

# Neural Networks

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# *Artificial Neural Networks*

- **Neural network:** *information processing paradigm inspired by biological nervous systems, such as our brain*
- Structure: large number of highly interconnected processing elements (*neurons*) working together
- Like people, they learn *from experience* (by example)

“Data processing system consisting of a large number of simple, highly interconnected processing elements (artificial neurons) in an architecture inspired by the structure of the cerebral cortex of the brain”

(Tsoukalas & Uhrig, 1997).

# History

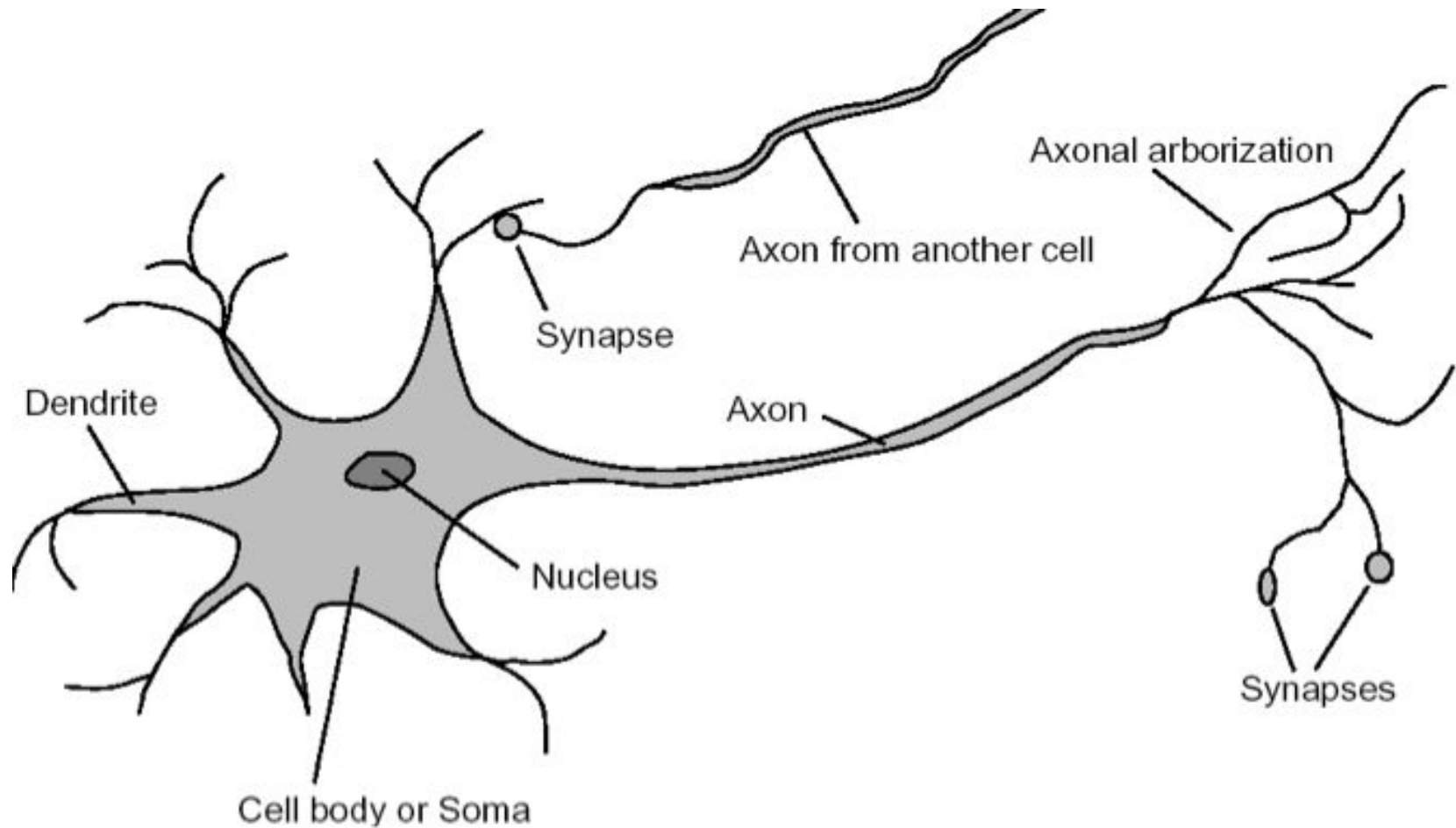
- **1943:** Warren McCulloch & Walter Pitts's first mathematical model of NN
- **1949:** Donald Hebb
  - "Hebbian learning rule"
- **1950s-1960s:** Rosenblatt
  - Perceptron
- **The "AI Winter" and Resurgence (1960s-1980s):**
- **1974:** Paul Werbos introduced the backpropagation algorithm
- **1980s-1990s:** Yann LeCun & others
  - Convolutional neural networks (CNNs)
- **1982:** John Hopfield
  - Hopfield networks
- **2000s-Present:** Deep learning
  - Advancements in computing power, GPUs,
- **2006:** Geoffrey Hinton
  - deep belief networks
- **2012:** AlexNet
  - a deep convolutional neural network
- **2010s-Present:**
  - Deep learning in various fields

# Neural Network

- A neural network is a **massively parallel, distributed processor**
- made up of simple processing units (**artificial neurons**).
- It **resembles the brain** in two respects:
  - – Knowledge is acquired by the network from its environment through a learning process
  - – Synaptic connection strengths among neurons are used to store the acquired knowledge.

- We are born with about 100 billion neurons
- A neuron may connect to as many as 100,000 other neurons
- Signals “move” via electrochemical signals
- The synapses release a chemical transmitter – the sum of which can cause a threshold to be reached – causing the neuron to “fire”
- Synapses can be inhibitory or excitatory

# Human Biological Neural



# The Biological Neuron

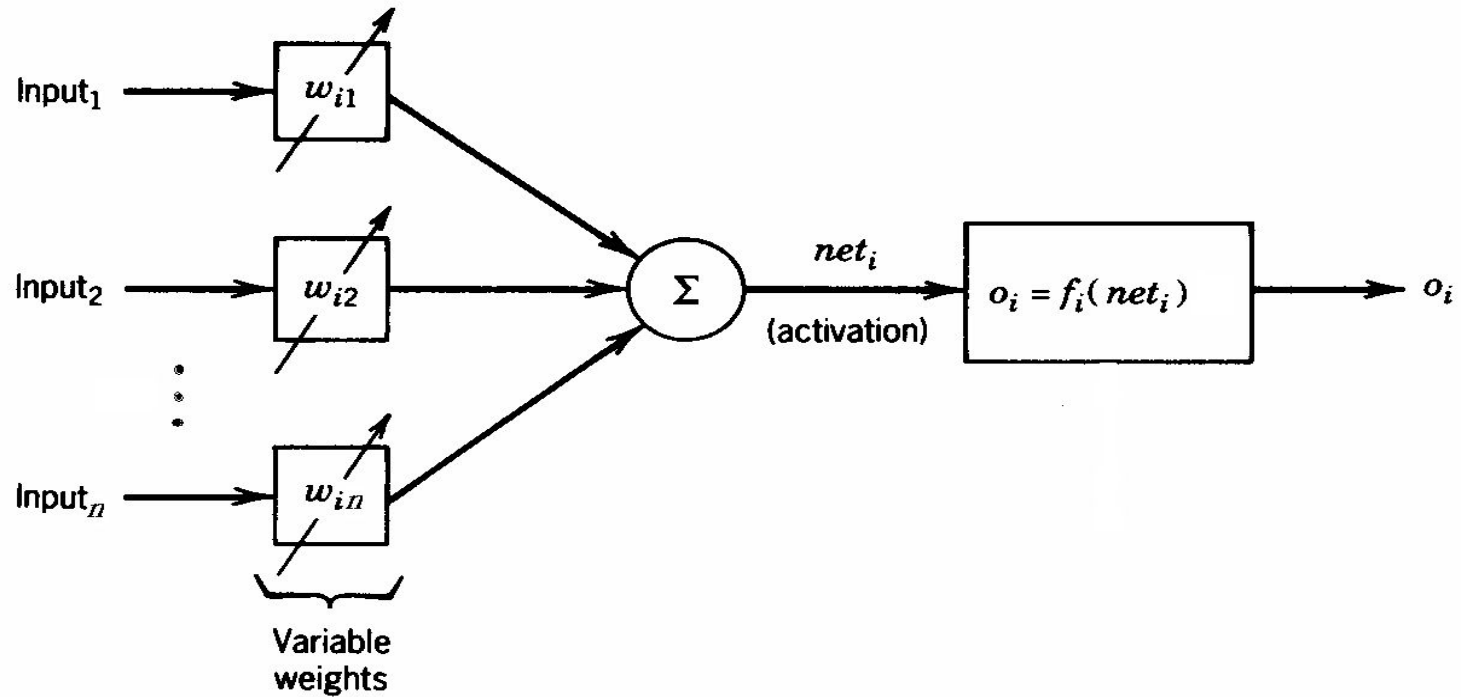
- A biological neuron has three types of main components; **dendrites**, **soma** (or cell body) and **axon**.
- Dendrites receives signals from other neurons.
- The soma, sums the incoming signals. When sufficient input is received, the cell fires; that is it transmit a signal over its axon to other cells.



- A neuron only fires if its input signal exceeds a certain amount (the **threshold**) in a short time period.
- Synapses vary in strength
  - Good connections allowing a large signal
  - Slight connections allow only a weak signal.

- Each neuron has a threshold value
- Each neuron has weighted inputs from other neurons
- The input signals form a weighted sum
- If the activation level exceeds the threshold, the neuron “fires”

# The Artificial Neuron



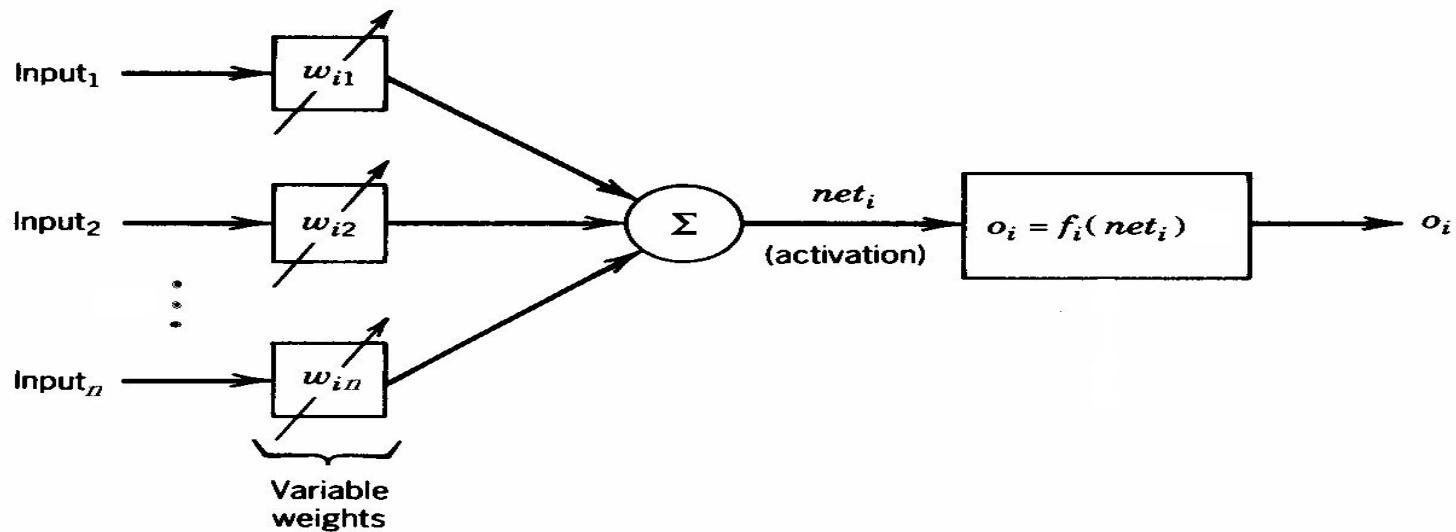
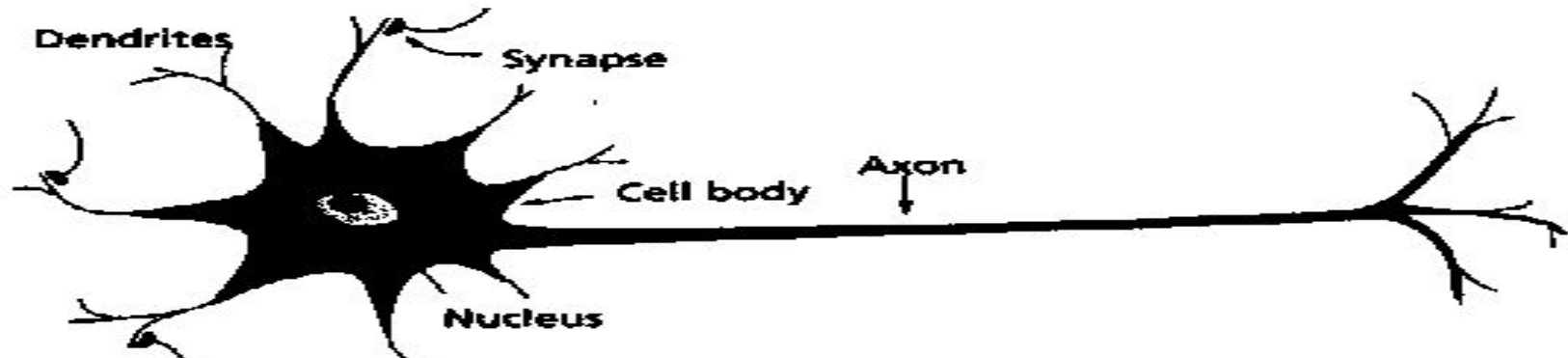
# Artificial Neuron

- Each hidden or output neuron has weighted input connections from each of the units in the preceding layer.
- The unit performs a weighted sum of its inputs, and subtracts its threshold value, to give its activation level.
- Activation level is passed through a sigmoid activation function to determine output.

# Weights in NN

- The strength of connection between the neurons is stored as a weight-value for the specific connection.
- Learning the solution to a problem involves changing the connection weights

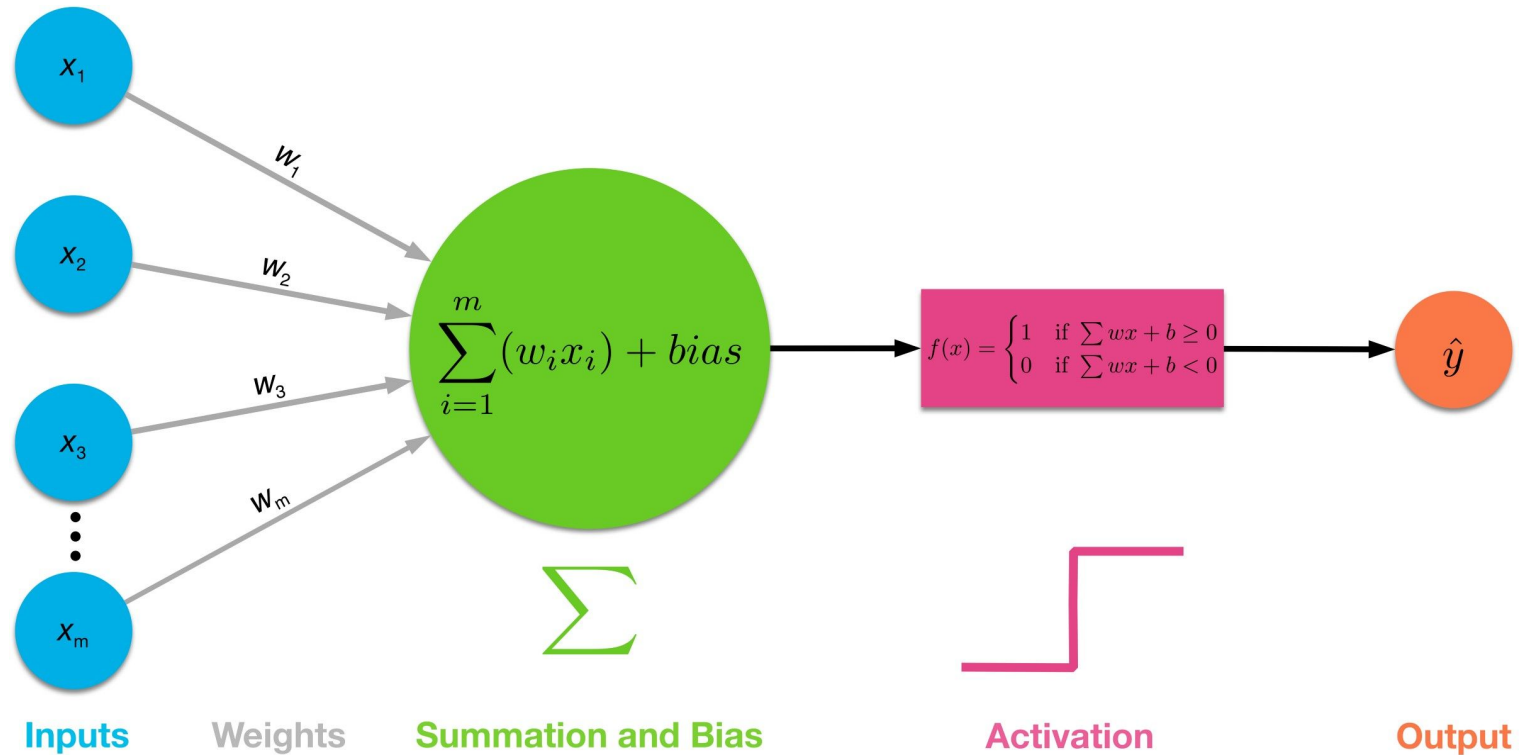
# Biological Vs Artificial Neuron



# Neuron Net

- A neural net consists of a large number of simple processing elements called **neurons, units, cells or nodes**.
- Each neuron is connected to other neurons by means of directed communication links, each with **associated weight**.
- The weight represent information being used by the net to solve a problem.

# A Neuron Model


















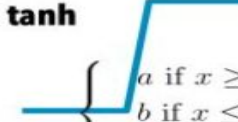
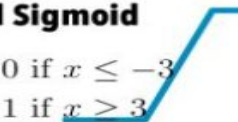
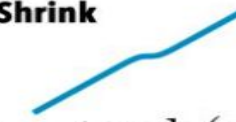

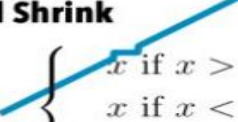
# Activation Function

Neural networks use non-linear activation functions, which help the network learn complex data, compute and learn almost any function, and provide accurate predictions.

# Common Activation Functions

1. **Sigmoid:** Outputs values between 0 and 1, often used in the output layer for binary classification.
2. **Tanh:** Outputs values between -1 and 1, zero-centered, which can help with faster convergence during training.
3. **ReLU (Rectified Linear Unit):** Outputs the input directly if positive, otherwise outputs 0. A popular choice for hidden layers due to its simplicity and ability to mitigate the vanishing gradient problem.
4. **Softmax:** Converts a vector of numbers into a probability distribution, commonly used in the output layer for multi-class classification.

## Neural Network Activation Functions: a small subset!

<b>ReLU</b>  $\max(0, x)$	<b>GELU</b>  $\frac{x}{2} \left( 1 + \tanh \left( \sqrt{\frac{2}{\pi}} (x + ax^3) \right) \right)$	<b>PReLU</b>  $\max(0, x)$
<b>ELU</b>  $\begin{cases} x & \text{if } x > 0 \\ \alpha(x \exp x - 1) & \text{if } x < 0 \end{cases}$	<b>Swish</b>  $\frac{x}{1 + \exp -x}$	<b>SELU</b>  $\alpha(\max(0, x) + \min(0, \beta(\exp x - 1)))$
<b>SoftPlus</b>  $\frac{1}{\beta} \log(1 + \exp(\beta x))$	<b>Mish</b>  $x \tanh \left( \frac{1}{\beta} \log(1 + \exp(\beta x)) \right)$	<b>RReLU</b>  $\begin{cases} x & \text{if } x \geq 0 \\ ax & \text{if } x < 0 \text{ with } a \sim \mathcal{R}(l, u) \end{cases}$
<b>HardSwish</b>  $\begin{cases} 0 & \text{if } x \leq -3 \\ x & \text{if } x \geq 3 \\ x(x+3)/6 & \text{otherwise} \end{cases}$	<b>Sigmoid</b>  $\frac{1}{1 + \exp(-x)}$	<b>SoftSign</b>  $\frac{x}{1 +  x }$
<b>Tanh</b>  $\tanh(x)$	<b>Hard tanh</b>  $\begin{cases} a & \text{if } x \geq a \\ b & \text{if } x \leq b \\ x & \text{otherwise} \end{cases}$	<b>Hard Sigmoid</b>  $\begin{cases} 0 & \text{if } x \leq -3 \\ 1 & \text{if } x \geq 3 \\ x/6 + 1/2 & \text{otherwise} \end{cases}$
<b>Tanh Shrink</b>  $x - \tanh(x)$	<b>Soft Shrink</b>  $\begin{cases} x - \lambda & \text{if } x > \lambda \\ x + \lambda & \text{if } x < -\lambda \\ 0 & \text{otherwise} \end{cases}$	<b>Hard Shrink</b>  $\begin{cases} x & \text{if } x > \lambda \\ x & \text{if } x < -\lambda \\ 0 & \text{otherwise} \end{cases}$

source: TheAiEdge.io

# Role of Activation Functions

- **Introduce non-linearity:** transform the weighted sum of inputs into a usable output, enabling the network to learn non-linear relationships in data.
- **Control neuron activation:** determine whether a neuron should "fire"
- **Normalize output:** Some activation functions, like sigmoid and tanh, squash the output into a specific range (e.g., 0-1 or -1 to 1), which can help with stability during training.

# Choosing an Activation Function

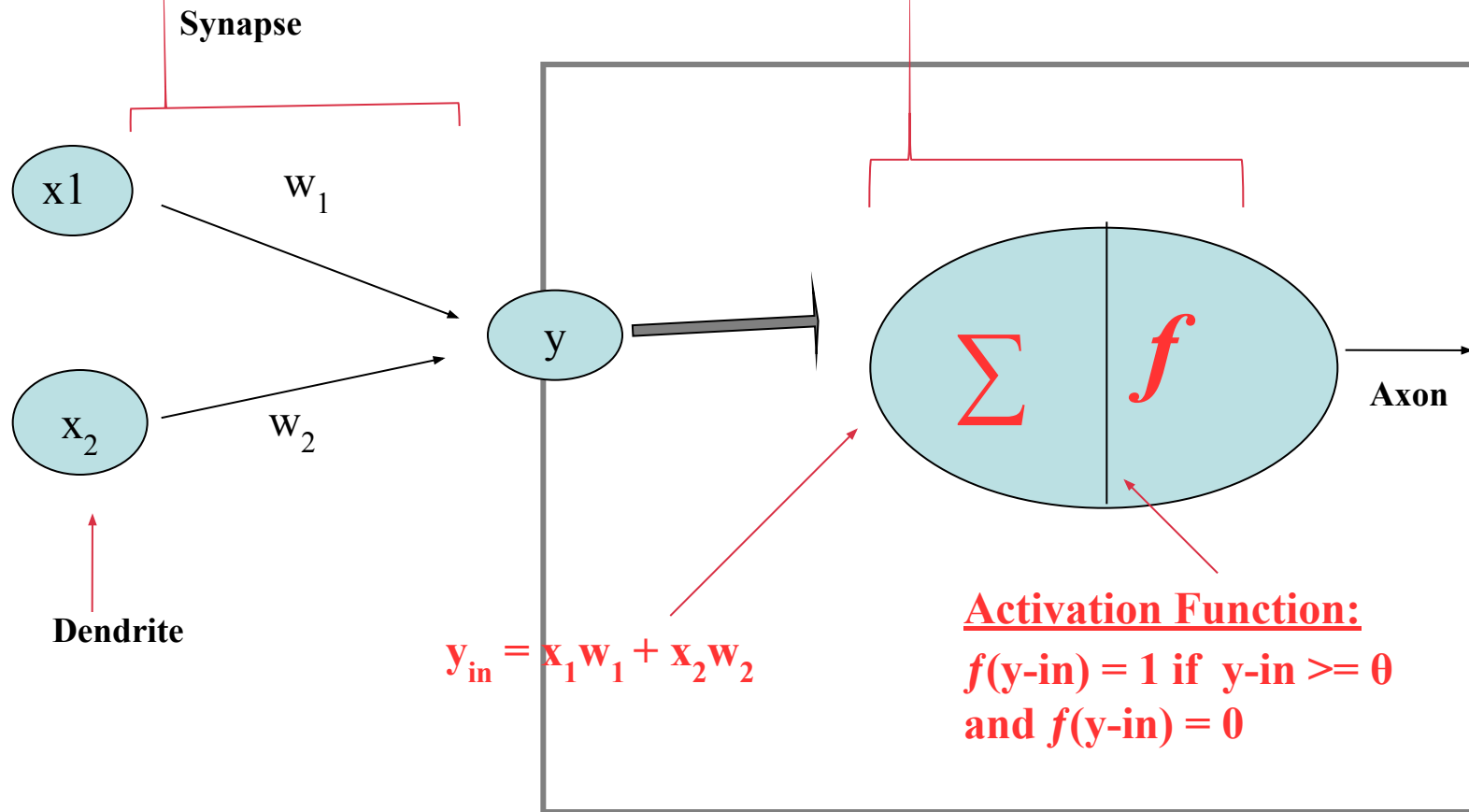
The choice of activation function depends on the specific task

- **Sigmoid** and **tanh** are often used in shallow networks or for specific tasks like binary classification,
- **Rectified Linear Unit (ReLU)** is a popular activation functions in deep learning models. The ReLU function is a piecewise linear function that outputs the input directly if it is positive; otherwise, it outputs zero. ReLU helps mitigate the **vanishing gradient problem**, which can hinder the training of deep neural networks.
- **Softmax** is used for multi-class classification tasks, while linear activation functions are suitable for linear regression problems.

- Each neuron has an internal state, called its **activation or activity level**, which is a function of the inputs it has received. Typically, a neuron sends its activation as a signal to several other neurons.
- It is important to note that a neuron can send only one signal at a time, although that signal is broadcast to several other neurons.

- Neural networks are configured for a specific application, such as pattern recognition or data classification, through a learning process
- In a biological system, learning involves adjustments to the synaptic connections between neurons same for artificial neural networks

# Artificial Neural





- A neuron receives input, determines the strength or the weight of the input, calculates the total weighted input, and compares the total weighted with a value (threshold)
- The value is in the range of 0 and 1
- If the total weighted input is greater than or equal the threshold value, the neuron will produce the output
- If the total weighted input is less than the threshold value, the output will be zero

# Types of NN

Single layer Perceptron

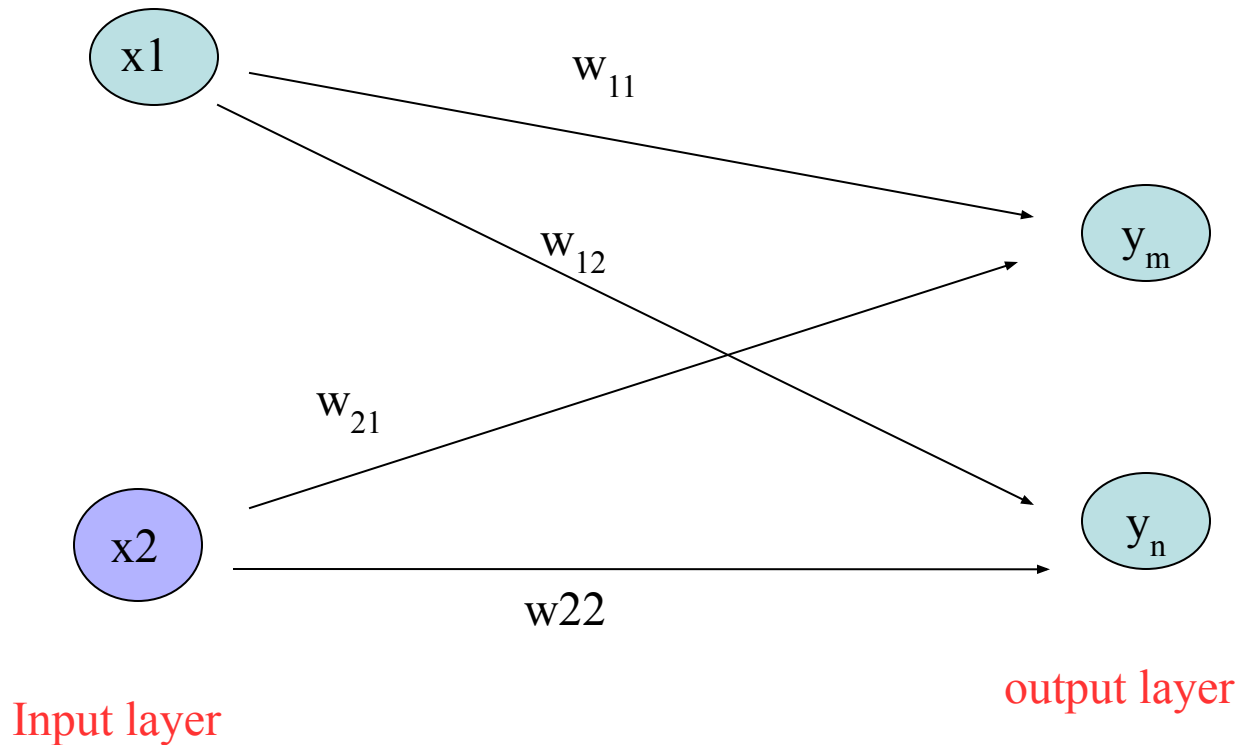
Multi Layer perceptron

Self Organizing maps

Deep learning

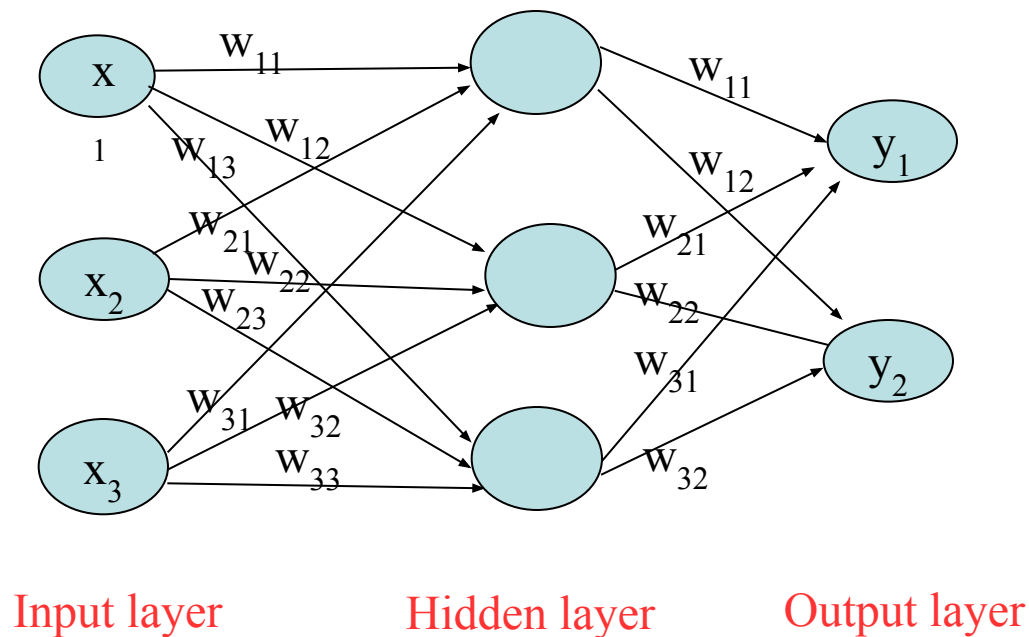
# Single Layer Perceptron

Input layer projecting into the output layer



# Multi Layer Perceptron

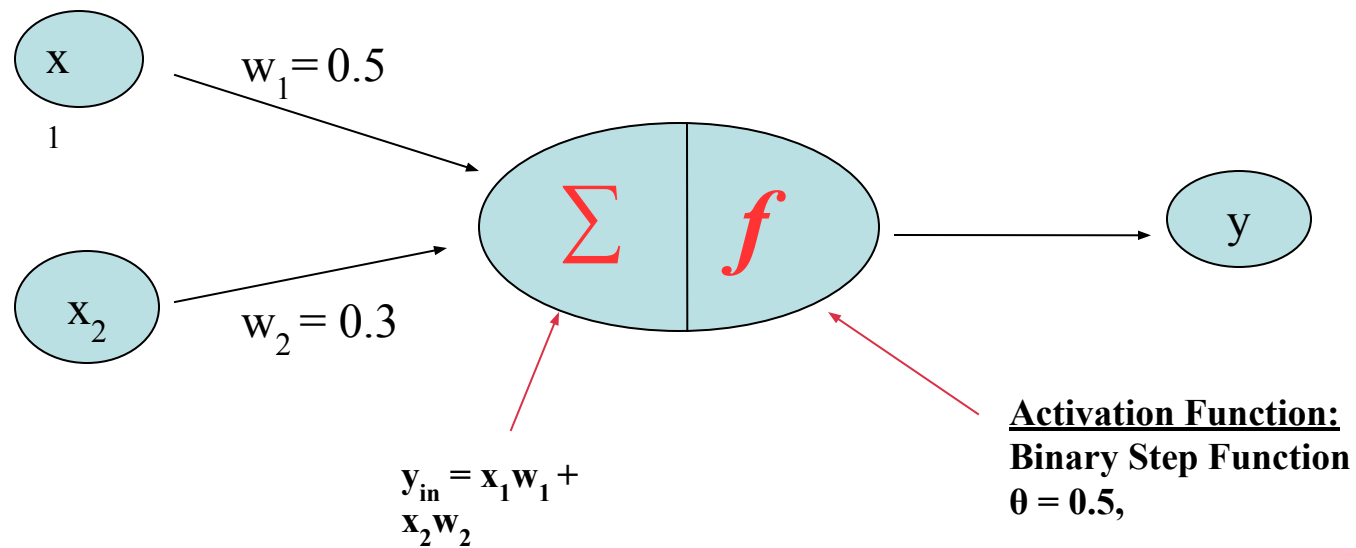
- One or more hidden layers.
- fully connected network



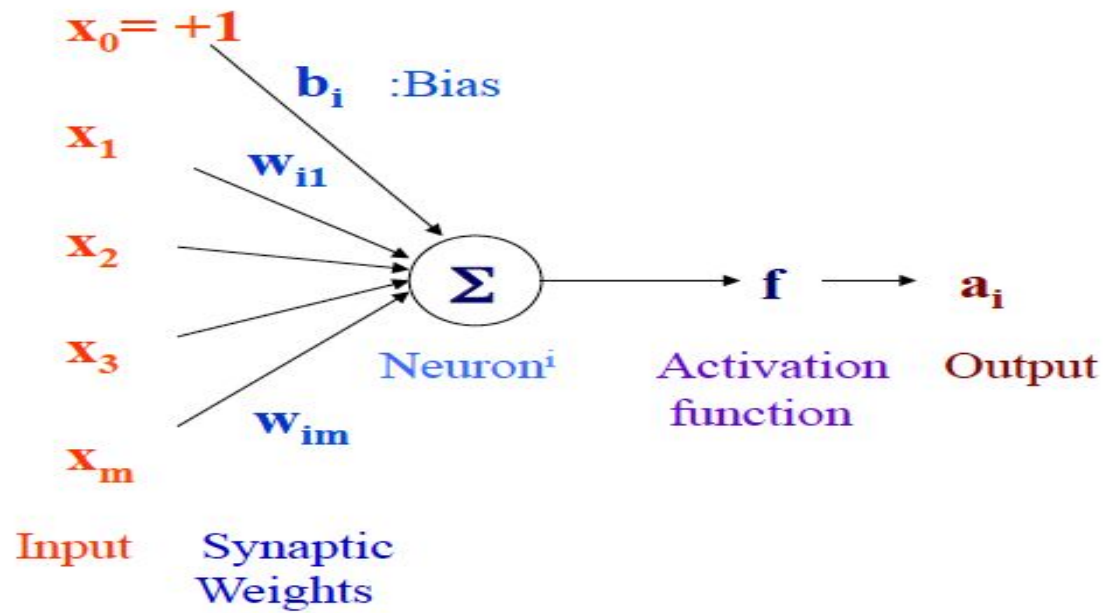
# Types of Layers

- The **input layer**: Introduces input values into the network
  - No activation function or other processing
- The **hidden layer(s)**: Perform classification of features
  - Two hidden layers are sufficient to solve any problem
  - Features imply more layers may be better
- The **output layer**: Functionally just like the hidden layers
  - Outputs are passed on to the world outside the neural network.

# Example



# NN with bias



# Calculating the Bias

An artificial neuron:

- computes the **weighted sum of its input** (called its net **input**)
- adds its bias
- passes this value through an **activation function**

We say that the neuron “**fires**” (i.e. becomes active) if its output is





# NN design

- Number of layers
  - Apparently, three layers is almost always good enough and better than four layers.
  - Also: fewer layers are faster in execution and training
- How many hidden nodes?
  - Many hidden nodes allow to learn more complicated patterns
  - Because of overtraining, almost always best to set the number of hidden nodes too low and then increase their numbers.

# NN Architecture

Even for a basic Neural Network, there are many design decisions to make:

1. # of hidden layers (depth)
2. # of units per hidden layer (width)
3. Type of activation function (nonlinearity)
4. Form of objective function

# NN application

- Signal processing
- Pattern recognition, e.g. handwritten characters or face identification.
- Diagnosis or mapping symptoms to a medical case.
- Speech recognition
- Human Emotion Detection
- Educational Loan Forecasting