# Consumption Heterogeneity: Micro Drivers and Macro Implications

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Johns Hopkins University, September 18, 2018

### Is Heterogeneity Important for Macroeconomics?

**Theory:** Consumption heterogeneity *potentially* very important for macroeconomic dynamics

Recent HANK models

**Empirics:** Ability to measure heterogeneity limited by

- Methods to measure MPCs
- Consumption data
- Household balance sheet data

#### Two Empirical Contributions

- 1 Method: New methodology to measure MPCs out of transitory and permanent income shocks
  - Builds on Blundell, Pistaferri, and Preston (2008)
  - Correctly accounts for the Time Aggregation Problem
- 2 Data: Panel data covering all Danish households 2004-2015
  - Large sample size reveals clear, systemic heterogeneity
  - Detailed household balance sheets allow us to infer implications for monetary policy transmission



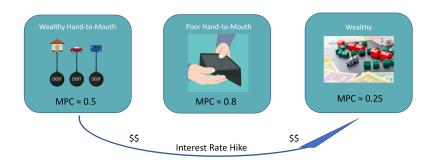


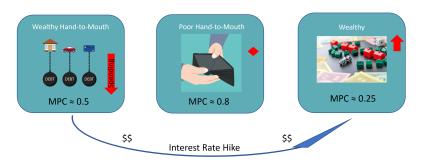


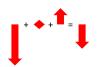












A one percentage point interest rate hike reduces aggregate expenditure by **35 basis points** through this *interest rate exposure channel* alone

Redistribution >> Intertemporal Substitution

### What has the Empirical MPC literature Found?

General consensus: MPCs are large ( $\approx 0.5$  including durables)

• For both expected and unexpected transitory shocks

Few studies have enough power to say much about the distribution of MPCs in the population

- Jappelli and Pistaferri (2014) Italian Survey Data
- Fuster, Kaplan, and Zafar (2018) NY Fed Survey
- Fagereng, Holm, and Natvik (2016) Norway Lottery Data
- Gelman (2016) Financial App Data

Liquid assets and income are key predictors of transitory MPC

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Liquid assets and income are key predictors of transitory MPC

Our method and data can uncover detailed heterogeneity - Many potential applications



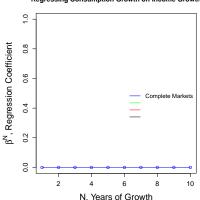
# How Are Consumption Responses Typically Measured?

#### Three methods:

- 1 (Natural) Experiments stimulus checks, lotteries etc
  - Few true experiments, especially for permanent shocks
  - Data limitations
- 2 Ask people
  - Unclear how to interpret
- 3 Use covariance structure of income and consumption
  - Empirical methods (until now!) have been flawed

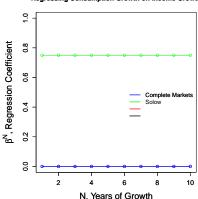
We develop a robust method based on 3

Exploit increasing importance of permanent shocks as the time over which growth is measured increases



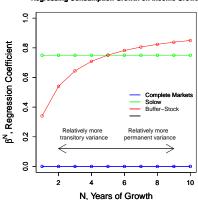
$$\Delta^{N}c_{i} = \alpha^{N} + \beta^{N}\Delta^{N}y_{i} + \varepsilon_{i}$$

Exploit increasing importance of permanent shocks as the time over which growth is measured increases



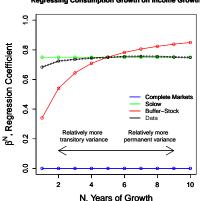
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### Regressing Consumption Growth on Income Growth Least Liquid β<sup>N</sup>, Regression Coefficient 9, 9.0 omplete Markets 4.0 Relatively more 2 10

N. Years of Growth

$$\Delta^{N} c_{i} = \alpha^{N} + \beta^{N} \Delta^{N} y_{i} + \varepsilon_{i}$$

### Aside: Why Not Blundell, Pistaferri and Preston 2008?

#### **Common Assumptions**

Income  $y_t$  is made up of:

- Permanent Income (random walk)
- Transitory Income (uncorrelated over time)

#### Key to BPP Identification

 $\Delta y_{t+1}$  is a *valid instrument* for transitory shocks in year t

- Negatively correlated with transitory shocks in year t
- Uncorrelated with permanent shocks in year t

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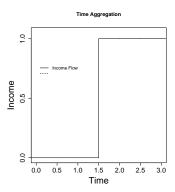
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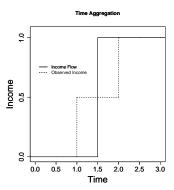
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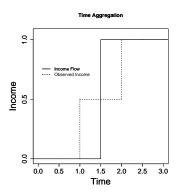
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Fails due to the Time Aggregation Problem



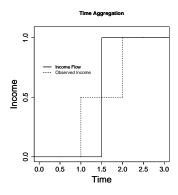




Permanent income growth is positively autocorrelated

BPP misinterprets *positive* permanent income shocks as *negative* transitory shocks

⇒ Thinks negative transitory shocks result in consumption *increasing* 



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→ Thinks negative transitory shocks result in consumption increasing

If the Permanent Income Hypothesis holds, BPP will estimate the MPC to be -0.6

We follow the spirit of Carroll & Samwick (1997):

Permanent income follows a random walk

$$p_t = p_{t-1} + \zeta_t$$

Total income includes a transitory component

$$y_t = p_t + \varepsilon_t$$

Growth over N years is:

$$\Delta^{N} y_{T} = (\zeta_{T-N+1} + \dots + \zeta_{T}) + \varepsilon_{T} - \varepsilon_{T-N}$$
$$\operatorname{Var}(\Delta^{N} y_{T}) = N \operatorname{Var}(\zeta) + 2 \operatorname{Var}(\varepsilon)$$

We follow the spirit of Carroll & Samwick (1997):

• If transitory income follows an MA(2) process:

$$y_t = \rho_t + \varepsilon_t + \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2}$$

$$\implies \operatorname{Var}(\Delta^N y_T) = N \underbrace{\operatorname{Var}(\zeta)}_{\mathsf{Perm var}} + 2 \underbrace{(1 + \theta_1^2 + \theta_2^2) \operatorname{Var}(\varepsilon)}_{\mathsf{"Total" trans var}} \text{ if } N \ge 3$$

Carroll & Samwick use N = 3, 4, 5 to identify permanent shock variance and "total" transitory shock variance

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- 1 How does time aggregation affect this identification?
- 2 What might the equivalent of "robust to MA(2) transitory shocks" be in continuous time?

Carroll & Samwick in Continuous Time with Aggregation

- To begin assume no persistence in the transitory shock
- p<sub>t</sub> and q<sub>t</sub> are independent martingale processes with independent increments

$$Var(p_t - p_{t-1}) = \sigma_p^2$$
$$Var(q_t - q_{t-1}) = \sigma_q^2$$

 Instantaneous income is equal to the flow of permanent income plus the transitory income component

$$dy_t = p_t dt + dq_t$$

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$$dy_t = p_t dt + dq_t$$

We observe  $\bar{y}_T$ , total income over year T:

$$\bar{y}_T = \int_{T-1}^T p_t dt + q_T - q_{T-1}$$

$$\implies \operatorname{Var}(\Delta^N \bar{y}_T) = (N - \frac{1}{3})\sigma_p + 2\sigma_q$$

Allow a generic persistence in transitory shock

Following shock, transitory income flow decays as:

$$f(t)$$
 where  $f(t) = 0$  if  $t > 2$ 

Generic Transitory Impulse Response, f(t)

$$y_t = p_t + \int_{t-2}^t f(t-s)dq_s$$

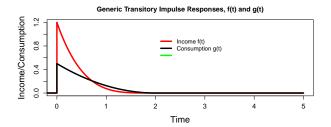
$$\implies \operatorname{Var}(\Delta^N \bar{y}_T) = (N - \frac{1}{3})\sigma_p^2 + 2\sigma_{\tilde{q}}^2 \text{ for } N \ge 3$$

where  $\tilde{q_T} = \int_{T-1}^T \int_{t-2}^t f(t-s) dq_s dt$  is the time aggregated transitory component of income



#### Assumptions on Consumption

- $\bullet$  Permanent: Consumption permanently moves by fraction  $\phi$  of the income shock
- Transitory: Allow for generic impulse response g(t) where g(t) = 0 for t > 2

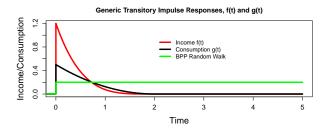


This is a key difference between what we assume and BPP



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This is a key difference between what we assume and BPP



Consumption flow is given by:

$$\begin{split} c_t &= \phi p_t + \int_{t-2}^t g(t-s) dq_s \\ \implies &\operatorname{Cov}(\Delta^N \bar{c_T}, \Delta^N \bar{y_T}) = \phi (N - \frac{1}{3}) \sigma_p^2 + 2\psi \sigma_{\tilde{q}}^2 \end{split}$$

where  $\psi = \frac{\operatorname{Cov}(\tilde{c},\tilde{q})}{\operatorname{Var}(\tilde{q})}$ , the regression coefficient of 'transitory' consumption on transitory income

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- $\phi$ : MPX out of permanent income shocks
- $\psi$ : MPX out of transitory income shocks

#### **Full Identification**

We use GMM on the equations:

$$\operatorname{Var}(\Delta^{N} \bar{y_{T}}) = (N - \frac{1}{3})\sigma_{p}^{2} + 2\sigma_{\tilde{q}}^{2}$$
$$\operatorname{Cov}(\Delta^{N} \bar{c_{T}}, \Delta^{N} \bar{y_{T}}) = \phi(N - \frac{1}{3})\sigma_{p}^{2} + 2\psi\sigma_{\tilde{q}}^{2}$$

with N = 3, 4, 5 (total of six equations) to identify the four unknowns:

- $\sigma_p^2$ : Permanent shock variance
- ullet  $\sigma_{\tilde{a}}^2$ : (Time aggregated) transitory shock variance
- $\phi$ : MPX out of permanent income shocks
- $\psi$ : MPX out of transitory income shocks

### Threats to Identification

	Direction of Bias	
	Perm MPX	Tran MPX
Persistent Consumption Response	+ve	-ve
Endogenous Income Shocks	Neutral	+ve
Income Measurement Error	Neutral	+ve
Permanent Shocks are $AR(1)$	Neutral	+ve
Non-linear MPX	?	?
Time-varying risk	?	?

### Data: Income

- Starting point: Register based micro data for all Danish households made available by Statistics Denmark
- Really good income data
  - We use after-tax income for the household head, based on third-party reported tax data
  - Restrict sample to heads aged 30-55
- We divide through by permanent income (mean income over all observed years) and take the residual after controlling for age, education, marital status etc. (along with interactions of these)

### Data: Expenditure

We use the identity

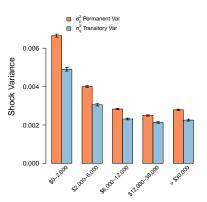
$$C_t \equiv Y_t - S_t = Y_t - P_t - \Delta NW$$

- Deposit and brokerage accounts all third party reported
- Works well for households with simple financial lives
- Main issue: Capital gains and losses
  - Exclude households where methodology will not work well (eg business owners)
  - Exclude housing wealth and years with housing transactions
  - Capital gains for stocks based on a diversified index
- Noisy, but perhaps better than surveys (Kuchler et al. 2018)
- Huge sample size advantage: sample covers 7.6 million observations over 2004-2015

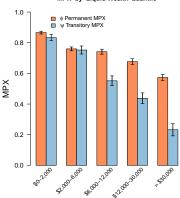


# MPX by Liquid Wealth

#### Permanent and Transitory Variance by Liquid Wealth Quantile



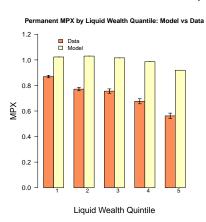
#### MPX by Liquid Wealth Quantile

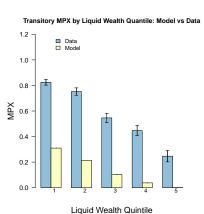


MPX by Net Wealth

### Model vs Data

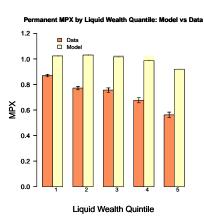
### How does a standard model compare with the data?

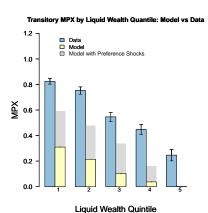




### Model vs Data

How does a standard model compare with the data?





We calculate the sufficient statistics from Auclert (2017)

Here we will focus on the *Interest Rate Exposure* channel:

lf

- 1 Households that *owe* a lot of floating rate debt have *high* MPCs
- 2 Households that own a lot of floating rate debt have low MPCs

Then lowering interest rates will on average *increase* consumption through redistribution

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Do we know if 1 and 2 hold? How can we measure the size of this effect?



Define *Unhedged Interest Rate Exposure* for household *i* as the total savings the household will invest at this year's interest rate:

$$URE_i = Y_i - C_i + A_i - L_i$$

#### Where

- $Y_i$  = Total after tax income
- $C_i$  = Total Expenditure, including interest payments
- $A_i = Maturing assets$
- $L_i$  = Maturing liabilities

Following a change in the interest rate dR, the size of the Interest Rate Exposure channel on household i's expenditure is:

$$dc_i = MPC_i URE_i \frac{dR}{R} \tag{1}$$

In aggregate, the size of this channel is given by:

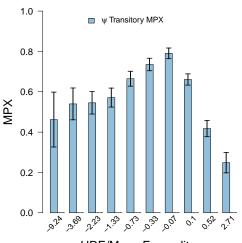
$$\frac{dC}{C} = \mathbb{E}_{I} \left( MPC_{i} \frac{URE_{i}}{\mathbb{E}_{I}(c_{i})} \right) \frac{dR}{R}$$

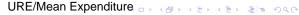
Define sufficient statistic:

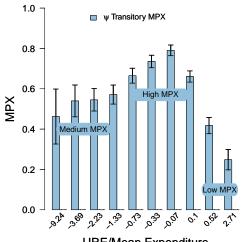
$$\mathcal{E}_{R} = \mathbb{E}_{I} \left( MPC_{i} \frac{URE_{i}}{\mathbb{E}_{I}(c_{i})} \right)$$

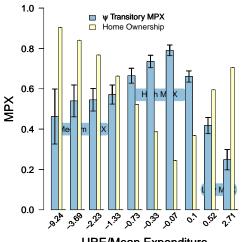
 $\implies$  Need to know the distribution of  $MPC_i$  with  $URE_i$ 

We can do that!

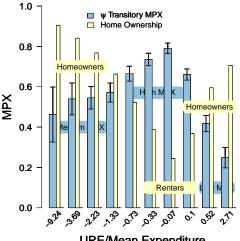




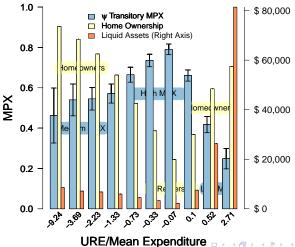




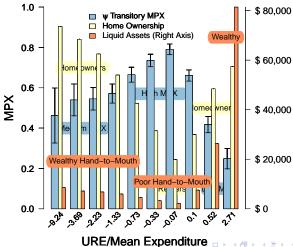














Total URE sums to zero - this is not true for our household sample

• -338bn Kr

	MPX	URE	$\mathcal{E}_R$ component
Estimation Sample	See Distribution	-57	-0.40
Young	0.5	-16	-0.07
Old	0.5	14	0.06
Pension Funds	0.1	31	0.03
Government	0.0	-19	0.00
Non-financial Corp.	0.1	-11	-0.01
Financial Sector	0.1	51	0.04
Rest of World	0.0	7	0.00
Total		-0	-0.35

Notes: URE numbers are in billions of 2015 USD.

The Five Transmission Channels:

Aggregate Income Channel

$$\frac{dC}{C} = \frac{dY}{M\frac{dY}{Y}} + \mathcal{E}_R \frac{dR}{R}$$

Interest Rate Exposure Channel

Earnings Heterogeity Channel  $\overbrace{+\gamma\mathcal{E}_{Y}\frac{dY}{Y}}^{+\gamma\mathcal{E}_{Y}\frac{dY}{Y}} \\ -\sigma\mathcal{S}\frac{dR}{R}$ 

Intertemporal Substitution Channel



Fisher Channel

#### The Five Transmission Channels:

Aggregate Income Channel

$$\frac{dC}{C} = \frac{dY}{M \frac{dY}{Y}}$$

$$+ \mathcal{E}_{P} \frac{dR}{M}$$

Interest Rate Exposure Channel

Earnings Heterogeity Channel

$$\begin{array}{c}
+\gamma \mathcal{E}_{Y} \frac{dY}{Y} \\
-\sigma \mathcal{S} \frac{dR}{R}
\end{array}$$

Intertemporal Substitution Channel

$$\mathcal{M}$$
 0.56  $\mathcal{E}_{Y}$  -0.03  $\mathcal{E}_{P}$  -0.81  $\mathcal{E}_{R}$  -0.35  $\mathcal{S}$  0.47



Fisher Channel

### The Five Transmission Channels:

Aggregate Income Channel

$$\frac{dC}{C} = \frac{\widetilde{M}\frac{dY}{Y}}{+\mathcal{E}_R}\frac{dR}{R}$$

Interest Rate Exposure Channel

Earnings Heterogeity Channel

$$\overbrace{+\gamma \mathcal{E}_{Y} \frac{dY}{Y}} \\
-\sigma \mathcal{S} \frac{dR}{R}$$

Intertemporal Substitution Channel

$$\mathcal{M}$$
 0.56  $\mathcal{E}_{Y}$  -0.03  $\mathcal{E}_{P}$  -0.81  $\mathcal{E}_{R}$  -0.35  $\mathcal{S}$  0.47

Compare  $\mathcal{E}_R$  to  $\sigma S$ :

 $\sigma$  in the range of 0.1 to 0.5 (maybe)

$$\sigma S \approx 0.06 - 0.28$$

Fisher Channel

We have data on value of household cars

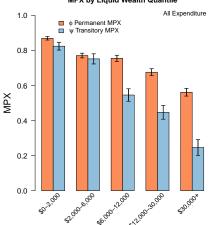
• Construct expenditure excluding car purchases and sales

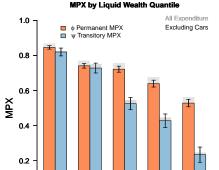
$$C_T^{\mathsf{nocar}} = C_T - \Delta \mathsf{CarValue}$$

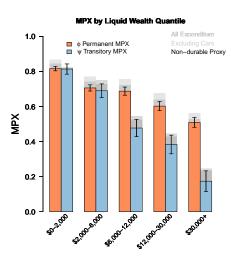
• Construct proxy for non durable consumption (Cars  $\approx$  42.1% durable expenditure)

$$C_T^{\text{nondurable}} = C_T - \frac{1}{0.421} \Delta \text{CarValue}$$







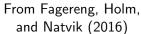


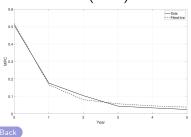
### Conclusion

- We have designed a new method to estimate consumption responses to income shocks
- It appears to work well, both in theory and practice
- We can use it to show that heterogeneity plays a key role in monetary policy transmission

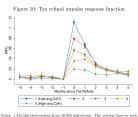
Thank you!

### Evidence of Consumption Decay Within 2 Years





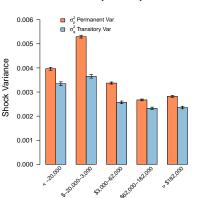
### From Gelman (2016)



Notes: 1,445,560 observations from 48,059 individuals. The vertical bars on each coefficient represent 95% confidence intervals using heteroskedasticity robust errors clustered at the individual level.

### MPX by Net Wealth





#### MPX by Net Wealth Quantile

