



Robotics, Vision and Control

Master's degree in Computer Engineering for Robotics and smart Industry

Project – Exam

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General overview

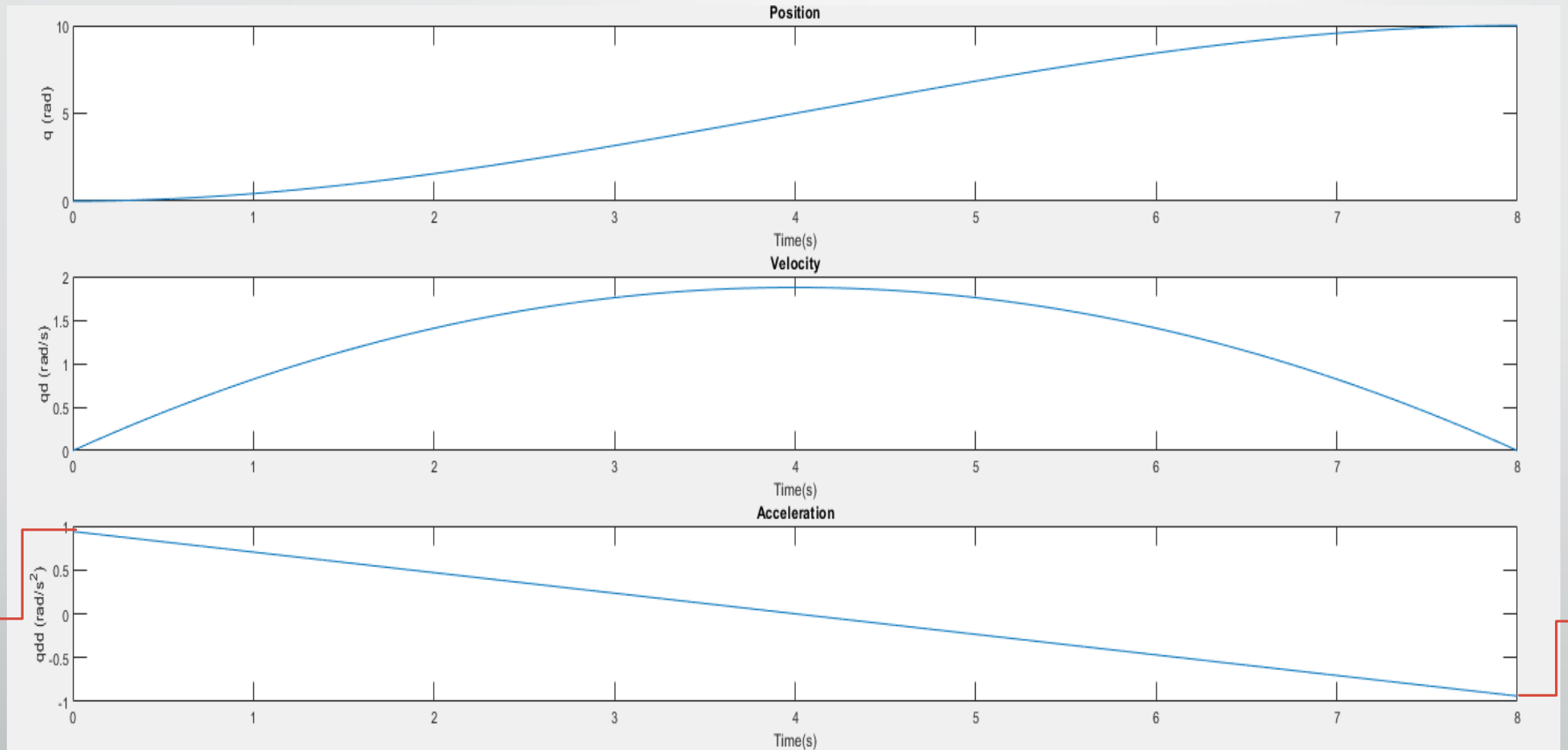
1. Robotics

- a. Point-to-point and multi points trajectory in configurational space
- b. Operational space trajectory
- c. Model-based trajectory

2. Vision

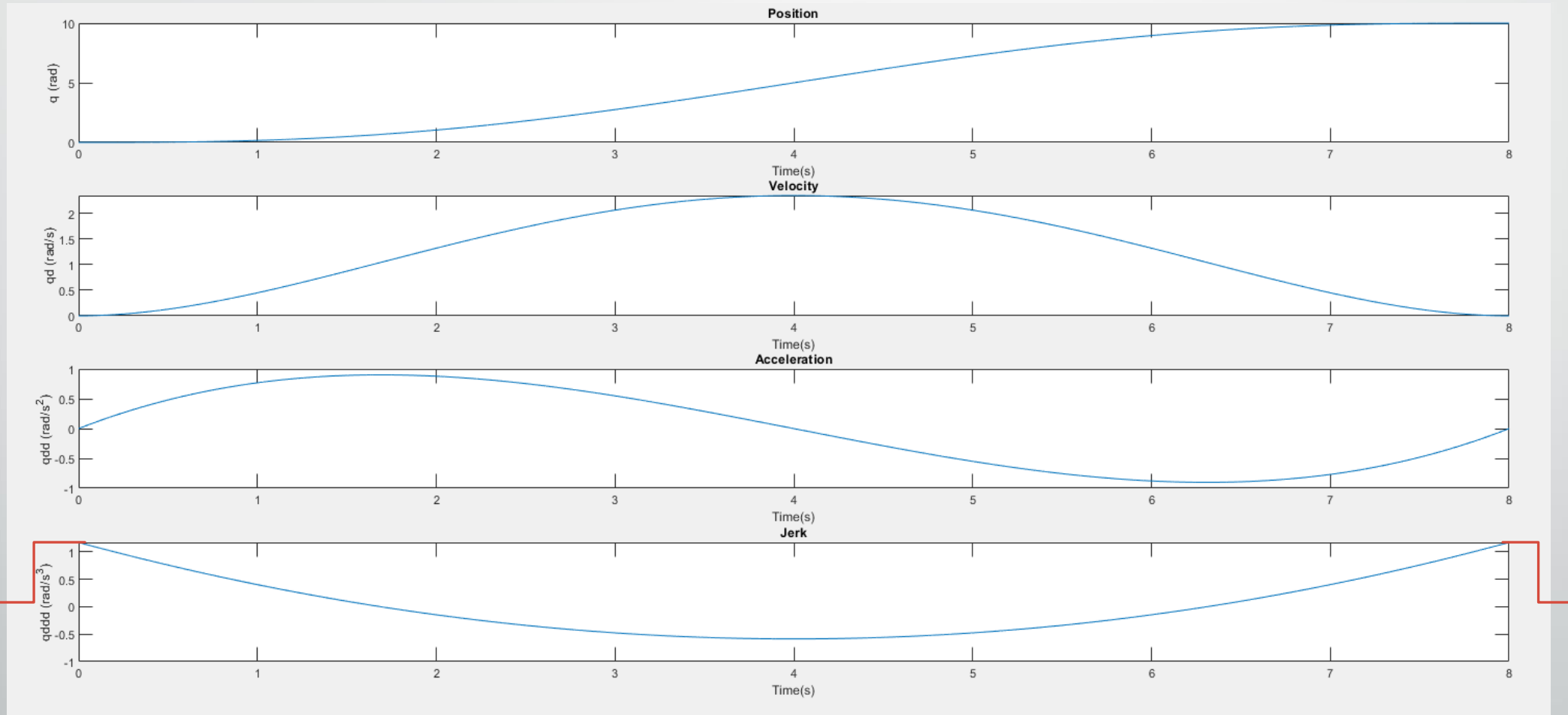
- a. 3D acquisition system
- b. Image analysis
- c. 3D analysis
- d. Hand eye calibration

3th-order polynomial



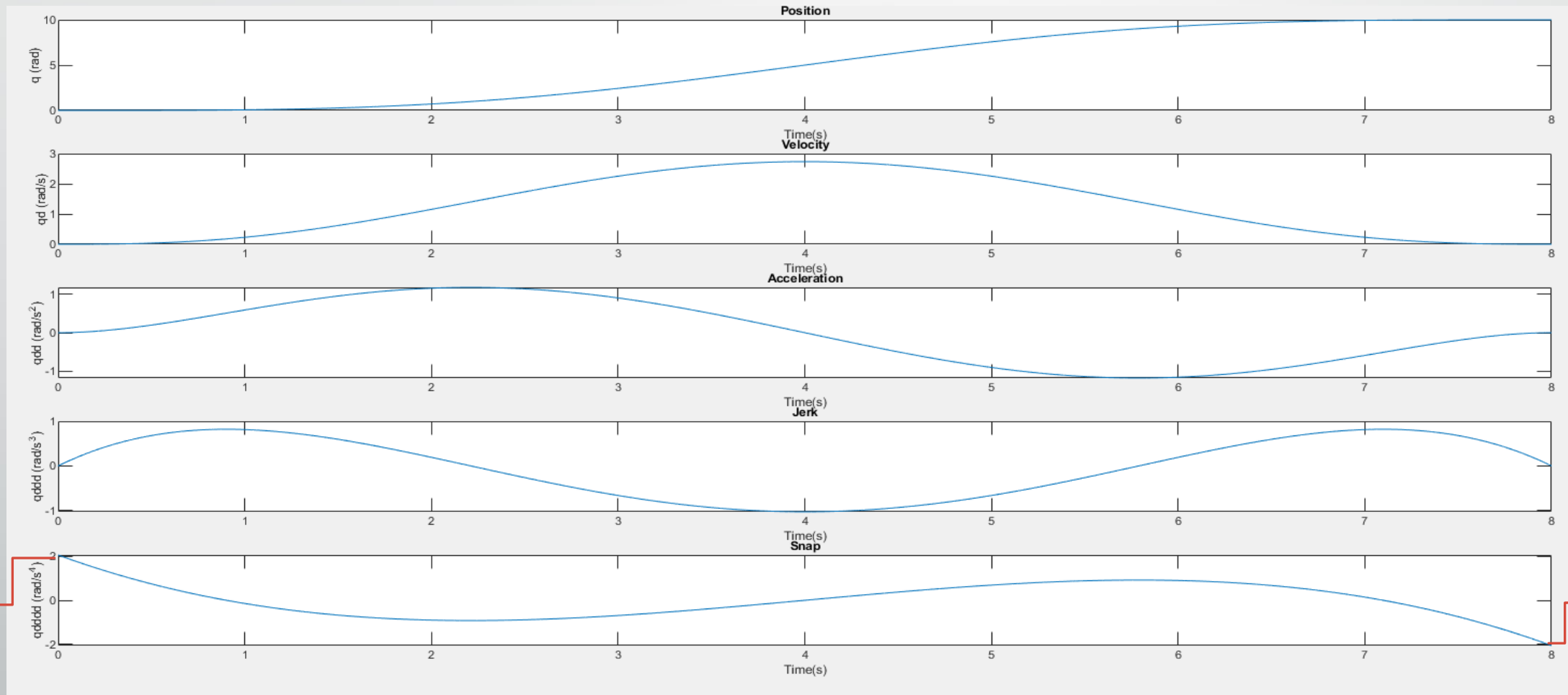
`[q, qd, qdd, T] = cubic_polynomials(qi, qf, dqi, dqf, ti, tf, Ts);`

5th-order polynomial



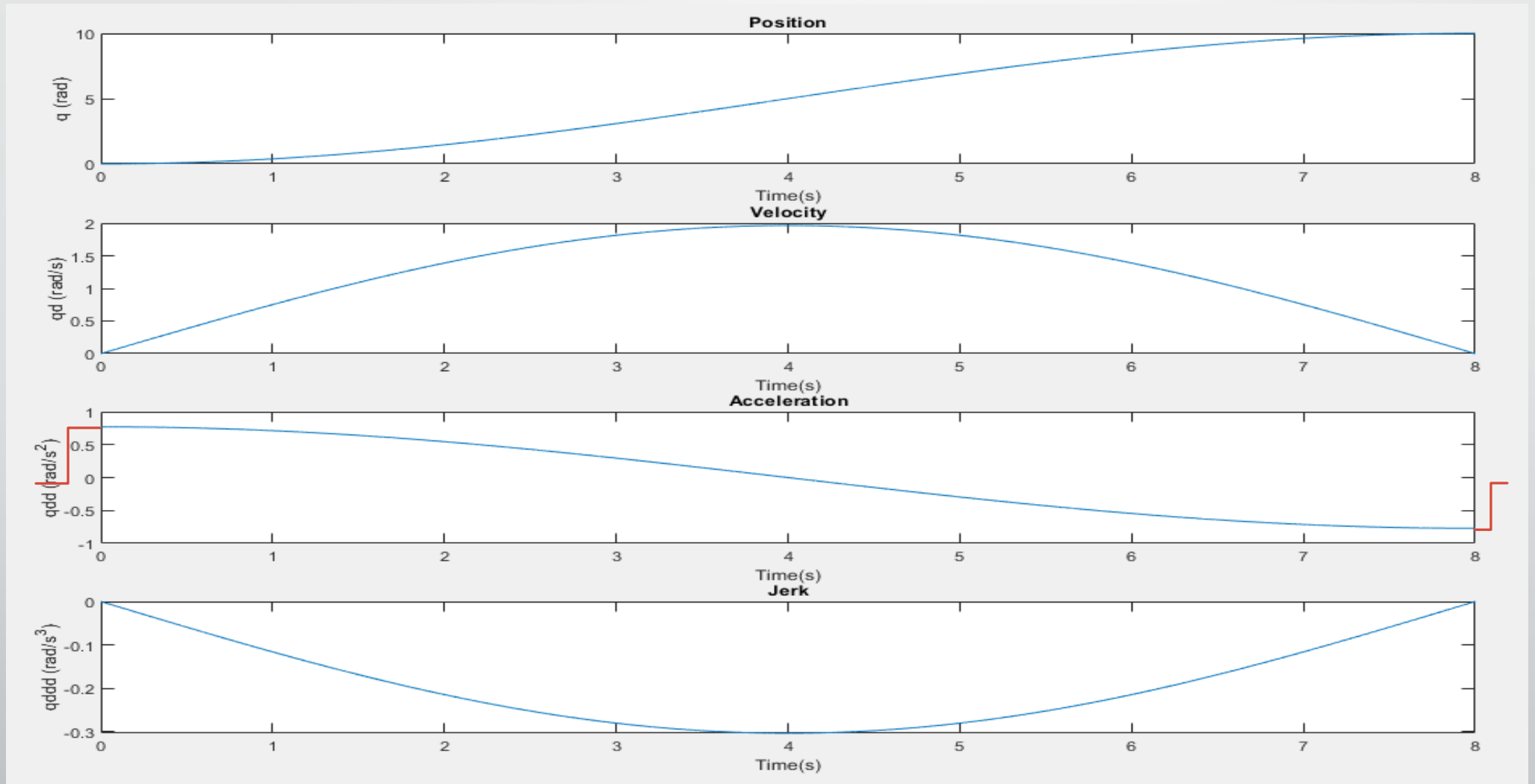
$[q, qd, qdd, qddd, T] = \text{fifth_polynomials}(q_i, q_f, dqi, dqf, ddqi, ddqf, t_i, t_f, T_s);$

7th-order polynomial



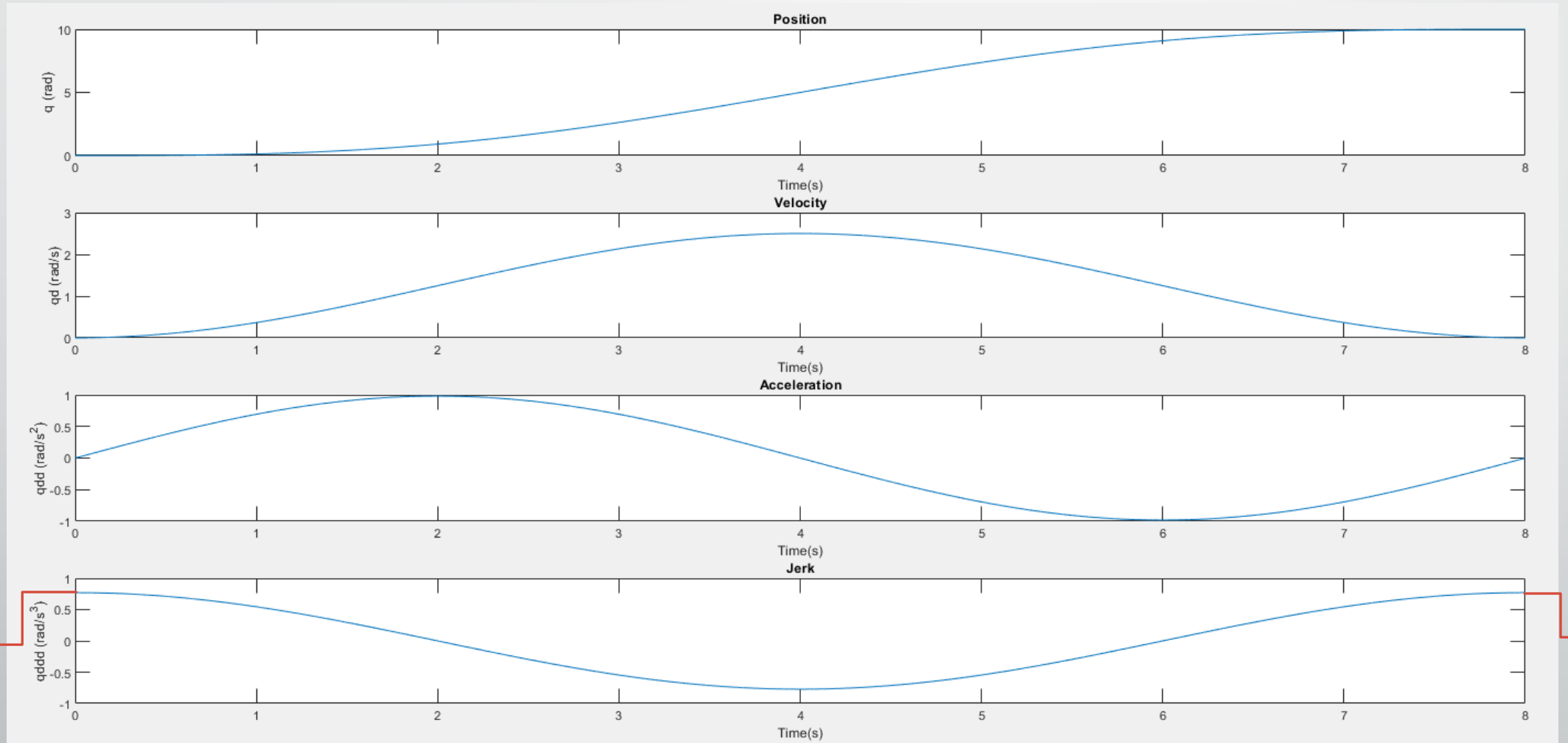
$[q, \dot{q}, \ddot{q}, \dddot{q}, \ddddot{q}, T] = \text{seventh_polynomials}(q_i, q_f, \dot{q}_i, \dot{q}_f, \ddot{q}_i, \ddot{q}_f, \dddot{q}_i, \dddot{q}_f, t_i, t_f, T_s);$

Harmonic trajectory



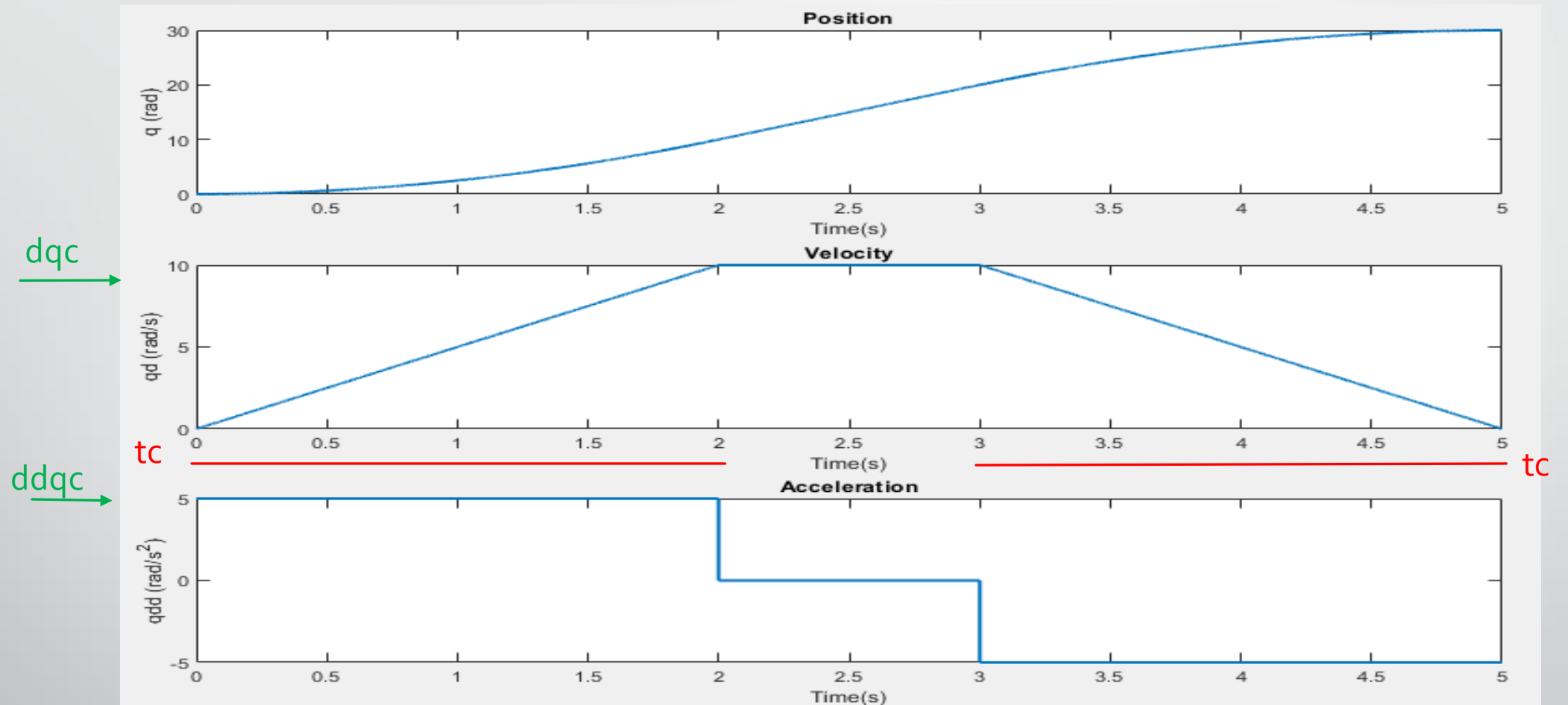
$[q, q\dot{d}, q\ddot{d}, q\dddot{d}, T] = \text{harmonicTrajectory}(q_i, q_f, t_i, t_f, T_s);$

Cycloidal trajectory



$[q, q_d, q_{dd}, q_{ddd}, T] = \text{cycloidalTrajectory}(q_i, q_f, t_i, t_f, T_s);$

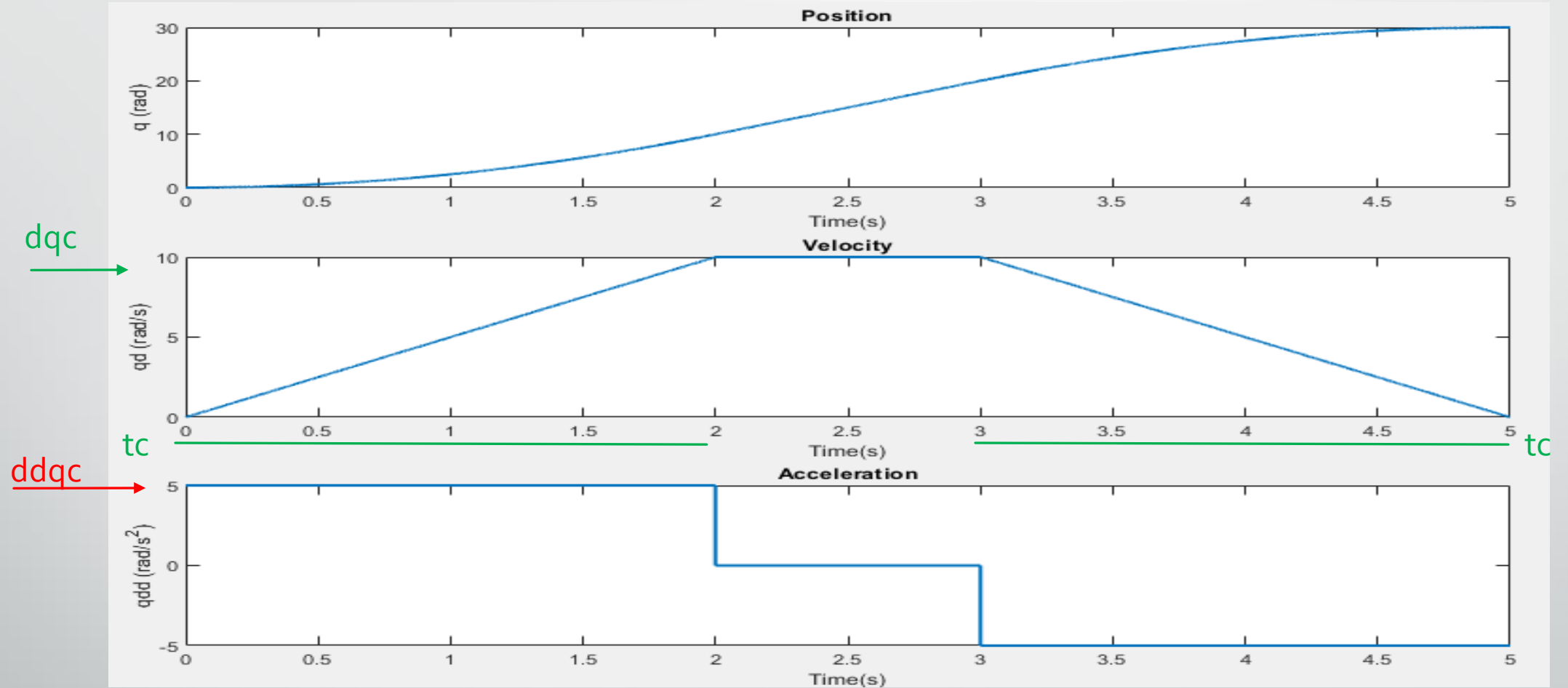
Symmetric trapezoidal trajectory – subcase 1



`[q, qd, qdd, T]= trapezoidalProfileSymmetric(tc, dqc, ddqc, ti, tf, qf, qi, Ts, subcase);`



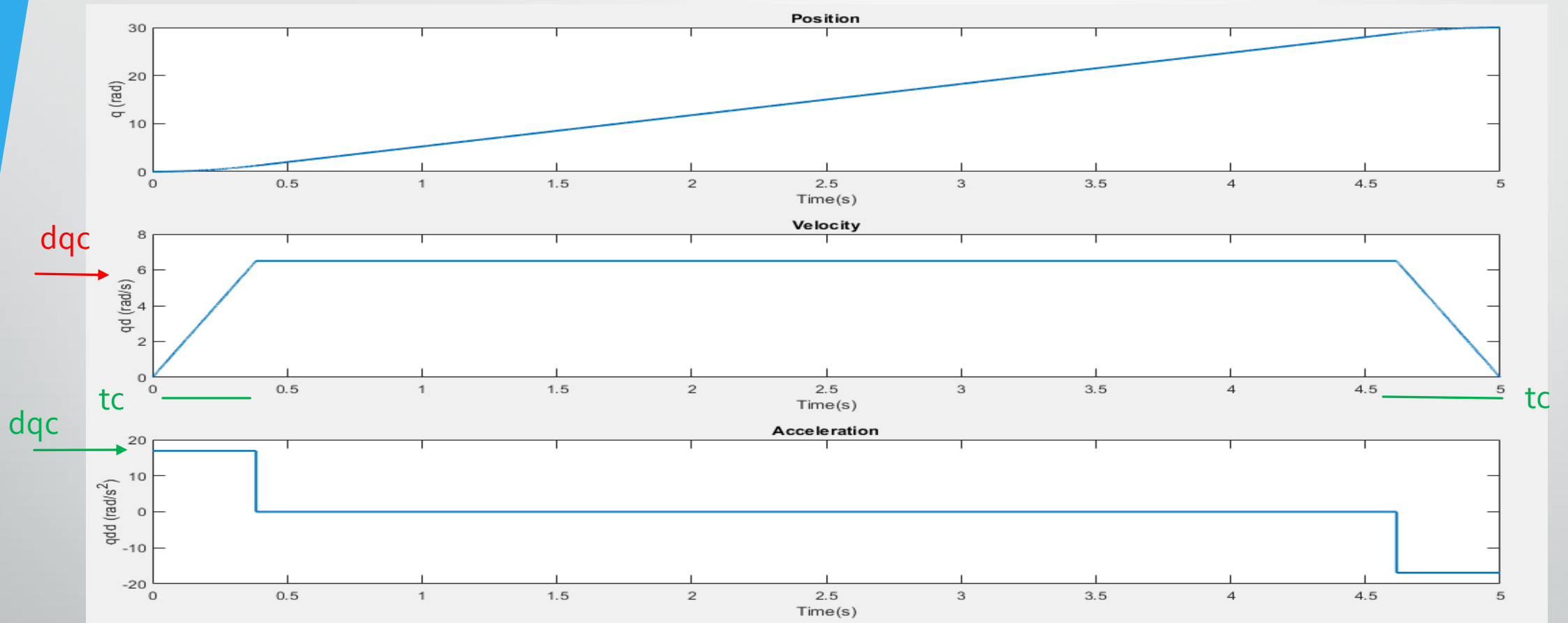
Symmetric trapezoidal trajectory – subcase 2



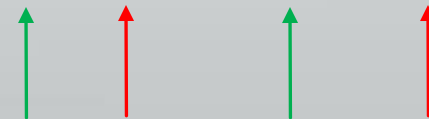
`[q, qd, qdd, T]= trapezoidalProfileSymmetric(tc, dqc, ddqc, ti, tf, qf, qi, Ts, subcase);`



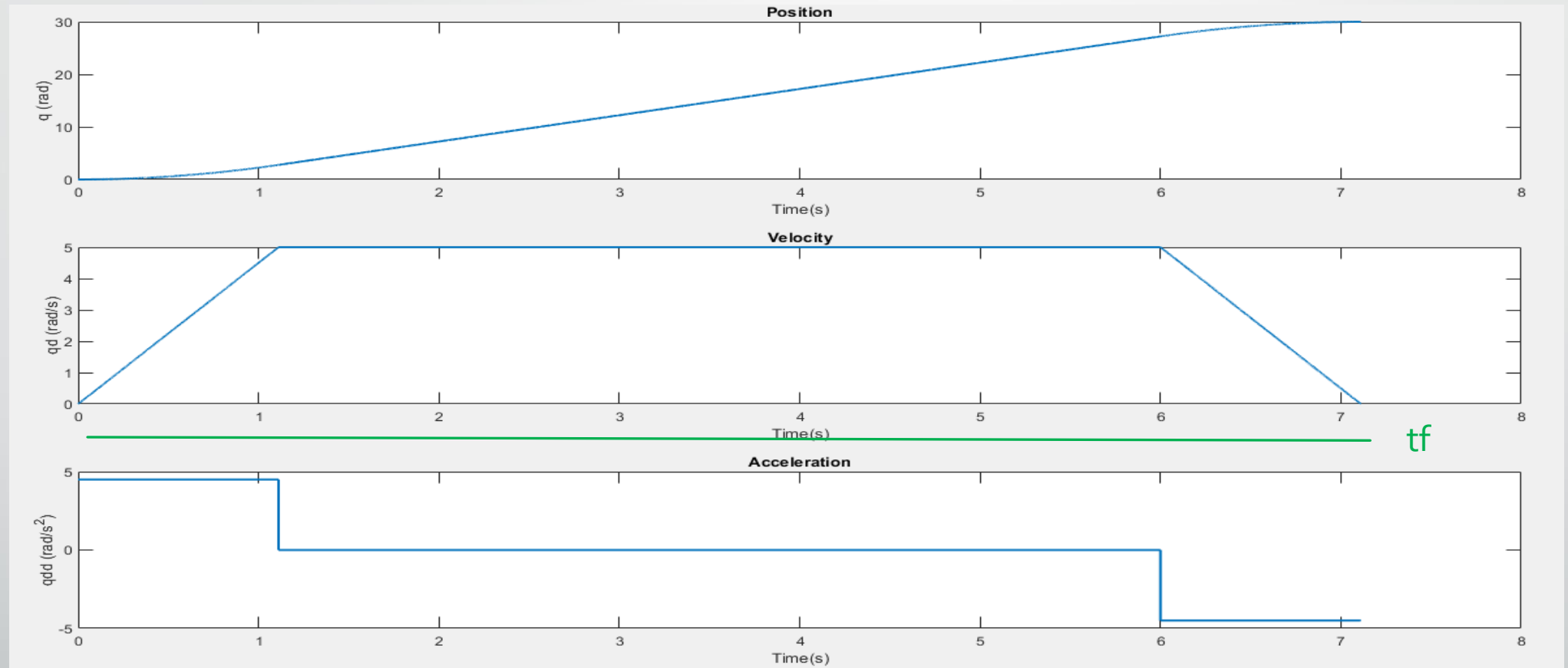
Symmetric trapezoidal trajectory – subcase 3



`[q, qd, qdd, T]= trapezoidalProfileSymmetric(tc, dqc, ddqc, ti, tf, qf, qi, Ts, subcase);`



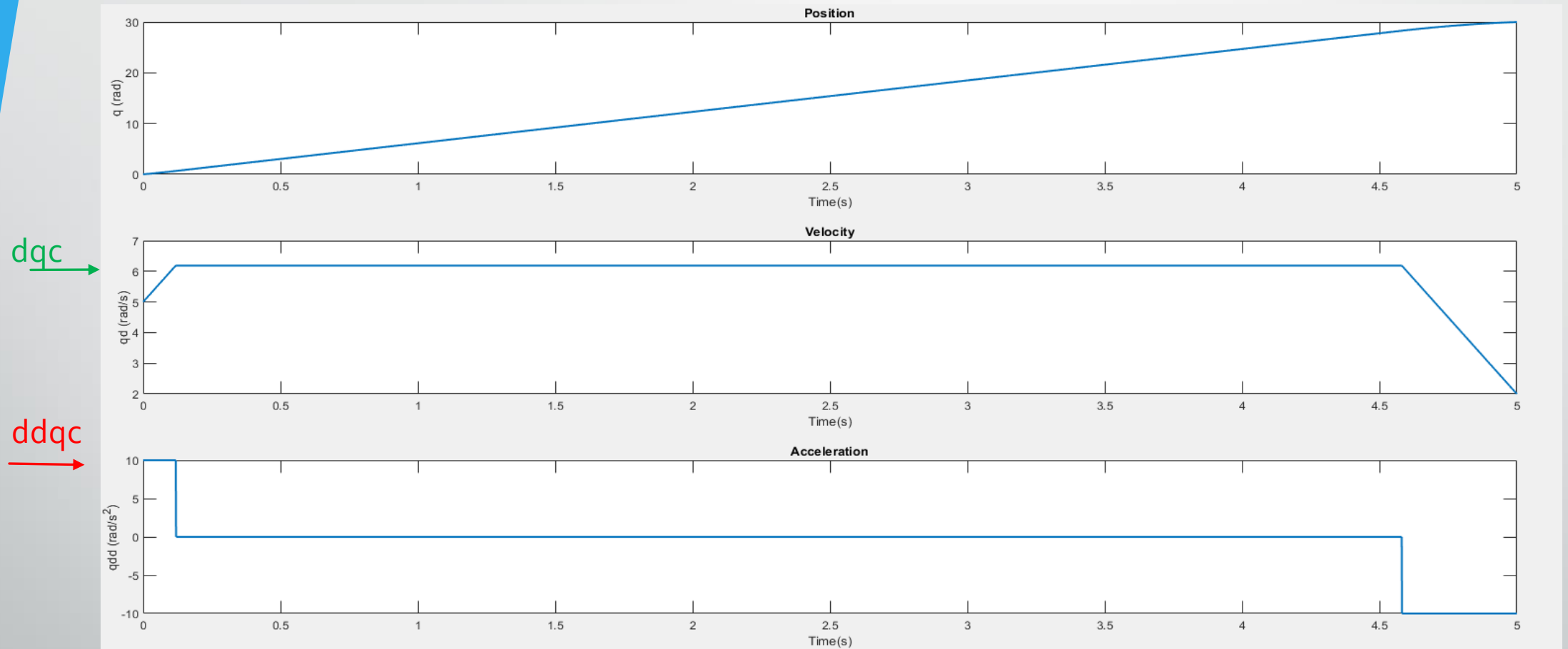
Symmetric trapezoidal trajectory – subcase 4



`[q, qd, qdd, T]= trapezoidalProfileSymmetric(tc, dqc, ddqc, ti, tf, qf, qi, Ts, subcase);`



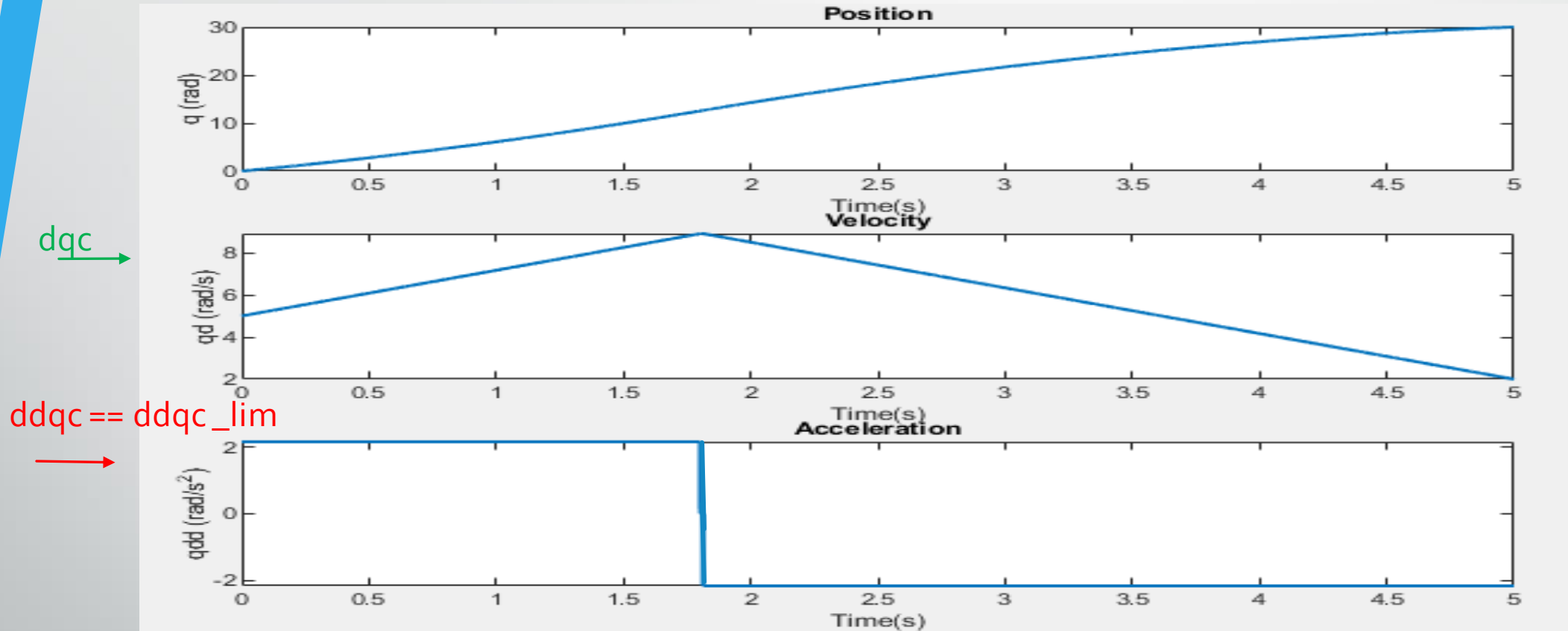
General trapezoidal trajectory – subcase 1



$[q, q\dot{d}, q\ddot{d}, T] = \text{trapezoidalProfileGeneral}(dq_c, ddq_c, t_i, t_f, q_f, q_i, dq_i, dq_f, T_s, \text{subcase});$



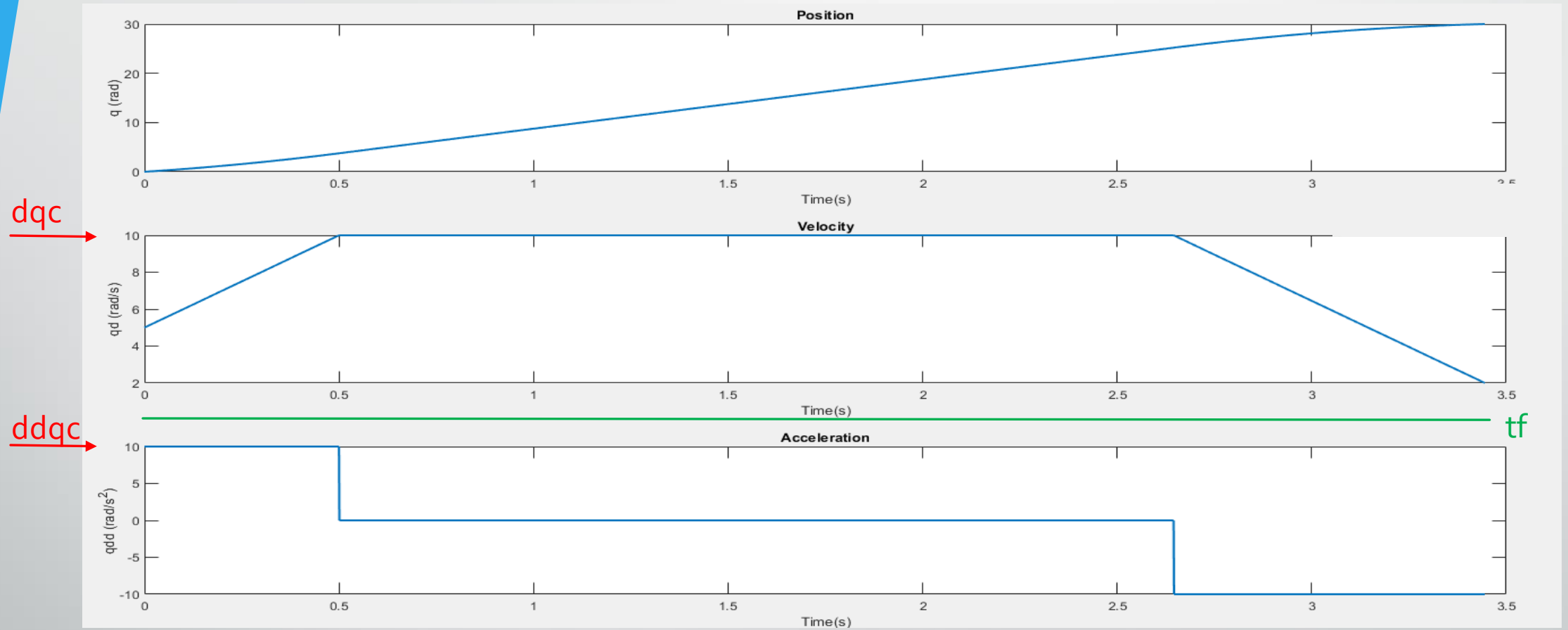
General trapezoidal trajectory – subcase 1



$[q, q\dot{d}, q\ddot{d}, T] = \text{trapezoidalProfileGeneral}(dq_c, ddq_c, t_i, t_f, q_f, q_i, dq_i, dq_f, T_s, \text{subcase});$



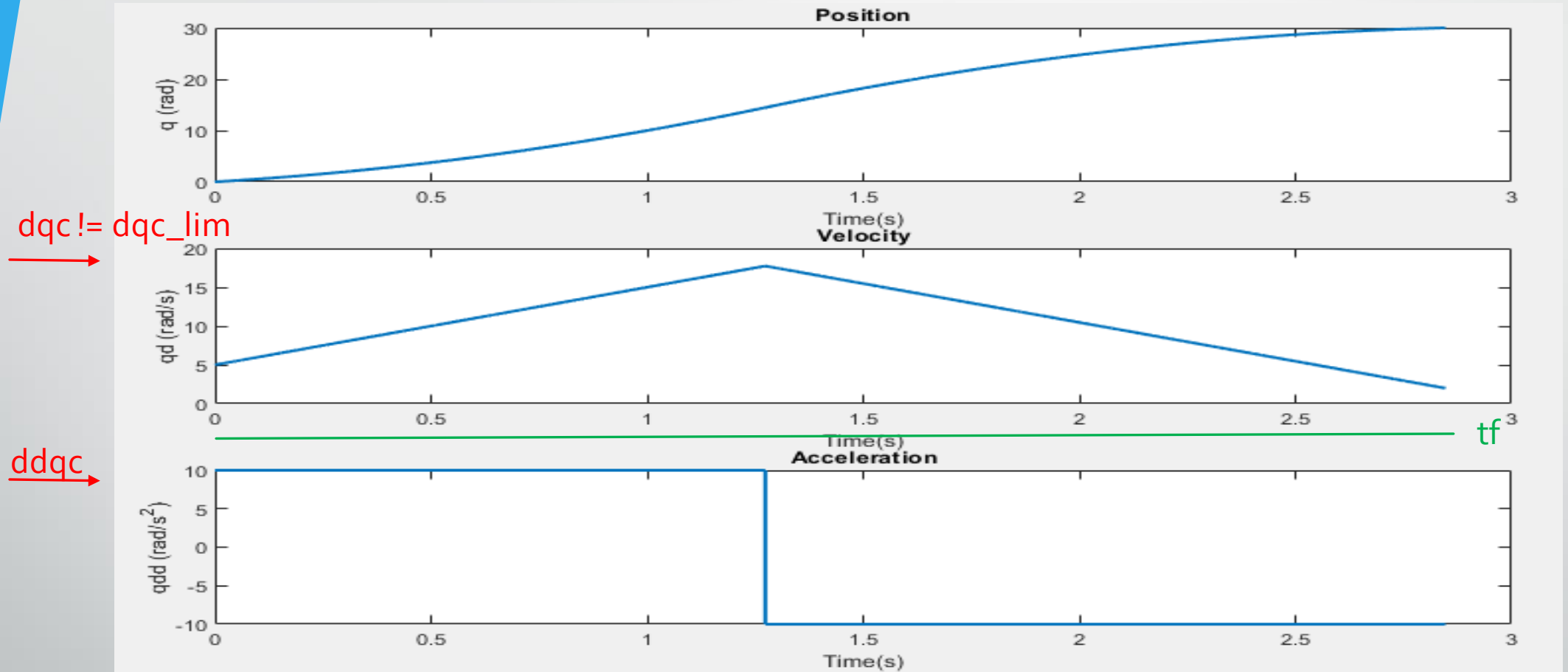
General trapezoidal trajectory – subcase 2



`[q, qd, qdd, T]= trapezoidalProfileGeneral(dqc, ddqc, ti, tf, qf, qi, dqi, dqf, Ts, subcase);`



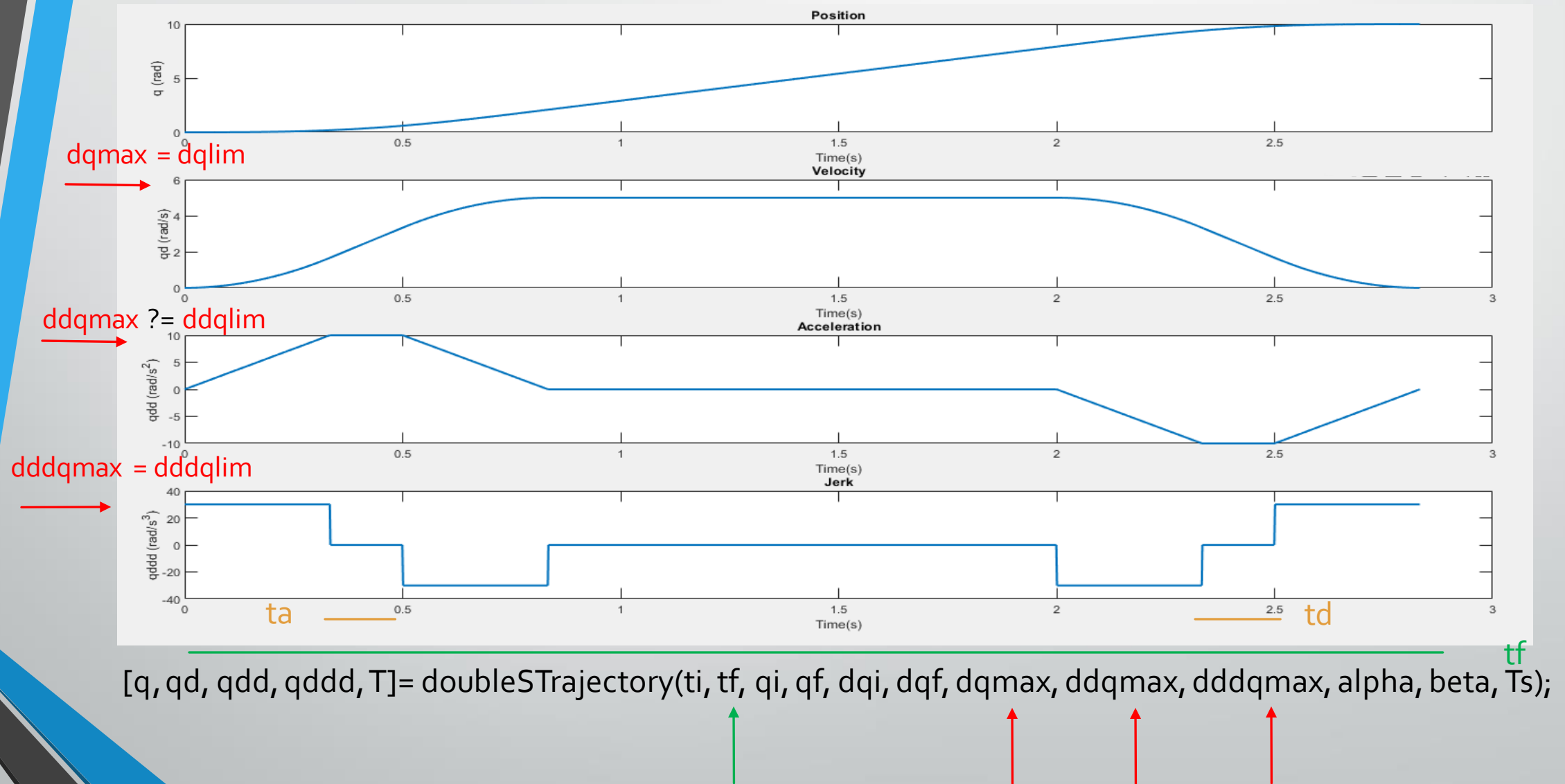
General trapezoidal trajectory – subcase 2



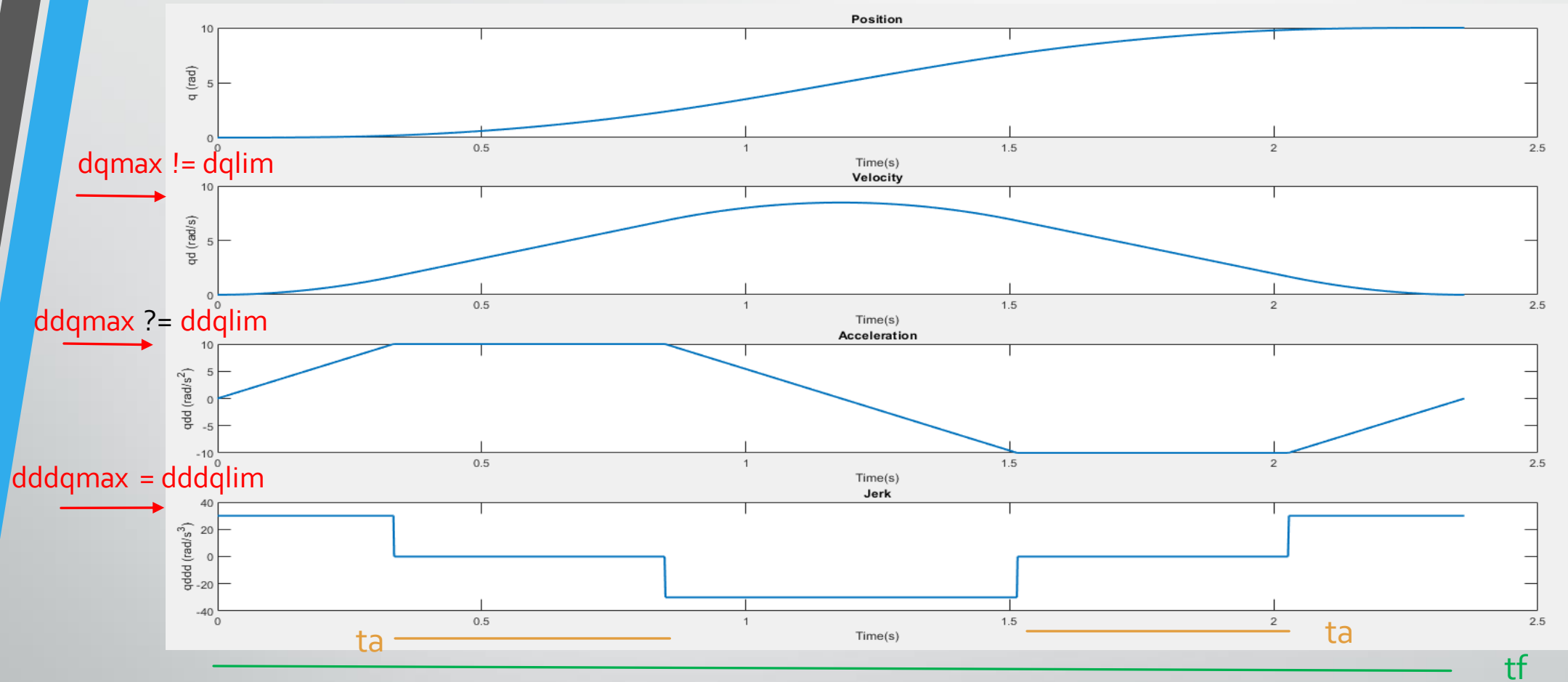
`[q, qd, qdd, T]= trapezoidalProfileGeneral(dqc, ddqc, ti, tf, qf, qi, dqi, dqf, Ts, subcase);`



Double S trajectory – subcase 1



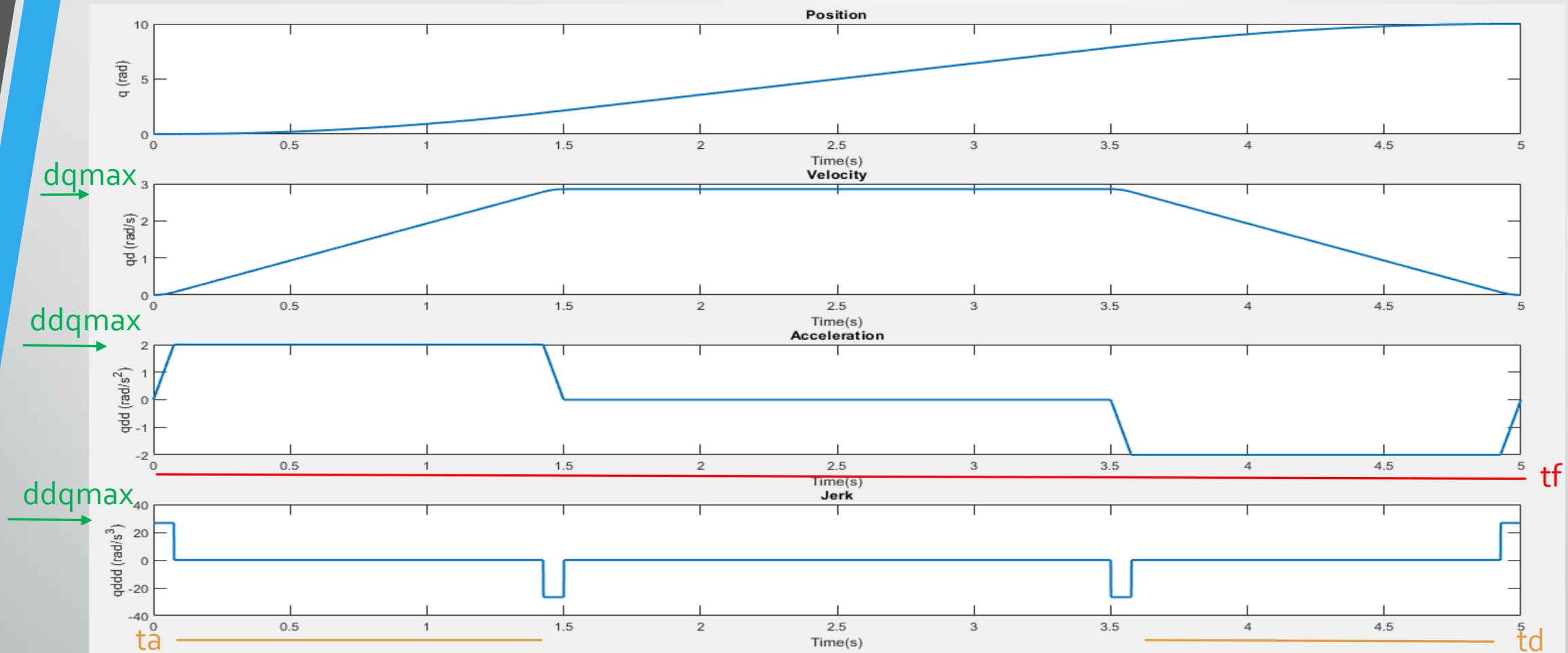
Double S trajectory – subcase 2



$[q, \dot{q}, \ddot{q}, \dddot{q}, T] = \text{doubleSTrajectory}(t_i, t_f, q_i, q_f, \dot{q}_i, \dot{q}_f, dq_{max}, ddq_{max}, dddq_{max}, \alpha, \beta, T_s);$



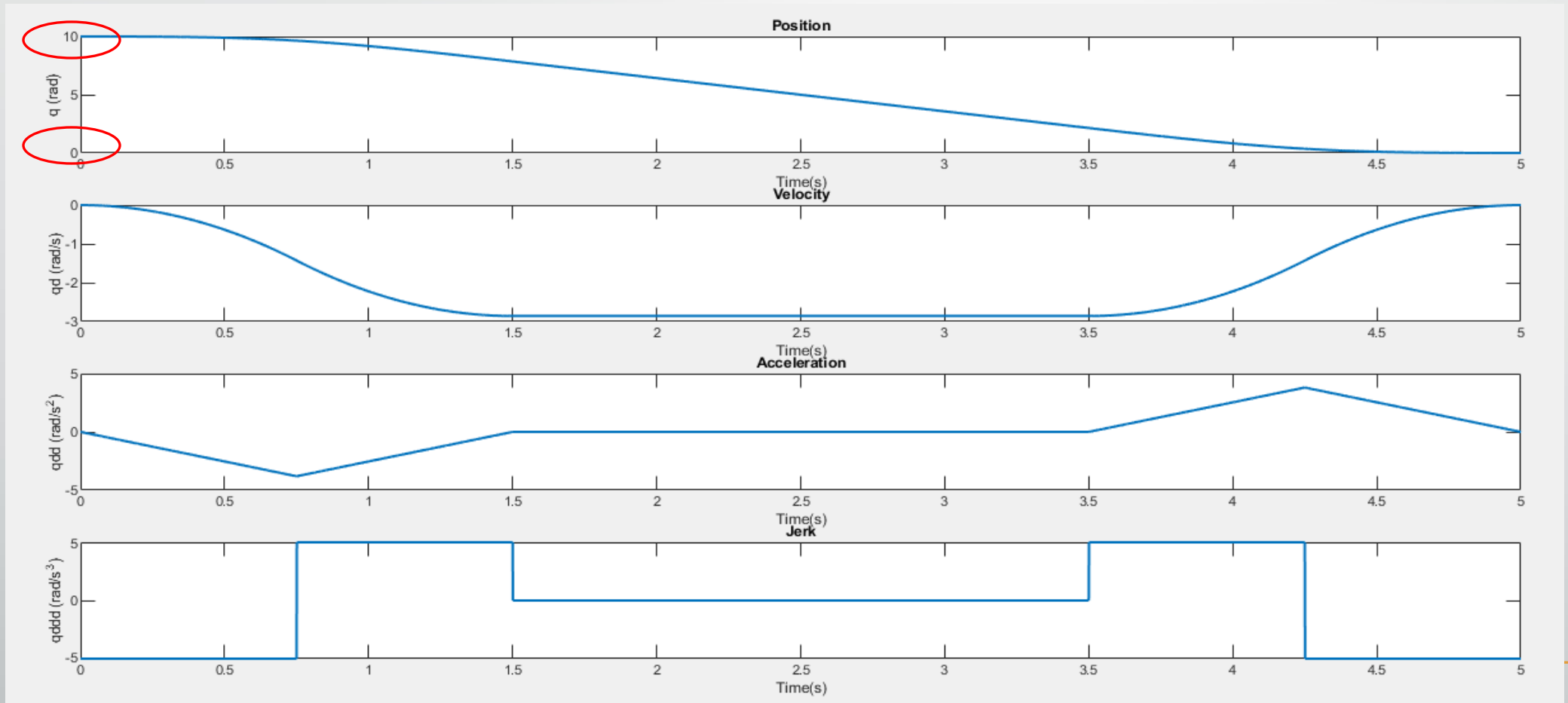
Double S trajectory – fixed duration



$[q, qd, qdd, qddd, T] = \text{doubleSTrajectory}(t_i, t_f, q_i, q_f, dq_i, dq_f, dq_{max}, ddq_{max}, dddq_{max}, \alpha, \beta, T_s);$

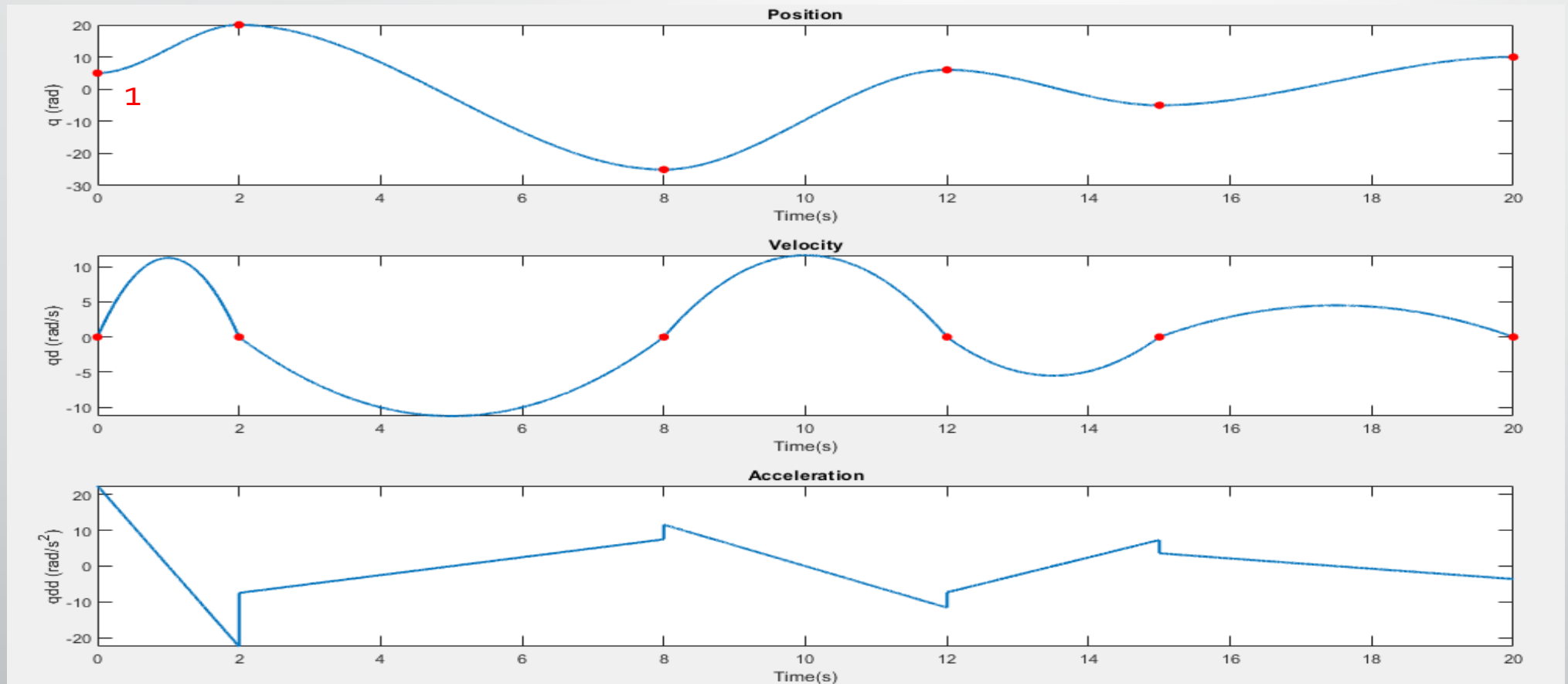


If $q_f < q_i$?



$[q_i, q_f, dq_i, dq_f] = \text{changeSign}(q_i, q_f, dq_i, dq_f);$

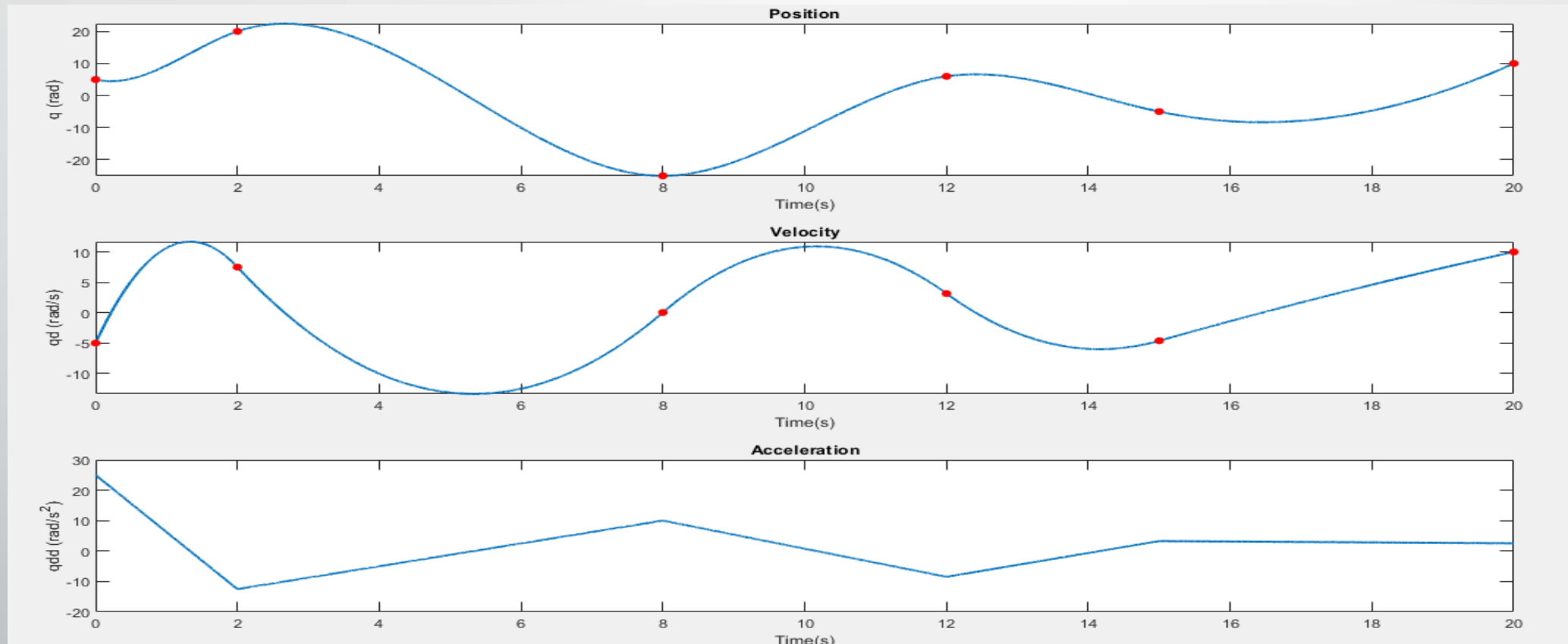
Computed velocities at path points and imposed velocity at initial/final points



$[q, q\dot{d}, q\ddot{d}, dqk, T] = \text{computedVelocities}(qk, tk, k, dq_i, dq_f, Ts);$



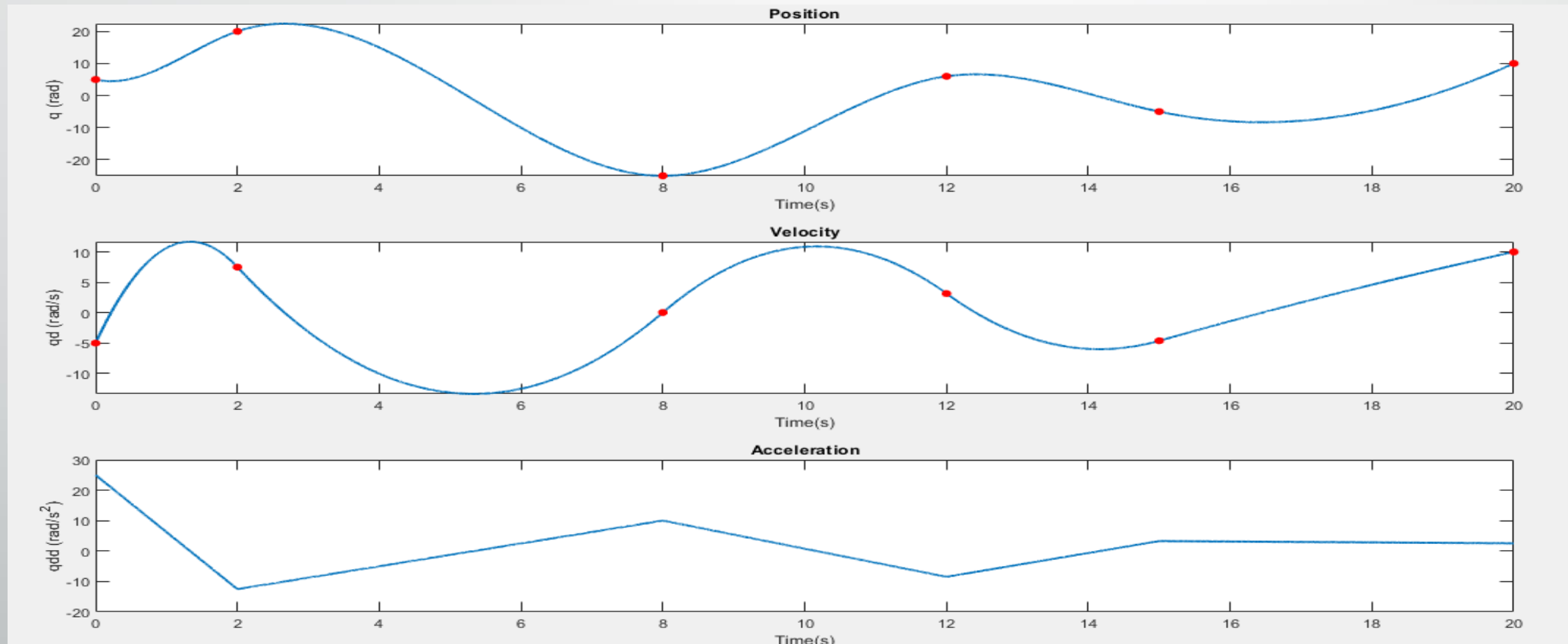
Continuous accelerations at path points and imposed velocity at initial/final points



$[q, q\dot{d}, q\ddot{d}, T, dqk] = \text{continuousAccelerations}(qk, tk, k, dq_i, dq_f, T_s);$



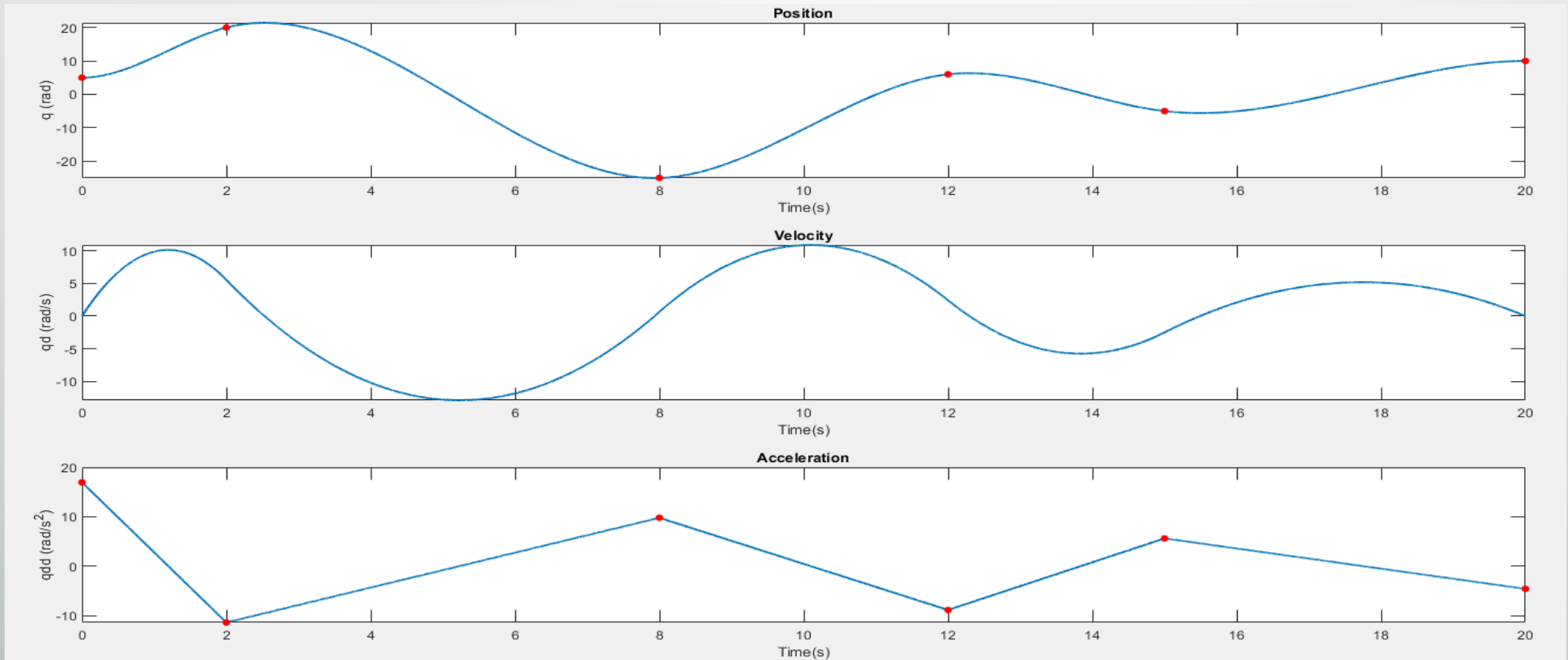
Continuous accelerations at path points and imposed velocity at initial/final points



$[q, q\dot{d}, q\ddot{d}, dqk\ T] = \text{continuousAccelerationsThomas}(q_k, t_k, k, dq_i, dq_f, T_s);$



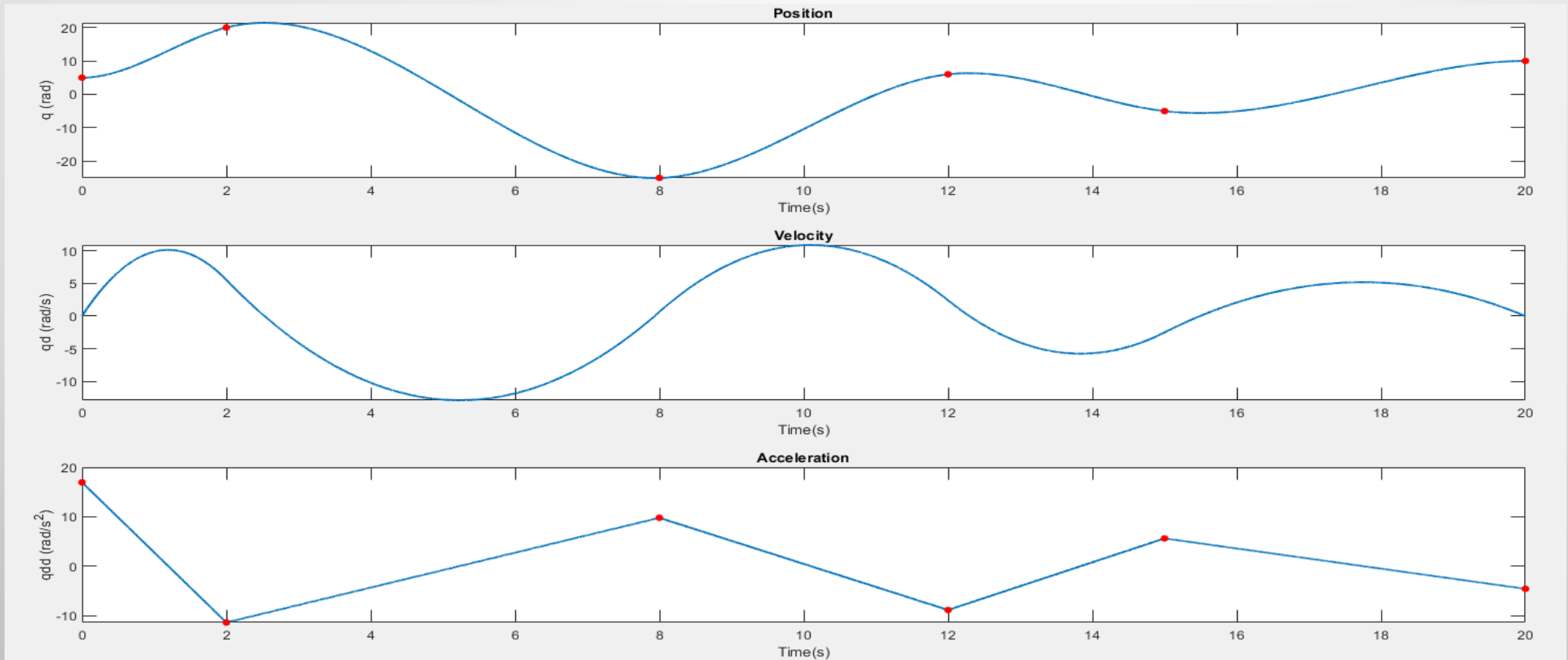
Cubic splines based on the accelerations with imposed initial/final velocities



$[q, q\dot{d}, q\ddot{d}, \ddot{d}q_k, T] = \text{continuousVelocities}(q_k, dq_i, dq_f, t_k, k, T_s);$



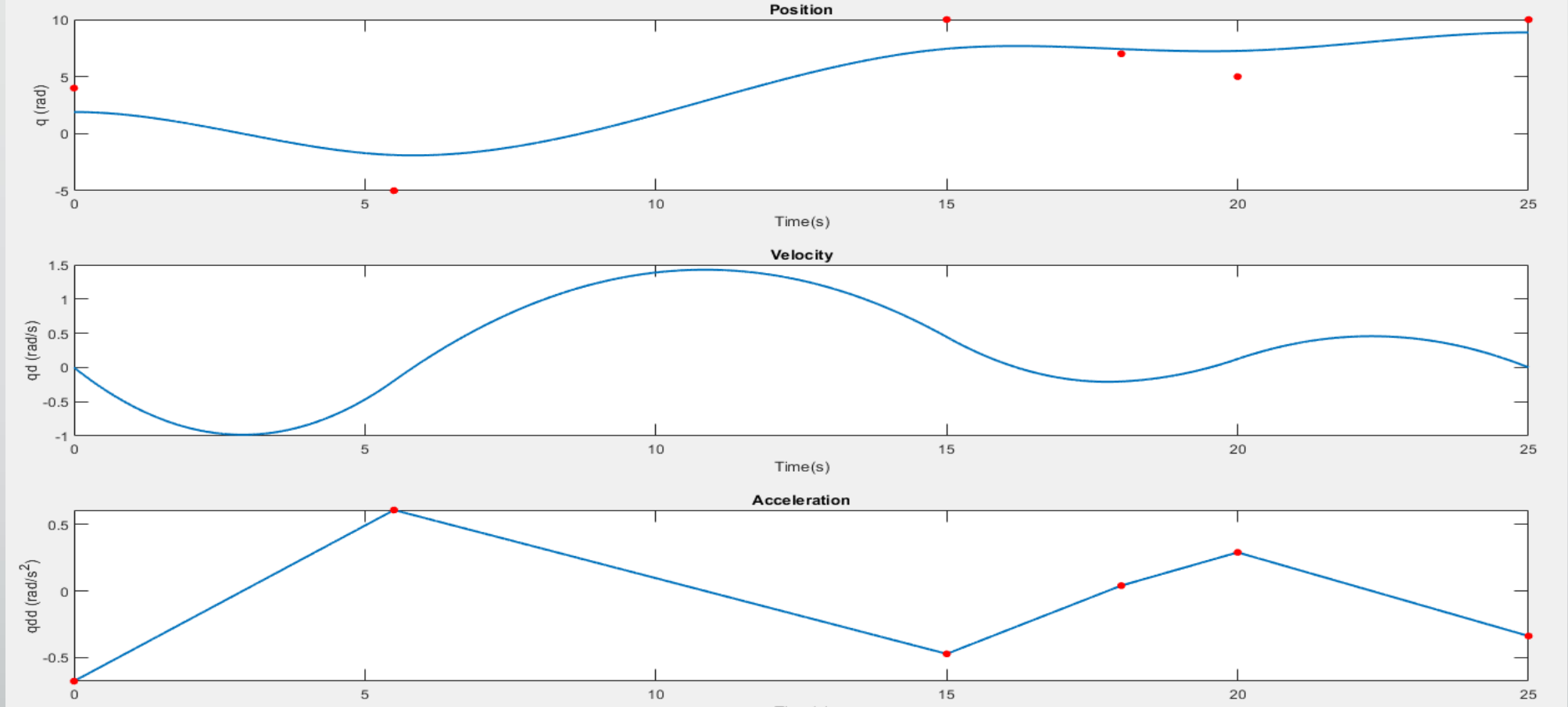
Cubic splines based on the accelerations with imposed initial/final velocities



$[q, q\dot{d}, q\ddot{d}, \ddot{d}q, T] = \text{continuousVelocitiesThomas}(q_k, t_k, k, d\dot{q}_i, d\dot{q}_f, T_s);$



Smoothing cubic splines



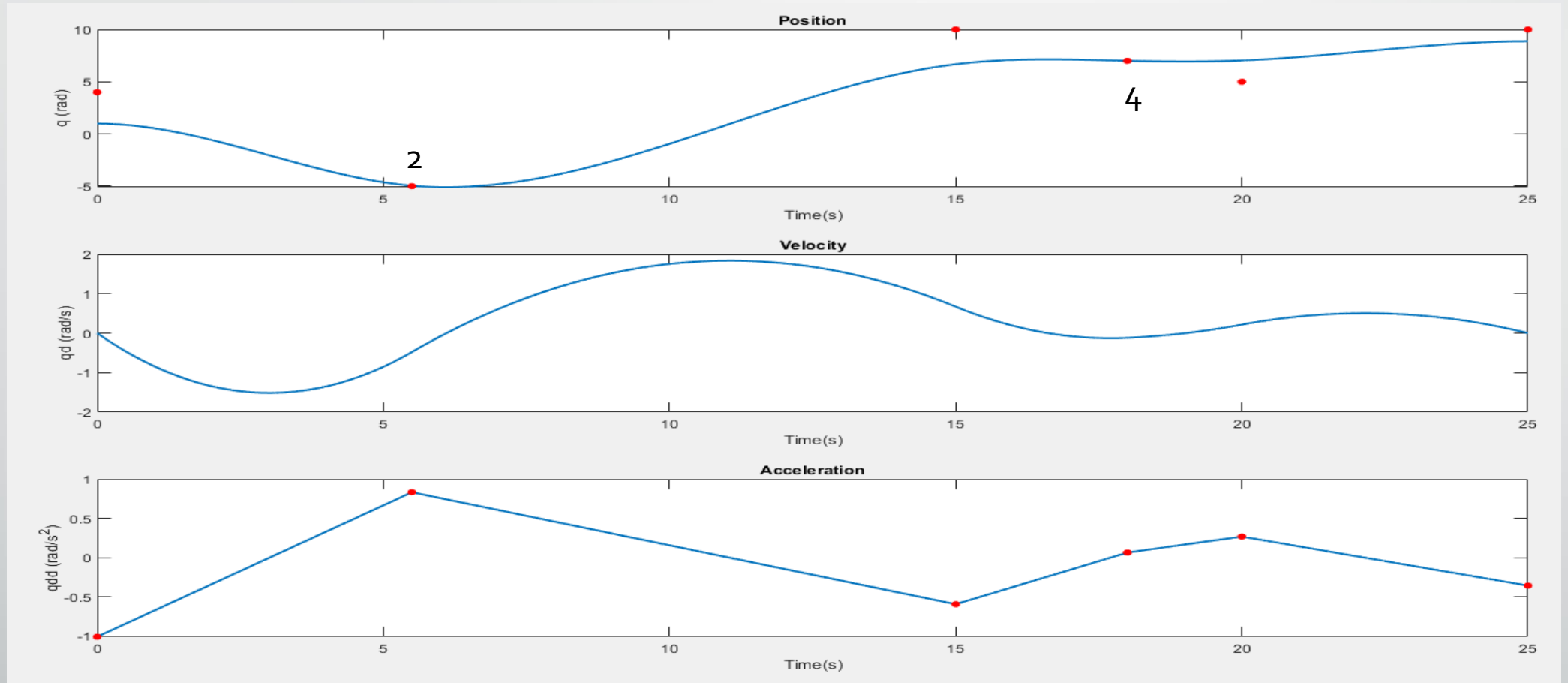
```
[q, qd, qdd, dds, T] = smoothingSplines(qk, tk, k, Ts, W, lambda);
```

```
W = diag([1, 1, 1, 1, 1, 1]);
```

```
mu = 0.1;
```



Smoothing cubic splines



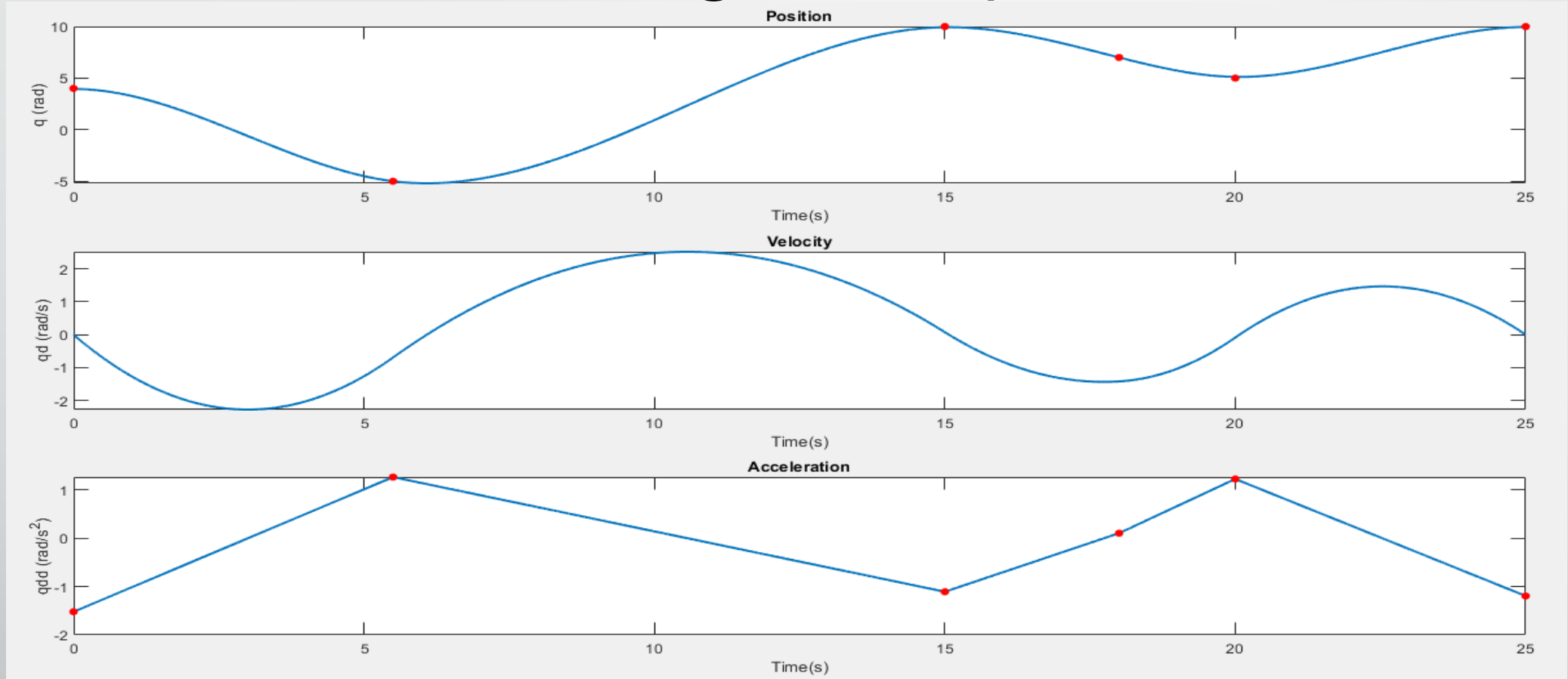
```
[q, qd, qdd, dds, T] = smoothingSplines(qk, tk, k, Ts, W, lambda);
```

```
W = diag([1, 100, 1, 100, 1, 1]);
```

```
mu = 0.1;
```



Smoothing cubic splines



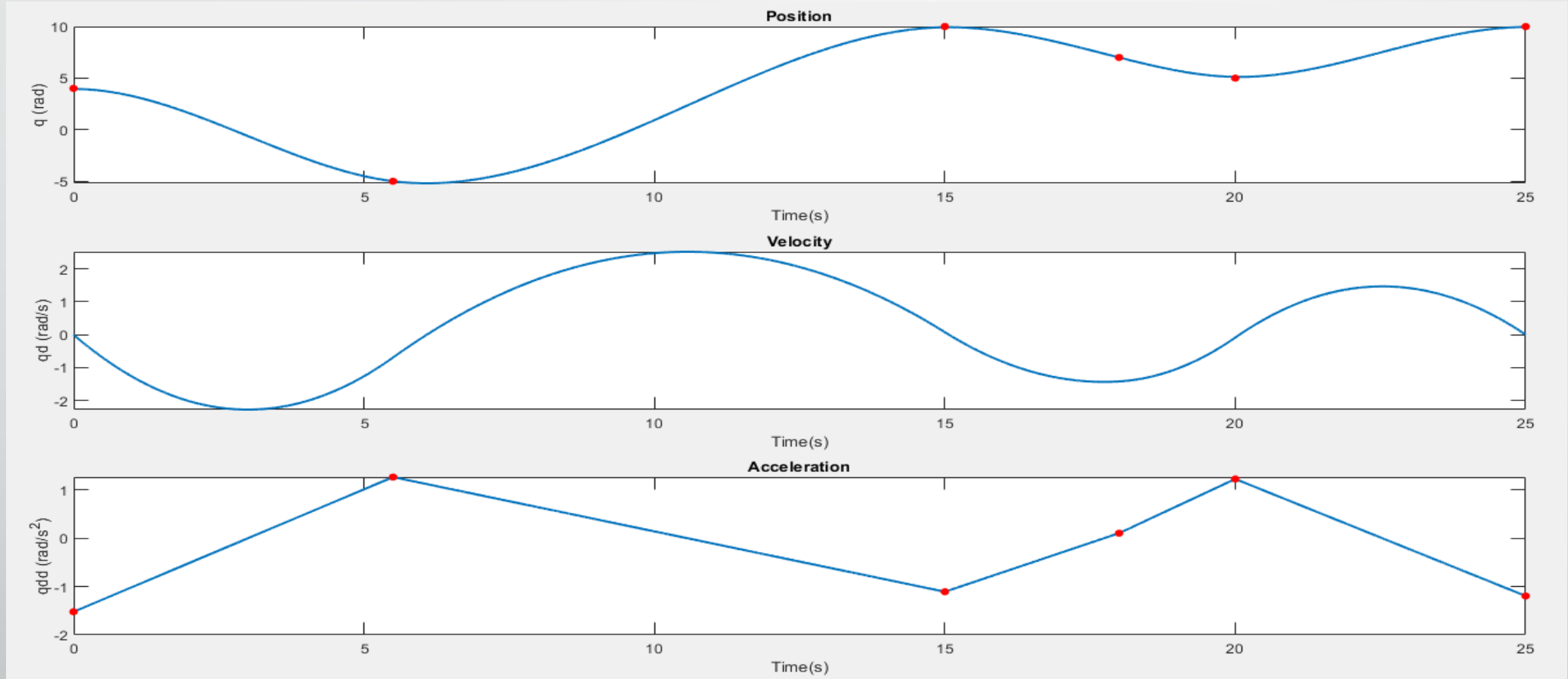
```
[q, qd, qdd, dds, T] = smoothingSplines(qk, tk, k, Ts, W, lambda);
```

```
W = diag([1, 100, 1, 100, 1, 1]);
```

```
mu = 0.9;
```



Smoothing cubic splines



```
[q, qd, qdd, dds, T] = smoothingSplines(qk, tk, k, Ts, W, lambda);
```

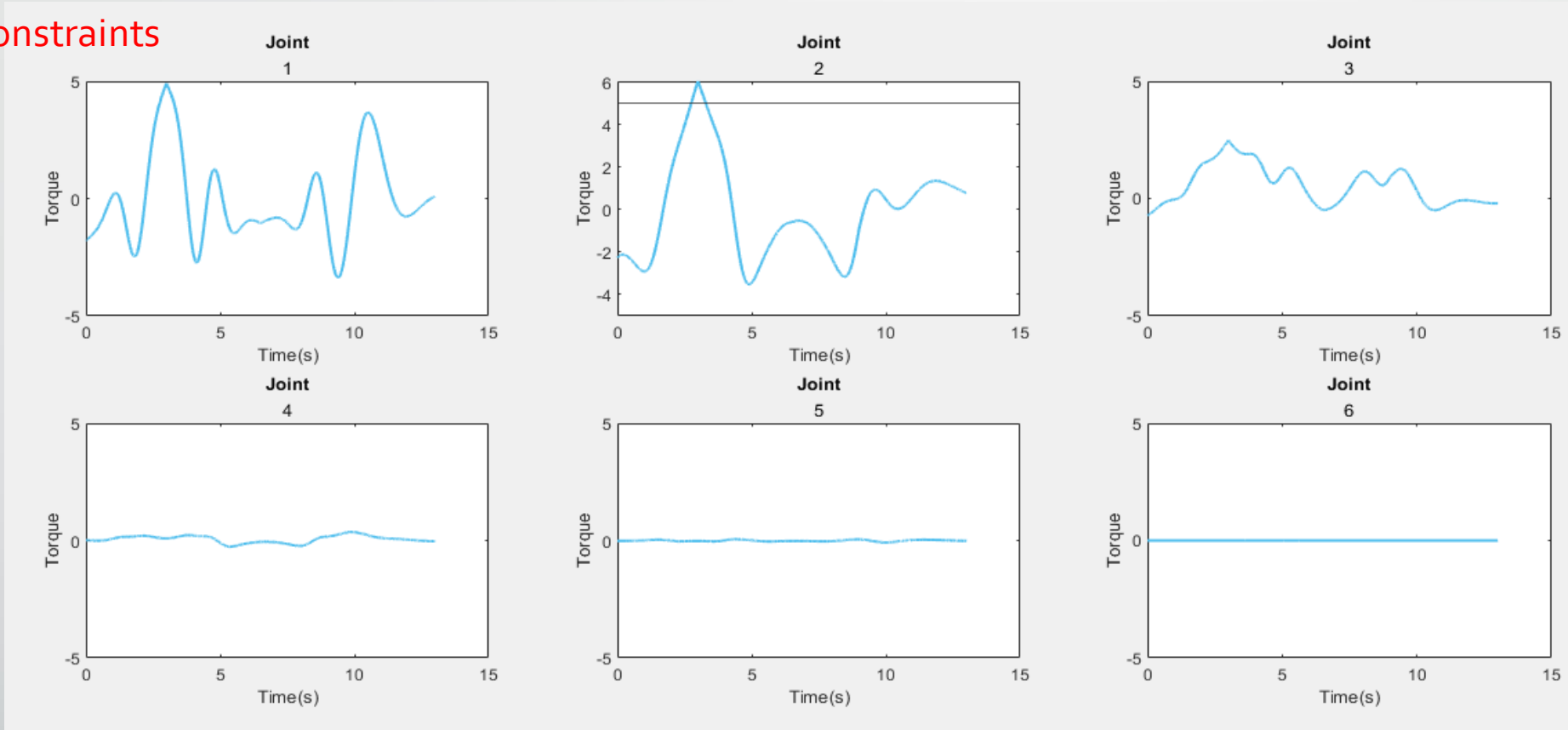
```
W = diag([1, 1, 1, 1, 1, 1]);
```

```
mu = 0.9;
```



Model-based Trajectory

tauConstraints

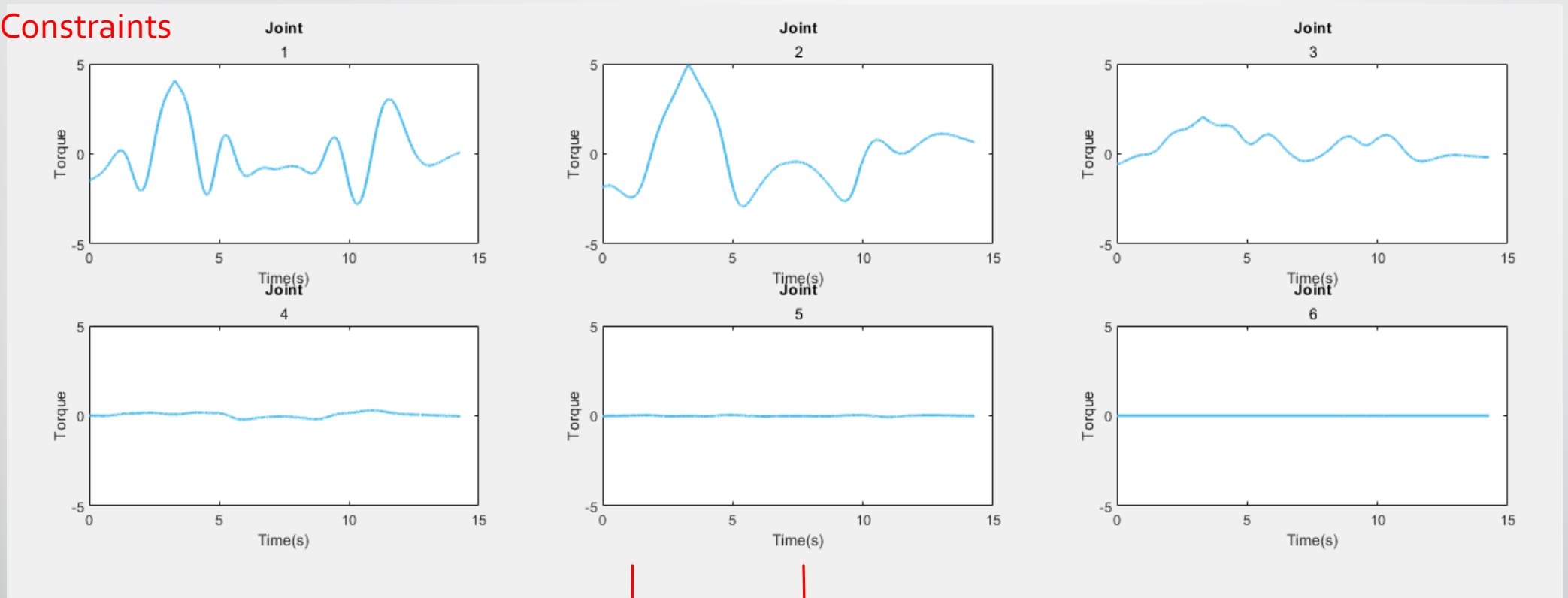


```
[q, dq, ddq, dqk, T_series] = continuousAccelerationsThomas(qk(i,:), tk, k(1,i), dq(i, 1), dqf(i, 1), Ts);
```

```
tauNoG(:,i) = inv_dyn_recursive_NewtonEulero(dh, DataPositions(:,i), DataVelocities(:,i), DataAccelerations(:,i), gravity) - g(:,i);
```

Model-based Trajectory

tauConstraints

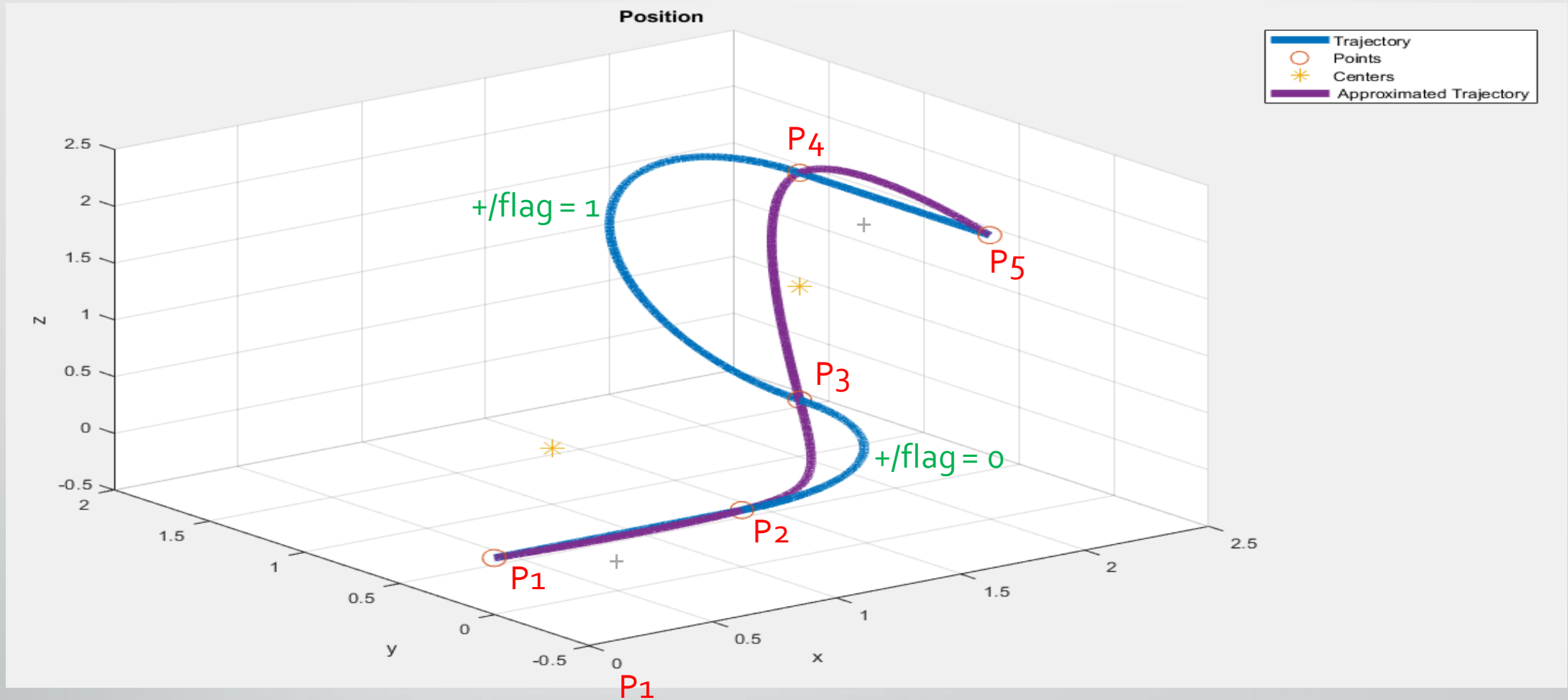


```
lambda = findLambda(tau, tauConstraints)
```

```
T = T/lambda; DataVelocities = DataVelocities*lambda;
```

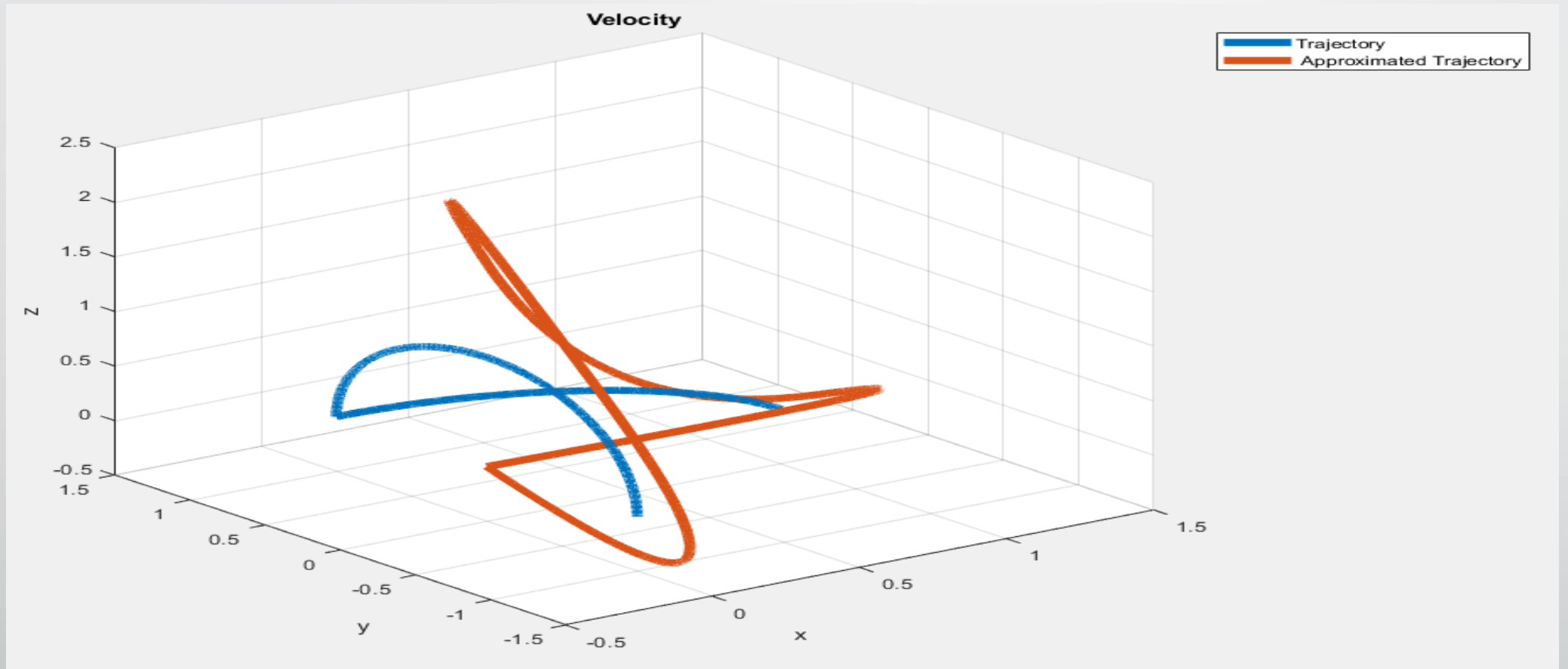
```
DataAccelerations = DataAccelerations*lambda^2;
```

3D trajectory



- + $[P, DP, DDP, DDDP, T, p \text{ dp}, ddp] = \text{linearMotion}(pi, pf, Ts, P, DP, DDP, DDDP, T);$
- + $[P, DP, DDP, DDDP, T, p, dp, ddp] = \text{circularMotion}(pi, pf, Ts, c, P, DP, DDP, DDDP, T, \text{flag});$
- $[Q, QD, QDD, T] = \text{cartesianApproximation}(Pg)$

3D trajectory

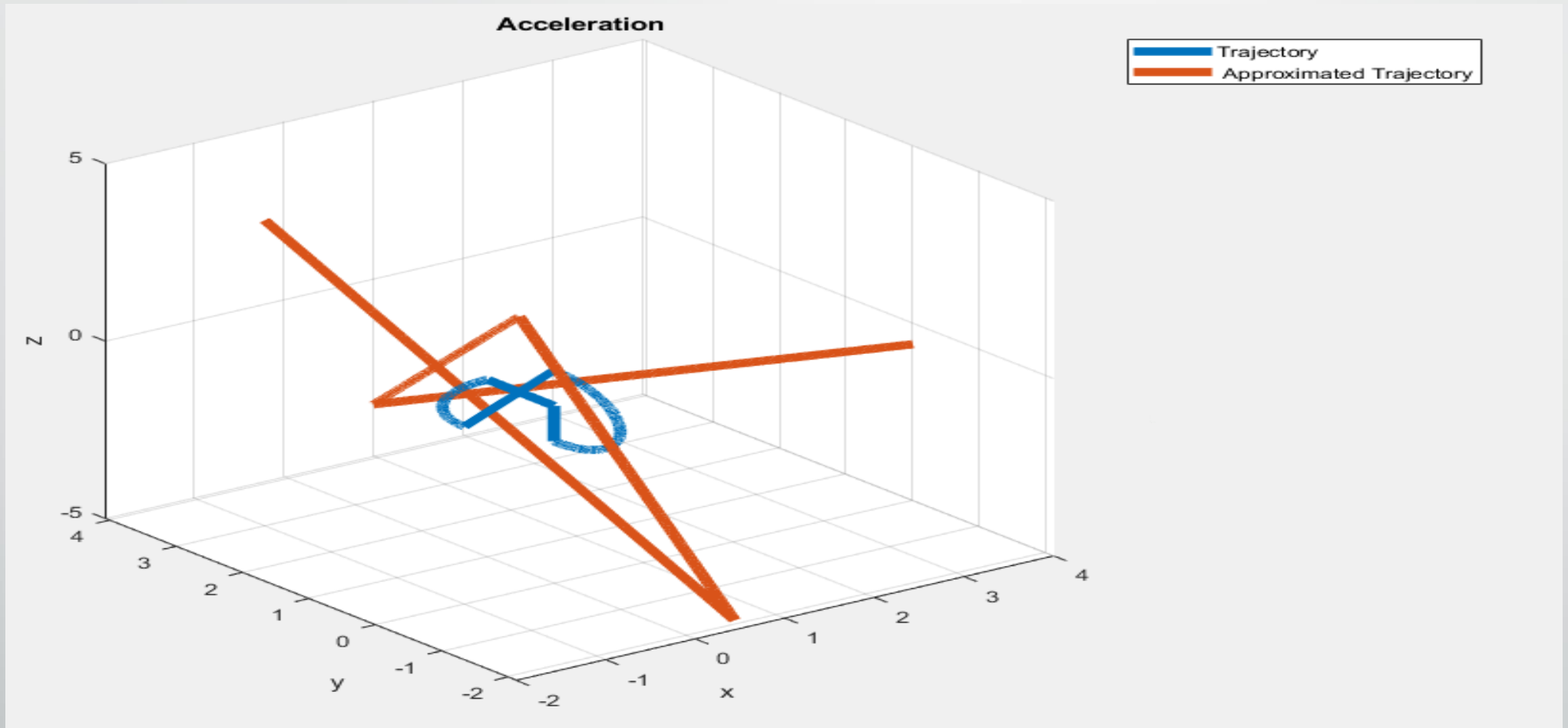


```
[P, DP, DDP, DDDP, T, p dp, ddp] = linearMotion(pi, pf, Ts, P, DP, DDP, DDDP, T);
```

```
[P, DP, DDP, DDDP, T, p, dp, ddp] = circularMotion(pi, pf, Ts, c, P, DP, DDP, DDDP, T, flag);
```

```
[Q, QD, QDD, T] = cartesianApproximation(Pg)
```


3D trajectory

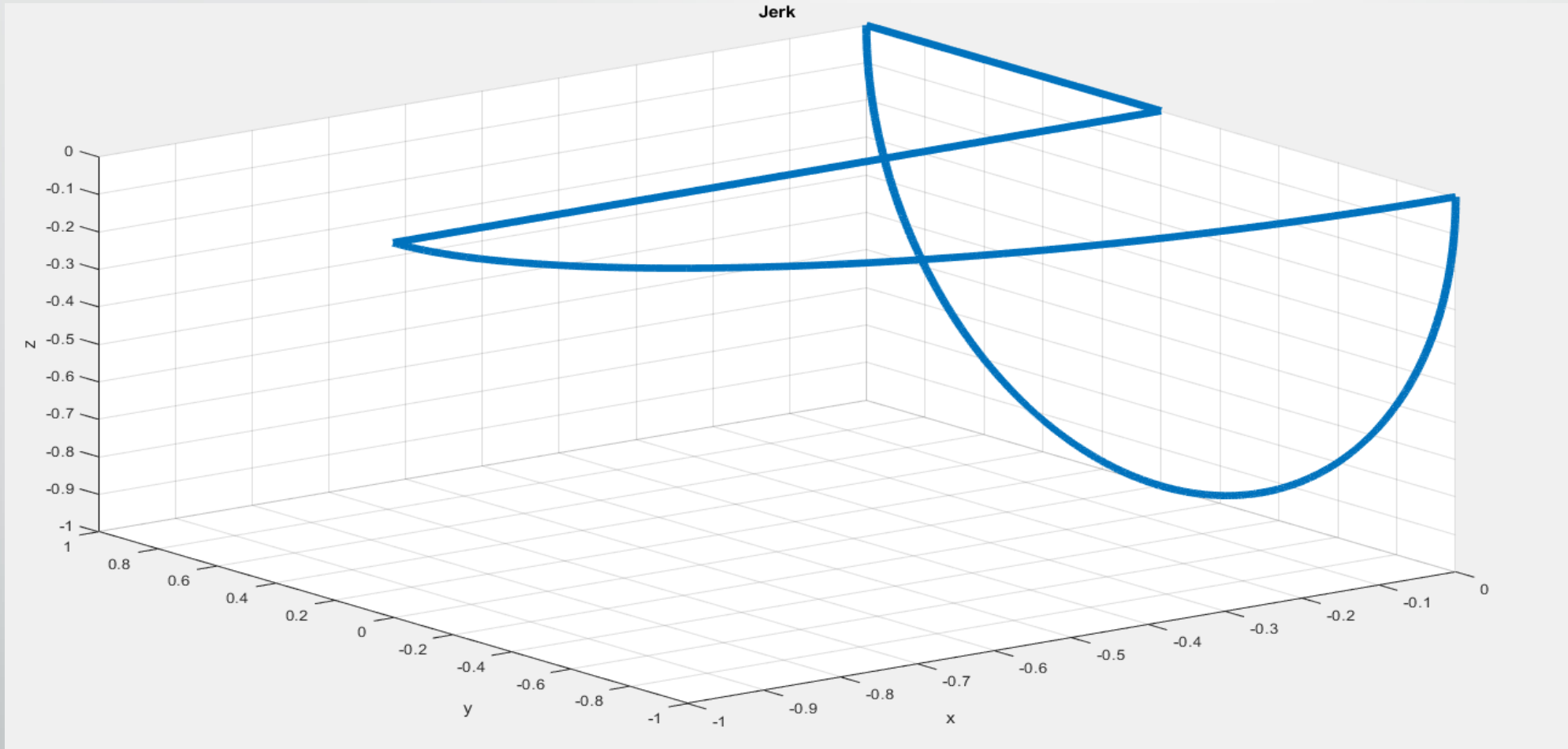


```
[P, DP, DDP, DDDP, T, p dp, ddp] = linearMotion(pi, pf, Ts, P, DP, DDP, DDDP, T);
```

```
[P, DP, DDP, DDDP, T, p, dp, ddp] = circularMotion(pi, pf, Ts, c, P, DP, DDP, DDDP, T, flag);
```

```
[Q, QD, QDD, T] = cartesianApproximation(Pg)
```

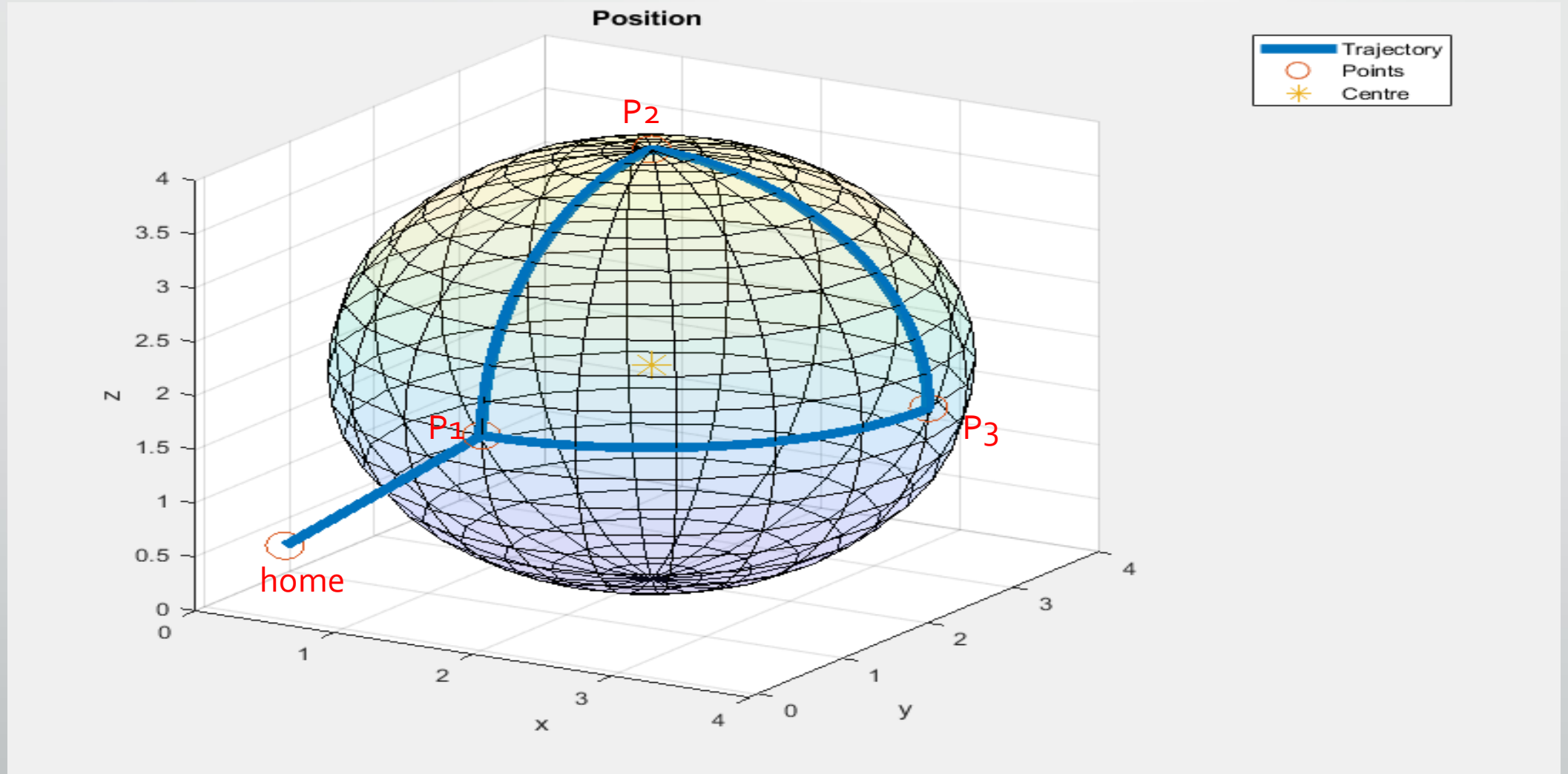
3D trajectory



```
[P, DP, DDP, DDDP, T, p dp, ddp] = linearMotion(pi, pf, Ts, P, DP, DDP, DDDP, T);
```

```
[P, DP, DDP, DDDP, T, p, dp, ddp] = circularMotion(pi, pf, Ts, c, P, DP, DDP, DDDP, T, flag);
```

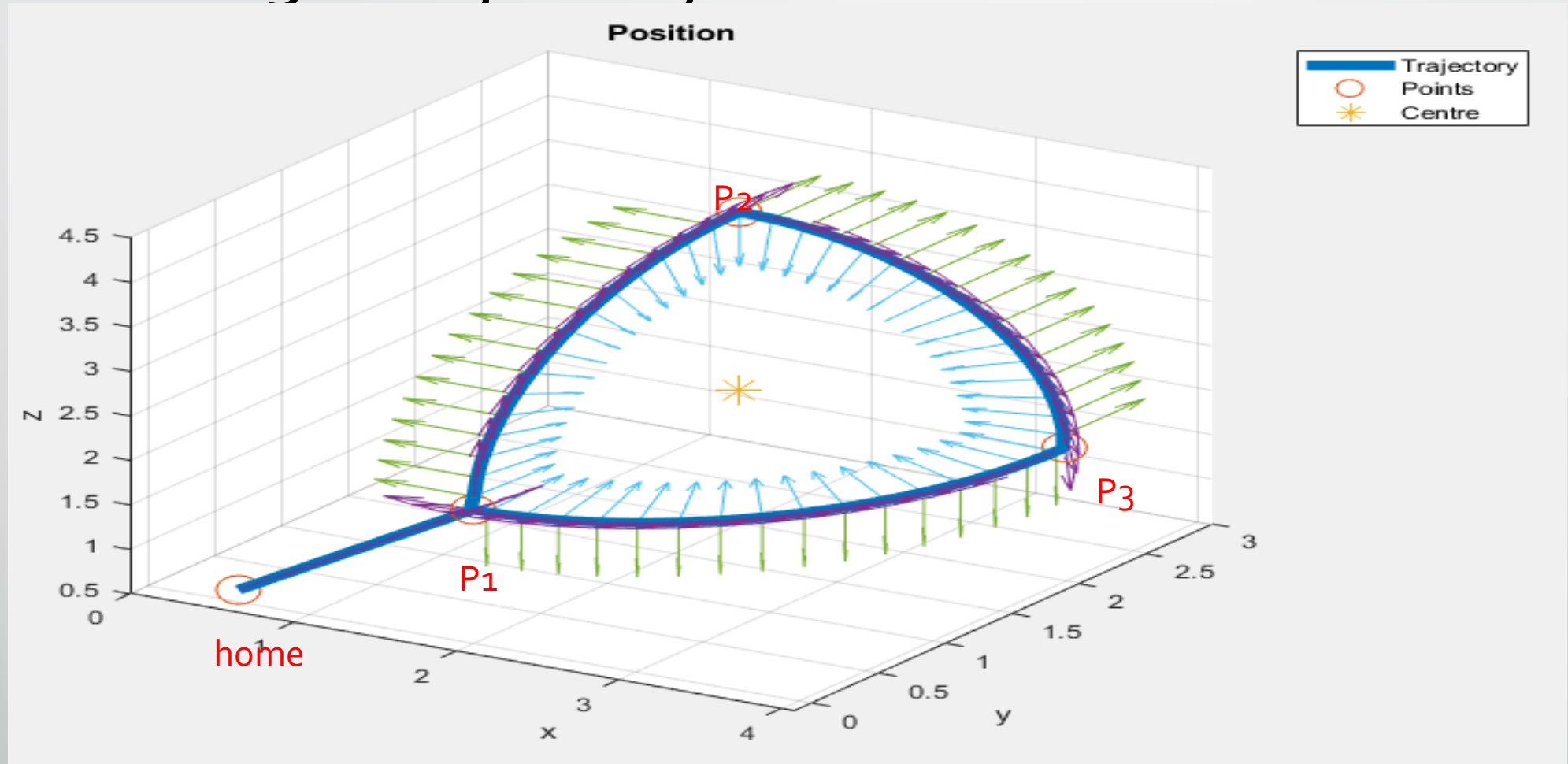
3D trajectory – Position



$[P_{\text{tilde}}, D_{\text{Ptilde}}, DD_{\text{Ptilde}}, T] = \text{linearTilde}(x_0(1:3), p_1, T_s, P_{\text{tilde}}, D_{\text{Ptilde}}, DD_{\text{Ptilde}}, T, t_i, t_f);$

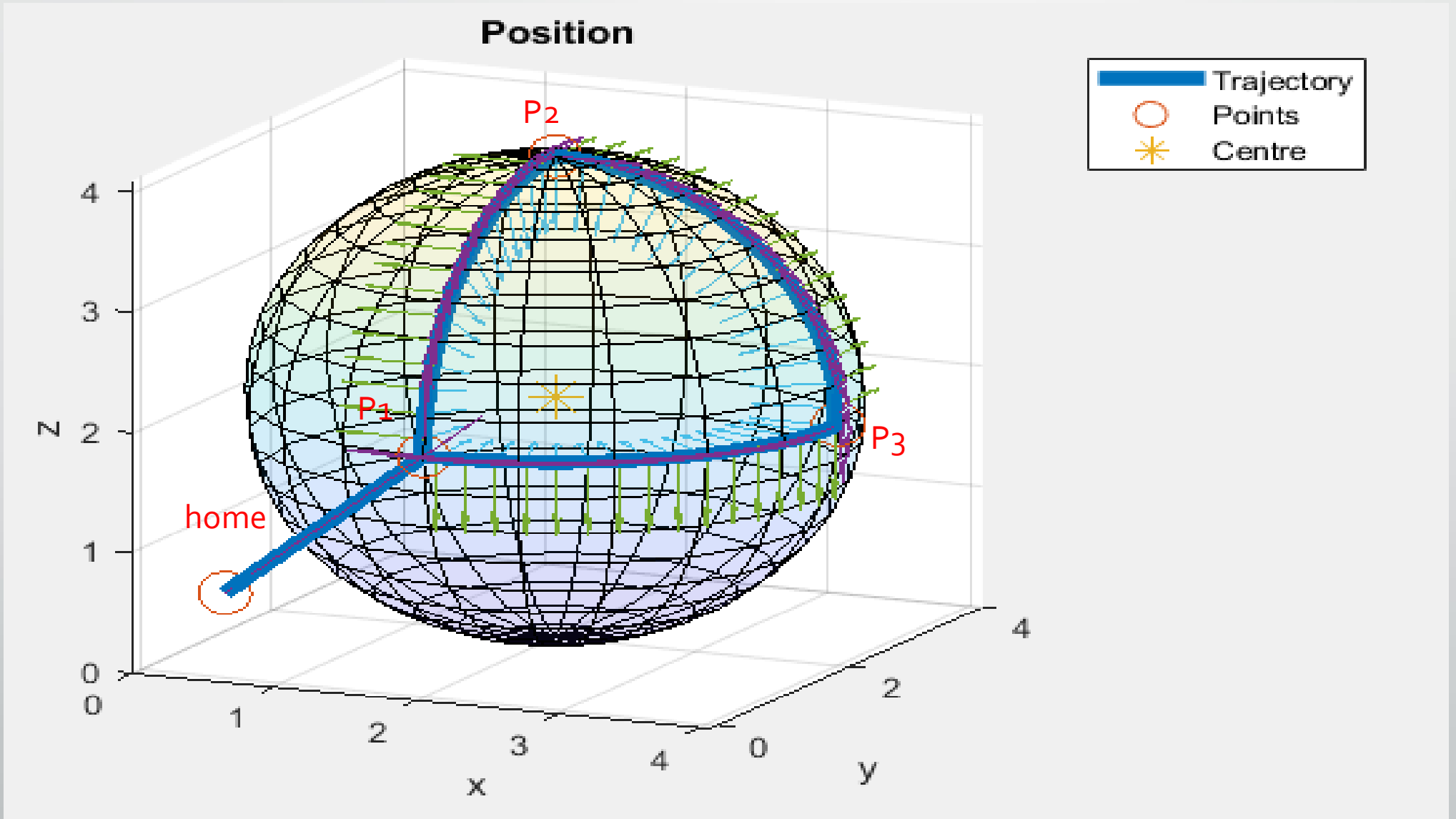
$[P_{\text{tilde}}, D_{\text{Ptilde}}, DD_{\text{Ptilde}}, T] = \text{circularTilde}(p_2, p_3, T_s, p_0', P_{\text{tilde}}, D_{\text{Ptilde}}, DD_{\text{Ptilde}}, T, \text{flag}, t_i, t_f);$

3D trajectory – EE Orientation

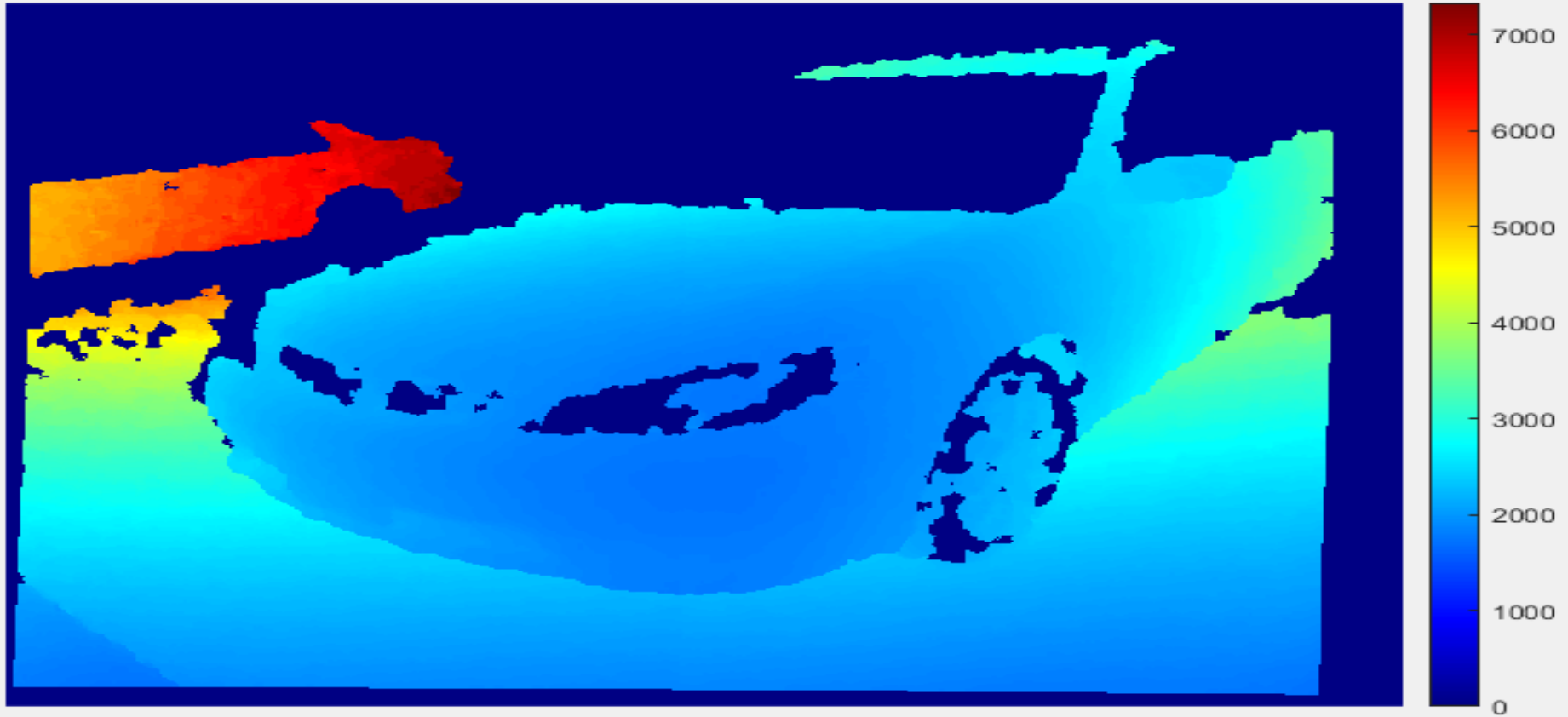


```
[Otilde, Dtilde, DDOtilde, TO, O_EE_t, O_EE_n, O_EE_b] = FrenetFrame(p, dp, ddp, ti, tf, p1, p2 ...  
Otilde, Dtilde, DDOtilde, TO, O_EE_t, O_EE_n, O_EE_b, Ts);
```

```
[Otilde, Dtilde, DDOtilde, TO] = EEOrientation(PHI_i, PHI_f, Ts, Otilde, Dtilde, DDOtilde, TO, ti, tf...  
pi, pf);
```

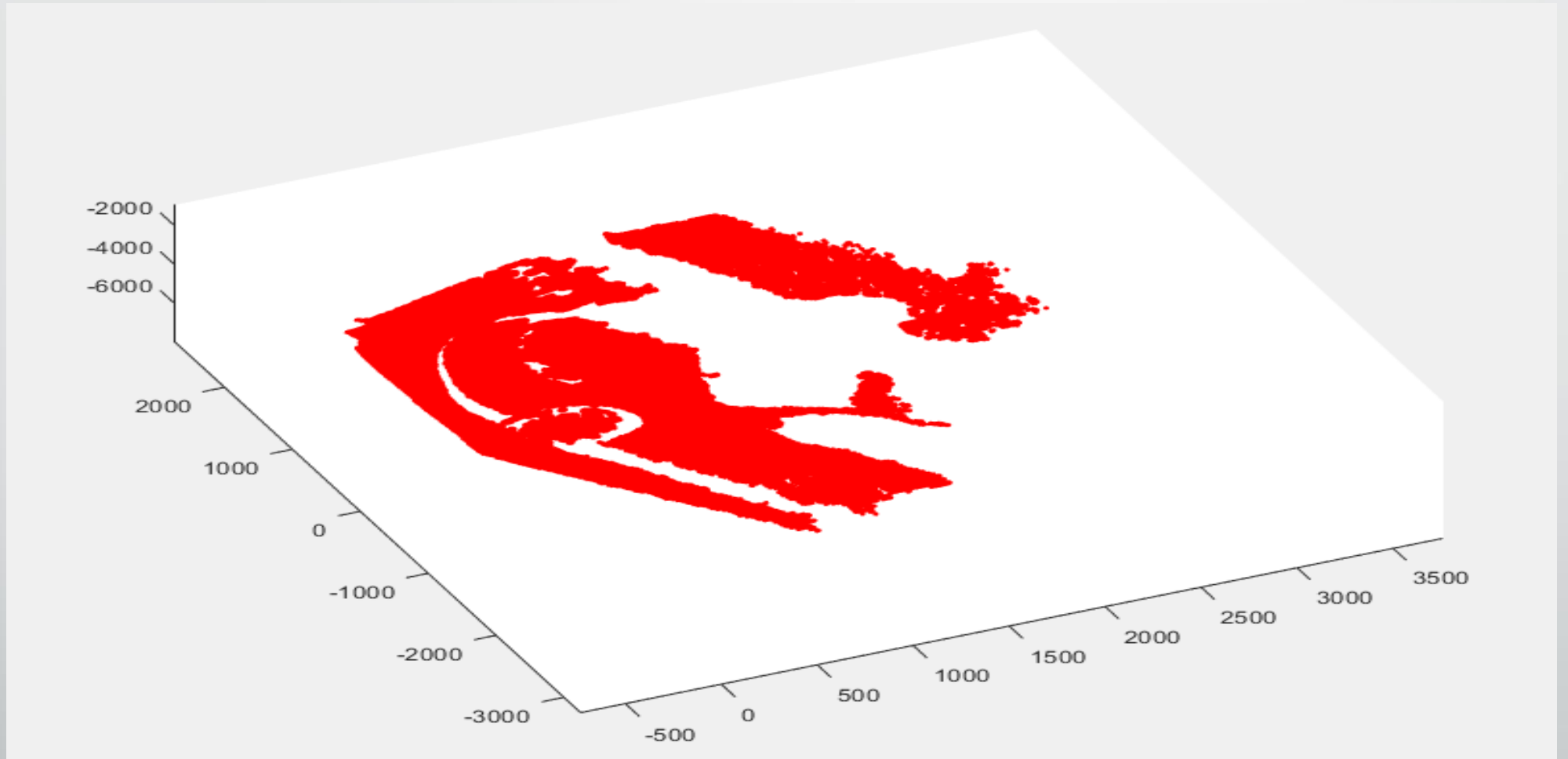


3D Acquisition – Depth image

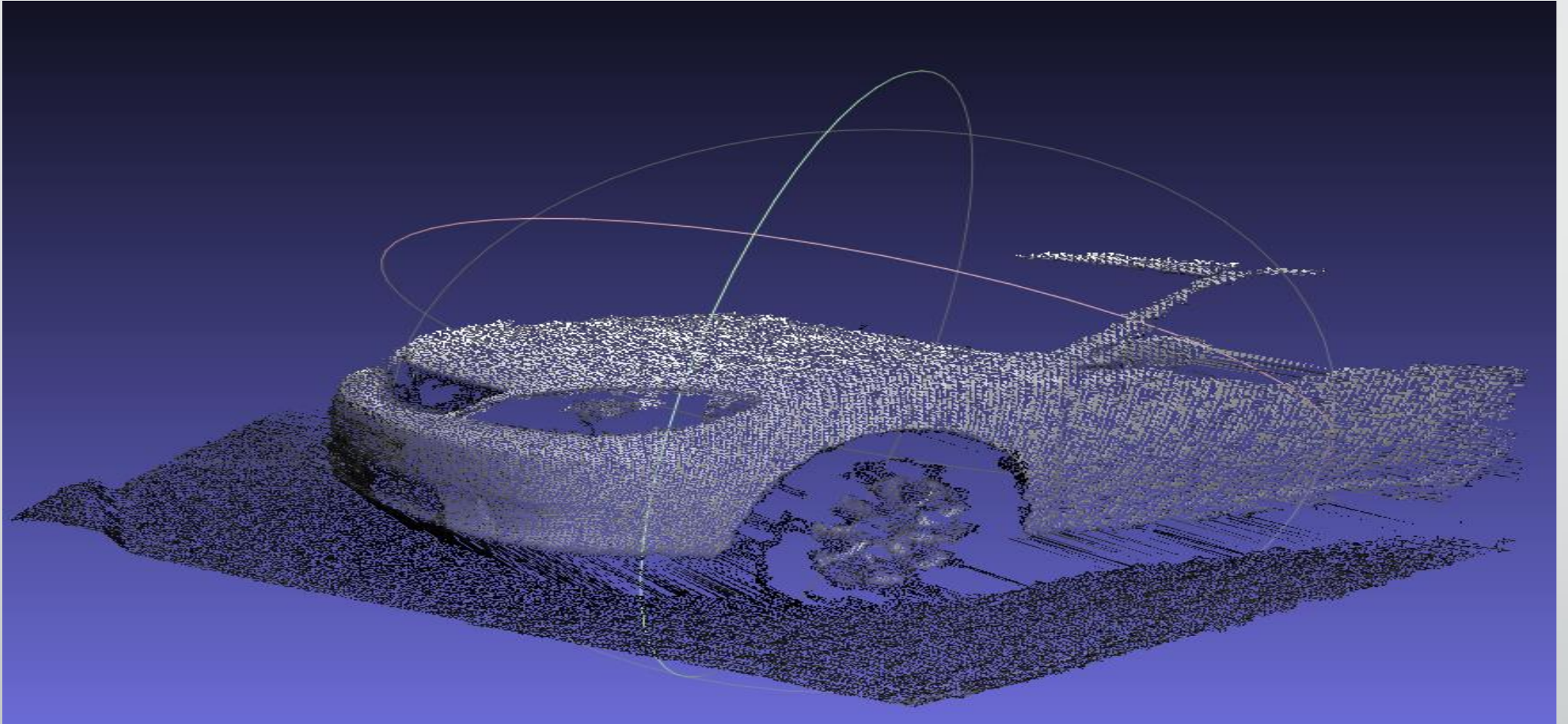


```
imshow(depth,[min(depth,[],'all'),max(depth,[],'all')]);  
colormap jet; colorbar; colormap;
```

3D Acquisition – Cloud Points



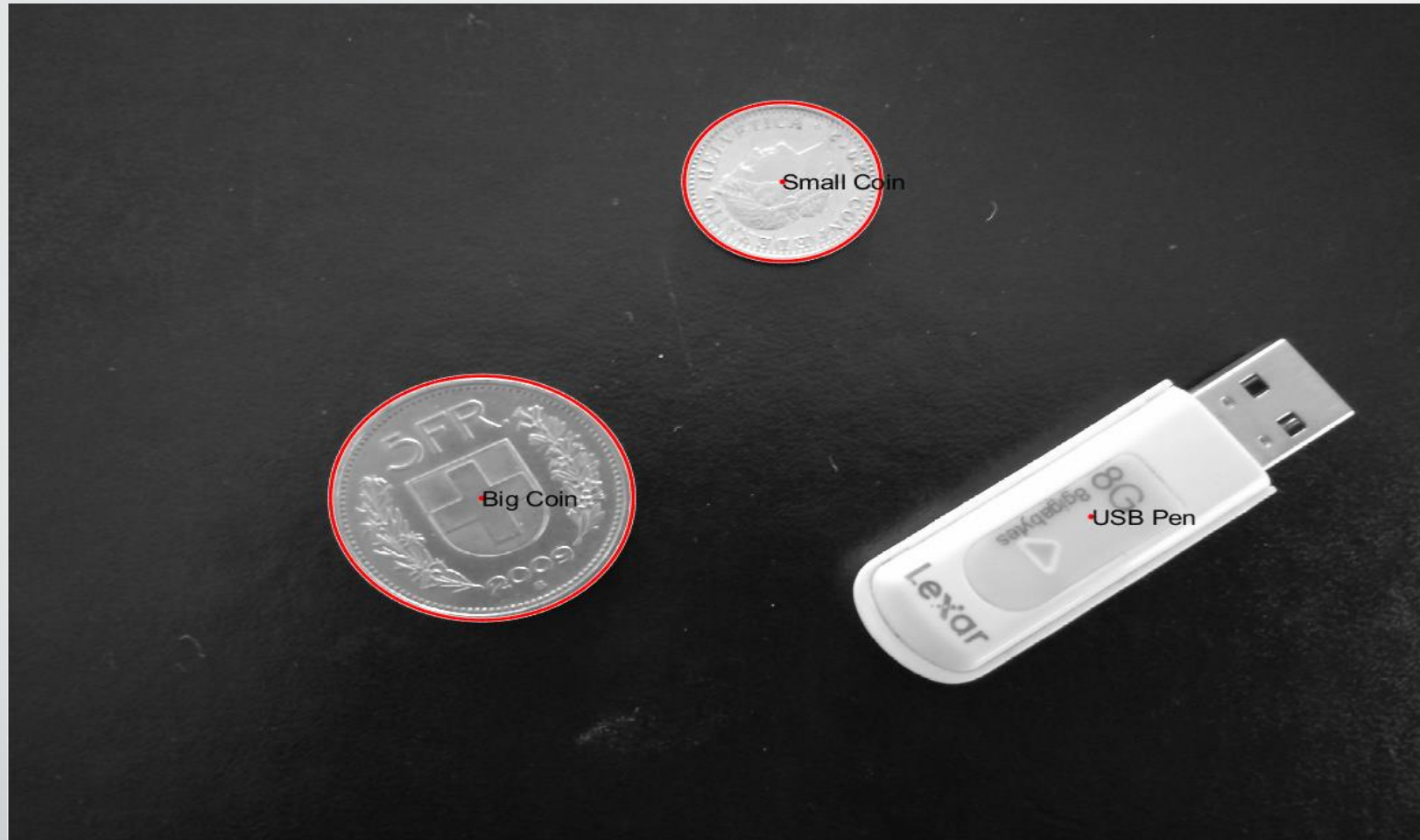
3D Acquisition – Cloud Points



```
exportMeshToPly(vertices, faces, vertex_color, name);
```

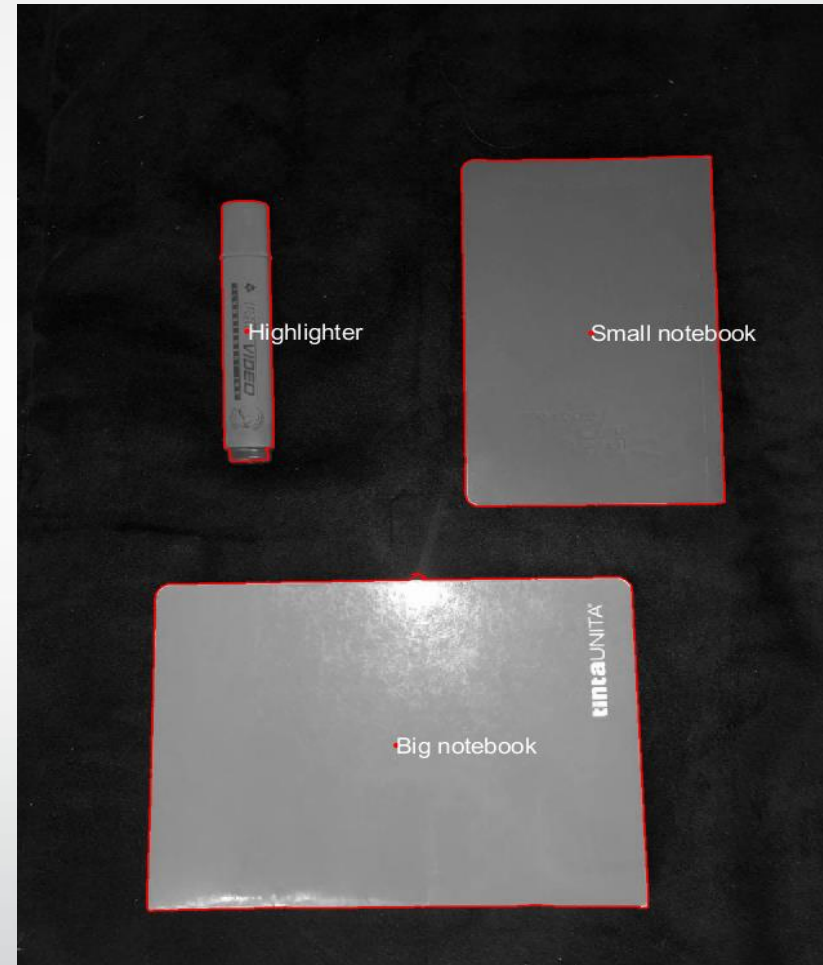


Image Analysis



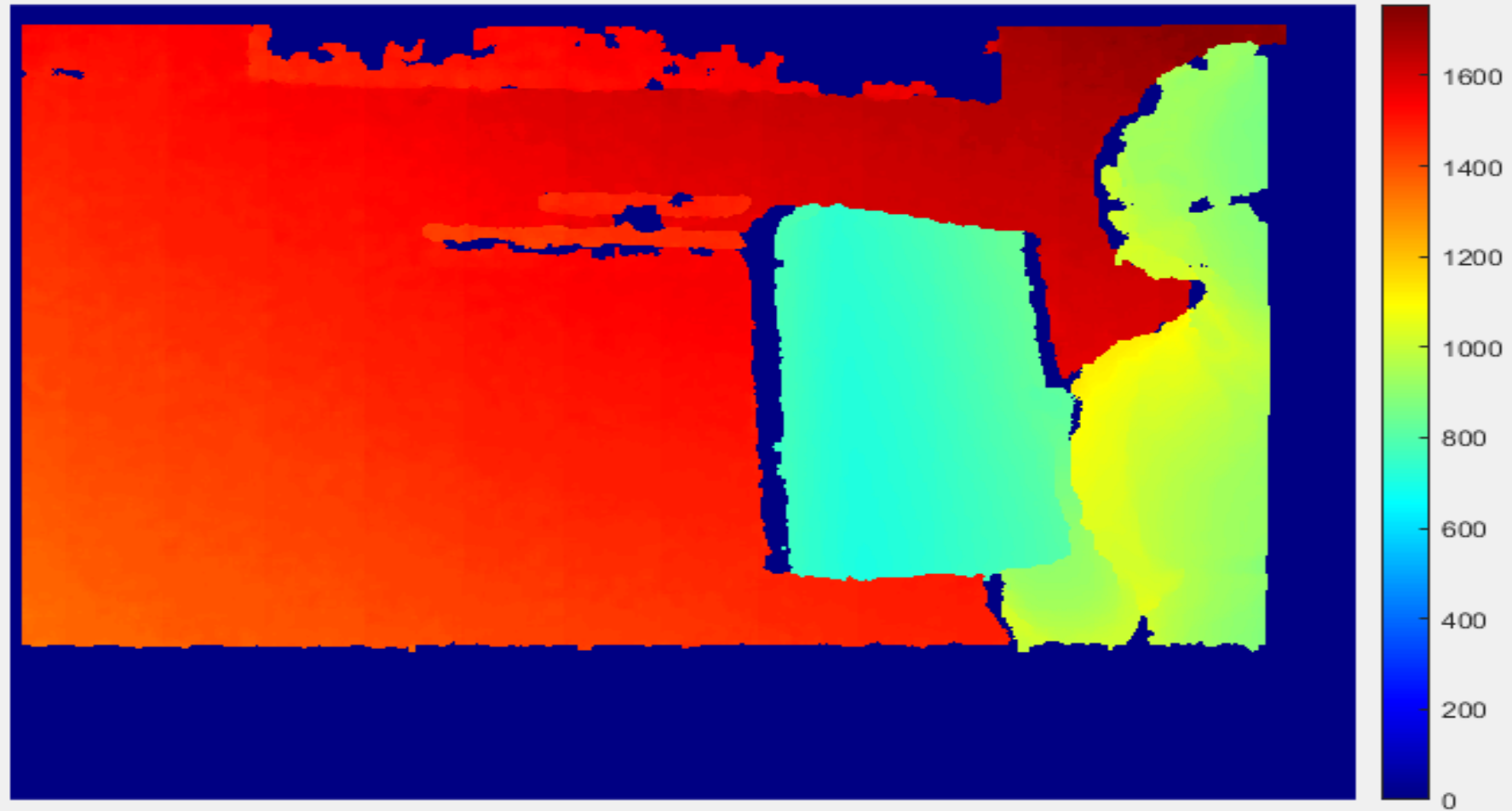
```
bw = imbinarize(I);  
stats = regionprops('table',bw,'Centroid', 'MajorAxisLength','MinorAxisLength','Area','Perimeter',  
'BoundingBox');
```

Image Analysis



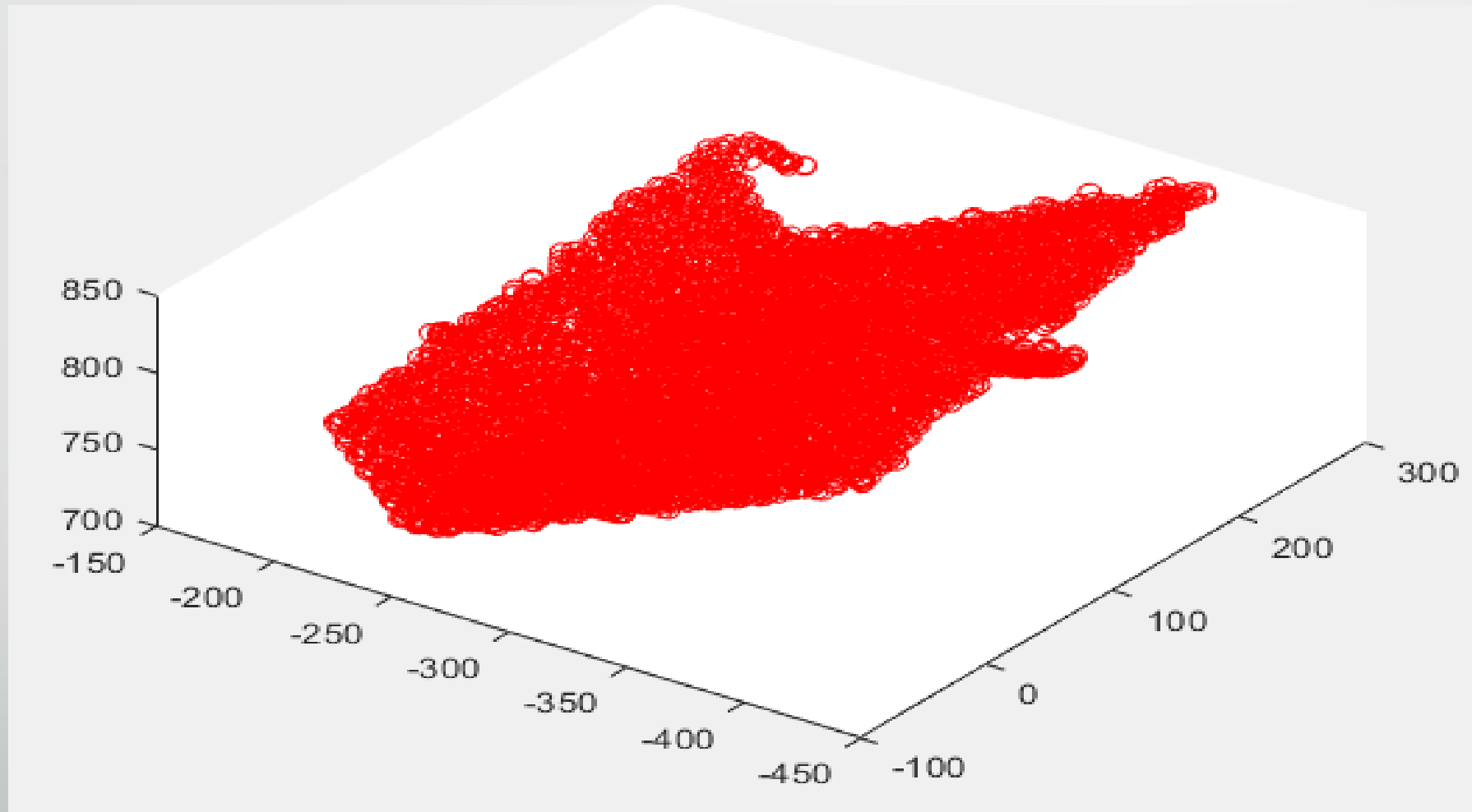
```
bw = imbinarize(I);  
stats = regionprops('table',bw,'Centroid', 'MajorAxisLength','MinorAxisLength','Area','Perimeter',  
'BoundingBox');
```

3D Analysis – Depth image

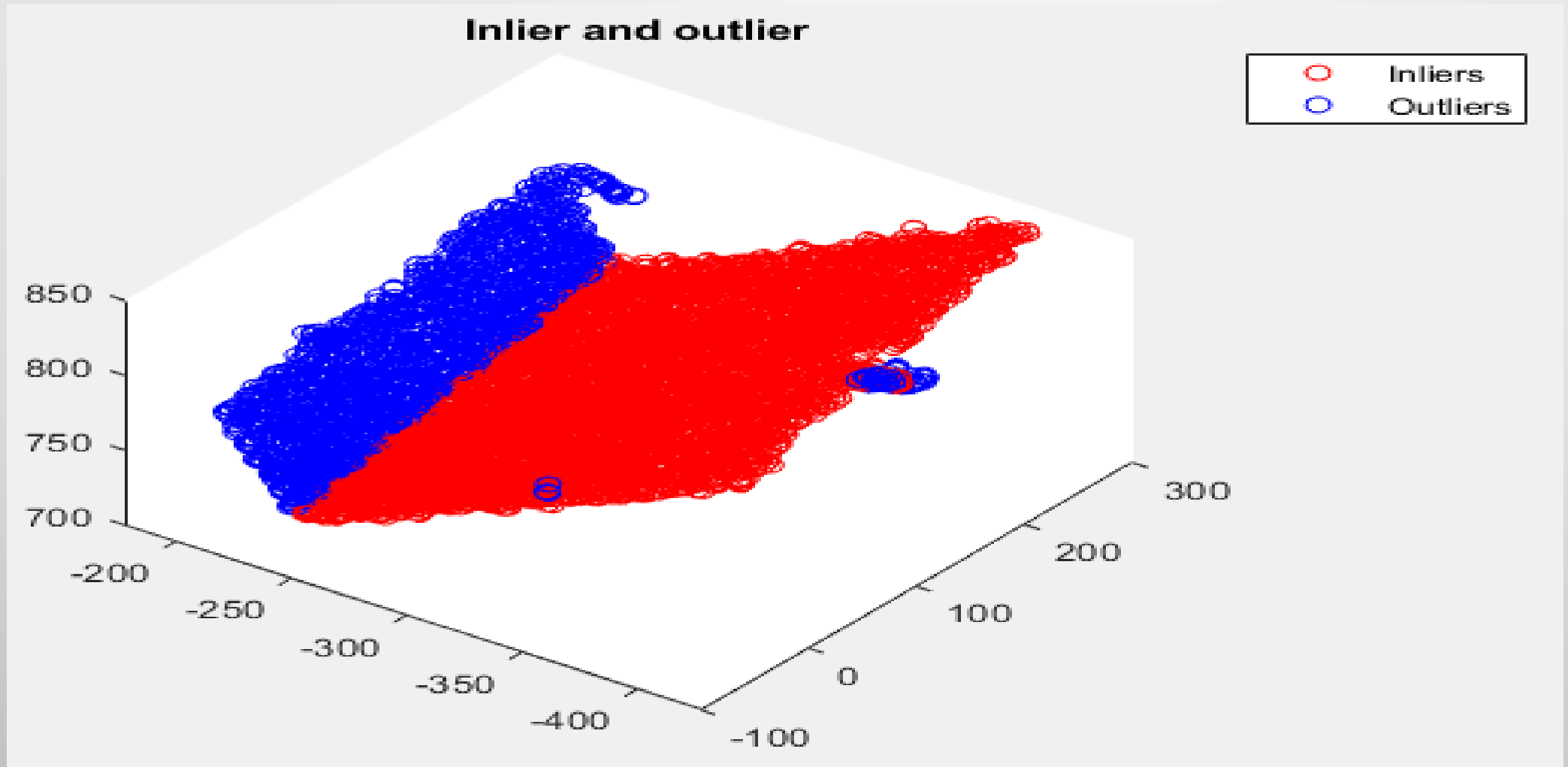


```
imshow(depth,[min(depth,[],'all'),max(depth,[],'all')]);  
colormap jet; colorbar; colormap;
```

3D Analysis – Cloud Points



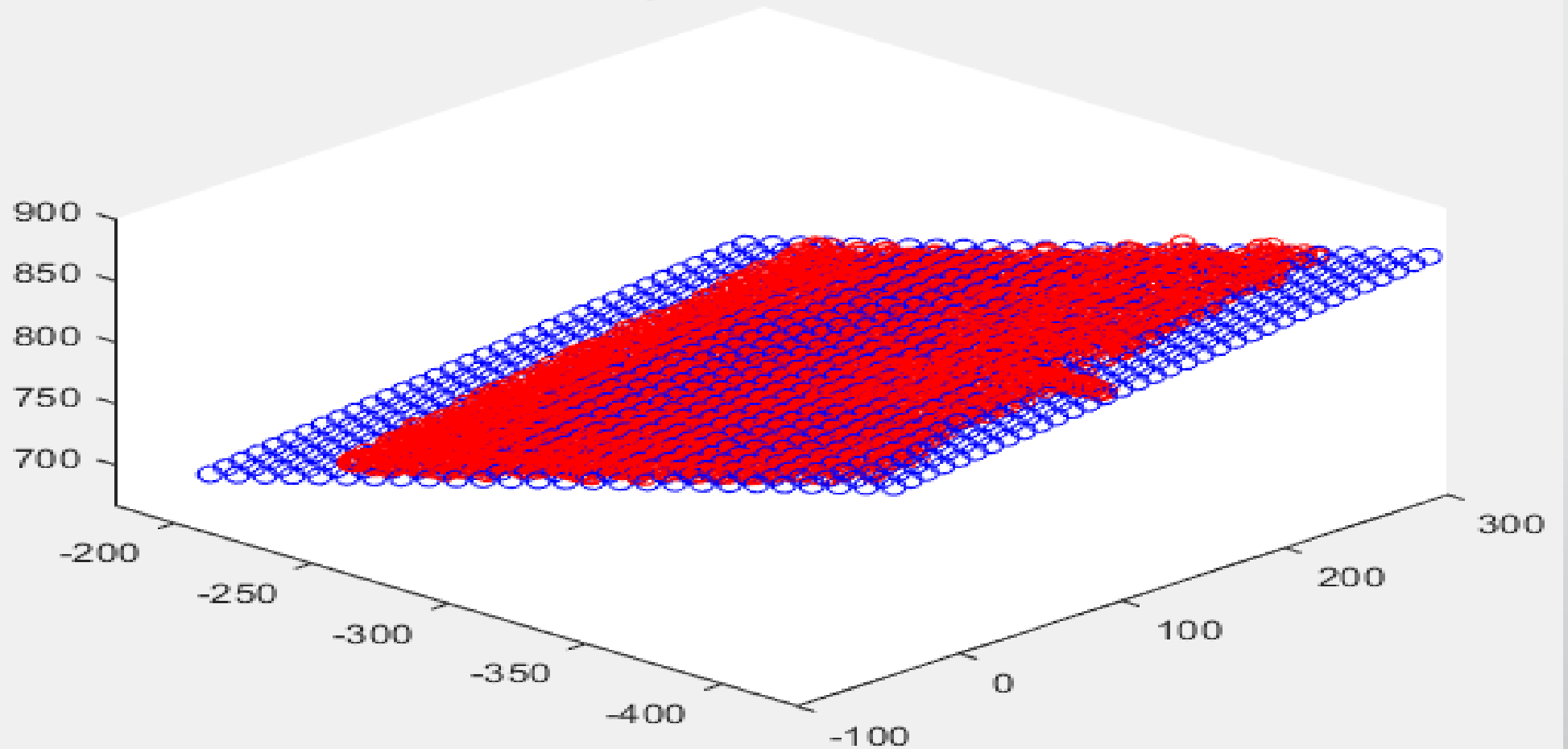
3D Analysis



```
[cloudPoints_fitted, outlier] = planeFitting(cloudPoints, a,b, c,d);
```

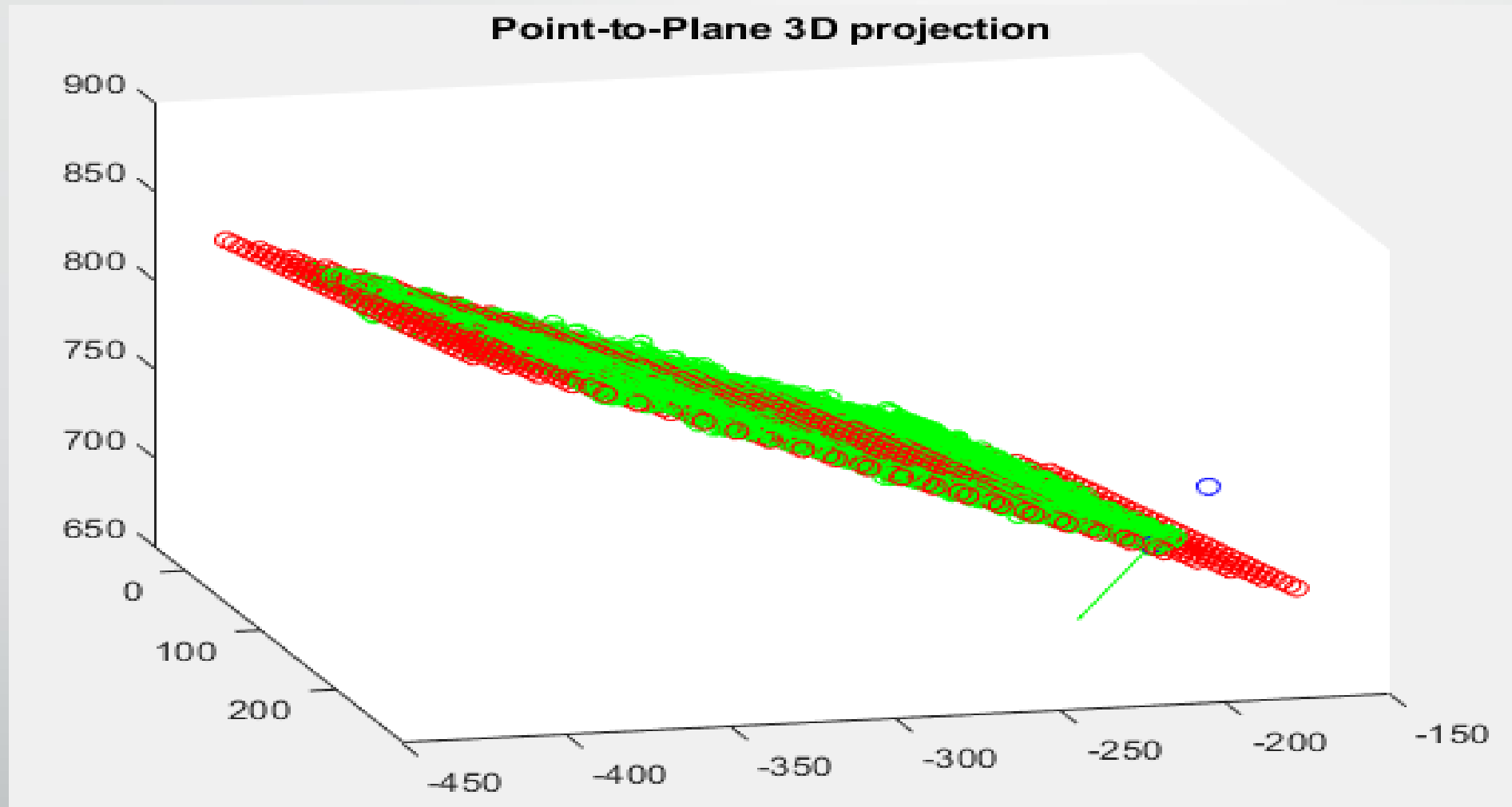
3D Analysis

Plane fitting vs Mathematical plane



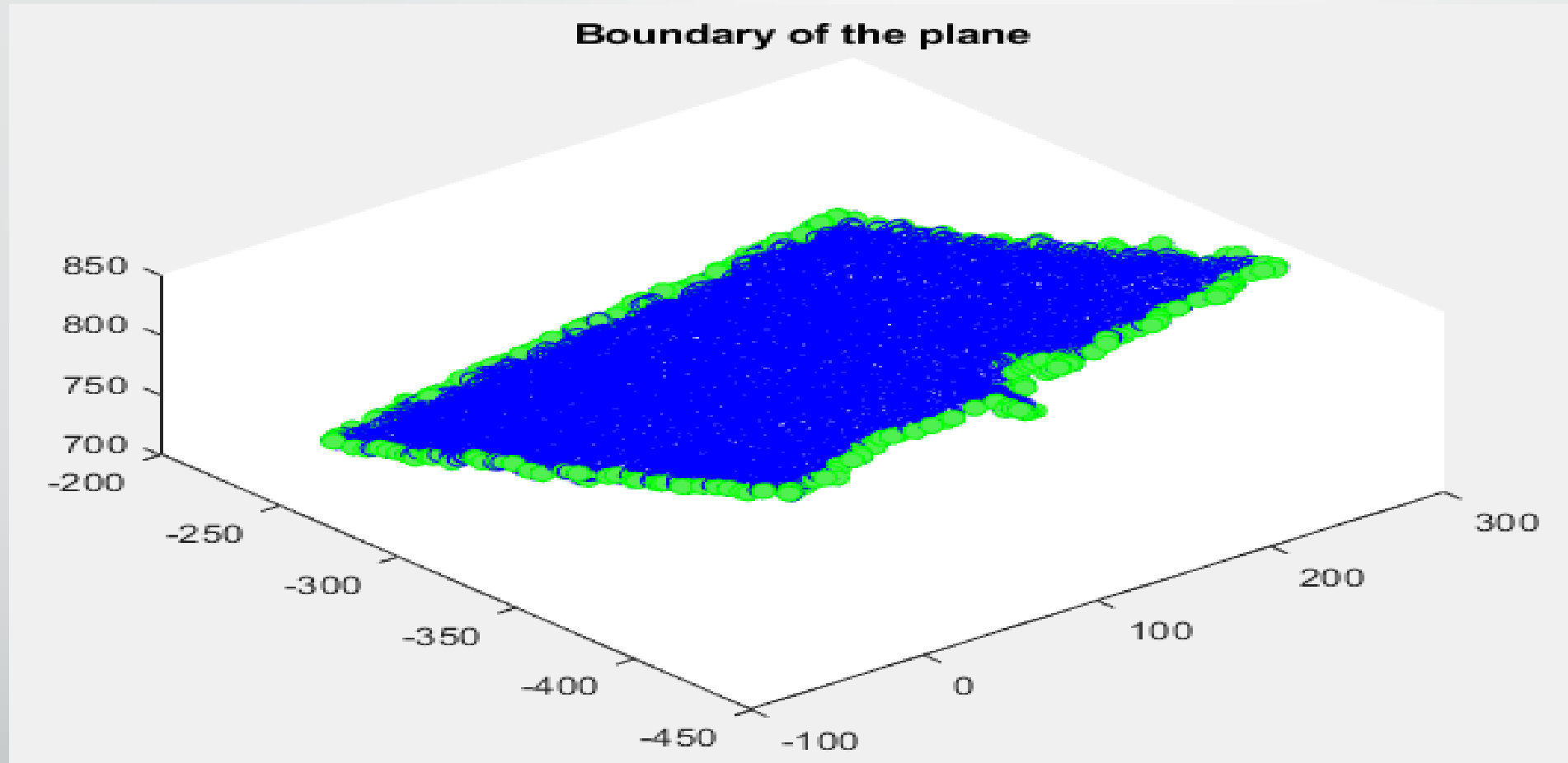
```
plane = pcfitplane(cloudPoint, 5);
```

3D Analysis



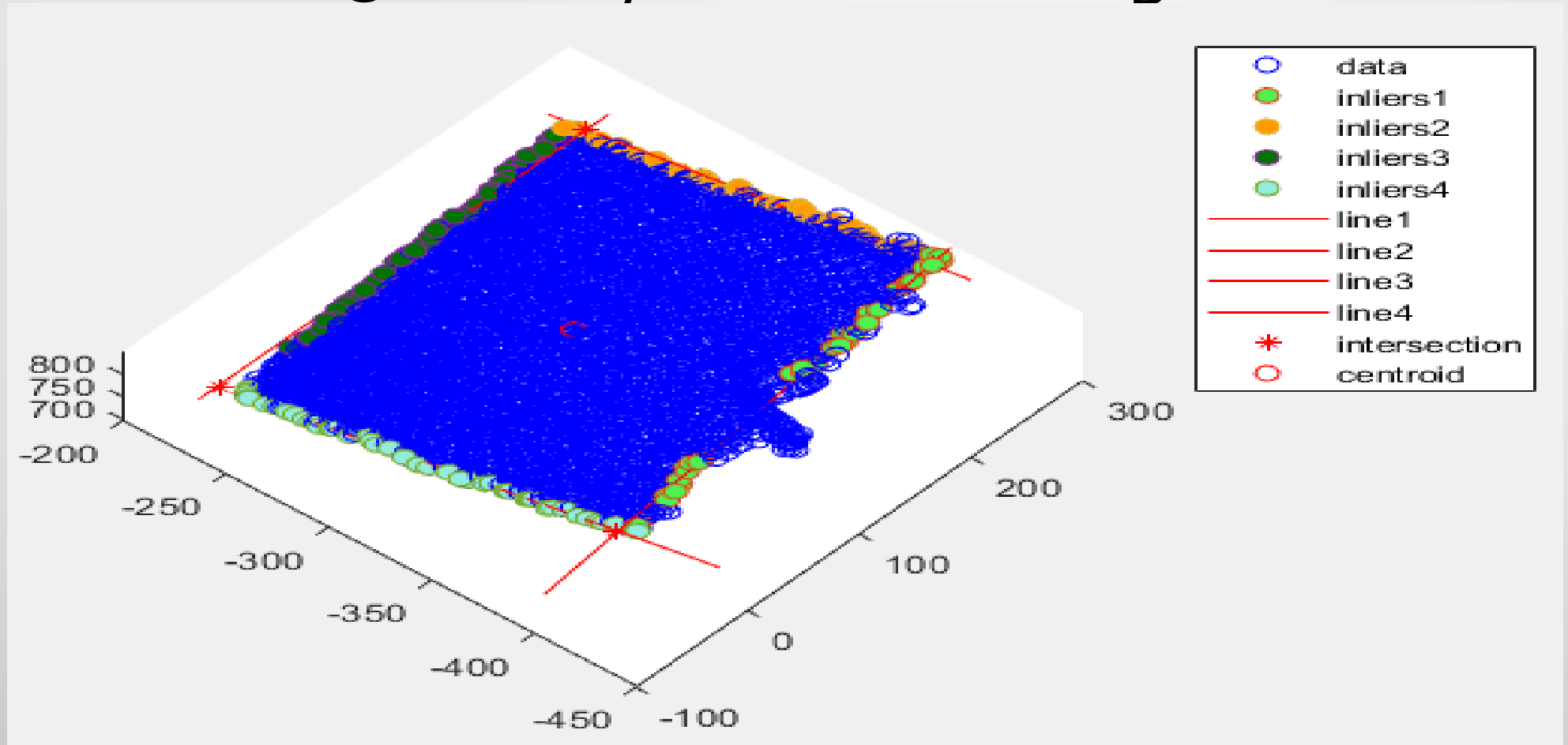
- `[projection] = point2plane_projection(normal, P1, Pplane);`

3D Analysis



```
boundIndex = (boundary(cloudPoints_fitted(:,1), cloudPoints_fitted(:,2), 1));  
boundPoints = cloudPoints_fitted(boundIndex,:);
```


3D Analysis – line fitting



```
[bestFit, outliers, inliers] = Ransac(data, k, t, d);  
[vertices] = findLineIntersection(bestFit1, bestFit2, bestFit3, bestFit4);  
[Theta] = angle2lines(line_intersection, L1, L2);  
[line_intersection] = lineIntersection(PA, PB, lines);
```



Thanks for your attention!