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Parallel Computing

Parallel Trigrams

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1 Introduction

The main goal of this project is to count the n -gram (the occurrences of n consecutive word) present in an input file. This will be addressed with two approaches: with the sequential implementation in Chapter 2 and with the parallel implementation in Chapter 3. After these two implementations we will evaluate the performance in Chapter 4, with particular focus on the speed-up.

1.1 Pre-processing

The pipeline that we followed for the input pre-processing consists in collect the input file and normalizing it.

1.1.1 Input collection

We have to collect some text to analyze. In our experiment we use *.txt* file.

1.1.2 Normalization

We want normalizing the input so that similar words will be represented by the same token, i.e., we want create equivalence classes that contain similar words. This help us to reduce the dimension of the word dictionary that composes the trigrams.

We addressed this in these ways:

- Bring all characters in lower case form.
- Remove all the punctuation like periods, commas and exclamation points.
- We maintain only one type of separator between the words, i.e. single space. This help us when we have to bound a word.

1.2 Hash table

We have to be able to count the trigrams; to address efficiently this goal we will use the hash-table.

1.2.1 Hash function

In a hash table we must define the hash function to calculate the table index of the elements. We have to calculate the index of strings, so we adopt the **Polynomial Rolling**

Hash [1]: given the string $c_1 \cdots c_n$, its hash value is defined by

$$H(c_1 \cdots c_n) = \sum_{i=1}^n (c_i \cdot p^{i-1}) \bmod M.$$

This approach to obtain the hash value is inefficient and dangerous for the overflow. We can exploit the distributive property of the module operation: given $H(c_1 \cdots c_i)$, we have that $H(c_1 \cdots c_i c_{i+1}) = (H(c_1 \cdots c_i) \cdot p + c_{i+1}) \bmod M$. This guarantee, with the correct choice of p and M like the one below, the absence of overflow.

1.2.2 Hash table characteristics

Considering what was said above, the hash table has these characteristics:

- The dimension of the index vector corresponde to the M value.
- We resolve the collisions with the open chain method: every position in the table is a pointer to the data that share the same hash value.
- Each node of the open chain is composed by the string (i.e., the n -gram) as key and the counter as value.

2 Sequential

In this chapter we present the main aspect of the sequential implementation to count the n -grams in an input.

2.1 Pipeline

Let's look the pipeline of our sequential algorithm. This was implemented in `main.c` file.

- We take a text file and we pre-processing it. The implementation write all the characters except for the space and the punctuation; between two tokens we write only a single space. After this step we have a normalized file in *data/normalized_file.txt*.
- TODO
- We iterate through the input and consider the current n -gram.
- We calculate the hash value of this n -gram.
- We scroll through the whole list related to the index calculated in the previous step:
 - If current n -gram matches one already found, we increase the related counter.
 - Although we insert as new node in the chain and initialize the counter to one.
- We pass to the next n -gram.

2.2 Hash table

In Section 1.2 we have defined our approach to the hash function. Now we must implement the hash table with its functionalities.

Let's start from the key value of the function, p and M . In general there is a rule of thumb that says to pick both values as prime numbers with M as large as possible. Starting from this:

- p : Must be greater than the dimension of the alphabet. Thanks to normalization, described in Section 1.1.2, our dictionary dimension isn't too much big. We took $p = 101$.

- M : The choice of M determines the load factor of the hash table, that can be defined as $\alpha = \frac{\text{number_of_stored_element}}{\text{table_dimension}}$. We can compute in the way that we can obtain $\alpha = \frac{\text{expected_unic_n-gram}}{1.5 \times \text{expected_unic_n-gram}} \approx 0.67 < 1$, that usually is a good load factor. To determine the *expected_unic_n-gram* the best option is use an empirical estimate sampling from the corpus like $\text{unic_sampling_n-gram} \times \frac{\text{total_words}}{\text{sampled_word}}$. For our goal this isn't a fundamental factor, so we took simply the prime number after 150K, i.e. $M = 150K$.

2.2.1 Overflow

Thanks to these choice and the calculation trick for the hash function, defined in Section 1.1.2, we are sure that we haven't overflow error if we store the intermediate result in 32 bits variable.

In fact, suppose that H_i can store in 32 bits we can prove that the intermediate variable used can be store in 32 bits: in the worst case we have that $\text{intermediate_var} = (M - 1) \cdot p + c_{\max} < 2^{32}$.

2.2.2 Implementation

The implementation of the hash table is in `hash_table.c` file.

In addition to the code, observe that the n -gram dimension (i.e., the n value) is defined in the `CMakeLists.txt` file. This gives us the possibility to pass this parameter from terminal when we execute the program.

3 Parallel

In this chapter we present the main aspect of the parallel implementation to count the 3-grams in an input.

4 Analysis

Bibliografia

- [1] Jakub PACHOCKI e Jakub RADOSZEWSKI. «Where to Use and How not to Use Polynomial String Hashing.» In: *Olympiads in Informatics 7* (2013).