CSE 241 Algorithms and Data Structures

8/31/2015

Fast Closest-Pair Algorithm

This handout gives pseudocode for the $\Theta(n \log n)$ closest-pair algorithm in the form I presented in class. In this handout and all future ones, I'm pretty sure the pseudocode is correct, but I make no iron-clad guarantees – if something looks wrong to you, think before you implement!

Keep in mind that the arrays ptsByX and ptsByY in the algorithm (a) are assumed to be sorted by x and y coordinate respectively and (b) are actually references to a common set of points, not two distinct point sets. n is the number of points.

```
CLOSESTPAIR(ptsByX, ptsByY, n)
  if n=1
      return \infty
  if n=2
      return distance(ptsByX[0], ptsByX[1])
  mid \leftarrow \lceil n/2 \rceil - 1

▷ divide into two subproblems

  copy ptsByX[0... mid] into new array XL in x order.
  copy ptsByX[mid+1...n-1] into new array XR in x order.
  copy ptsByY into arrays YL and YR in y order, s.t.
       XL and YL refer to same points, as do XR and YR
  distL \leftarrow ClosestPair(XL, YL, \lceil n/2 \rceil)
                                                                                 ▷ conquer
  distR \leftarrow ClosestPair(XR, YR, \lfloor n/2 \rfloor)
  midPoint \leftarrow ptsByX[mid]
                                                                                ▷ combine
  lrDist \leftarrow \min(distL, distR)
  Construct array yStrip, in increasing y order, of all
       points p in ptsByY s.t. |p.x - \text{mid.}x| < \text{lrDist}
  minDist \leftarrow lrDist
  for j in 0 ... yStrip.length -2 do
      k \leftarrow j + 1
      while k \leq yStrip.length - 1 and
               yStrip[k].y - yStrip[j].y < lrDist do
          d \leftarrow \text{distance}(\text{yStrip}[j], \text{yStrip}[k])
          \min \text{Dist} \leftarrow \min(\min \text{Dist}, d)
          k++
  return minDist
```