_back(Edge(a, 0, G[a].size() - 1));
  int maxflow() {
    int ret = 0;
    while (bfs()) ret += flow(s, inf);
    return ret;
};
```

2.2 Min cost Max flow

```
struct MincostMaxflow {
   struct Edge {
     int to, rev, cap, w;
     Edge() {}
     Edge(int a, int b, int c, int d): to(a), cap(b), w(
        c), rev(d) {}
   };
   int n, s, t;
   vector<int> p, id, d;
   bitset<maxm> inque;
   vector<Edge> G[maxn];
   pair<int, int> spfa() {
     p.assign(n, -1);
```

```
d.assign(n, inf);
    id.assign(n, -1);
    d[s] = 0; p[s] = s;
    queue<int> que; que.push(s); inque[s] = true;
    while (que.size()) {
      int tmp = que.front(); que.pop();
      inque[tmp] = false;
      int i = 0;
      for (auto e : G[tmp]) {
        if (e.cap > 0 \& d[e.to] > d[tmp] + e.w) {
          d[e.to] = d[tmp] + e.w;
          p[e.to] = tmp;
          id[e.to] = i;
          if (!inque[e.to]) que.push(e.to), inque[e.to]
     = true;
        ++i:
      }
    if (d[t] == inf) return make_pair(-1, -1);
    int a = inf;
    for (int i = t; i != s; i = p[i]) {
      a = min(a, G[p[i]][id[i]].cap);
    for (int i = t; i != s; i = p[i]) {
      Edge &e = G[p[i]][id[i]];
      e.cap -= a; G[e.to][e.rev].cap += a;
    return make_pair(a, d[t]);
  MincostMaxflow(int _n, int _s, int _t): n(_n), s(_s),
     t(_t) {
    fill(G, G + maxn, vector<Edge>());
  void add_edge(int a, int b, int cap, int w) {
    G[a].push_back(Edge(b, cap, w, (int)G[b].size()));
    G[b].push\_back(Edge(a, 0, -w, (int)G[a].size() - 1)
  pair<int, int> maxflow() {
  int mxf = 0, mnc = 0;
    while (true) {
      pair<int,</pre>
                int> res = spfa();
      if (res.first == -1) break;
      mxf += res.first; mnc += res.first * res.second;
    return make_pair(mxf, mnc);
  }
};
```

2.3 Maximum bipartite matching

```
struct MaximumMatching {
  vector<int> G[maxn], mt;
  int n;
  bitset<maxn> v;
  MaximumMatching(int n): n(n) {
    fill(G, G + maxn, vector<int>());
    v.reset();
  void add_edge(int a, int b) {
    G[a].push_back(b);
  bool dfs(int now) {
    v[now] = true;
    for (int u : G[now]) {
  if (mt[u] == -1 || !v[mt[u]] && dfs(mt[u])) {
        mt[u] = now;
        return true;
      }
    }
    return false;
  int solve() {
    mt.assign(n, -1);
    int ret = 0;
    for (int i = 0; i < n; ++i) {
      memset(v, false, sizeof(v));
      if (dfs(i)) ++ret;
```

```
return ret;
}
};
```

2.4 Maximum weighted bipartite matching

```
struct Hungarian {
  vector<int> lx, ly, match;
  vector<vector<int>> w;
  int n;
  bitset<maxn> s, t;
  bool dfs(int now) {
     s[now] = true;
     for (int i = 0; i < n; ++i) {
       if (lx[now] + ly[i] == w[now][i] && !t[i]) {
          t[i] = true;
          if (match[i] == -1 \mid | dfs(match[i])) {
            match[i] = now;
            return true:
         }
       }
     }
     return false;
   void relabel() {
     int a = inf;
     for (int i = 0; i < n; ++i) if (s[i]) {
       for (int j = 0; j < n; ++j) if (!t[j]) {
         a = min(a, lx[i] + ly[j] - w[i][j]);
     for (int i = 0; i < n; ++i) {
  if (s[i]) lx[i] -= a;
  if (t[i]) ly[i] += a;</pre>
  Hungarian(int n): n(n) {
     w.assign(n, vector<int>());
    for (int i = 0; i < n; ++i) w[i].assign(n, 0);
lx.assign(n, 0); ly.assign(n, 0);
match.assign(n, -1);</pre>
  void add_edge(int a, int b, int c) {
     w[a][b] = c;
   int solve() {
     for (int i = 0; i < n; ++i) for (int j = 0; j < n;
     ++j) lx[i] = max(lx[i], w[i][j]);
     for (int i = 0; i < n; ++i) {
  while (true) {</pre>
          s.reset(); t.reset();
          if (dfs(i)) break;
          else relabel();
     int ans = 0;
     for (int i = 0; i < n; ++i) ans += w[match[i]][i];
     return ans;
};
```

3 Math

3.1 FFT

```
const double pi = acos(-1);
const complex<double> I(0, 1);
complex<double> omega[maxn + 1];

void prefft() {
  for (int i = 0; i <= maxn; ++i) omega[i] = exp(i * 2
     * pi / maxn * I);
}
void fft(vector<complex<double>>& a, int n, bool inv=
     false) {
  int basic = maxn / n;
```

```
int theta = basic;
  for (int m = n; m >= 2; m >>= 1) {
    int h = m \gg 1;
    for (int i = 0; i < h; ++i) {
      complex<double> w = omega[inv ? maxn - (i * theta
     % maxn) : i * theta % maxn];
      for (int j = i; j < n; j += m) {
        int k = j + h;
        complex<double> x = a[j] - a[k];
        a[j] += a[k];
        a[k] = w * x;
    theta = (theta * 2) % maxn;
  int i = 0;
  for (int j = 1; j < n - 1; ++j) {
  for (int k = n >> 1; k > (i ^= k); k >>= 1);
    if (j < i) swap(a[i], a[j]);</pre>
  if (inv) for (int i = 0; i < n; ++i) a[i] /= (double)
void invfft(vector<complex<double>>& a, int n) {
  fft(a, n, true);
```

3.2 Miller-Rabin

```
// n < 4759123141
                      chk = [2, 7, 61]
9780504, 17952650227
long long fpow(long long a, long long n, long long mod)
  long long ret = 1LL;
  for (; n; n >>= 1) {
    if (n & 1) ret = (__int128)ret * (__int128)a % mod;
a = (__int128)a * (__int128)a % mod;
  return ret;
bool check(long long a, long long u, long long n, int t
  a = fpow(a, u, n);
  if (a == 0) return true;
  if (a == 1 \mid \mid a == n - 1) return true;
  for (int i = 0; i < t; ++i) {
    a = (__int128)a * (__int128)a % n;
     if (a == 1) return false;
    if (a == n - 1) return true;
  }
  return false:
bool is_prime(long long n) {
  if (n < 2) return false;
  if (n % 2 == 0) return n == 2;
  long long u = n - 1; int t = 0;
  for (; u & 1; u >>= 1, ++t);
for (long long i : chk) {
   if (!check(i, u, n, t)) return false;
  return true;
}
```

3.3 Extend GCD

```
template <typename T> tuple<T, T, T> extgcd(T a, T b) {
  if (!b) return make_tuple(a, 1, 0);
  T d, x, y;
  tie(d, x, y) = extgcd(b, a % b);
  return make_tuple(d, y, x - (a / b) * y);
}
```

3.4 Matrix

```
template <typename T> class Matrix {
  public:
    int n, m, mod;
     vector<vector<T>> mat;
    Matrix(int n, int m, int mod=0, bool I=false): n(n)
     , m(m), mod(mod) {
       mat.resize(n)
       for (int i = 0; i < n; ++i) mat[i].resize(m);</pre>
       if (!I) return;
       for (int i = 0; i < n; ++i) mat[i][i] = 1;
    Matrix operator+(const Matrix& rhs) const {
       Matrix ret(n, m, mod);
       for (int i = 0; i < n; ++i) {
         for (int j = 0; j < m; ++j) {
  ret.mat[i][j] = mat[i][j] + rhs.mat[i][j];</pre>
            if (mod) ret.mat[i][j] %= mod;
         }
       return ret;
     Matrix operator-(const Matrix& rhs) const {
       Matrix ret(n, m, mod);
       for (int i = 0; i < n; ++i) {
  for (int j = 0; j < m; ++j) {</pre>
            ret.mat[i][j] = mat[i][j] - rhs.mat[i][j];
            if (mod)
              ret.mat[i][j] %= mod;
              ret.mat[i][j] += mod;
              ret.mat[i][j] %= mod;
           }
         }
       }
       return ret;
     Matrix operator*(const Matrix& rhs) const {
       Matrix ret(n, rhs.m, mod);
       for (int i = 0; i < n; ++i) {
         for (int j = 0; j < rhs.m; ++j) {
  for (int k = 0; k < m; ++k) {
    if (mod) ret.mat[i][j] = (ret.mat[i][j] +</pre>
     mat[i][k] * rhs.mat[k][j] % mod) % mod;
              else ret.mat[i][j] += mat[i][k] * rhs.mat[k
     ][j];
         }
       return ret;
};
```

4 Graph

4.1 Strongly connected components

```
struct SCC {
  vector<int> G[maxn], R[maxn], topo;
  int n, nscc;
  vector<int> scc, sz;
 bitset<maxn> v;
  void dfs(int now) {
   v[now] = true;
scc[now] = nscc;
    ++sz[nscc];
    for (int u : G[now]) if (!v[u]) {
      dfs(u);
  void rdfs(int now) {
    v[now] = true;
    for (int u : R[now]) if (!v[u]) {
      rdfs(u);
    topo.push_back(now);
  SCC(): {}
```

4.2 Heavy-Light Decomposition

```
struct HeavyLightDecomp {
  vector<int> G[maxn];
  vector<int> tin, top, dep, maxson, sz, p;
  int n, t;
  void dfs(int now, int fa, int d) {
    dep[now] = d;
    maxson[now] = -1;
    sz[now] = 1;
    p[now] = fa;
    for (int u : G[now]) if (u != fa) {
      dfs(u, now, d + 1);
      sz[now] += sz[u];
      if (maxson[now] == -1 \mid | sz[u] > sz[maxson[now]])
     maxson[now] = u;
  void link(int now, int tp) {
    top[now] = tp;
    tin[now] = ++t;
    if (maxson[now] == -1) return;
    link(maxson[now], tp);
    for (int u : G[now]) if (u != p[now]) {
       if (u == maxson[now]) continue;
      link(u, u);
    }
  HeavyLightDecomp(int n): n(n) {
    tin.assign(n, 0); top.assign(n, 0); dep.assign(n,
    maxson.assign(n, 0); sz.assign(n, 0); p.assign(n,
    0);
  void add_edge(int a, int b) {
    G[a].push_back(b);
    G[b].push_back(a);
  void build() {
    dfs(0, -1, 0);
link(0, 0);
  int lca(int a, int b) {
  int ta = top[a], tb = top[b];
    while (ta != tb) {
      if (dep[ta] < dep[tb]) {</pre>
        swap(ta, tb); swap(a, b);
      a = p[ta]; ta = top[a];
    if (a == b) return a;
    return dep[a] < dep[b] ? a : b;</pre>
  vector<pair<int, int>> get_path(int a, int b) {
  int ta = top[a], tb = top[b];
    vector<pair<int, int>> ret;
while (ta != tb) {
      if (dep[ta] < dep[tb]) {</pre>
        swap(ta, tb); swap(a, b);
```

```
ret.push_back(make_pair(tin[ta], tin[a]));
    a = p[ta]; ta = top[a];
    ret.push_back(make_pair(min(tin[a], tin[b]), max(
        tin[a], tin[b])));
    return ret;
}
return ret;
}
```

4.3 Centroid Decomposition

```
vector<pair<int, int>> G[maxn];
int sz[maxn], mx[maxn];
bool v[maxn];
vector<int> vtx;
void get_center(int now) {
  v[now] = true; vtx.push_back(now);
sz[now] = 1; mx[now] = 0;
  for (int u : G[now]) if (!v[u]) {
    get_center(u);
    mx[now] = max(mx[now], sz[u]);
    sz[now] += sz[u];
}
void get_dis(int now, int d, int len) {
  dis[d][now] = cnt;
  v[now] = true;
  for (auto u : G[now]) if (!v[u.first]) {
    get_dis(u, d, len + u.second);
void dfs(int now, int fa, int d) {
  get_center(now);
  v[i] = false;
 get_dis(c, d, 0);
for (int i : vtx) v[i] = false;
v[c] = true; vtx.clear();
  dep[c] = d; p[c] = fa;
  for (auto u : G[c]) if (u.first != fa && !v[u.first])
    dfs(u.first, c, d + 1);
  }
}
```

4.4 2-Satisfiability

```
struct TwoSat {
 vector<int> G[maxn << 1];</pre>
 bitset<maxn << 1> v;
 vector<int> s;
 int c:
 bool dfs(int now) {
    if (v[now ^ 1]) return false;
   if (v[now]) return true;
   v[now] = true;
    s[c++] = now;
    for (int u : G[now]) if (!dfs(u)) return false;
    return true;
 TwoSat() {
   s.assign(maxn << 1, 0);
    v.reset();
 void add_edge(int a, int b) {
    G[a].push_back(b);
 bool solve() {
    for (int i = 0; i < maxn << 1; i += 2) {
      if (!v[i] && !v[i + 1]) {
        c = 0;
```

```
if (!dfs(i)) {
    while (c) v[s[--c]] = false;
    if (!dfs(i + 1)) return false;
    }
  }
}
return true;
}
```

5 Data Structures

5.1 Treap

```
namespace Treap {
   struct Node {
     int val, pri, sz;
Node *lc, *rc;
Node(T v): pri(rand()), val(v) {
       lc = rc = nullptr;
        sz = 1;
     void pull() {
        sz = size(lc) + size(rc) + 1;
   inline int size(Node* t) {
     return t ? t->sz : 0;
   Node *merge(Node *a, Node *b) {
      if (!a || !b) return a ? a : b;
      if (a->pri > b->pri) {
        a \rightarrow rc = merge(a \rightarrow rc, b);
        a->pull();
        return a:
     } else {
        b \rightarrow lc = merge(a, b \rightarrow lc);
        b->pull();
        return b;
   void split(Node *t, int k, Node *&a, Node *&b) {
     if (!t) { a = b = nullptr; return; }
     if (t->val <= k) {
        a = t;
        split(t->rc, k, a->rc, b);
        a->pull();
     } else {
        b = t;
        split(t->lc, k, a, b->lc);
        b->pull();
     }
   int kth(Node *t, int k) {
  if (size(t->lc) + 1 == k) return t->val;
  if (size(t->lc) + 1 > k) return kth(t->lc, k);
     return kth(t->rc, k - size(t->lc) - 1);
   void clear(Node *t) {
     if (!t) return;
     if (t->lc) clear(t->lc);
     if (t->rc) clear(t->rc);
     delete t;
}
```

5.2 Leftlist Tree

```
namespace LeftlistTree {
    struct Node {
        T val;
        int s;
        Node *lc, *rc;
        Node(T v): val(v) {
            lc = rc = nullptr;
        s = 1;
    }
}
```

```
}
  inline int rank(Node* t) {
    return t ? t->s : 0;
  Node *merge(Node *a, Node *b) {
    if (!a | l | !b) return a ? a : b;
    if (a->val < b->val) swap(a, b);
    a \rightarrow rc = merge(a \rightarrow rc, b);
    if (rank(a->lc) < rank(a->rc)) swap(a->lc, a->rc);
    a \rightarrow s = rank(a \rightarrow rc) + 1;
    return a;
  void clear(Node *t) {
    if (!t) return;
    if (t->lc) clear(t->lc);
    if (t->rc) clear(t->rc);
    delete t;
}
```

6 Geometry

6.1 Points

```
struct pt {
  double x, y;
  pt(): x(0.0), y(0.0) {}
  pt(double x, double y): x(x), y(y) {}
  pt operator+(const pt& a) const { return pt(x + a.x, y + a.y); }
  pt operator-(const pt& a) const { return pt(x - a.x, y - a.y); }
  double operator*(const pt& a) const { return x * a.x + y * a.y; }
  double operator^(const pt& a) const { return x * a.y - y * a.x; }
  bool operator<(const pt& a) const { return x = a.x ? y < a.y : x < a.x; }
};</pre>
```

6.2 Convex Hull

```
double cross(const pt& o, const pt& a, const pt& b) {
 return (a - o) ^ (b - o);
int rsd:
vector<pt> convex_hull(vector<pt> p) {
 sort(p.begin(), p.end());
  int m = 0;
 vector<pt> ret(2 * p.size());
 for (int i = 0; i < p.size(); ++i) {</pre>
    while (m \ge 2 \& cross(ret[m - 2], ret[m - 1], p[i])
    1) < 0) --m;
    ret[m++] = p[i];
 rsd = m - 1;
 for (int i = p.size() - 2, t = m + 1; i >= 0; --i) {
   while (m >= t && cross(ret[m - 2], ret[m - 1], p[i
    ]) < 0) --m;
    ret[m++] = p[i];
 ret.resize(m - 1);
 return ret;
```

6.3 Rotating Caliper

```
void rotating_caliper(vector<pt> p) {
  vector<pt> ch = convex_hull(p);
  int tbz = ch.size();
  int lpr = 0, rpr = rsd;
```

```
// ch[lpr], ch[rpr]
while (lpr < rsd | | rpr < tbz - 1) {
    if (lpr < rsd && rpr < tbz - 1) {
        pt rvt = ch[rpr + 1] - ch[rpr];
        pt lvt = ch[lpr + 1] - ch[lpr];
        if ((lvt ^ rvt) < 0) ++lpr;
        else ++rpr;
    }
    else if (lpr == rsd) ++rpr;
    else ++lpr;
    // ch[lpr], ch[rpr]
}</pre>
```

6.4 Closest Pair

```
pt p[maxn];
double dis(const pt& a, const pt& b) {
  return sqrt((a - b) * (a - b));
double closest_pair(int l, int r) {
  if (l == r) return inf;
  if (r - l == 1) return dis(p[l], p[r]);
  int m = (l + r) >> 1;
  double d = min(closest_pair(l, m), closest_pair(m +
    1, r));
  vector<int> vec;
  for (int i = m; i >= l && fabs(p[m].x - p[i].x) < d;
    --i) vec.push_back(i);
  for (int i = m + 1; i \le r \& fabs(p[m].x - p[i].x) <
     d; ++i) vec.push_back(i);
  sort(vec.begin(), vec.end(), [=](const int& a, const
    int& b) { return p[a].y < p[b].y; });</pre>
  for (int i = 0; i < vec.size(); ++i)</pre>
    for (int j = i + 1; j < vec.size() && fabs(p[vec[j]
    ]].y - p[vec[i]].y) < d; ++j) {
      d = min(d, dis(p[vec[i]], p[vec[j]]));
    }
  }
  return d;
}
```

7 String

7.1 KMP

7.2 Suffix Array

```
struct SuffixArray {
  int sa[maxn], tmp[2][maxn], c[maxn], _lcp[maxn], r[
    maxn], n;
  string s;
  SparseTable st;
  void suffixarray() {
    int* rank = tmp[0];
}
```

```
int* nRank = tmp[1];
  int A = 128;
  for (int i = 0; i < A; ++i) c[i] = 0;
  for (int i = 0; i < s.length(); ++i) c[rank[i] = s[
  for (int i = 1; i < A; ++i) c[i] += c[i - 1];
  for (int i = s.length() - 1; i \ge 0; --i) sa[--c[s[
  i]]] = i;
  for (int n = 1; n < s.length(); n *= 2) {</pre>
    for (int i = 0; i < A; ++i) c[i] = 0;
for (int i = 0; i < s.length(); ++i) c[rank[i]</pre>
    for (int i = 1; i < A; ++i) c[i] += c[i - 1];
    int* sa2 = nRank;
    int r = 0;
    for (int i = s.length() - n; i < s.length(); ++i)</pre>
   sa2[r++] = i;
    for (int i = 0; i < s.length(); ++i) if (sa[i] >=
   n) sa2[r++] = sa[i] - n;
  for (int i = s.length() - 1; i >= 0; --i) sa[--c[
rank[sa2[i]]]] = sa2[i];
    nRank[sa[0]] = r = 0;
    for (int i = 1; i < s.length(); ++i) {
  if (!(rank[sa[i - 1]] == rank[sa[i]] && sa[i -</pre>
  1] + n < s.length() && rank[sa[i - 1] + n] == rank[
  sa[i] + n])) r++;
      nRank[sa[i]] = r;
    swap(rank, nRank);
    if (r == s.length() - 1) break;
    A = r + 1;
  }
void solve() {
  suffixarray();
  for (int i = 0; i < n; ++i) r[sa[i]] = i;
  int ind = 0; _lcp[0] = 0;
  for (int i = 0; i < n; ++i) {
  if (!r[i]) { ind = 0; continue; }</pre>
    while (i + ind < n \&\& s[i + ind] == s[sa[r[i] -
  1] + ind]) ++ind;
    _{lcp[r[i]]} = ind ? ind-- : 0;
  st = SparseTable(n, _lcp);
int lcp(int L, int R) {
  if (L == R) return n - L - 1;
  L = r[L]; R = r[R];
  if (L > R) swap(L, R);
  ++L:
  return st.query(L, R);
SuffixArray(string s): s(s), n(s.length()) {}
SuffixArray() {}
```

7.3 Z algorithm

```
int z[maxn];
void z_function(const string& s) {
    memset(z, 0, sizeof(z));
    z[0] = (int)s.length();
    int l = 0, r = 0;
    for (int i = 1; i < s.length(); ++i) {
        z[i] = max(0, min(z[i - l], r - i + 1));
        while (i + z[i] < s.length() && s[z[i]] == s[i + z[i]]) {
            l = i; r = i + z[i];
            ++z[i];
        }
    }
}</pre>
```

7.4 Rolling hash primes

```
const int mod[] = { 479001599, 433494437, 1073807359,
    1442968193, 715827883 }
```

```
8 Dynamic Programming
```

| const int $p[] = { 101, 233, 457, 173, 211 }$

8.1 Linear convex hull optimization

```
struct ConvexHull {
   // Max convex hull
   deque<pair<int, int>> dq;
   bool check(const pair<int, int>& l1, const pair<int,
      int>& 12, int x) {
     // for min case, replace <= with >=
return l1.first * x + l1.second <= l2.first * x +</pre>
      12.second;
   bool elim(const pair<int, int>& 11, const pair<int,
  int>& 12, const pair<int, int>& 1) {
  return (double)(l1.second - l2.second) / (double)(
      12.first - l1.first) <= (double)(l.second - l2.</pre>
      second) / (double)(12.first - l.first);
   int query(int x) {
     while (dq.size() \ge 2 \& check(dq[0], dq[1], x)) dq
      .pop_front();
      return dq.front().first * x + dq.front().second;
   void add(int a, int b) {
     while (dq.size() >= 2 && elim(dq[dq.size() - 1], dq
      [dq.size() - 2], make_pair(a, b))) dq.pop_back();
      dq.push_back(make_pair(a, b));
};
```

8.2 Divide and conquer optimization

```
int dp[maxk][maxn], f[maxk][maxn];

void go(int k, int l, int r, int fl, int fr) {
    if (l > r) return;
    int m = (l + r) >> 1;
    f[k][m] = -1;
    for (int i = fl; i <= min(m - 1, fr); ++i) {
        int t = dp[k - 1][i] + f(i + 1, m);
        if (t > dp[k][m]) {
            dp[k][m] = t;
            f[k][m] = i;
        }
    }
    go(k, l, m - 1, fl, f[k][m]);
    go(k, m + 1, r, f[k][m], fr);
}

void solve() {
    for (int i = 1; i <= k; ++i) go(i, 1, n, 0, n - 1);
}</pre>
```