

Consumption Heterogeneity: Micro Drivers and Macro Implications

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Johns Hopkins University, September 18, 2018

Is Heterogeneity Important for Macroeconomics?

Theory: Consumption heterogeneity is *potentially* very important for macroeconomic dynamics

- e.g. Recent HANK models

Macroeconomic events can redistribute wealth between High and Low MPC households, affecting aggregate consumption

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Macroeconomic events can redistribute wealth between High and Low MPC households, affecting aggregate consumption

Empirics: Testing and quantifying these effects often boils down to measuring the distribution of MPC along some dimension of redistribution

Ability to do so is limited by:

- Methods to measure MPCs
- Consumption data
- Household balance sheet data

What does this paper do?

Two Empirical Contributions

- 1 **Method:** New methodology to measure MPCs out of transitory and permanent income shocks
 - Builds on Blundell, Pistaferri, and Preston (2008)
 - Correctly accounts for the Time Aggregation Problem
- 2 **Data:** Panel data covering all Danish households 2004-2015
 - Large sample size reveals clear, systemic heterogeneity
 - Detailed household balance sheets allow us to infer implications for monetary policy transmission

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- 2 Data:** Panel data covering all Danish households 2004-2015
 - Large sample size reveals clear, systemic heterogeneity
 - Detailed household balance sheets allow us to infer implications for monetary policy transmission

We also test to what extent a buffer-stock model can fit the observed distribution of MPC with liquid wealth

What does this paper find?

Wealthy Hand-to-Mouth



Poor Hand-to-Mouth



Wealthy



What does this paper find?

Wealthy Hand-to-Mouth



$MPC \approx 0.5$

Poor Hand-to-Mouth



$MPC \approx 0.8$

Wealthy



$MPC \approx 0.25$

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\$\$

Interest Rate Hike

\$\$

What does this paper find?



A **one percentage point** interest rate hike reduces aggregate expenditure by **35 basis points** through this ***interest rate exposure channel*** alone

Redistribution >> Intertemporal Substitution

What has the Empirical MPC literature Found?

General consensus: **MPCs are large** (≈ 0.5 including durables)

- For both expected and unexpected transitory shocks

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Few studies have enough power to say much about the distribution of MPCs in the population

- Jappelli and Pistaferri (2014) Italian Survey Data
- Fuster, Kaplan, and Zafar (2018) NY Fed Survey
- Fagereng, Holm, and Natvik (2016) Norway Lottery Data
- Gelman (2016) Financial App Data

Liquid assets and **income** are key predictors of transitory MPC

Our method and data can uncover detailed heterogeneity - Many potential applications

How Are Consumption Responses Typically Measured?

Three methods:

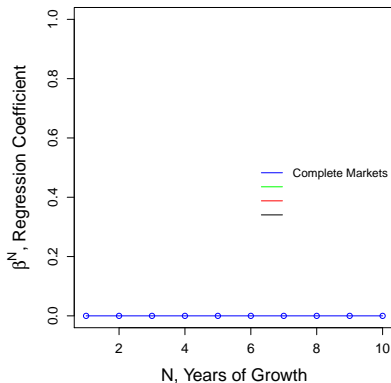
- 1 (Natural) Experiments - stimulus checks, lotteries etc
 - Few true experiments, especially for permanent shocks
 - Data limitations
- 2 Ask people
 - Unclear how to interpret
- 3 Make identifying restrictions on income and consumption dynamics
 - Empirical methods (until now!) have been flawed

We develop a robust method based on 3

Methodology Intuition and Suggestive Findings

Exploit increasing importance of permanent shocks as the time over which growth is measured increases

Regressing Consumption Growth on Income Growth

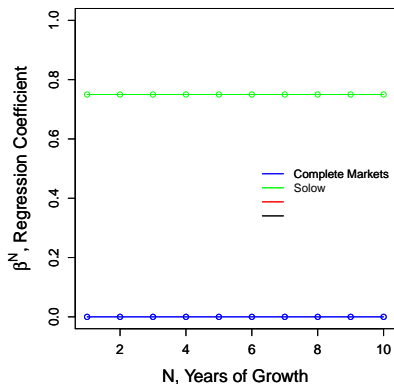


$$\Delta^N c_i = \alpha^N + \beta^N \Delta^N y_i + \varepsilon_i$$

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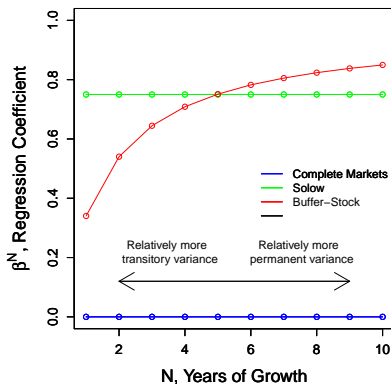


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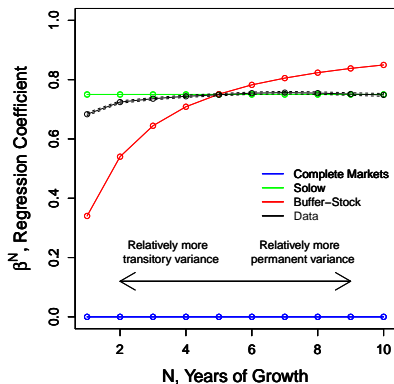


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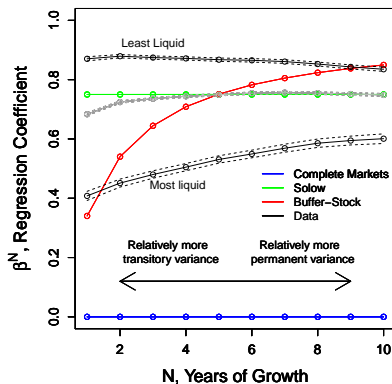


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Aside: Why Not Blundell, Pistaferri and Preston 2008?

Common Assumptions

Income y_t is made up of:

- Permanent Income (random walk)
- Transitory Income (uncorrelated over time)

Key to BPP Identification

Δy_{t+1} is a *valid instrument* for transitory shocks in year t

- Negatively correlated with transitory shocks in year t
- Uncorrelated with permanent shocks in year t

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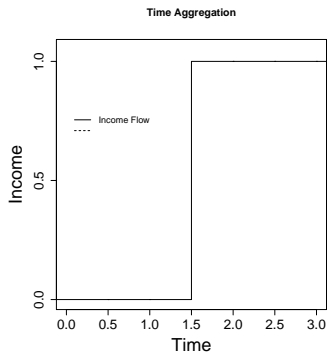
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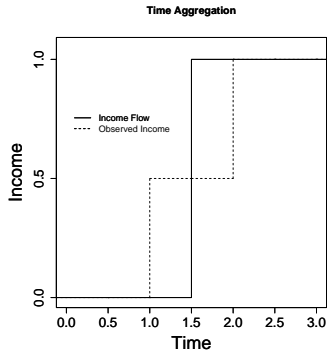
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Fails due to the **Time Aggregation Problem**

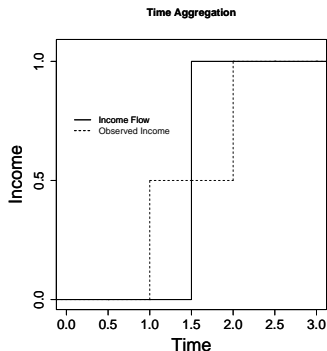
Time Aggregation Problem (Crawley 2018)



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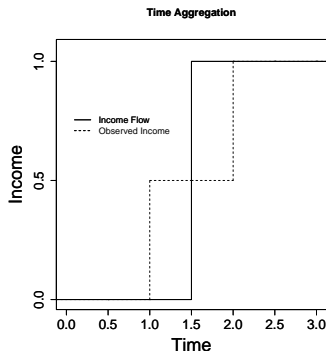


Observed permanent income growth is *positively* autocorrelated

BPP misinterprets *positive* permanent income shocks as *negative* transitory shocks

⇒ Thinks negative transitory shocks result in consumption *increasing*

Time Aggregation Problem (Crawley 2018)



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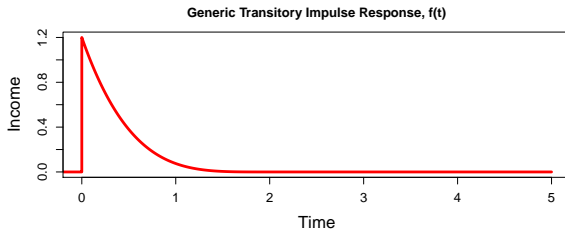
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If the Permanent Income Hypothesis holds, BPP will estimate the MPC to be -0.6

Identification Restrictions: Income

Income flow consists of:

- Permanent Income (random walk)
- Transitory Income (persistence < 2 years)

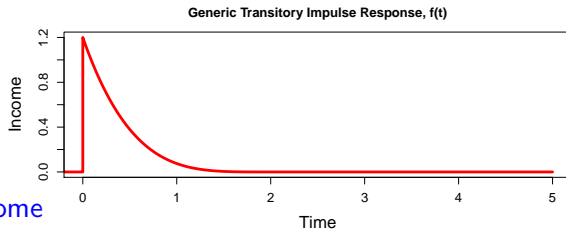


$$y_t = \underbrace{p_t}_{\text{Permanent income flow}} + \underbrace{\int_{t-2}^t f(t-s) dq_s}_{\text{Transitory income flow}}$$

Identification Restrictions: Income

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Observed Income



$$\bar{y}_T = \int_{T-1}^T y_t dt = \int_{T-1}^T p_t dt + \int_{T-1}^T \int_{t-2}^t f(t-s) dq_s dt$$



Time Aggregation

Identification Restrictions: Income

$$\bar{y}_T = \int_{T-1}^T p_t dt + \int_{T-1}^T \int_{t-2}^t f(t-s) dq_s dt$$

$$\Delta^N \bar{y}_T = \bar{y}_T - \bar{y}_{T-N}$$

$$\begin{aligned}
 &= \int_{T-1}^T (p_t - p_{T-1}) dt - \int_{T-N-1}^{T-N} (p_t - p_{T-N}) dt \\
 &\quad + (p_{T-1} - p_{T-N}) \quad \xrightarrow{\text{Independent increments}} \quad \text{Var} = \left(\frac{1}{3} + \frac{1}{3} + N-1\right) \sigma_p^2 \\
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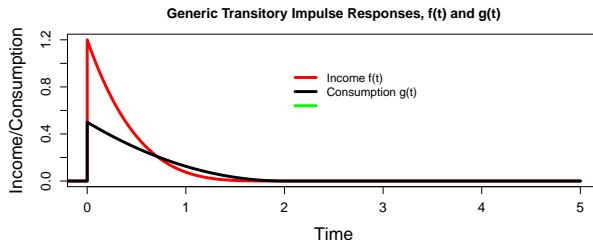
$$\implies \text{Var}(\Delta^N \bar{y}_T) = \left(N - \frac{1}{3}\right) \sigma_p^2 + 2\sigma_q^2 \text{ for } N \geq 3$$

Identification Restrictions: Consumption

Assumptions on Consumption

- Permanent: Consumption permanently moves by fraction ϕ of the income shock
- Transitory: Persistence < 2 years

Evidence

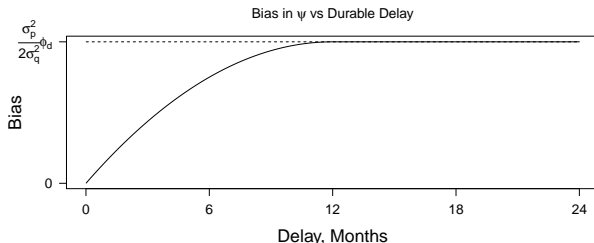


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This is a key difference between what we assume and BPP

Identification Restrictions: Consumption

Consumption flow is given by:

$$c_t = \phi p_t + \int_{t-2}^t g(t-s) dq_s$$

$$\implies \text{Cov}(\Delta^N \bar{c}_T, \Delta^N \bar{y}_T) = \phi(N - \frac{1}{3})\sigma_p^2 + 2\psi\sigma_{\tilde{q}}^2$$

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- ϕ : MPX out of permanent income shocks
- ψ : MPX out of transitory income shocks

Marginal **P**ropensity to e**X**pend (includes durables)

Full Identification

We use GMM on the equations:

$$\text{Var}(\Delta^N \bar{y}_T) = (N - \frac{1}{3})\sigma_p^2 + 2\sigma_{\tilde{q}}^2$$

$$\text{Cov}(\Delta^N \bar{c}_T, \Delta^N \bar{y}_T) = \phi(N - \frac{1}{3})\sigma_p^2 + 2\psi\sigma_{\tilde{q}}^2$$

with $N = 3, 4, 5$ (and $T = 2007, \dots, 2015$) to identify the four unknowns:

- σ_p^2 : Permanent shock variance
- $\sigma_{\tilde{q}}^2$: (Time aggregated) transitory shock variance
- ϕ : MPX out of permanent income shocks
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Data

What we need:

- Panel Data on Income and Expenditure
- Household Balance Sheet Data (detail on nominal assets)

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Income:

- Starting point: Register based micro data for all Danish households made available by Statistics Denmark
 - We use after-tax income for the household head, based on third-party reported tax data
 - Restrict sample to heads aged 30-55
- We divide through by permanent income (mean income over all observed years) and take the residual after controlling for age, education, marital status etc. (along with interactions of these)

Data: Expenditure

We impute expenditure from the budget constraint

$$C_t \equiv Y_t - S_t = Y_t - P_t - \Delta NW$$

- Deposit and brokerage accounts all third party reported
- Works well for households with simple financial lives
- Main issue: Capital gains and losses
 - Exclude households where methodology will not work well (eg business owners)
 - Exclude housing wealth and years with housing transactions
 - Capital gains for stocks based on a diversified index
- Noisy, but perhaps better than surveys (Kuchler et al. 2018)
- Huge sample size advantage: sample covers 7.6 million observations over 2004-2015

Data: When is Measurement Error a Problem?

Our method has the same measurement error issues as the regressions:

$$\Delta^N c_i = \alpha^N + \beta^N \Delta^N y_i + \varepsilon_i$$

That is:

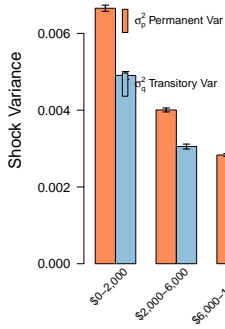
- 1 Measurement error in $\Delta^N y_i$ leads to attenuation bias
- 2 Measurement error in $\Delta^N c_i$ should be uncorrelated with $\Delta^N y_i$

When might 2 fail?

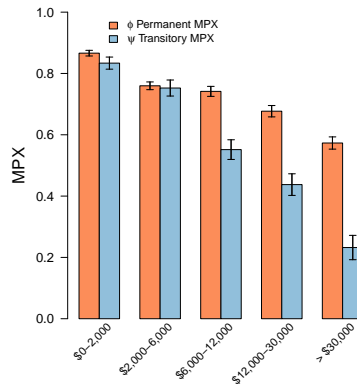
- When a proportion of assets are held off balance sheet
- When returns are correlated with *changes* in income (e.g. own stock in the company you work for)
- When insurance is provided by friends and family

Results by Liquid Wealth

Permanent and Transitory Variance by Liquid Wealth Quantile

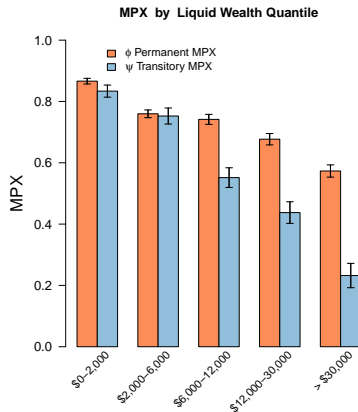
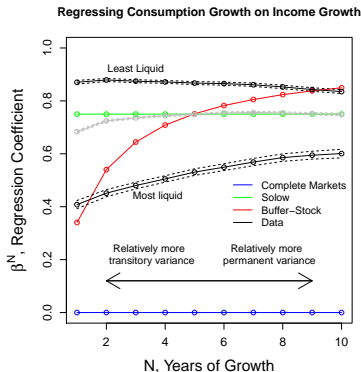


MPX by Liquid Wealth Quantile



MPX by Net Wealth

MPX Results are Robust to Misspecification



MPX by Net Wealth

Monetary Policy: Auclert's Decomposition

How does Monetary Policy Effect Aggregate Consumption?

- Intertemporal Substitution
- Aggregate Income

} Representative Agent Channels

Monetary Policy: Auclert's Decomposition

→ Dominates in Rep. Agent NK models

How does Monetary Policy Effect Aggregate Consumption?

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→ Large in Spender-Saver, or TANK models

Monetary Policy: Auclert's Decomposition

How does Monetary Policy Effect Aggregate Consumption?

- Intertemporal Substitution
 - Aggregate Income
 - Fisher (Inflationary debt relief)
 - Earnings Heterogeneity
 - Interest Rate Exposure
- } Representative Agent Channels
- } Redistribution Channels

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How can we *empirically* measure the size of the redistribution channels?

Need to know the distribution of MPCs along the relevant dimension of redistribution

Interest Rate Exposure: Auclert's Experiment

- Real interest rate increases 1% for 1 year
- Hold constant income and inflation

How does the subsequent redistribution impact aggregate consumption?

Dimension of Redistribution: Unhedged Interest Rate Exposure

Interest Rate Exposure: Dimension of Redistribution

Define **Unhedged Interest Rate Exposure** for household i as the total savings the household will invest at this year's interest rate:

$$URE_i = Y_i - C_i + A_i - L_i$$

Where

- Y_i = Total after tax income
- C_i = Total Expenditure, including interest payments
- A_i = Maturing assets
- L_i = Maturing liabilities

Following a change in the interest rate dR , the size of the Interest Rate Exposure channel on household i 's expenditure is:

$$dc_i = MPC_i URE_i \frac{dR}{R}$$

Interest Rate Exposure: Aggregation

Aggregate to find size of channel:

$$dc_i = MPC_i URE_i \frac{dR}{R}$$

$$\Rightarrow \frac{dC}{C} = \mathbb{E}_I \left(MPC_i \frac{URE_i}{\mathbb{E}_I(c_i)} \right) \frac{dR}{R}$$

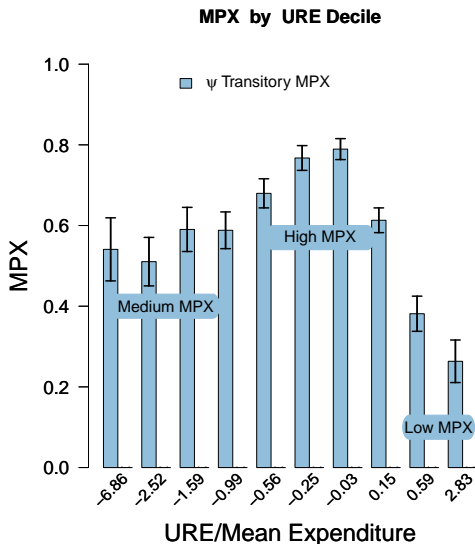
Define sufficient statistic:

$$\mathcal{E}_R = \mathbb{E}_I \left(MPC_i \frac{URE_i}{\mathbb{E}_I(c_i)} \right)$$

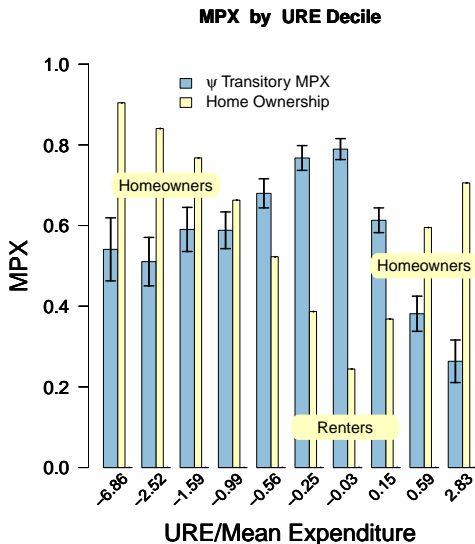
\Rightarrow Need to know the distribution of MPC_i with URE_i

We can do that!

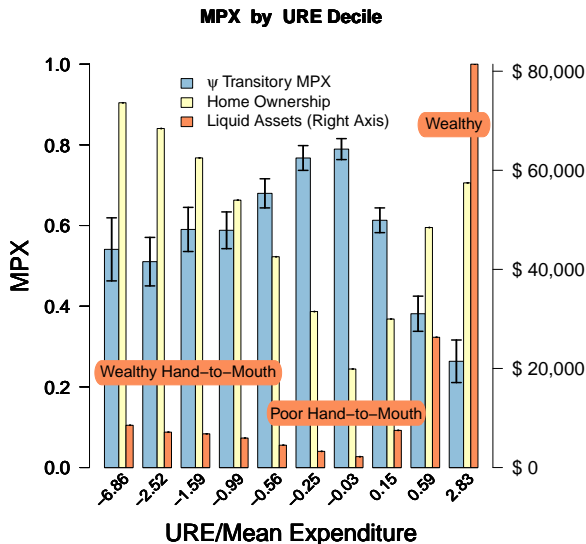
Interest Rate Exposure: MPX Distribution



Interest Rate Exposure: MPX Distribution



Interest Rate Exposure: MPX Distribution



Interest Rate Exposure: Out of Sample

Total URE sums to zero - this is not true for our household sample

- -57bn USD

	MPX	URE	\mathcal{E}_R component
Estimation Sample	See Distribution	-57	-0.30
Young	0.5	-16	-0.07
Old	0.5	14	0.06
Pension Funds	0.1	31	0.03
Government	0.0	-19	0.00
Non-financial Corp.	0.1	-11	-0.01
Financial Sector	0.1	51	0.04
Rest of World	0.0	7	0.00
Total		-0	-0.25

Notes: URE numbers are in billions of 2015 USD.

All Five Transmission Channels

$$\frac{dC}{C} = \underbrace{\mathcal{M} \frac{dY}{Y}}_{\text{Aggregate Income Channel}} + \underbrace{\mathcal{E}_R \frac{dR}{R}}_{\text{Interest Rate Exposure Channel}} + \underbrace{+\gamma \mathcal{E}_Y \frac{dY}{Y}}_{\text{Earnings Heterogeneity Channel}} + \underbrace{-\sigma \mathcal{S} \frac{dR}{R}}_{\text{Intertemporal Substitution Channel}} + \underbrace{-\mathcal{E}_P \frac{dP}{P}}_{\text{Fisher Channel}}$$

\mathcal{M}	0.55
\mathcal{E}_Y	-0.02
\mathcal{E}_P	-0.81
\mathcal{E}_R	-0.25
\mathcal{S}	0.47

All Five Transmission Channels

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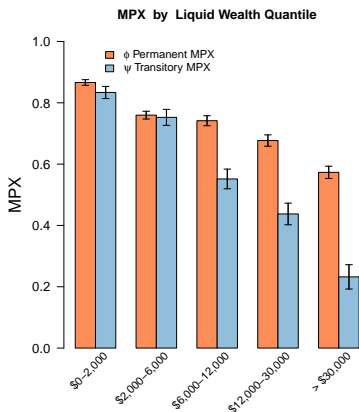
Compare \mathcal{E}_R to σS :

σ in the range of 0.1 to 0.5
(maybe)

$$\sigma S \approx 0.05 - 0.25$$

Aim of Modeling Exercise

Can we calibrate a standard Buffer-Stock saving model to fit the distribution of MPC with liquid wealth?



Key features:

- High overall Transitory MPC
- Decreasing with liquid wealth

Benchmark Model

Households maximize expected utility

$$\mathbb{E}_t \sum_{i=t}^{\infty} \beta^i u(\mathbf{c}_i)$$

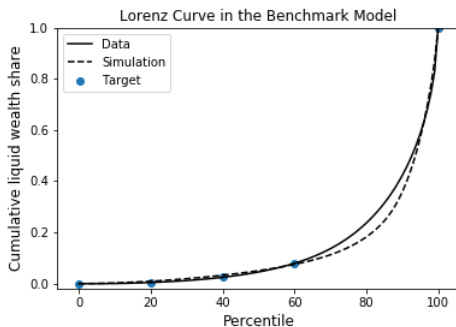
with:

- Permanent and Transitory shocks to income (calibrated to Danish data)
- Saving in one (liquid) asset
- No borrowing
- CRRA utility, $\rho = 2$

Benchmark Model: Fitting the Liquid Wealth Distribution

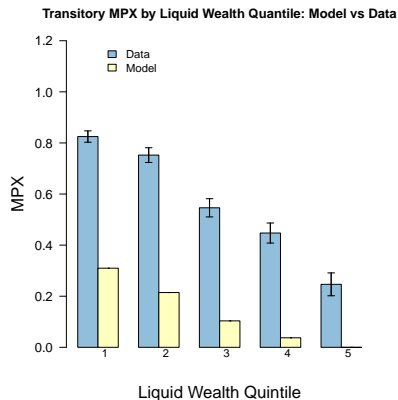
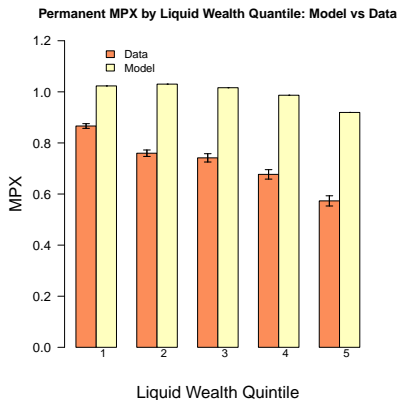
Ex-ante heterogeneity in the discount rate

$\beta^i \sim \text{Unif}[\beta_{\text{low}}, \beta_{\text{high}}]$ Chosen to fit level and distribution of liquid wealth (especially at the low end)



Benchmark Model: Results

Simulate panel of data and estimate ϕ and ψ



Taste Shock Model

First order problem: Transitory MPCs are too low

Need to lower β 's without reducing savings

Is income risk the only source of precautionary saving?

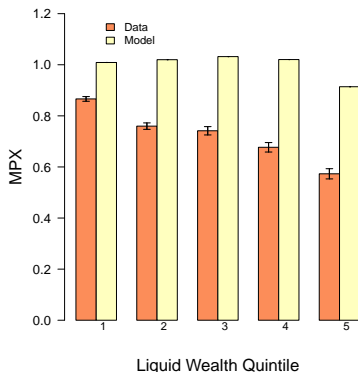
- In the data, expenditure FAR for volatile than income
- Surprise expenses can be large

Simple extension - add large taste shocks

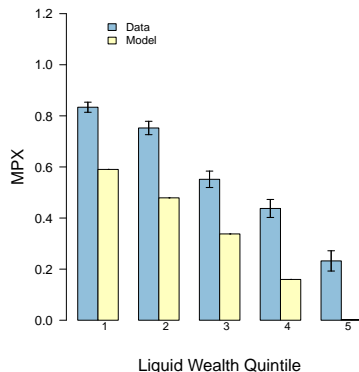
$$\mathbb{E}_t \sum_{i=t}^{\infty} \beta^i \chi_i u(\mathbf{c}_i)$$

Taste Shock Model: Results

Permanent MPX by Liquid Wealth Quintile: Model vs Data



Transitory MPX by Liquid Wealth Quintile: Model vs Data



Conclusion

- We have designed a new method to estimate consumption responses to income shocks
- It appears to work well, both in theory and practice
- We can use it to show that heterogeneity plays a key role in monetary policy transmission

Thank you!

Durables

We have data on value of household cars

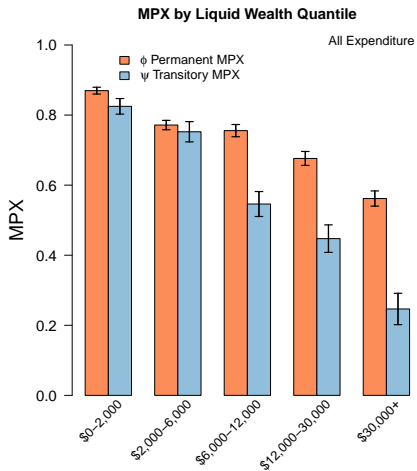
- Construct expenditure excluding car purchases and sales

$$C_T^{\text{nocar}} = C_T - \Delta \text{CarValue}$$

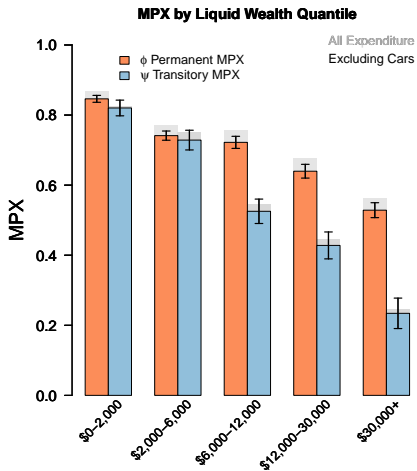
- Construct proxy for non durable consumption (Cars $\approx 42.1\%$ durable expenditure)

$$C_T^{\text{nondurable}} = C_T - \frac{1}{0.421} \Delta \text{CarValue}$$

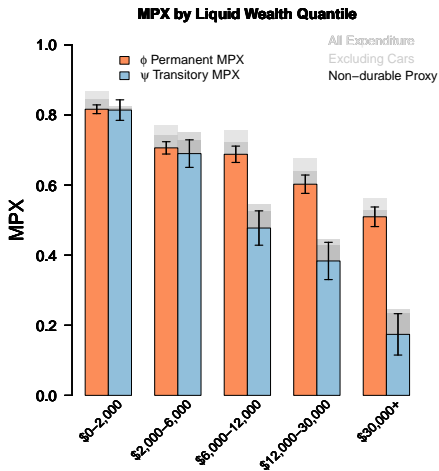
Durables



Durables

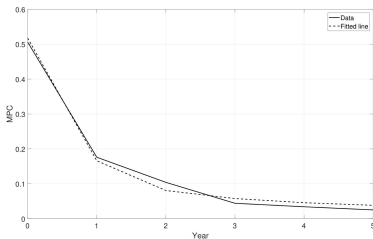


Durables



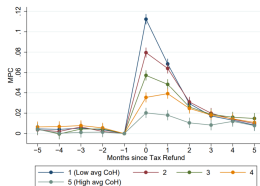
Evidence of Consumption Decay Within 2 Years

From Fagereng, Holm,
and Natvik (2016)

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From Gelman (2016)

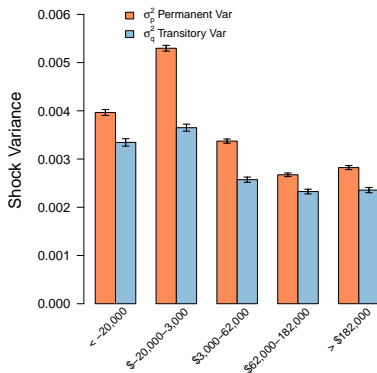
Figure 10: Tax refund impulse response function



Notes: 1,445,560 observations from 48,050 individuals. The vertical bars on each coefficient represent 95% confidence intervals using heteroskedasticity robust errors clustered at the individual level.

MPX by Net Wealth

Permanent and Transitory Variance by Net Wealth Quantile



MPX by Net Wealth Quantile

