

TECNOLÓGICO DE MONTERREY

FUNDAMENTOS DE COMPUTACIÓN

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## Homework 11

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# 1 Problems

Solve the following problems:

1. Provide a parallel algorithm for merging two lists of  $n/2$  keys each. State the number of processors used and compute the metrics  $S_p$ ,  $E_p$  and  $R_p$ .
2. Given the binary fan-in technique described in class to calculate the maximum of  $n$  numbers, calculate its speed-up ratio and its efficiency with respect to the sequential tournament version of the algorithm.
3. Prove (and provide an example) that the multiplication of two  $n \times n$  matrices can be conducted by a PRAM program in  $O(\log_2 n)$  steps if  $n^3$  processors are available.
4. Let a binary operation take  $k$  cycles to complete when done serially. If this operation is pipelined using a  $k$ -segment pipe, show that the resulting speed-up in computing  $n$  operations is

$$S_k = \frac{nk}{n + k - 1}$$