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## 1 Basic

### 1.1 vimrc

```
syn on
se ai nu ru mouse=a
se cin et ts=4 sw=4 sts=4
so $VIMRUNTIME/mswin.vim
colo desert
se gfn=Monospace\ 15
execute pathogen#infect()
```

### 1.2 Fast Integer Input

```
#define getchar gtx

inline int gtx() {
    const int N = 1048576;
    static char buffer[N];
    static char *p = buffer, *end = buffer;
    if (p == end) {
        if ((end = buffer + fread(buffer, 1, N, stdin)) ==
            buffer) return EOF;
        p = buffer;
    }
    return *p++;
}

template <typename T>
inline bool rit(T& x) {
    char __c = 0; bool flag = false;
    while (__c = getchar(), (__c < '0' && __c != '-') ||
        __c > '9') if (__c == -1) return false;
    __c == '-' ? (flag = true, x = 0) : (x = __c - '0');
    while (__c = getchar(), __c >= '0' && __c <= '9') x =
        x * 10 + __c - '0';
    if (flag) x = -x;
    return true;
}

template <typename T, typename ...Args>
inline bool rit(T& x, Args& ...args) { return rit(x) &&
    rit(args...); }
```

### 1.3 Big Integer

```
#include <bits/stdc++.h>

struct Int {
    std::vector<int> dig;
    bool sgn;
    Int() {
        dig.push_back(0);
        sgn = true;
    }
    Int(int n) {
        sgn = n >= 0;
        while (n) {
            dig.push_back(n % 10);
            n /= 10;
        }
        if (dig.size() == 0) dig.push_back(0);
    }
    Int(std::string s) {
        int i = 0; sgn = true;
        if (s[i] == '-') sgn = false, ++i;
        for (i = 0; i < s.length(); ++i) dig.push_back(s[i] - '0');
        reverse(dig.begin(), dig.end());
    }
    Int(const std::vector<int>& d, const bool& s = true) {
        dig = std::vector<int>(d.begin(), d.end());
        sgn = s;
    }
    Int(const Int& n) {
```

```

    sgn = n.sgn;
    dig = n.dig;
}
bool operator<(const Int& rhs) const {
    if (sgn && !rhs.sgn) return true;
    if (!sgn && rhs.sgn) return false;
    if (!sgn && !rhs.sgn) return Int(dig) > Int(rhs.dig);
    if (dig.size() < rhs.dig.size()) return true;
    if (dig.size() > rhs.dig.size()) return false;
    for (int i = dig.size() - 1; i >= 0; --i) {
        if (dig[i] != rhs.dig[i]) return dig[i] < rhs.dig[i];
    }
    return false;
}
bool operator==(const Int& rhs) const {
    if (sgn != rhs.sgn) return false;
    return dig == rhs.dig;
}
bool operator>(const Int& rhs) const {
    return !(*this < rhs) && !(*this == rhs);
}
bool operator<(const int& n) const {
    return *this < Int(n);
}
bool operator>(const int& n) const {
    return *this > Int(n);
}
bool operator==(const int& n) const {
    return *this == Int(n);
}
Int operator+(const Int& rhs) const {
    bool res = true;
    if (!sgn && !rhs.sgn) res = false;
    else if (!sgn && rhs.sgn) return *this - rhs;
    else if (sgn && !rhs.sgn) return rhs - *this;
    std::vector<int> v1 = dig, v2 = rhs.dig;
    if (v2.size() > v1.size()) swap(v1, v2);
    int car = 0;
    std::vector<int> nvec;
    for (int i = 0; i < v2.size(); ++i) {
        int k = v1[i] + v2[i] + car;
        nvec.push_back(k % 10);
        car = k / 10;
    }
    for (int i = v2.size(); i < v1.size(); ++i) {
        int k = v1[i] + car;
        nvec.push_back(k % 10);
        car = k / 10;
    }
    return Int(nvec, res);
}
Int operator-(const Int& rhs) const {
    if (*this < rhs) {
        std::vector<int> nvec = (rhs - *this).dig;
        return Int(nvec, false);
    }
    if (*this == rhs) return Int(0);
    std::vector<int> v1 = dig, v2 = rhs.dig;
    std::vector<int> nvec;
    for (int i = 0; i < v2.size(); ++i) {
        int k = v1[i] - v2[i];
        if (k < 0) {
            for (int j = i + 1; j < v1.size(); ++j) if (v1[j] > 0) {
                --v1[j]; k += 10;
                break;
            }
        }
        nvec.push_back(k);
    }
    int rind = v1.size() - 1;
    while (rind >= v2.size() && v1[rind] == 0) --rind;
    for (int i = v2.size(); i <= rind; ++i) {
        nvec.push_back(v1[i]);
    }
    return Int(nvec);
}
Int operator+(const int& n) const {
    return *this + Int(n);
}

```

```

Int operator-(const int& n) const {
    return *this - Int(n);
}
Int& operator+=(const Int& n) {
    *this = (*this + n);
    return *this;
}
Int& operator-=(const Int& n) {
    *this = (*this - n);
    return *this;
}
Int& operator+=(const int& n) {
    *this += Int(n);
    return *this;
}
Int& operator-=(const int& n) {
    *this -= Int(n);
    return *this;
}
friend std::istream& operator>>(std::istream& in, Int
    & n) {
    std::string s; in >> s;
    n = Int(s);
    return in;
}
friend std::ostream& operator<<(std::ostream& out,
    const Int& n) {
    if (!n.sgn) out << "-";
    for (int i = n.dig.size() - 1; i >= 0; --i) out <<
        n.dig[i];
    return out;
}
};

int main() {
    Int a, b; std::cin >> a >> b;
    std::cout << a << ' ' << b << std::endl;
    Int c = a - b;
    std::cout << c << std::endl;
    return 0;
}

```

## 2 Flow

### 2.1 Dinic

```

struct Dinic {
    int n, s, t;
    vector<int> level;
    struct Edge {
        int to, rev, cap;
        Edge() {}
        Edge(int a, int b, int c): to(a), cap(b), rev(c) {}
    };
    vector<Edge> G[maxn];
    bool bfs() {
        level.assign(n, -1);
        level[s] = 0;
        queue<int> que; que.push(s);
        while (que.size()) {
            int tmp = que.front(); que.pop();
            for (auto e : G[tmp]) {
                if (e.cap > 0 && level[e.to] == -1) {
                    level[e.to] = level[tmp] + 1;
                    que.push(e.to);
                }
            }
        }
        return level[t] != -1;
    }
    int flow(int now, int low) {
        if (now == t) return low;
        int ret = 0;
        for (auto &e : G[now]) {
            if (e.cap > 0 && level[e.to] == level[now] + 1) {
                int tmp = flow(e.to, min(e.cap, low - ret));
                e.cap -= tmp; G[e.to][e.rev].cap += tmp;
            }
        }
    }
}

```

```

        ret += tmp;
    }
}
if (ret == 0) level[now] = -1;
return ret;
}
Dinic(int _n, int _s, int _t): n(_n), s(_s), t(_t) {
    fill(G, G + maxn, vector<Edge>());
}
void add_edge(int a, int b, int c) {
    G[a].push_back(Edge(b, c, G[b].size()));
    G[b].push_back(Edge(a, 0, G[a].size() - 1));
}
int maxflow() {
    int ret = 0;
    while (bfs()) ret += flow(s, inf);
    return ret;
}
};

```

## 2.2 MinCostMaxFlow

```

struct MincostMaxflow {
    struct Edge {
        int to, rev, cap, w;
        Edge() {}
        Edge(int a, int b, int c, int d): to(a), cap(b), w(
            c), rev(d) {}
    };
    int n, s, t;
    vector<int> p, id, d;
    bitset<maxn> inque;
    vector<Edge> G[maxn];
    pair<int, int> spfa() {
        p.assign(n, -1);
        d.assign(n, inf);
        id.assign(n, -1);
        d[s] = 0; p[s] = s;
        queue<int> que; que.push(s); inque[s] = true;
        while (que.size()) {
            int tmp = que.front(); que.pop();
            inque[tmp] = false;
            int i = 0;
            for (auto e : G[tmp]) {
                if (e.cap > 0 && d[e.to] > d[tmp] + e.w) {
                    d[e.to] = d[tmp] + e.w;
                    p[e.to] = tmp;
                    id[e.to] = i;
                    if (!inque[e.to]) que.push(e.to), inque[e.to]
                        = true;
                }
                ++i;
            }
            if (d[t] == inf) return make_pair(-1, -1);
            int a = inf;
            for (int i = t; i != s; i = p[i]) {
                a = min(a, G[p[i]][id[i]].cap);
            }
            for (int i = t; i != s; i = p[i]) {
                Edge &e = G[p[i]][id[i]];
                e.cap -= a; G[e.to][e.rev].cap += a;
            }
            return make_pair(a, d[t]);
        }
    }
    MincostMaxflow(int _n, int _s, int _t): n(_n), s(_s),
        t(_t) {
        fill(G, G + maxn, vector<Edge>());
    }
    void add_edge(int a, int b, int cap, int w) {
        G[a].push_back(Edge(b, cap, w, (int)G[b].size()));
        G[b].push_back(Edge(a, 0, -w, (int)G[a].size() - 1)
            );
    }
    pair<int, int> maxflow() {
        int mxf = 0, mnc = 0;
        while (true) {
            pair<int, int> res = spfa();
            if (res.first == -1) break;
            mxf += res.first; mnc += res.first * res.second;
        }
    }
};

```

```

    }
    return make_pair(mxf, mnc);
}
};

```

## 2.3 Maximum weighted Bipartite matching

```

struct Hungarian {
    vector<int> lx, ly, match;
    vector<vector<int>> w;
    int n;
    bitset<maxn> s, t;
    bool dfs(int now) {
        s[now] = true;
        for (int i = 0; i < n; ++i) {
            if (lx[now] + ly[i] == w[now][i] && !t[i]) {
                t[i] = true;
                if (match[i] == -1 || dfs(match[i])) {
                    match[i] = now;
                    return true;
                }
            }
        }
        return false;
    }
    void relabel() {
        int a = inf;
        for (int i = 0; i < n; ++i) if (s[i]) {
            for (int j = 0; j < n; ++j) if (!t[j]) {
                a = min(a, lx[i] + ly[j] - w[i][j]);
            }
        }
        for (int i = 0; i < n; ++i) {
            if (s[i]) lx[i] -= a;
            if (t[i]) ly[i] += a;
        }
    }
    Hungarian(int n): n(n) {
        w.assign(n, vector<int>());
        for (int i = 0; i < n; ++i) w[i].assign(n, 0);
        lx.assign(n, 0); ly.assign(n, 0);
        match.assign(n, -1);
    }
    void add_edge(int a, int b, int c) {
        w[a][b] = c;
    }
    int solve() {
        for (int i = 0; i < n; ++i) for (int j = 0; j < n;
            ++j) lx[i] = max(lx[i], w[i][j]);
        for (int i = 0; i < n; ++i) {
            while (true) {
                s.reset(); t.reset();
                if (dfs(i)) break;
                else relabel();
            }
        }
        int ans = 0;
        for (int i = 0; i < n; ++i) ans += w[match[i]][i];
        return ans;
    }
};

```

## 3 Math

### 3.1 FFT

```

const double pi = acos(-1);
const complex<double> I(0, 1);
complex<double> omega[maxn + 1];

void prefft() {
    for (int i = 0; i <= maxn; ++i) omega[i] = exp(i * 2
        * pi / maxn * I);
}
void fft(vector<complex<double>>& a, int n, bool inv=
    false) {

```

```

int basic = maxn / n;
int theta = basic;
for (int m = n; m >= 2; m >= 1) {
    int h = m > 1;
    for (int i = 0; i < h; ++i) {
        complex<double> w = omega[inv ? maxn - (i * theta
% maxn) : i * theta % maxn];
        for (int j = i; j < n; j += m) {
            int k = j + h;
            complex<double> x = a[j] - a[k];
            a[j] += a[k];
            a[k] = w * x;
        }
    }
    theta = (theta * 2) % maxn;
}
int i = 0;
for (int j = 1; j < n - 1; ++j) {
    for (int k = n > 1; k > (i ^= k); k >= 1);
    if (j < i) swap(a[i], a[j]);
}
if (inv) for (int i = 0; i < n; ++i) a[i] /= (double)
n;
}
void invfft(vector<complex<double>>& a, int n) {
    fft(a, n, true);
}

```

### 3.2 Miller-Rabin

```

// n < 4759123141   chk = [2, 7, 61]
// n < 1122004669633 chk = [2, 13, 23, 1662803]
// n < 2^64         chk = [2, 325, 9375, 28178, 450775,
9780504, 1795265022]

long long fpow(long long a, long long n, long long mod)
{
    long long ret = 1LL;
    for (; n >= 1) {
        if (n & 1) ret = (__int128)ret * (__int128)a % mod;
        a = (__int128)a * (__int128)a % mod;
    }
    return ret;
}
bool check(long long a, long long u, long long n, int t
) {
    a = fpow(a, u, n);
    if (a == 0) return true;
    if (a == 1 || a == n - 1) return true;
    for (int i = 0; i < t; ++i) {
        a = (__int128)a * (__int128)a % n;
        if (a == 1) return false;
        if (a == n - 1) return true;
    }
    return false;
}
bool is_prime(long long n) {
    if (n < 2) return false;
    if (n % 2 == 0) return n == 2;
    long long u = n - 1; int t = 0;
    for (; u & 1; u >= 1, ++t);
    for (long long i : chk) {
        if (!check(i, u, n, t)) return false;
    }
    return true;
}

```

### 3.3 Extend GCD

```

template <typename T> tuple<T, T, T> extgcd(T a, T b) {
    if (!b) return make_tuple(a, 1, 0);
    T d, x, y;
    tie(d, x, y) = extgcd(b, a % b);
    return make_tuple(d, y, x - (a / b) * y);
}

```

### 3.4 Matrix

```

template <typename T> class Matrix {
public:
    int n, m, mod;
    vector<vector<T>> mat;
    Matrix(int n, int m, int mod=0, bool I=false): n(n)
, m(m), mod(mod) {
        mat.resize(n);
        for (int i = 0; i < n; ++i) mat[i].resize(m);
        if (!I) return;
        for (int i = 0; i < n; ++i) mat[i][i] = 1;
    }
    Matrix operator+(const Matrix& rhs) const {
        Matrix ret(n, m, mod);
        for (int i = 0; i < n; ++i) {
            for (int j = 0; j < m; ++j) {
                ret.mat[i][j] = mat[i][j] + rhs.mat[i][j];
                if (mod) ret.mat[i][j] %= mod;
            }
        }
        return ret;
    }
    Matrix operator-(const Matrix& rhs) const {
        Matrix ret(n, m, mod);
        for (int i = 0; i < n; ++i) {
            for (int j = 0; j < m; ++j) {
                ret.mat[i][j] = mat[i][j] - rhs.mat[i][j];
                if (mod) {
                    ret.mat[i][j] %= mod;
                    ret.mat[i][j] += mod;
                    ret.mat[i][j] %= mod;
                }
            }
        }
        return ret;
    }
    Matrix operator*(const Matrix& rhs) const {
        Matrix ret(n, rhs.m, mod);
        for (int i = 0; i < n; ++i) {
            for (int j = 0; j < rhs.m; ++j) {
                for (int k = 0; k < m; ++k) {
                    if (mod) ret.mat[i][j] = (ret.mat[i][j] +
mat[i][k] * rhs.mat[k][j] % mod) % mod;
                    else ret.mat[i][j] += mat[i][k] * rhs.mat[k
][j];
                }
            }
        }
        return ret;
    }
};

```

## 4 Graph

### 4.1 Strongly connected components

```

struct SCC {
    vector<int> G[maxn], R[maxn], topo;
    int n, nscc;
    vector<int> scc, sz;
    bitset<maxn> v;
    void dfs(int now) {
        v[now] = true;
        scc[now] = nscc;
        ++sz[nscc];
        for (int u : G[now]) if (!v[u]) {
            dfs(u);
        }
    }
    void rdfs(int now) {
        v[now] = true;
        for (int u : R[now]) if (!v[u]) {
            rdfs(u);
        }
        topo.push_back(now);
    }
    SCC(): {}
}

```

```

SCC(int n): n(n) {
    scc.assign(n, 0); sz.assign(n, 0);
}
void add_edge(int a, int b) {
    G[a].push_back(b);
    R[b].push_back(a);
}
void solve() {
    v.reset();
    for (int i = 0; i < n; ++i) if (!v[i]) rdfs(i);
    reverse(topo.begin(), topo.end());
    v.reset();
    for (int i : topo) if (!v[i]) {
        ++nsc;
        dfs(i);
    }
}
};

```

## 4.2 Heavy-Light Decomposition

```

struct HeavyLightDecomp {
    vector<int> G[maxn];
    vector<int> tin, top, dep, maxson, sz, p;
    int n, t;
    void dfs(int now, int fa, int d) {
        dep[now] = d;
        maxson[now] = -1;
        sz[now] = 1;
        p[now] = fa;
        for (int u : G[now]) if (u != fa) {
            dfs(u, now, d + 1);
            sz[now] += sz[u];
            if (maxson[now] == -1 || sz[u] > sz[maxson[now]])
                maxson[now] = u;
        }
    }
    void link(int now, int tp) {
        top[now] = tp;
        tin[now] = ++t;
        if (maxson[now] == -1) return;
        link(maxson[now], tp);
        for (int u : G[now]) if (u != p[now]) {
            if (u == maxson[now]) continue;
            link(u, u);
        }
    }
    HeavyLightDecomp(int n): n(n) {
        t = 0;
        tin.assign(n, 0); top.assign(n, 0); dep.assign(n, 0);
        maxson.assign(n, 0); sz.assign(n, 0); p.assign(n, 0);
    }
    void add_edge(int a, int b) {
        G[a].push_back(b);
        G[b].push_back(a);
    }
    void build() {
        dfs(0, -1, 0);
        link(0, 0);
    }
    int lca(int a, int b) {
        int ta = top[a], tb = top[b];
        while (ta != tb) {
            if (dep[ta] < dep[tb]) {
                swap(ta, tb); swap(a, b);
            }
            a = p[ta]; ta = top[a];
        }
        if (a == b) return a;
        return dep[a] < dep[b] ? a : b;
    }
    vector<pair<int, int>> get_path(int a, int b) {
        int ta = top[a], tb = top[b];
        vector<pair<int, int>> ret;
        while (ta != tb) {
            if (dep[ta] < dep[tb]) {
                swap(ta, tb); swap(a, b);
            }
        }
    }
}

```

```

        ret.push_back(make_pair(tin[ta], tin[a]));
        a = p[ta]; ta = top[a];
    }
    ret.push_back(make_pair(min(tin[a], tin[b]), max(
        tin[a], tin[b])));
    return ret;
}
};

```

## 4.3 2-Satisfiability

```

struct TwoSat {
    vector<int> G[maxn << 1];
    bitset<maxn << 1> v;
    vector<int> s;
    int c;
    bool dfs(int now) {
        if (v[now ^ 1]) return false;
        if (v[now]) return true;
        v[now] = true;
        s[c++] = now;
        for (int u : G[now]) if (!dfs(u)) return false;
        return true;
    }
    TwoSat() {
        s.assign(maxn << 1, 0);
        v.reset();
    }
    void add_edge(int a, int b) {
        G[a].push_back(b);
    }
    bool solve() {
        for (int i = 0; i < maxn << 1; i += 2) {
            if (!v[i] && !v[i + 1]) {
                c = 0;
                if (!dfs(i)) {
                    while (c) v[s[--c]] = false;
                    if (!dfs(i + 1)) return false;
                }
            }
        }
        return true;
    }
}
};

```

## 5 Data Structures

### 5.1 Treap

```

struct Treap {
#define size(t) (t ? t->sz : 0)
    struct Node {
        int val;
        int pri, sz;
        Node *lc, *rc;
        Node(T v): pri(rand()), val(v) {
            lc = rc = nullptr;
            sz = 1;
        }
        void pull() {
            sz = size(lc) + size(rc) + 1;
        }
    } *root;
    Node *merge(Node *a, Node *b) {
        if (!a || !b) return a ? a : b;
        if (a->pri > b->pri) {
            a->rc = merge(a->rc, b);
            a->pull();
            return a;
        } else {
            b->lc = merge(a, b->lc);
            b->pull();
            return b;
        }
    }
    void split(Node *t, int k, Node *&a, Node *&b) {

```

```

    if (!t) { a = b = nullptr; return; }
    if (t->val <= k) {
        a = t;
        split(t->rc, k, a->rc, b);
        a->pull();
    } else {
        b = t;
        split(t->lc, k, a, b->lc);
        b->pull();
    }
}
int kth(Node *t, int k) {
    if (size(t->lc) + 1 == k) return t->val;
    if (size(t->lc) + 1 > k) return kth(t->lc, k);
    return kth(t->rc, k - size(t->lc) - 1);
}
void clear(Node *t) {
    if (!t) return;
    if (t->lc) clear(t->lc);
    if (t->rc) clear(t->rc);
    delete t;
}
Treap(unsigned seed=time(nullptr)) {
    srand(seed);
    root = nullptr;
}
~Treap() {
    clear(root);
    root = nullptr;
}
void insert(int val) {
    Node *a, *b;
    split(root, val - 1, a, b);
    root = merge(merge(a, new Node(val)), b);
}
void erase(int val) {
    Node *a, *b, *c, *d;
    split(root, val - 1, a, b);
    split(b, val, c, d);
    c = merge(c->lc, c->rc);
    root = merge(a, merge(c, d));
}
int find(int k) {
    return kth(root, k);
}
#undef size
};

```

## 5.2 Leftlist Tree

```

template <typename T> class LeftlistTree {
private:
#define rank(t) (t ? t->s : 0)
    struct Node {
        T val;
        int s;
        Node *lc, *rc;
        Node(T v): val(v) {
            lc = rc = nullptr;
            s = 1;
        }
    } *root;
    Node *merge(Node *a, Node *b) {
        if (!a || !b) return a ? a : b;
        if (a->val < b->val) swap(a, b);
        a->rc = merge(a->rc, b);
        if (rank(a->lc) < rank(a->rc)) swap(a->lc, a->rc);
        a->s = rank(a->rc) + 1;
        return a;
    }
    void clear(Node *t) {
        if (!t) return;
        if (t->lc) clear(t->lc);
        if (t->rc) clear(t->rc);
        delete t;
    }
public:
    LeftlistTree() {
        root = nullptr;
    }

```

```

    }
    void push(T val) {
        root = merge(root, new Node(val));
    }
    void pop() {
        T ret = root->val;
        Node *tmp = root;
        root = merge(root->lc, root->rc);
        delete tmp;
    }
    T top() {
        return root->val;
    }
    void merge(LeftlistTree t) {
        root = merge(root, t->root);
    }
};

```

## 6 Geometry

### 6.1 Points

```

struct pt {
    double x, y;
    pt(): x(0.0), y(0.0) {}
    pt(double x, double y): x(x), y(y) {}
    pt operator+(const pt& a) const { return pt(x + a.x,
        y + a.y); }
    pt operator-(const pt& a) const { return pt(x - a.x,
        y - a.y); }
    double operator*(const pt& a) const { return x * a.x
        + y * a.y; }
    double operator^(const pt& a) const { return x * a.y
        - y * a.x; }
    bool operator<(const pt& a) const { return x == a.x ?
        y < a.y : x < a.x; }
};

```

### 6.2 Convex Hull

```

double cross(const pt& o, const pt& a, const pt& b) {
    return (a - o) ^ (b - o);
}

int rsd;

vector<pt> convex_hull(vector<pt> p) {
    sort(p.begin(), p.end());
    int m = 0;
    vector<pt> ret(2 * p.size());
    for (int i = 0; i < p.size(); ++i) {
        while (m >= 2 && cross(ret[m - 2], ret[m - 1], p[i]) < 0) --m;
        ret[m++] = p[i];
    }
    rsd = m - 1;
    for (int i = p.size() - 2, t = m + 1; i >= 0; --i) {
        while (m >= t && cross(ret[m - 2], ret[m - 1], p[i]) < 0) --m;
        ret[m++] = p[i];
    }
    ret.resize(m - 1);
    return ret;
}

```

### 6.3 Rotating Caliper

```

void rotating_caliper(vector<pt> p) {
    vector<pt> ch = convex_hull(p);
    int tbz = ch.size();
    int lpr = 0, rpr = rsd;
    // ch[lpr], ch[rpr]
    while (lpr < rsd || rpr < tbz - 1) {
        if (lpr < rsd && rpr < tbz - 1) {

```

```

    pt rvt = ch[rpr + 1] - ch[rpr];
    pt lvt = ch[lpr + 1] - ch[lpr];
    if ((lvt ^ rvt) < 0) ++lpr;
    else ++rpr;
}
else if (lpr == rsd) ++rpr;
else ++lpr;
// ch[lpr], ch[rpr]
}
}

```

## 7 String

### 7.1 KMP

```

int f[maxn];

int kmp(const string& a, const string& b) {
    f[0] = -1; f[1] = 0;
    for (int i = 1, j = 0; i < b.size() - 1; f[++i] = ++j) {
        if (b[i] == b[j]) f[i] = f[j];
        while (j != -1 && b[i] != b[j]) j = f[j];
    }
    for (int i = 0, j = 0; i - j + b.size() <= a.size(); ++i, ++j) {
        while (j != -1 && a[i] != b[j]) j = f[j];
        if (j == b.size() - 1) return i - j;
    }
    return -1;
}

```

### 7.2 Suffix Array

```

struct SuffixArray {
    int sa[maxn], tmp[2][maxn], c[maxn], _lcp[maxn], r[
        maxn], n;
    string s;
    SparseTable st;
    void suffixarray() {
        int* rank = tmp[0];
        int* nRank = tmp[1];
        int A = 128;
        for (int i = 0; i < A; ++i) c[i] = 0;
        for (int i = 0; i < s.length(); ++i) c[rank[i] = s[
            i]]++;
        for (int i = 1; i < A; ++i) c[i] += c[i - 1];
        for (int i = s.length() - 1; i >= 0; --i) sa[--c[s[
            i]]] = i;
        for (int n = 1; n < s.length(); n *= 2) {
            for (int i = 0; i < A; ++i) c[i] = 0;
            for (int i = 0; i < s.length(); ++i) c[rank[i
                ]]++;
            for (int i = 1; i < A; ++i) c[i] += c[i - 1];
            int* sa2 = nRank;
            int r = 0;
            for (int i = s.length() - n; i < s.length(); ++i)
                sa2[r++] = i;
            for (int i = 0; i < s.length(); ++i) if (sa[i] >=
                n) sa2[r++] = sa[i] - n;
            for (int i = s.length() - 1; i >= 0; --i) sa[--c[
                rank[sa2[i]]]] = sa2[i];
            nRank[sa[0]] = r = 0;
            for (int i = 1; i < s.length(); ++i) {
                if (!rank[sa[i - 1]] == rank[sa[i]] && sa[i -
                    1] + n < s.length() && rank[sa[i - 1] + n] == rank[
                    sa[i] + n])) r++;
                nRank[sa[i]] = r;
            }
            swap(rank, nRank);
            if (r == s.length() - 1) break;
            A = r + 1;
        }
    }
    void solve() {
        suffixarray();
    }
}

```

```

for (int i = 0; i < n; ++i) r[sa[i]] = i;
int ind = 0; _lcp[0] = 0;
for (int i = 0; i < n; ++i) {
    if (!r[i]) { ind = 0; continue; }
    while (i + ind < n && s[i + ind] == s[sa[r[i] -
        1] + ind]) ++ind;
    _lcp[r[i]] = ind ? ind-- : 0;
}
st = SparseTable(n, _lcp);
}
int lcp(int L, int R) {
    if (L == R) return n - L - 1;
    L = r[L]; R = r[R];
    if (L > R) swap(L, R);
    ++L;
    return st.query(L, R);
}
SuffixArray(string s): s(s), n(s.length()) {}
SuffixArray() {}
};

```

## 8 Dynamic Programming

### 8.1 DP optimizations

$dp[k][n] = \max_{i < n} dp[k-1][i] + f(i+1, n)$  and the monotony  $t[k][i] \leq t[k][j], \forall i < j$  holds