

Consumption Heterogeneity: Micro Drivers and Macro Implications

Edmund Crawley & Andreas Kuchler

SAIS October 10, 2018

We estimate the **sensitivity of consumption**
to permanent and transitory **shocks to income**
for **different groups** of households

Hasn't This Been Done Before?

Yes, but...

Our **method** addresses bias in previous results

Our **data** allows sharp focus on household heterogeneity

Hasn't This Been Done Before?

Time Aggregation Problem

Yes, but...



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Our **data** allows sharp focus on household heterogeneity



Sample size in millions
Detailed balance sheet

Why Do We Care? (as macroeconomists)

- 1) Heterogenous agent models have testable micro behavior
- 2) Quantify Macro Implications

Why Do We Care? (as macroeconomists)

e.g. Consumption smoothing requires liquid wealth



1) Heterogenous agent models have testable micro behavior

2) Quantify Macro Implications



e.g. Redistribution in Monetary Policy

What do we find? (Redistribution in Monetary Policy)



What do we find? (Redistribution in Monetary Policy)



Medium MPX
 ≈ 0.5



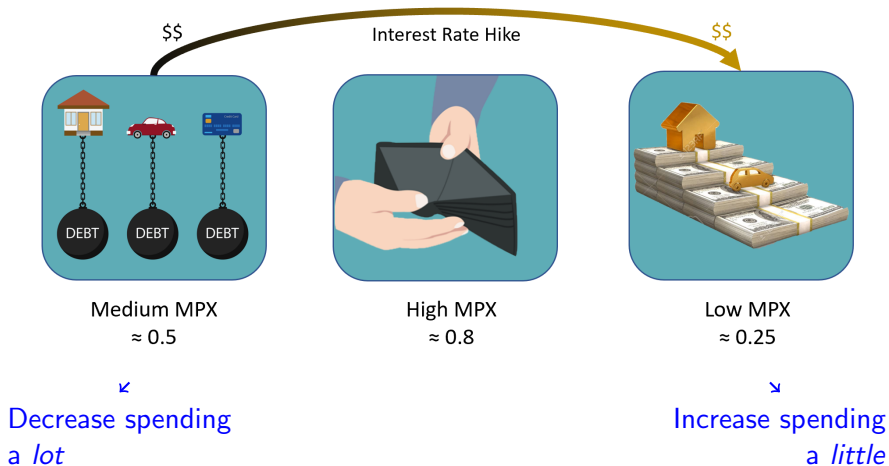
High MPX
 ≈ 0.8



Low MPX
 ≈ 0.25

MPX: Marginal Propensity to eXpend (includes durables)

What do we find? (Redistribution in Monetary Policy)



What do we find? (Redistribution in Monetary Policy)



1yr rate \uparrow 1%

Aggregate Spending \downarrow 26 basis points



Through this redistribution channel *alone*

Reduced Form Approach

Identifying Restrictions on

Income

and

Consumption

In **Continuous** Time

Reduced Form Approach

Identifying Restrictions on

Income \longrightarrow Permanent (random walk) shocks
Transitory (< 2 years) shocks

and

Consumption

In **Continuous** Time

Reduced Form Approach

Identifying Restrictions on



In **Continuous** Time

Reduced Form Approach

Identifying Restrictions on

Income → Permanent (random walk) shocks
Transitory (<2 years) shocks

and

Consumption → Permanent (random walk) response
Transitory (<2 years) response

In **Continuous** Time → Time Aggregation Problem

Reduced Form Approach

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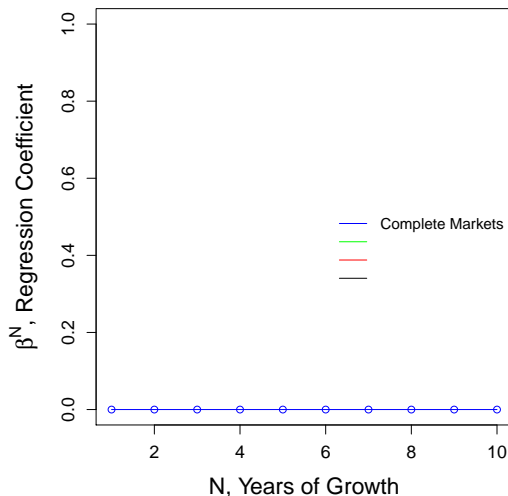
In **Continuous** Time \longrightarrow Time Aggregation Problem

But first some intuition: Naïvely Regress

Change in Consumption on Change in Income (over N years)

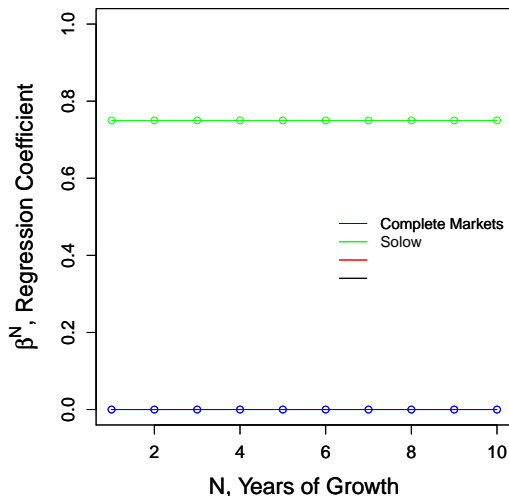
Naïve Regression: Consumption Growth on Income Growth

$$\Delta^N c_i = \alpha^N + \beta^N \Delta^N y_i + \varepsilon_i$$



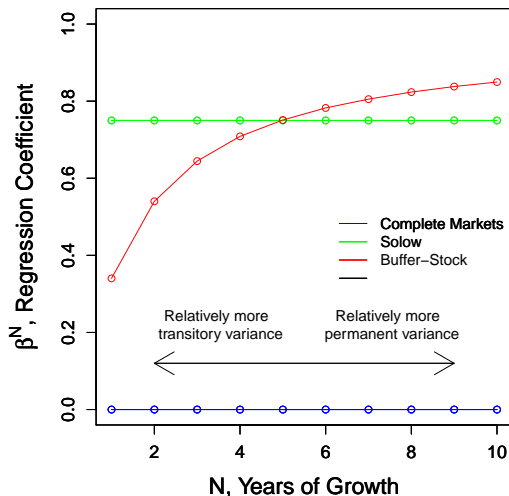
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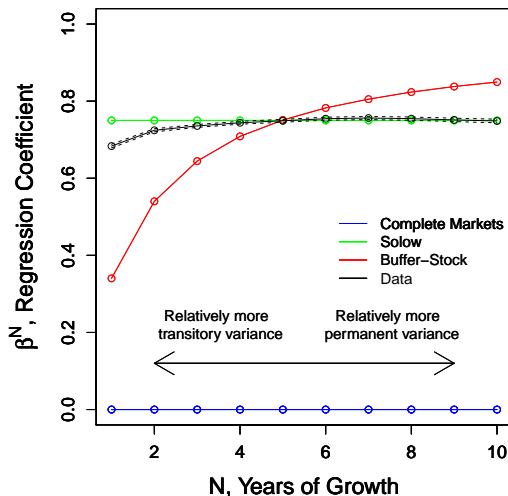
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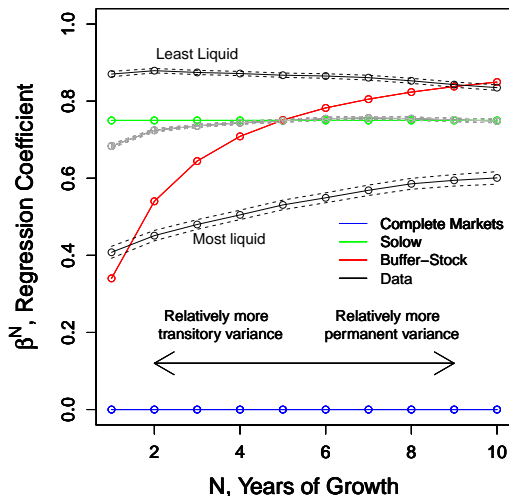
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$$\Delta^N c_i = \alpha^N + \beta^N \Delta^N y_i + \varepsilon_i$$



Why Not Blundell, Pistaferri and Preston 2008?

Key to BPP Identification

Transitory shock year t

$\Delta y_{t+1} = \Delta p_{t+1} + \Delta \varepsilon_{t+1}$ is a *valid instrument* for ε_t



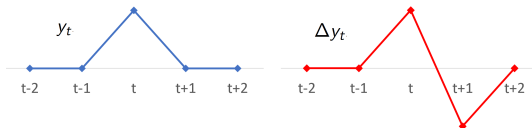
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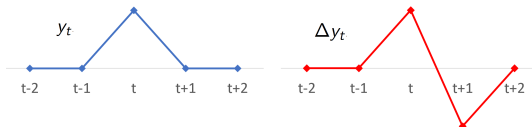
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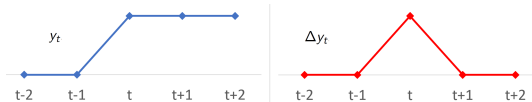
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- Uncorrelated with permanent shocks in year t



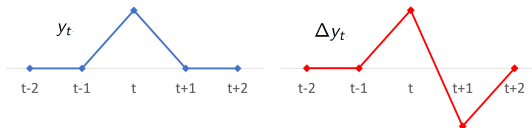
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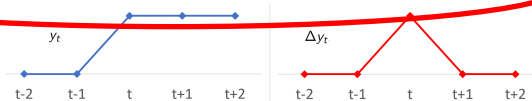
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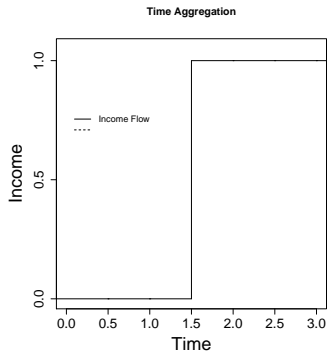


- Uncorrelated with permanent shocks in year t

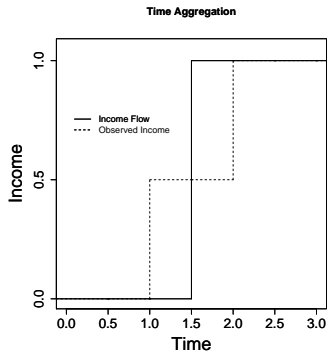


Fails due to the **Time Aggregation Problem**

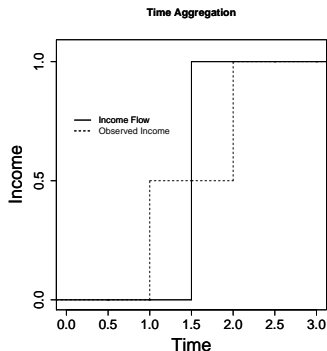
Time Aggregation Problem (Crawley 2018)



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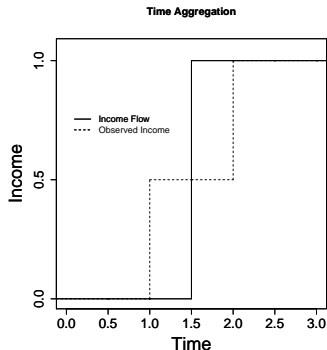


Observed permanent income growth is *positively* autocorrelated

BPP misinterprets *positive* permanent income shocks as *negative* transitory shocks

⇒ Thinks negative transitory shocks result in consumption *increasing*

Time Aggregation Problem (Crawley 2018)



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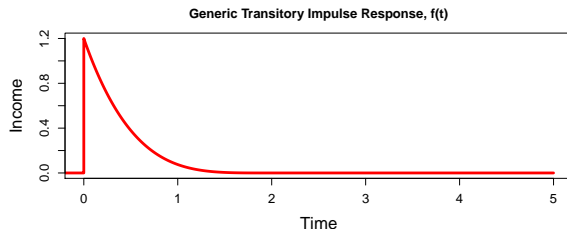
BPP misinterprets *positive* permanent income shocks as *negative* transitory shocks

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If the Permanent Income Hypothesis holds, BPP will estimate the MPC to be -0.6

Identification Restrictions: Income Process

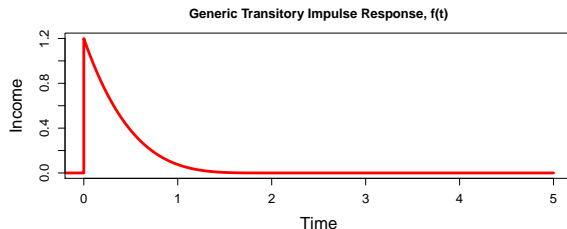
- Permanent Income (random walk)
- Transitory Income (persistence < 2 years)



$$y_t = \underbrace{p_t}_{\text{Permanent income flow}} + \underbrace{\int_{t-2}^t f(t-s)dq_s}_{\text{Transitory income flow}}$$

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Observed Income

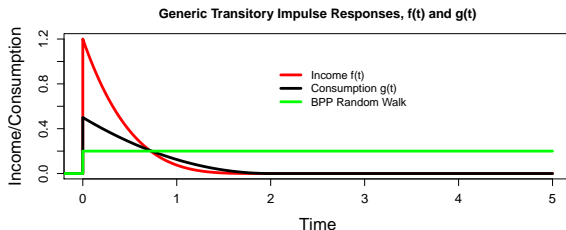
$$\bar{y}_T = \int_{T-1}^T y_t dt = \int_{T-1}^T p_t dt + \int_{T-1}^T \int_{t-2}^t f(t-s) dq_s dt$$

Time Aggregation

Identification Restrictions: Consumption Response

- Permanent: Moves by fraction ϕ of shock
- Transitory: Persistence < 2 years

Evidence



$$c_t = \phi p_t + \int_{t-2}^t g(t-s) dq_s$$

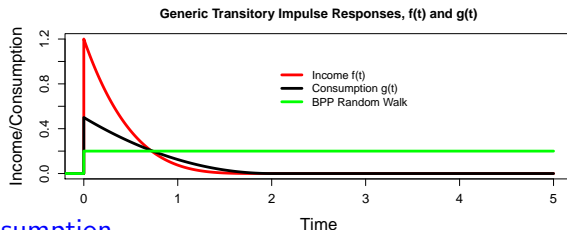
Permanent consumption flow

Transitory consumption flow

Identification Restrictions: Consumption Response

- Permanent: Moves by fraction ϕ of shock
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Evidence



Observed Consumption

$$\bar{c}_T = \int_{T-1}^T c_t dt = \int_{T-1}^T \phi p_t dt + \int_{T-1}^T \int_{t-2}^t g(t-s) dq_s dt$$

Time Aggregation

We use GMM on the equations:

$$\text{Var}(\Delta^N \bar{y}_T) = (N - \frac{1}{3})\sigma_p^2 + 2\sigma_{\tilde{q}}^2$$

$$\text{Cov}(\Delta^N \bar{c}_T, \Delta^N \bar{y}_T) = \phi(N - \frac{1}{3})\sigma_p^2 + 2\psi\sigma_{\tilde{q}}^2$$

with $N = 3, 4, 5$ (and $T = 2007, \dots, 2015$) to identify:

- σ_p^2 : Permanent shock variance
- $\sigma_{\tilde{q}}^2$: (Time aggregated) transitory shock variance
- ϕ : MPX out of permanent income shocks
- ψ : MPX out of transitory income shocks

where ψ is the regression coefficient of 'transitory' consumption on transitory income

What we need:

- Panel Data on Income and Expenditure
- Household Balance Sheet Data (detail on nominal assets)

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Income:

- Starting point: Register based micro data for all Danish households made available by Statistics Denmark
 - We use after-tax income for the household head, based on third-party reported tax data
 - Restrict sample to heads aged 30-55
- We divide through by permanent income (mean income over all observed years) and take the residual after controlling for age, education, marital status etc. (along with interactions of these)

We impute expenditure from the budget constraint

$$C_t \equiv Y_t - S_t = Y_t - P_t - \Delta NW$$

- Deposit and brokerage accounts all third party reported
- Works well for households with simple financial lives
- Main issue: Capital gains and losses
 - Exclude households where methodology will not work well (eg business owners)
 - Exclude housing wealth and years with housing transactions
 - Capital gains for stocks based on a diversified index
- Noisy, but perhaps better than surveys (Kuchler et al. 2018)
- Huge sample size advantage: sample covers 7.6 million observations over 2004-2015

Data: When is Measurement Error a Problem?

Our method has the same measurement error issues as the regressions:

$$\Delta^N c_i = \alpha^N + \beta^N \Delta^N y_i + \varepsilon_i$$

That is:

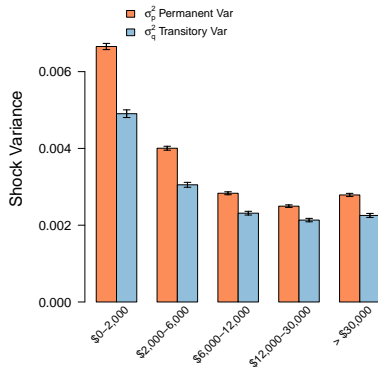
- 1 Measurement error in $\Delta^N y_i$ leads to attenuation bias
- 2 Measurement error in $\Delta^N c_i$ should be uncorrelated with $\Delta^N y_i$

When might 2 fail?

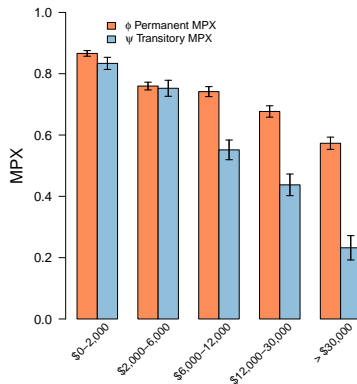
- When a proportion of assets are held off balance sheet
- When returns are correlated with *changes* in income (e.g. own stock in the company you work for)
- When insurance is provided by friends and family

Results by Liquid Wealth

Permanent and Transitory Variance by Liquid Wealth Quantile

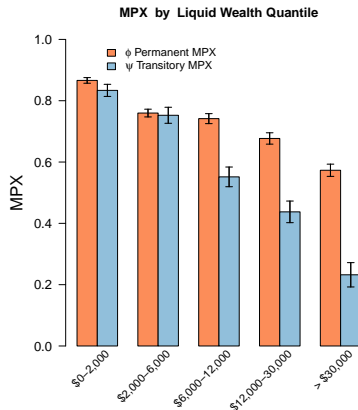
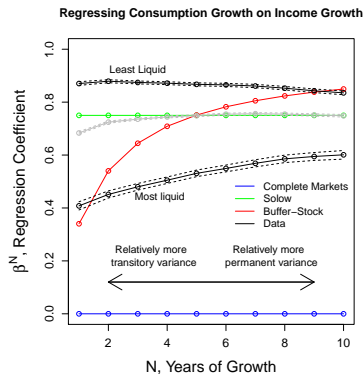


MPX by Liquid Wealth Quantile



MPX by Net Wealth

MPX Results are Robust to Misspecification



MPX by Net Wealth

Monetary Policy: Auclert's Decomposition

How does Monetary Policy Effect Aggregate Consumption?

- Intertemporal Substitution
- Aggregate Income

} Representative Agent Channels

Monetary Policy: Auclert's Decomposition

→ Dominates in Rep. Agent NK models

How does Monetary Policy Effect Aggregate Consumption?

- Intertemporal Substitution
- Aggregate Income

} Representative Agent Channels

→ Large in Spender-Saver, or TANK models

Monetary Policy: Auclert's Decomposition

How does Monetary Policy Effect Aggregate Consumption?

- Intertemporal Substitution
 - Aggregate Income
 - Fisher (Inflationary debt relief)
 - Earnings Heterogeneity
 - Interest Rate Exposure
- } Representative Agent Channels
- } Redistribution Channels

Monetary Policy: Auclert's Decomposition

How does Monetary Policy Effect Aggregate Consumption?

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How can we *empirically* measure the size of the redistribution channels?

Need to know the distribution of MPCs along the relevant dimension of redistribution

- Real interest rate increases 1% for 1 year
- Hold constant income and inflation

How does the subsequent redistribution impact aggregate consumption?

Dimension of Redistribution: Unhedged Interest Rate Exposure

Interest Rate Exposure: Dimension of Redistribution

Define **Unhedged Interest Rate Exposure** for household i as the total savings the household will invest at this year's interest rate:

$$URE_i = Y_i - C_i + A_i - L_i$$

Where

- Y_i = Total after tax income
- C_i = Total Expenditure, including interest payments
- A_i = Maturing assets
- L_i = Maturing liabilities

Following a change in the interest rate dR , the size of the Interest Rate Exposure channel on household i 's expenditure is:

$$dc_i = MPC_i URE_i \frac{dR}{R}$$

Interest Rate Exposure: Aggregation

Aggregate to find size of channel:

$$\begin{aligned} dc_i &= MPC_i URE_i \frac{dR}{R} \\ \Rightarrow \frac{dC}{C} &= \mathbb{E}_I \left(MPC_i \frac{URE_i}{\mathbb{E}_I(c_i)} \right) \frac{dR}{R} \end{aligned}$$

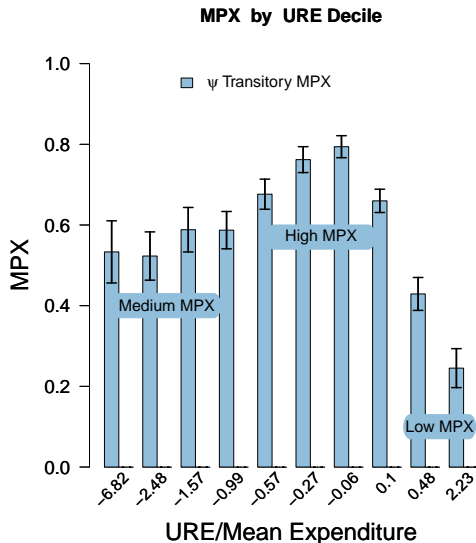
Define sufficient statistic:

$$\mathcal{E}_R = \mathbb{E}_I \left(MPC_i \frac{URE_i}{\mathbb{E}_I(c_i)} \right)$$

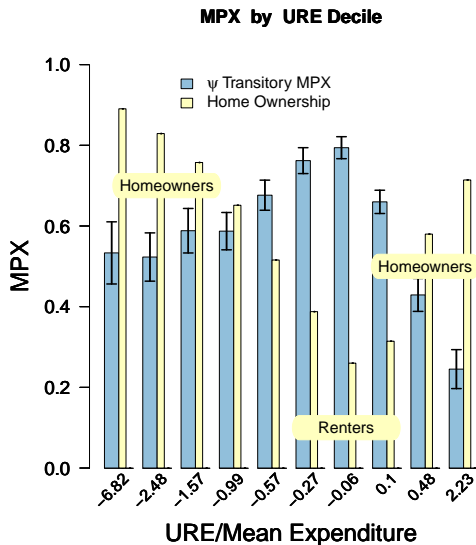
\Rightarrow Need to know the distribution of MPC_i with URE_i

We can do that!

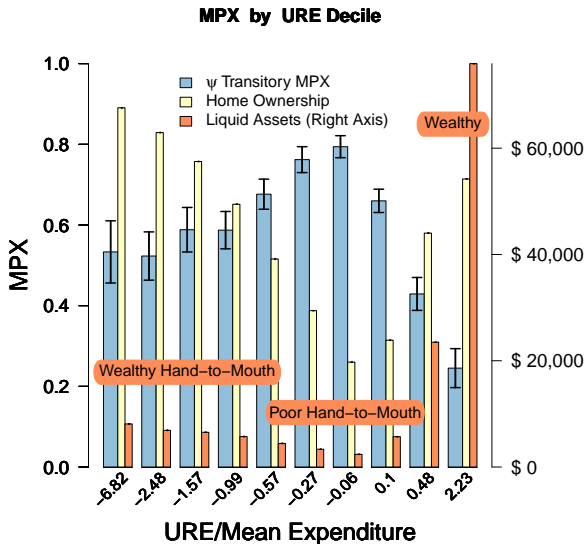
Interest Rate Exposure: MPX Distribution



Interest Rate Exposure: MPX Distribution



Interest Rate Exposure: MPX Distribution



Interest Rate Exposure: Out of Sample

Total URE sums to zero - this is not true for our household sample

- -57bn USD

	MPX	URE	\mathcal{E}_R component
Estimation Sample	See Distribution	-61	-0.29
Young	0.5	-15	-0.06
Old	0.5	6	0.02
Pension Funds	0.1	37	0.03
Government	0.0	-23	0.00
Non-financial Corp.	0.1	-13	-0.01
Financial Sector	0.1	61	0.05
Rest of World	0.0	9	0.00
Total		0	-0.26

Notes: URE numbers are in billions of 2015 USD.

All Five Transmission Channels

$$\frac{dC}{C} = \underbrace{\mathcal{M} \frac{dY}{Y}}_{\text{Aggregate Income Channel}} + \underbrace{\mathcal{E}_R \frac{dR}{R}}_{\text{Interest Rate Exposure Channel}} + \underbrace{+\gamma \mathcal{E}_Y \frac{dY}{Y}}_{\text{Earnings Heterogeity Channel}} + \underbrace{-\sigma \mathcal{S} \frac{dR}{R}}_{\text{Intertemporal Substitution Channel}} + \underbrace{-\mathcal{E}_P \frac{dP}{P}}_{\text{Fisher Channel}}$$

\mathcal{M}	0.52
\mathcal{E}_Y	-0.03
\mathcal{E}_P	-0.75
\mathcal{E}_R	-0.26
\mathcal{S}	0.49

All Five Transmission Channels

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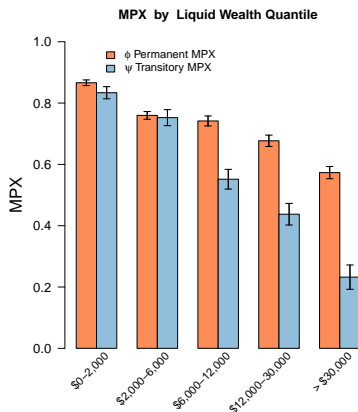
Compare \mathcal{E}_R to σS :

σ in the range of 0.1 to 0.5
(maybe)

$$\sigma S \approx 0.05 - 0.25$$

Aim of Modeling Exercise

Can we calibrate a standard Buffer-Stock saving model to fit the distribution of MPC with liquid wealth?



Key features:

- High overall Transitory MPC
- Decreasing with liquid wealth

Households maximize expected utility

$$\mathbb{E}_t \sum_{i=t}^{\infty} \beta^i u(\mathbf{c}_i)$$

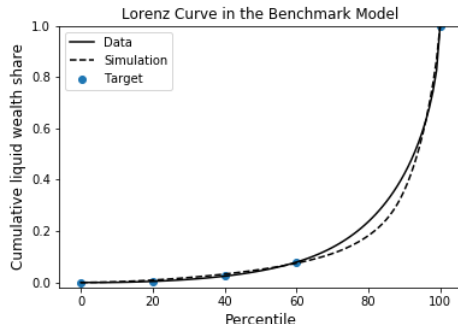
with:

- Permanent and Transitory shocks to income (calibrated to Danish data)
- Saving in one (liquid) asset
- No borrowing
- CRRA utility, $\rho = 2$

Benchmark Model: Fitting the Liquid Wealth Distribution

Ex-ante heterogeneity in the discount rate

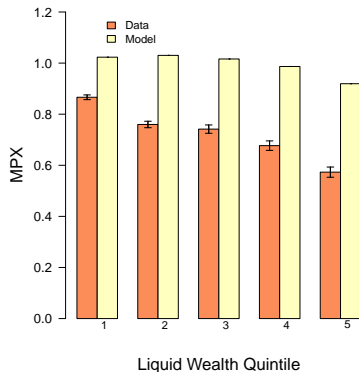
$\beta^i \sim \text{Unif}[\beta_{\text{low}}, \beta_{\text{high}}]$ Chosen to fit level and distribution of liquid wealth (especially at the low end)



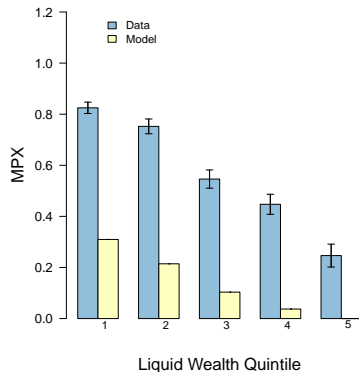
Benchmark Model: Results

Simulate panel of data and estimate ϕ and ψ

Permanent MPX by Liquid Wealth Quintile: Model vs Data



Transitory MPX by Liquid Wealth Quintile: Model vs Data



First order problem: Transitory MPCs are too low

Need to lower β 's without reducing savings

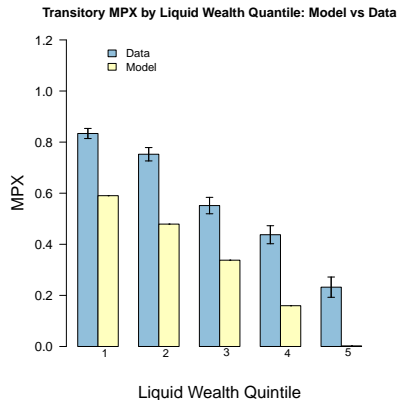
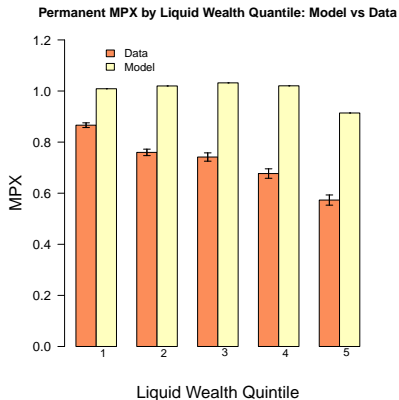
Is income risk the only source of precautionary saving?

- In the data, expenditure FAR for volatile than income
- Surprise expenses can be large

Simple extension - add large taste shocks

$$\mathbb{E}_t \sum_{i=t}^{\infty} \beta^i \chi_i u(\mathbf{c}_i)$$

Taste Shock Model: Results



- We have designed a new method to estimate consumption responses to income shocks
- It appears to work well, both in theory and practice
- We can use it to show that heterogeneity plays a key role in monetary policy transmission

Thank you!

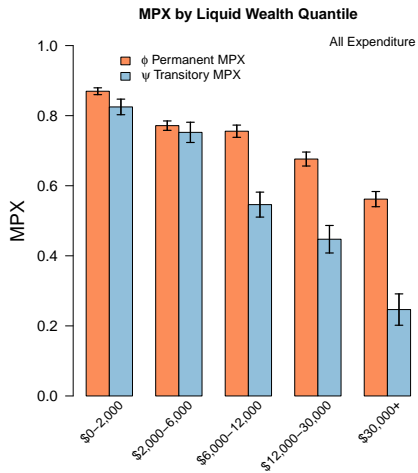
We have data on value of household cars

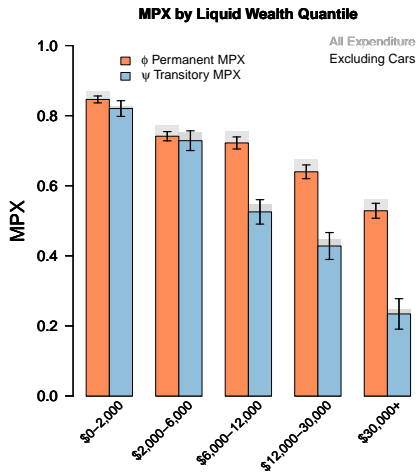
- Construct expenditure excluding car purchases and sales

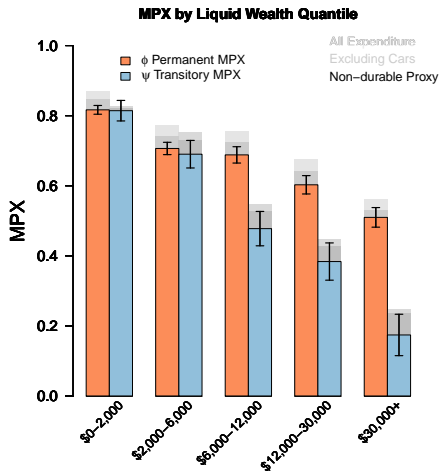
$$C_T^{\text{nocar}} = C_T - \Delta\text{CarValue}$$

- Construct proxy for non durable consumption (Cars $\approx 42.1\%$ durable expenditure)

$$C_T^{\text{non durable}} = C_T - \frac{1}{0.421} \Delta\text{CarValue}$$

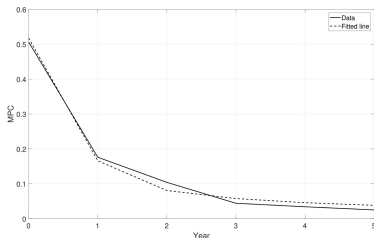






Evidence of Consumption Decay Within 2 Years

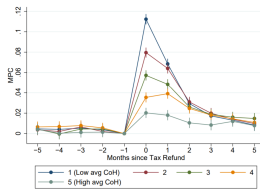
From Fagereng, Holm,
and Natvik (2016)



Back

From Gelman (2016)

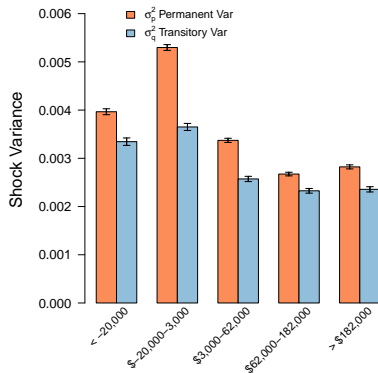
Figure 10: Tax refund impulse response function



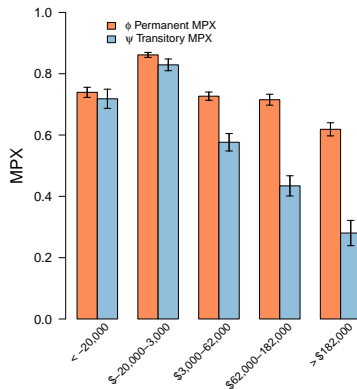
Notes: 1,445,560 observations from 48,050 individuals. The vertical bars on each coefficient represent 95% confidence intervals using heteroskedasticity robust errors clustered at the individual level.

MPX by Net Wealth

Permanent and Transitory Variance by Net Wealth Quantile



MPX by Net Wealth Quantile



Back