

# Consumption Heterogeneity: Micro Drivers and Macro Implications

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GRIPS-UT

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Viewpoints and conclusions stated in this paper are the responsibility of the authors alone and do not necessarily reflect the viewpoints of the Federal Reserve Board or Danmarks Nationalbank.

# What Do We Do?

We estimate the **consumption response**  
to permanent and transitory **shocks to income**  
for **different groups** of households

# Hasn't This Been Done Before?

Yes, but...

Our **method** addresses bias in previous results

Our **data** allows sharp focus on household heterogeneity

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## Time Aggregation Problem

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Sample size in millions  
Detailed balance sheet

# Why Do We Care? (as macroeconomists)

- 1) Heterogenous agent models have testable micro behavior
- 2) Quantify Macro Implications

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e.g. Consumption smoothing requires liquid wealth



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e.g. Redistribution in Monetary Policy



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Low Liquid Wealth Households:

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High Liquid Wealth Households:

- Large Response to Transitory Shocks (25 cents per dollar)
- Small Response to Permanent Shocks (60 cents per dollar)

relative to Permanent Income Hypothesis or Buffer-Stock models

# What do we find? (Redistribution in Monetary Policy)



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Medium MPX  
 $\approx 0.5$



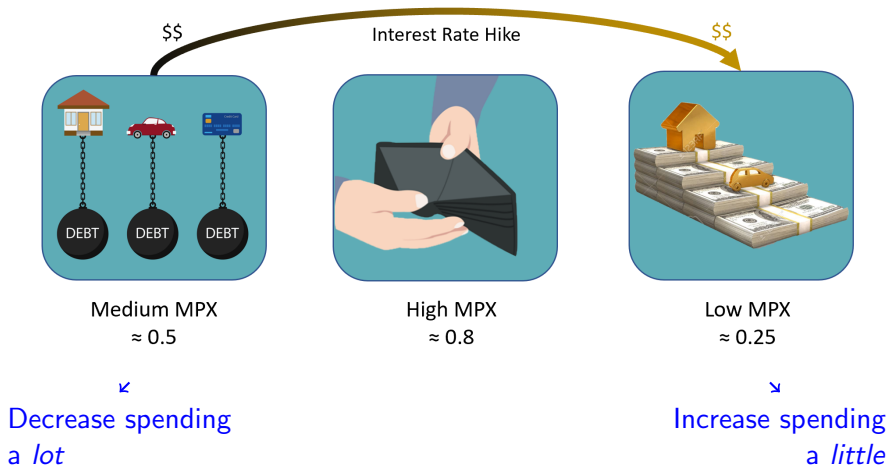
High MPX  
 $\approx 0.8$



Low MPX  
 $\approx 0.25$

MPX: Marginal Propensity to eXpend (includes durables)

# What do we find? (Redistribution in Monetary Policy)



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1yr rate  $\uparrow$  1%

Aggregate Spending  $\downarrow$  26 basis points



Through this redistribution channel *alone*

# How Do We Do This? Reduced Form Approach

Identifying Restrictions on

**Income**

and

**Consumption**

In **Continuous** Time

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Identifying Restrictions on

**Income**  Permanent (random walk) shocks  
Transitory (<2 years) shocks

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In **Continuous** Time  Time Aggregation Problem

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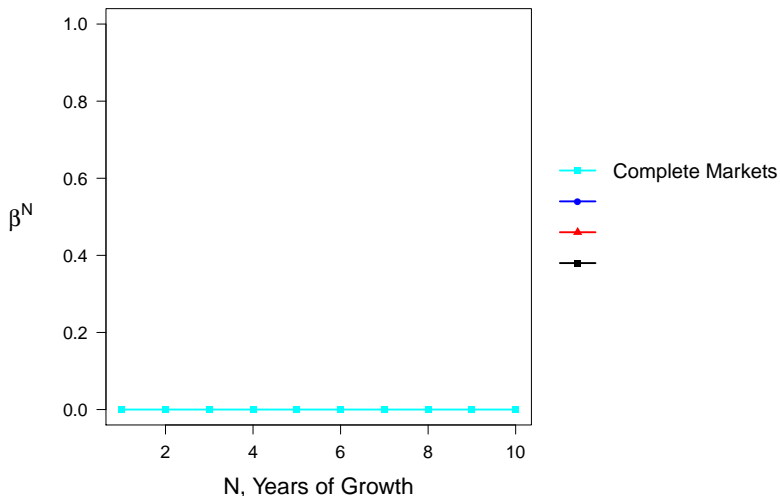
In **Continuous** Time  Time Aggregation Problem

But first some intuition: Naïvely Regress

Change in Consumption on Change in Income (over N years)

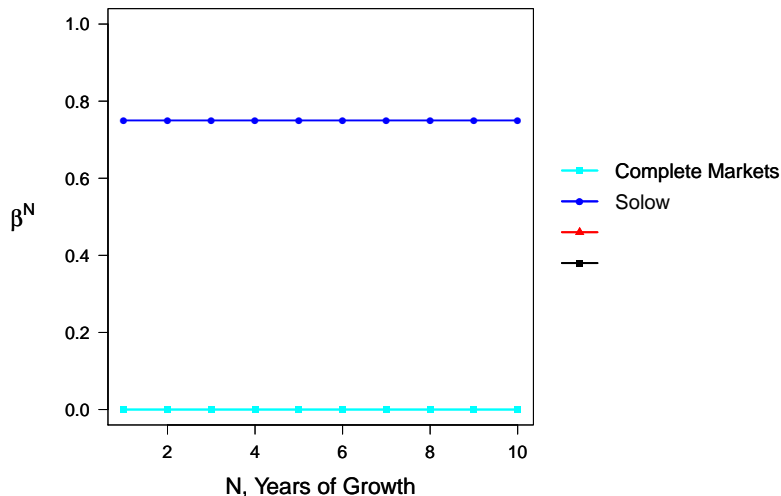
# Naïve Regression: Consumption Growth on Income Growth

$$\Delta^N c_i = \alpha^N + \beta^N \Delta^N y_i + \varepsilon_i$$



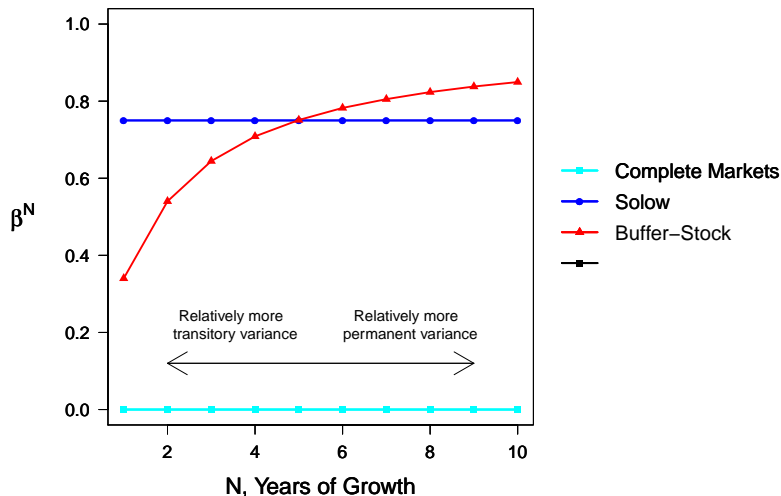
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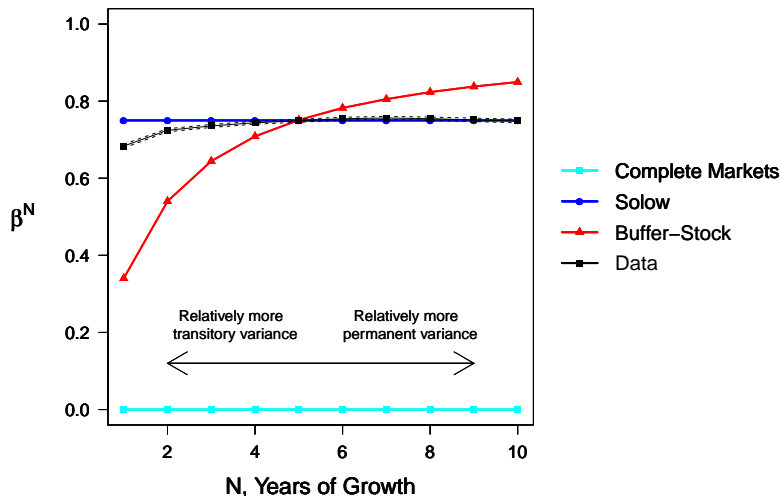
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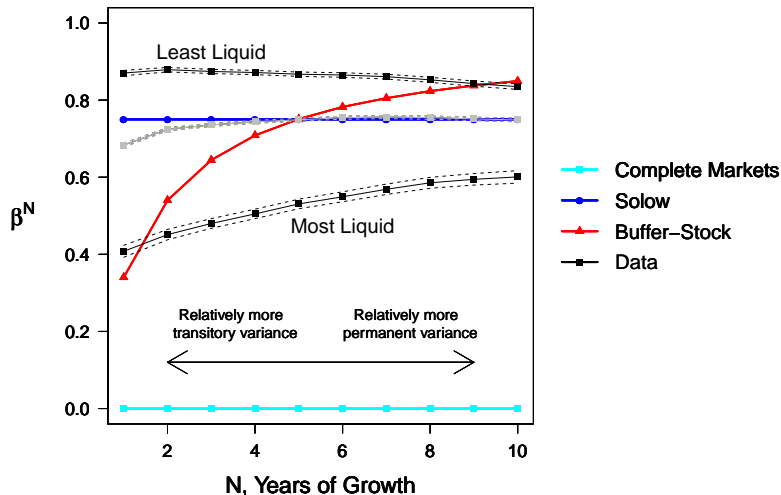
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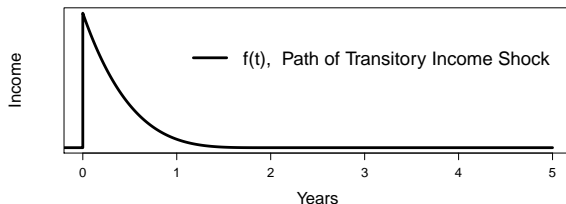
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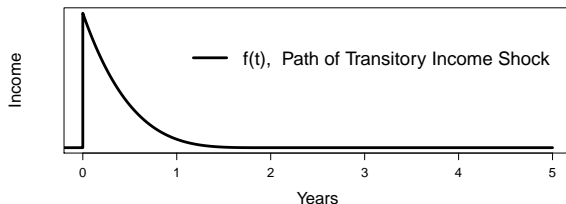
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- Permanent Income (random walk)
- Transitory Income (persistence  $< 2$  years)



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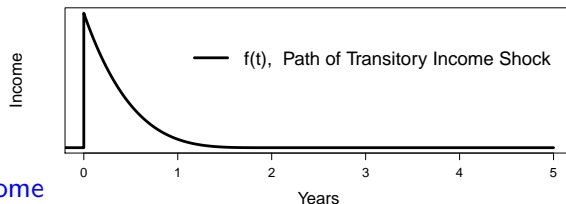
$$y_t = p_t + \int_{t-2}^t f(t-s) dq_s$$

Below the equation, two blue arrows point from the terms to their descriptions:

- A blue arrow points from  $p_t$  to the text "Permanent income flow".
- A blue arrow points from  $\int_{t-2}^t f(t-s) dq_s$  to the text "Transitory income flow".

# Identification Restrictions: Income Process

- Permanent Income (random walk)
- Transitory Income (persistence < 2 years)



Observed Income

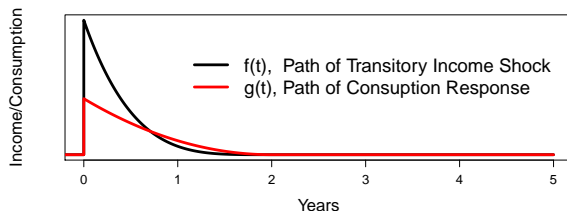
$$\bar{y}_T = \int_{T-1}^T y_t dt = \int_{T-1}^T p_t dt + \int_{T-1}^T \int_{t-2}^t f(t-s) dq_s dt$$

Time Aggregation

# Identification Restrictions: Consumption Response

- Permanent: Moves by fraction  $\phi$  of shock
- Transitory: Persistence  $< 2$  years

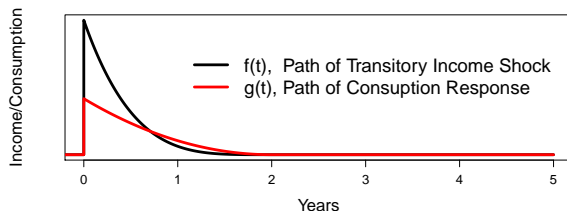
Evidence



# Identification Restrictions: Consumption Response

- Permanent: Moves by fraction  $\phi$  of shock
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Evidence



$$c_t = \phi p_t + \int_{t-2}^t g(t-s) dq_s$$

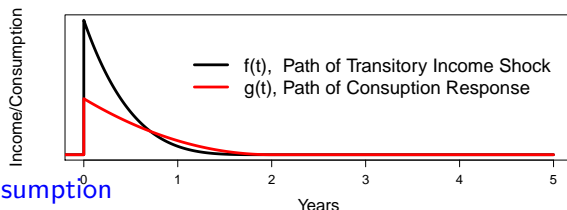
Permanent consumption flow

Transitory consumption flow

# Identification Restrictions: Consumption Response

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Evidence



Observed Consumption

$$\bar{c}_T = \int_{T-1}^T c_t dt = \int_{T-1}^T \phi p_t dt + \int_{T-1}^T \int_{t-2}^t g(t-s) dq_s dt$$

Time Aggregation

We use GMM on the equations:

$$\begin{aligned}\text{Var}(\Delta^N \bar{y}_T) &= \left(N - \frac{1}{3}\right) \sigma_p^2 + 2\sigma_{\tilde{q}}^2 \\ \text{Cov}(\Delta^N \bar{c}_T, \Delta^N \bar{y}_T) &= \phi \left(N - \frac{1}{3}\right) \sigma_p^2 + 2\psi \sigma_{\tilde{q}}^2\end{aligned}$$

with  $N = 3, 4, 5$  (and  $T = 2007, \dots, 2015$ ) to identify:

- $\sigma_p^2$ : Permanent shock variance
- $\sigma_{\tilde{q}}^2$ : (Time aggregated) transitory shock variance
- $\phi$ : MPX out of permanent income shocks
- $\psi$ : MPX out of transitory income shocks

where  $\psi$  is the regression coefficient of 'transitory' consumption on transitory income

# Why Not Blundell, Pistaferri and Preston 2008?

## Key to BPP Identification

Transitory shock year  $t$

$\Delta y_{t+1} = \Delta p_{t+1} + \Delta \varepsilon_{t+1}$  is a *valid instrument* for  $\varepsilon_t$





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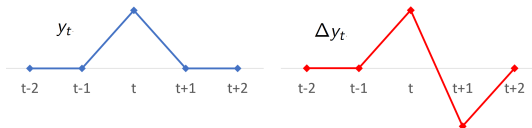
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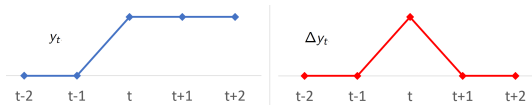
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- Uncorrelated with permanent shocks in year  $t$



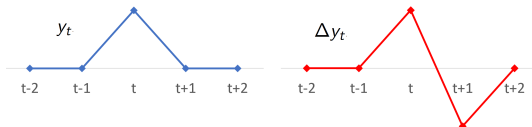
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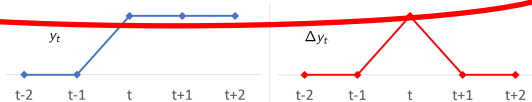
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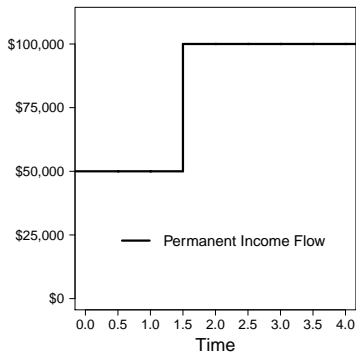


- Uncorrelated with permanent shocks in year  $t$

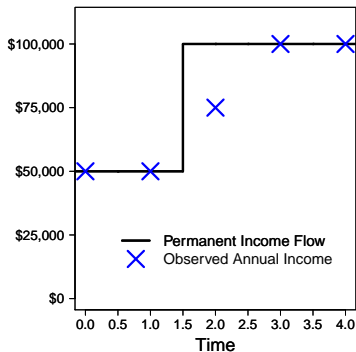


Fails due to the **Time Aggregation Problem**

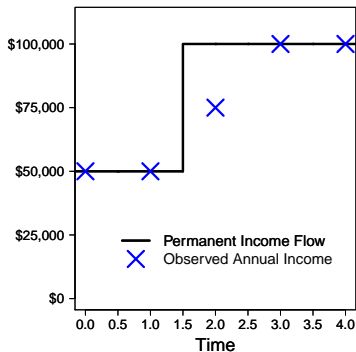
# Time Aggregation Problem in BPP (Crawley 2018)



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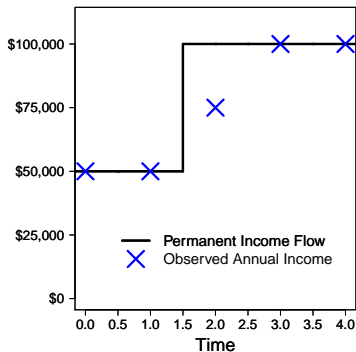


Observed permanent income growth is *positively* autocorrelated

BPP misinterprets *positive* permanent income shocks as *negative* transitory shocks

⇒ Thinks negative transitory shocks result in consumption *increasing*

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If the Permanent Income Hypothesis holds, BPP will estimate the MPC to be -0.6

What we need:

- Panel Data on **Income** and **Expenditure**
- Household **Balance Sheets**



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What we have: Registry data for all Danish households

- **Income**

Third party reported

After-tax, restrict to heads aged 30-55

- **Balance Sheet**

Wealth on 31 Dec

Asset category, mortgage tenure

Danish Mortgage Market

- **Expenditure**

No *direct* measure of spending

Intertemporal budget constraint

$$\text{Expenditure} = \text{Income} - \text{Saving}$$

Intertemporal budget constraint

$$\begin{aligned} \text{Expenditure} &= \text{Income} - \text{Saving} \\ &\quad \downarrow \\ &= \text{Change in Net Worth} \\ &\quad (\text{adj. for capital gains}) \end{aligned}$$

## Intertemporal budget constraint

$$\text{Expenditure} = \text{Income} - \text{Saving}$$

↓  
= Change in Net Worth  
(adj. for capital gains)

- Works well for households with simple financial lives
- Problem: Capital gains
  - Houses off balance sheet (exclude transaction years)
  - Exclude business owners
  - Capital gains based on a diversified index
- Noisy, but perhaps better than surveys (Kuchler et al. 2018)
- Huge sample size advantage: sample covers 7.6 million observations over 2004-2015

### Summary Statistics

# Data: When is Measurement Error a Problem?

We have the same issues as the regression:

$$\Delta c_i = \alpha + \beta \Delta y_i + \varepsilon_i$$

That is measurement error in:

$\Delta y_i$  leads to attenuation bias

$\Delta c_i$  should be uncorrelated with  $\Delta y_i$

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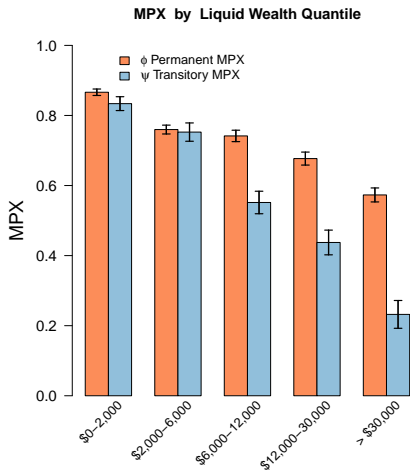
High quality income data

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When might this fail?

- Off balance sheet saving
- Returns correlated with *changes* in income (e.g. stock compensation)
- When insurance is provided by friends and family

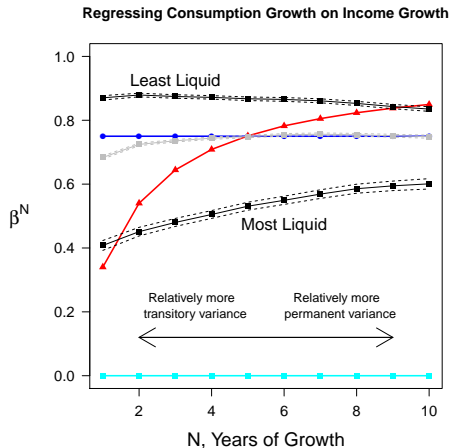
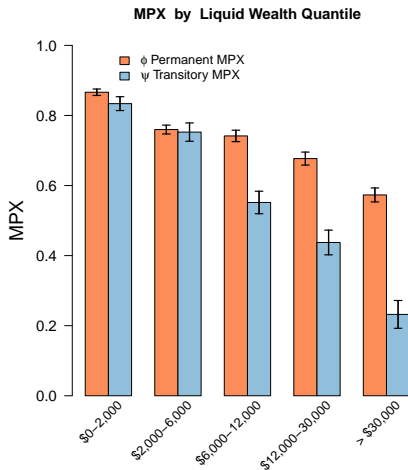
# Results by Liquid Wealth



MPX by Net Wealth



# MPX Results are Robust to Misspecification



MPX by Net Wealth

# Monetary Policy: Auclert's Decomposition

How does Monetary Policy Effect Aggregate Consumption?

- Intertemporal Substitution
- Aggregate Income

} Representative Agent Channels

# Monetary Policy: Auclert's Decomposition

→ Dominates in Rep. Agent NK models

How does Monetary Policy Effect Aggregate Consumption?

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→ Large in Spender-Saver, or TANK models

# Monetary Policy: Auclert's Decomposition

How does Monetary Policy Effect Aggregate Consumption?

- Intertemporal Substitution
  - Aggregate Income
  - Fisher (Inflationary debt relief)
  - Earnings Heterogeneity
  - Interest Rate Exposure
- } Representative Agent Channels
- } Redistribution Channels

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How can we *empirically* measure the size of the redistribution channels?

Need to know the distribution of MPCs along the relevant dimension of redistribution

## **Key assumption:**

Households treat redistribution like an income shock

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## Experiment

Short term real interest rate  $\uparrow$  1% for 1 year

Hold constant income and inflation

How does subsequent **redistribution** impact **aggregate consumption**?

Dimension of Redistribution: **Unhedged Interest Rate Exposure**

# Unhedged Interest Rate Exposure

URE Definition: Net savings made at this year's interest rate

$$URE_i = Y_i - C_i + A_i - L_i$$

Where

- $Y_i$  = Total after tax income
- $C_i$  = Total Expenditure, including interest payments
- $A_i$  = Maturing assets
- $L_i$  = Maturing liabilities



# Unhedged Interest Rate Exposure

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Interest rate change  $dR \implies$  Household  $i$ 's spending changes by:

$$dc_i = MPC_i URE_i \frac{dR}{R}$$

through the Interest Rate Exposure Channel *alone*.

# Interest Rate Exposure: Aggregation

Aggregate to find size of channel:

$$\begin{aligned} dc_i &= MPC_i URE_i \frac{dR}{R} \\ \Rightarrow \frac{dC}{C} &= \mathbb{E}_I \left( MPC_i \frac{URE_i}{\mathbb{E}_I(c_i)} \right) \frac{dR}{R} \end{aligned}$$

Define sufficient statistic:

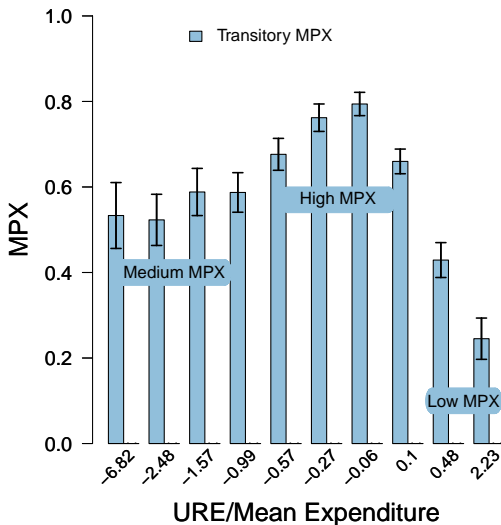
$$\mathcal{E}_R = \mathbb{E}_I \left( MPC_i \frac{URE_i}{\mathbb{E}_I(c_i)} \right)$$

$\Rightarrow$  Need to know the distribution of  $MPC_i$  with  $URE_i$

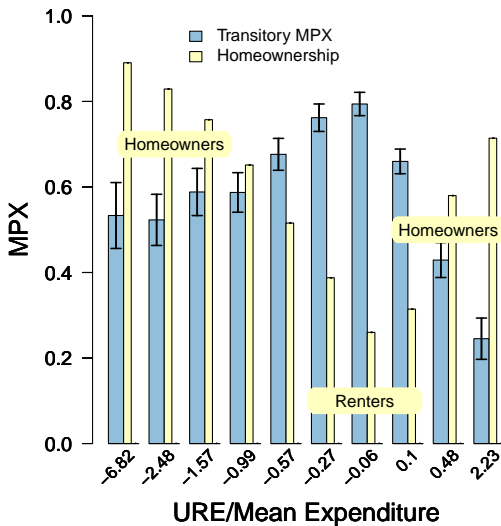
We can do that!

Out of Sample Assumptions

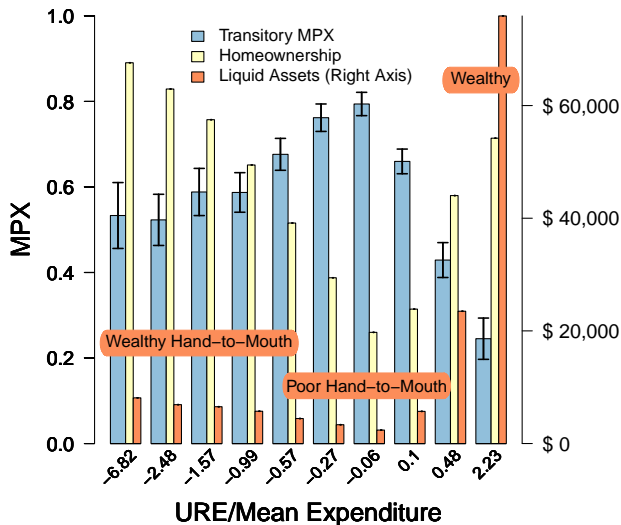
# MPX by Unhedged Interest Rate Exposure



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# All Five Transmission Channels

$$\frac{dC}{C} = \underbrace{\mathcal{M} \frac{dY}{Y}}_{\text{Aggregate Income Channel}} + \underbrace{\gamma \mathcal{E}_Y \frac{dY}{Y}}_{\text{Earnings Heterogeneity Channel}} + \underbrace{-\mathcal{E}_P \frac{dP}{P}}_{\text{Fisher Channel}} + \underbrace{+\mathcal{E}_R \frac{dR}{R}}_{\text{Interest Rate Exposure Channel}} + \underbrace{-\sigma \mathcal{S} \frac{dR}{R}}_{\text{Intertemporal Substitution Channel}}$$

---

|                 |       |
|-----------------|-------|
| $\mathcal{M}$   | 0.52  |
| $\mathcal{E}_Y$ | -0.03 |
| $\mathcal{E}_P$ | -0.75 |
| $\mathcal{E}_R$ | -0.26 |
| $\mathcal{S}$   | 0.49  |

---

# All Five Transmission Channels

$$\frac{dC}{C} = \underbrace{\mathcal{M} \frac{dY}{Y}}_{\text{Aggregate Income Channel}} + \underbrace{\mathcal{E}_R \frac{dR}{R}}_{\text{Interest Rate Exposure Channel}} + \underbrace{+\gamma \mathcal{E}_Y \frac{dY}{Y}}_{\text{Earnings Heterogeneity Channel}} + \underbrace{-\sigma S \frac{dR}{R}}_{\text{Intertemporal Substitution Channel}} + \underbrace{-\mathcal{E}_P \frac{dP}{P}}_{\text{Fisher Channel}}$$

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| $S$             | 0.49  |

Compare  $\mathcal{E}_R$  to  $\sigma S$ :

$\sigma \approx 0.1$  Best, Cloyne, Ilzetzi,  
and Kleven (2018)

$$\sigma S \approx 0.05$$

We have data on value of household cars

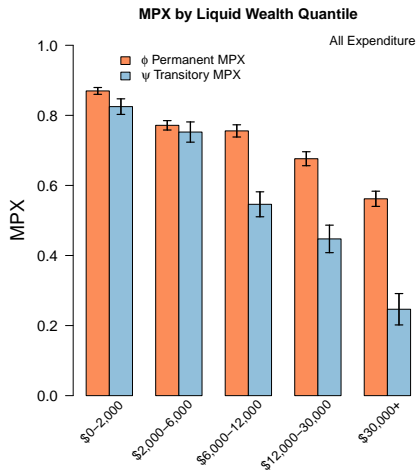
- Construct expenditure excluding car purchases and sales

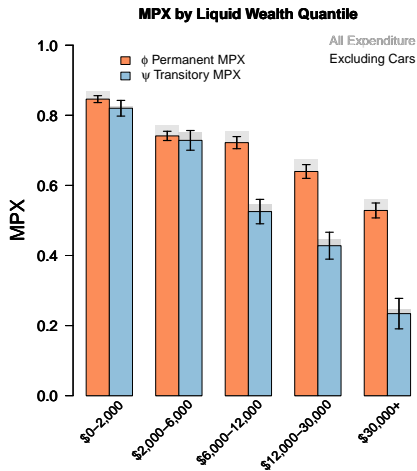
$$C_T^{\text{nocar}} = C_T - \Delta\text{CarValue}$$

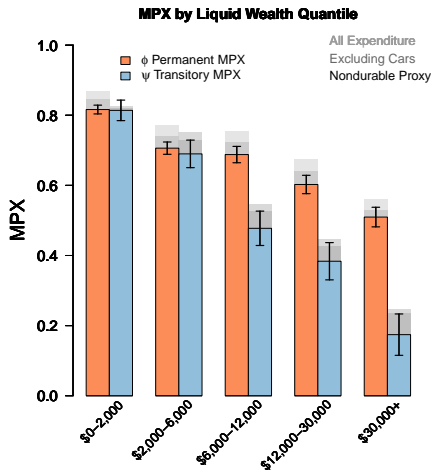
- Construct proxy for non durable consumption (Cars  $\approx$  42.1% durable expenditure)

$$C_T^{\text{nondurable}} = C_T - \frac{1}{0.421} \Delta\text{CarValue}$$









## New Method to Estimate Consumption Behavior

- Corrects for Bias in BPP
- Estimates align with natural experiment literature
- Potential to use on a wide variety of datasets and applications

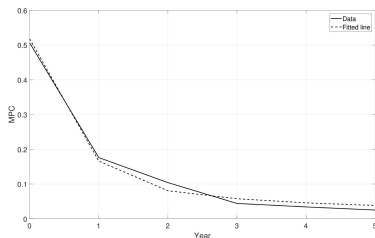
## Applied to Danish Registry Data

- Sample Size  $\implies$  Sharp Focus on Heterogeneity
- High MPC from transitory shocks, Low MPC from Permanent shocks
- Quantify Monetary Policy Transmission Channels

Thank you!

# Evidence of Consumption Decay Within 2 Years

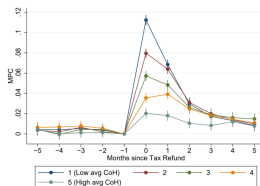
From Fagereng, Holm,  
and Natvik (2016)



Back

From Gelman (2016)

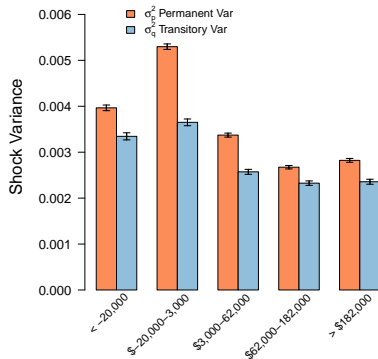
Figure 10: Tax refund impulse response function



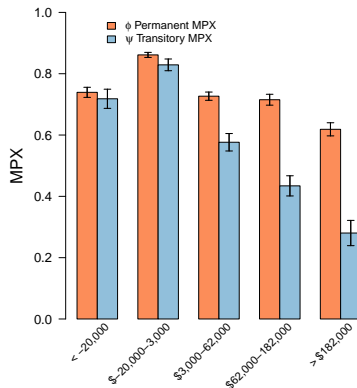
Notes: 1,445,560 observations from 48,050 individuals. The vertical bars on each coefficient represent 95% confidence intervals using heteroskedasticity robust errors clustered at the individual level.

# MPX by Net Wealth

Permanent and Transitory Variance by Net Wealth Quantile



MPX by Net Wealth Quantile



Back

# Interest Rate Exposure: Out of Sample

*Total* URE sums to zero - this is not true for our household sample

|                          | MPX                     | URE        | $\mathcal{E}_R$ component |
|--------------------------|-------------------------|------------|---------------------------|
| <b>Estimation Sample</b> | <b>See Distribution</b> | <b>-61</b> | <b>-0.29</b>              |
| Young                    | 0.5                     | -15        | -0.06                     |
| Old                      | 0.5                     | 6          | 0.02                      |
| Pension Funds            | 0.1                     | 37         | 0.03                      |
| Government               | 0.0                     | -23        | 0.00                      |
| Non-financial Corp.      | 0.1                     | -13        | -0.01                     |
| Financial Sector         | 0.1                     | 61         | 0.05                      |
| Rest of World            | 0.0                     | 9          | 0.00                      |
| <b>Total</b>             |                         | <b>0</b>   | <b>-0.26</b>              |

**Notes:** URE numbers are in billions of 2015 USD.

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# Summary Statistics

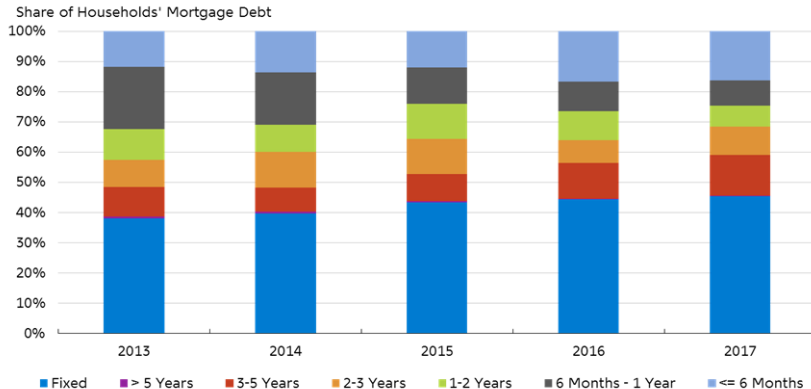
|                        | Estimation Sample |         |         | Population (Age 30-55) |         |         |
|------------------------|-------------------|---------|---------|------------------------|---------|---------|
|                        | Mean              | Median  | Std Dev | Mean                   | Median  | Std Dev |
| After Tax Income       | 59,261            | 57,804  | 28,819  | 58,312                 | 53,304  | 68,799  |
| Consumption            | 52,680            | 48,344  | 28,581  | 54,022                 | 46,373  | 38,126  |
| Liquid Assets          | 18,438            | 6,856   | 33,016  | 23,331                 | 6,578   | 81,473  |
| Net Worth              | 74,937            | 19,115  | 157,295 | 85,799                 | 12,952  | 564,404 |
| Homeowner              | 0.57              | 1.00    | 0.50    | 0.50                   | 1.00    | 0.50    |
| Car Owner              | 0.66              | 1.00    | 0.47    | 0.55                   | 1.00    | 0.50    |
| Higher Education       | 0.31              | 0.00    | 0.46    | 0.33                   | 0.00    | 0.47    |
| Age                    | 43.5              | 44.0    | 7.1     | 42.5                   | 42.0    | 7.3     |
| URE                    | -28,052           | -12,627 | 108,382 | -47,589                | -19,374 | 243,604 |
| NNP                    | -109,685          | -65,810 | 156,523 | -158,321               | -85,207 | 542,498 |
| No. Household-year obs | 7,664,360         |         |         | 18,050,340             |         |         |

**Notes:** Values are 2015 USD. Age refers to the age in 2008 of the main income earner in the household. For the purposes of calculation of consumption in the population, top and bottom 1% in terms of consumption have been excluded. URE and NNP can only be calculated in the period 2009-2015 due to mortgage information being insufficiently detailed in the previous years.

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# Danish Mortgage Market



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