

Causality

EC 421, Set 10

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Prologue

Schedule

Last Time

Autocorrelation and nonstationarity

Today

Causality

Upcoming

Assignments

Causality

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Intro

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2. **Causal estimation:**[†] Estimate the actual data-generating process—learning about the true, population model that explains how y changes when we change x_j —focuses on β_j . Accuracy of \hat{y} is not important.

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For the rest of the term, we will focus on **causally estimating** β_j .

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Causality

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Many of these challenges relate to **exogeneity**, i.e., $E[u_i|X] = 0$.
Causality requires us to **hold all else constant** (*ceterus paribus*).

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- What **causes** some countries to grow and others to decline?
- What **caused** the capital riot?
- Did lax regulation **cause** Texas's recent energy problems?
- **How** does the number of police officers affect crime?
- What is the **effect** of better air quality on test scores?
- Do longer prison sentences **decrease** crime?
- How did cannabis legalization **affect** mental health/opioid addiction?

Causality

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New saying:

| Correlation plus exogeneity is causation.

Let's work through a few examples.

Causation

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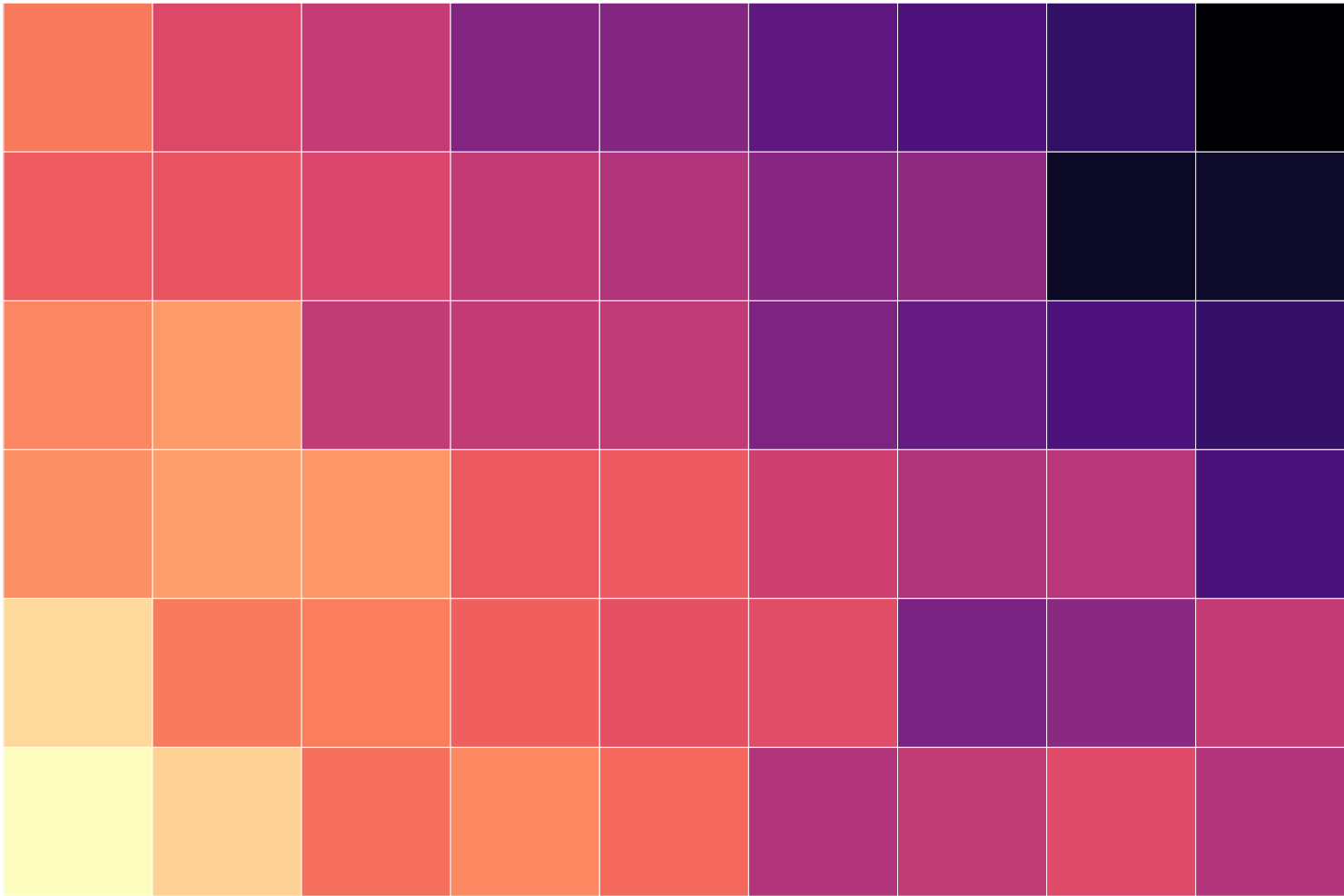
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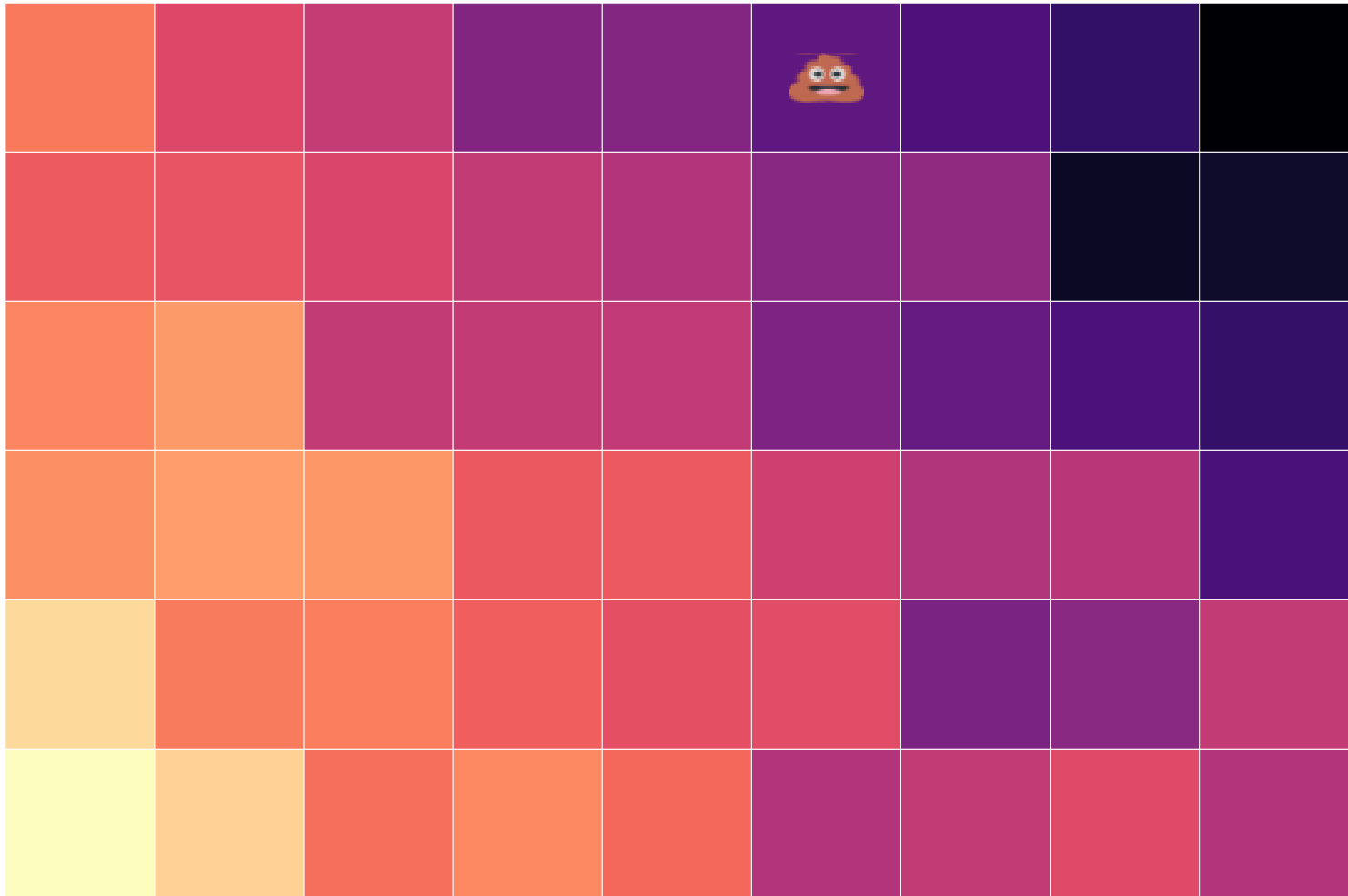
54 equal-sized plots

01	02	03	04	05	06	07	08	09
10	11	12	13	14	15	16	17	18
19	20	21	22	23	24	25	26	27
28	29	30	31	32	33	34	35	36
37	38	39	40	41	42	43	44	45
46	47	48	49	50	51	52	53	54

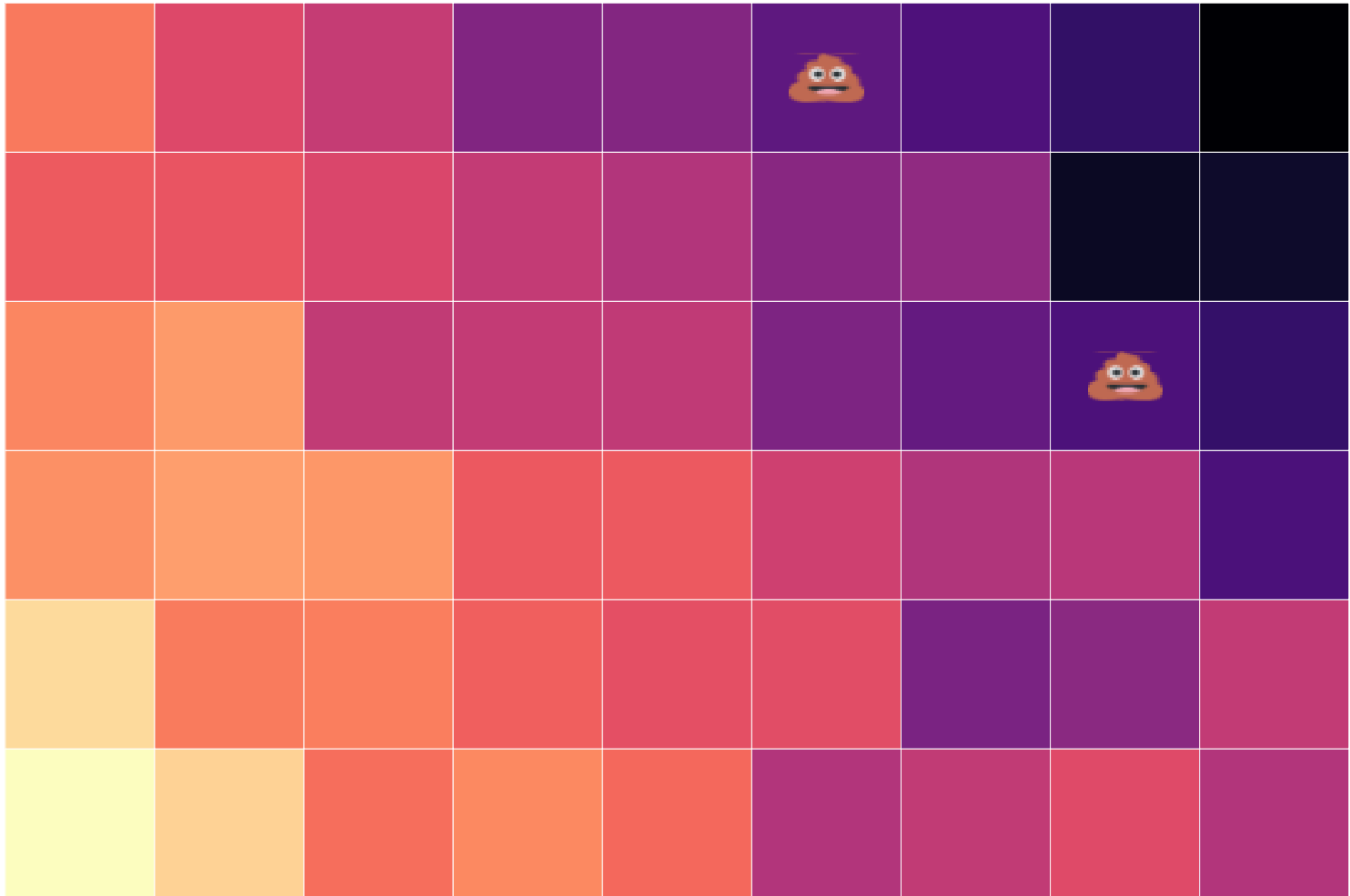
54 equal-sized plots of varying quality



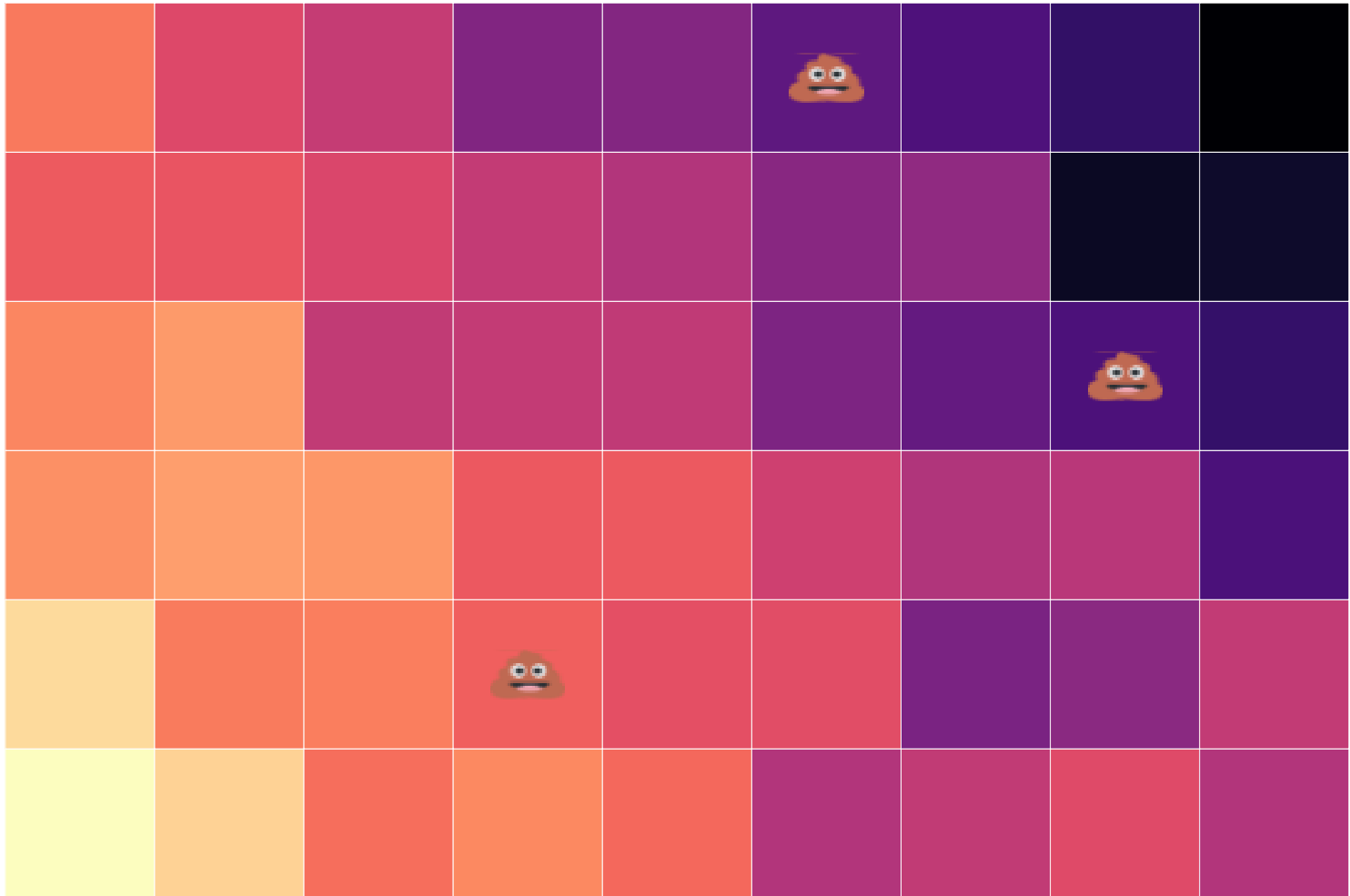
54 equal-sized plots of varying quality plus randomly assigned treatment



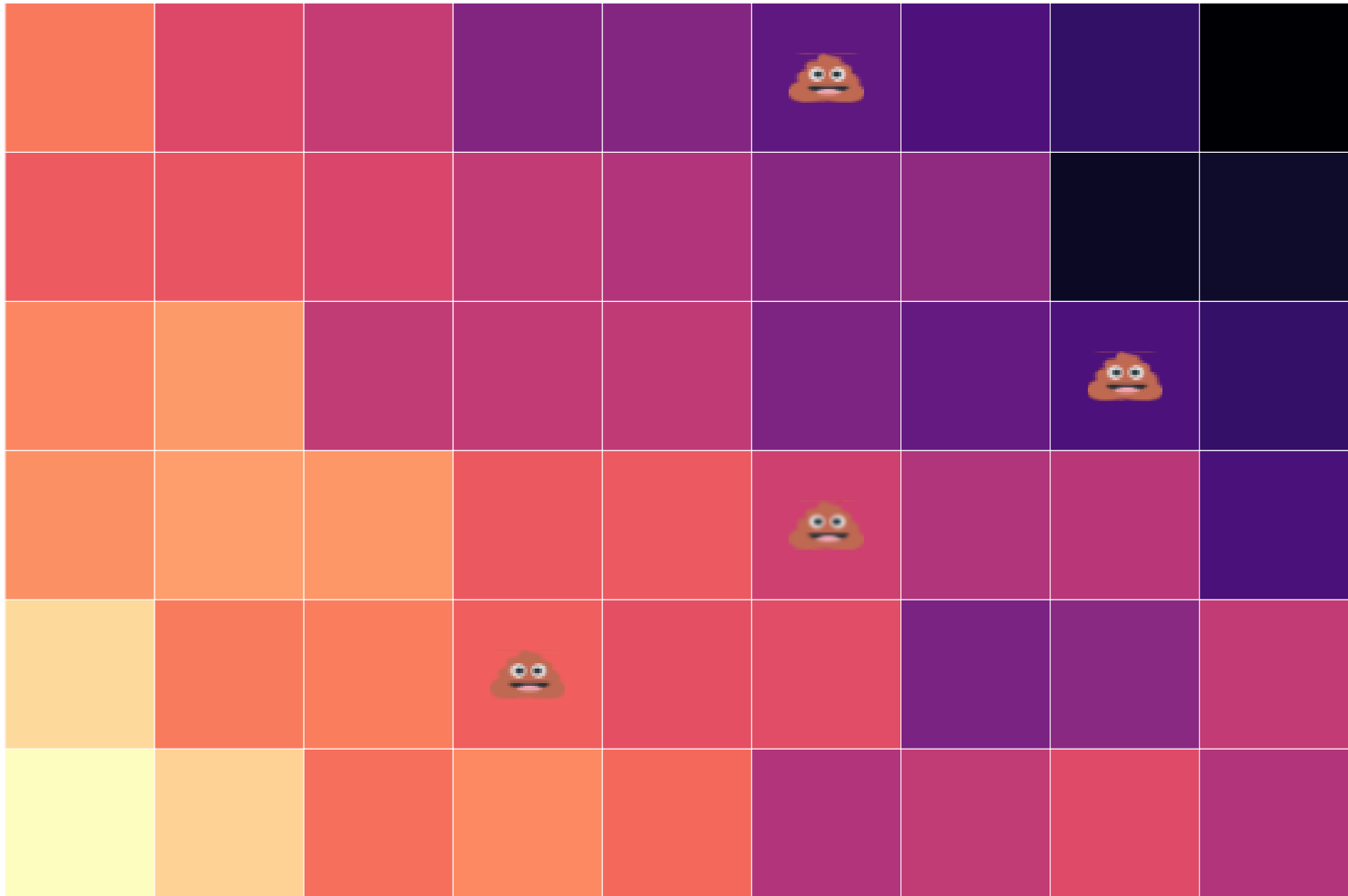
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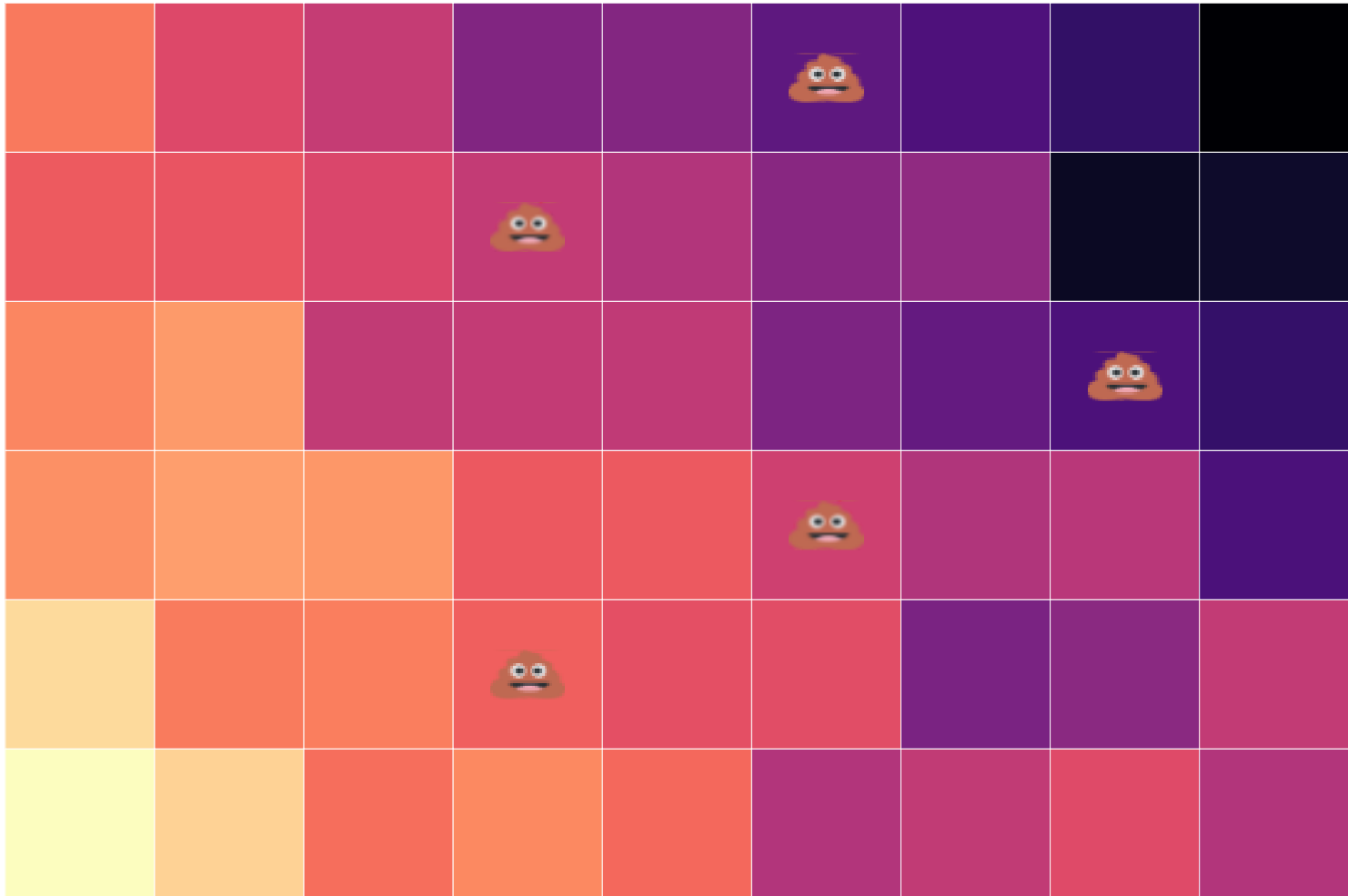
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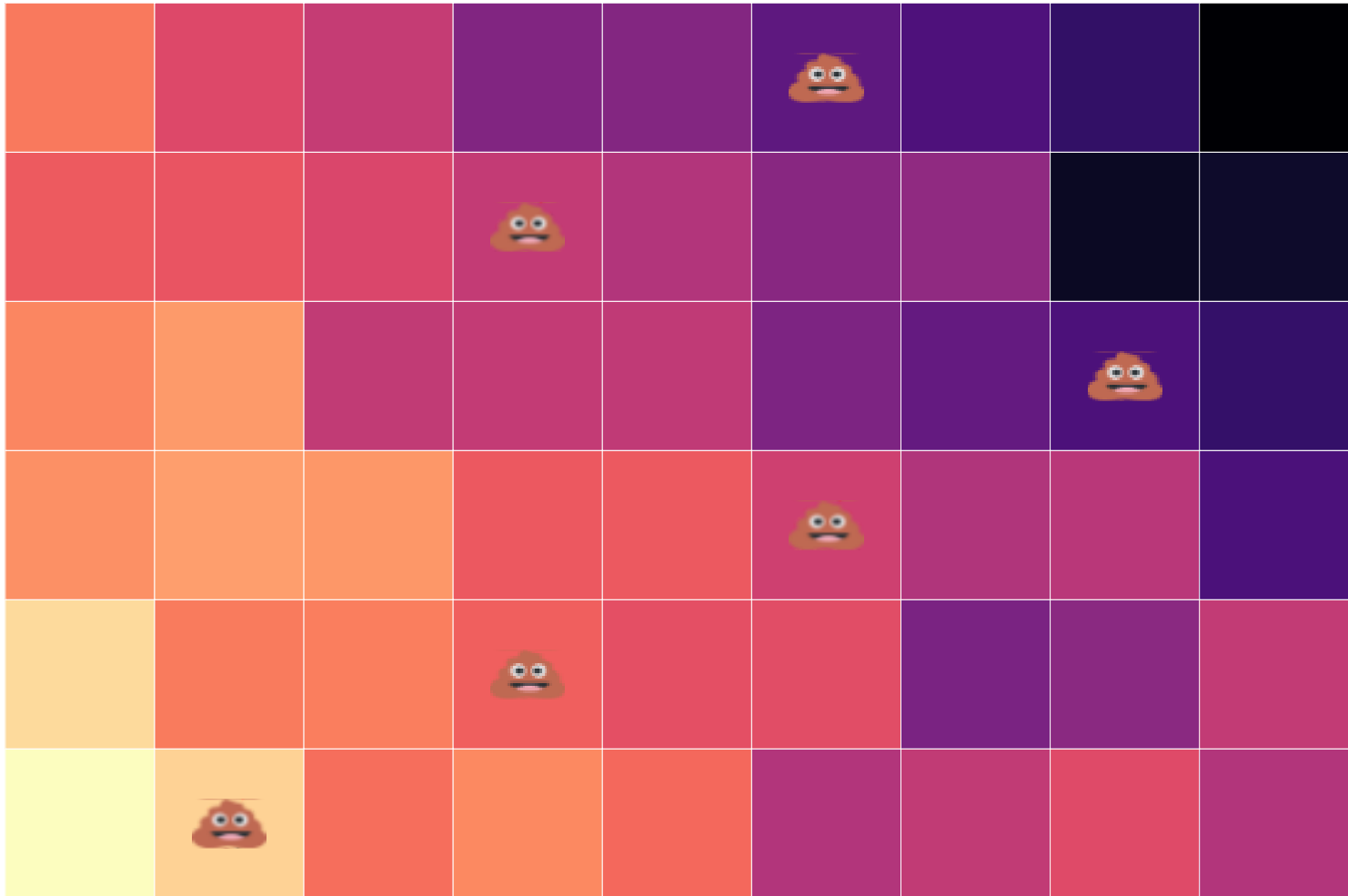
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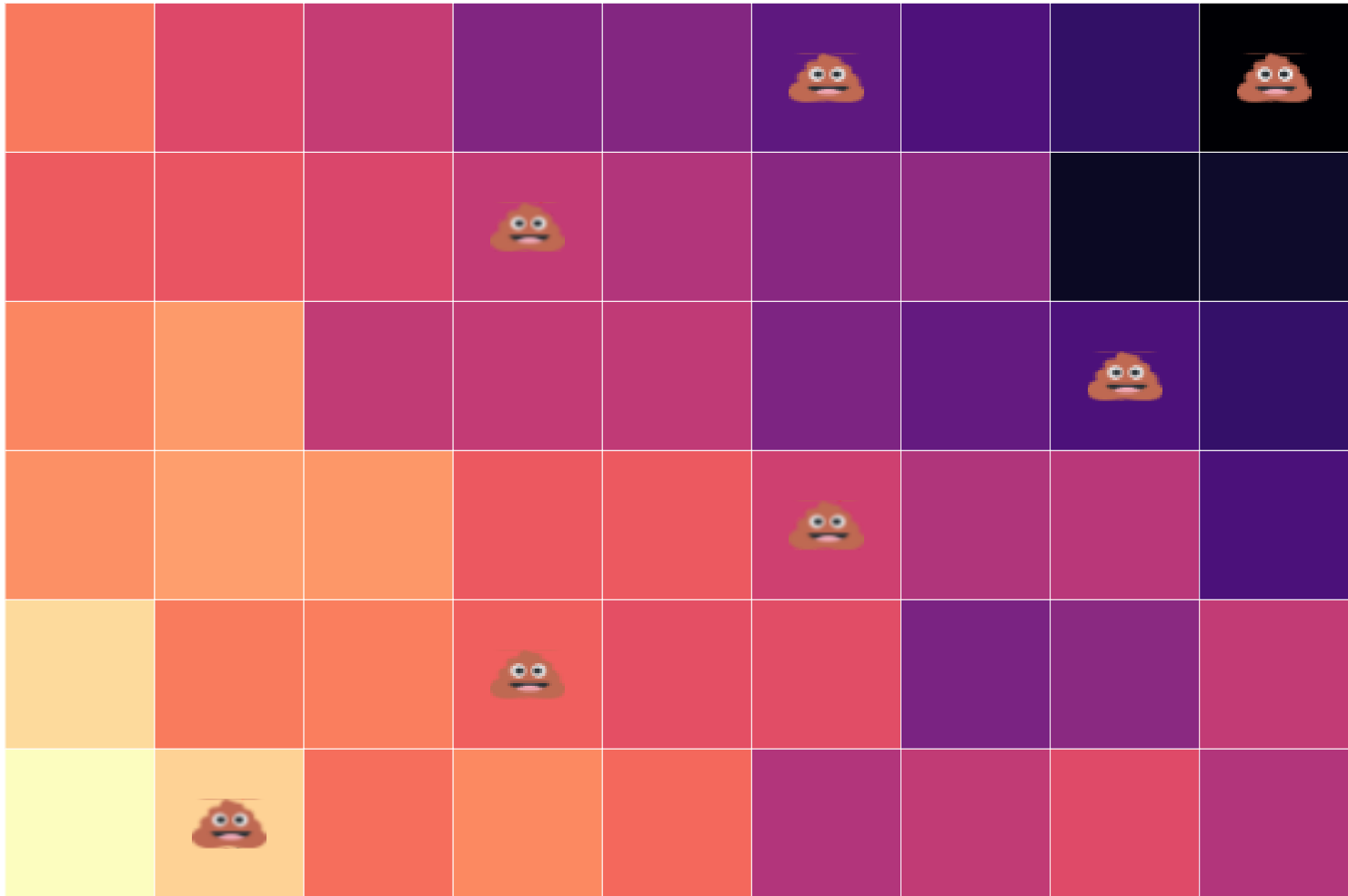
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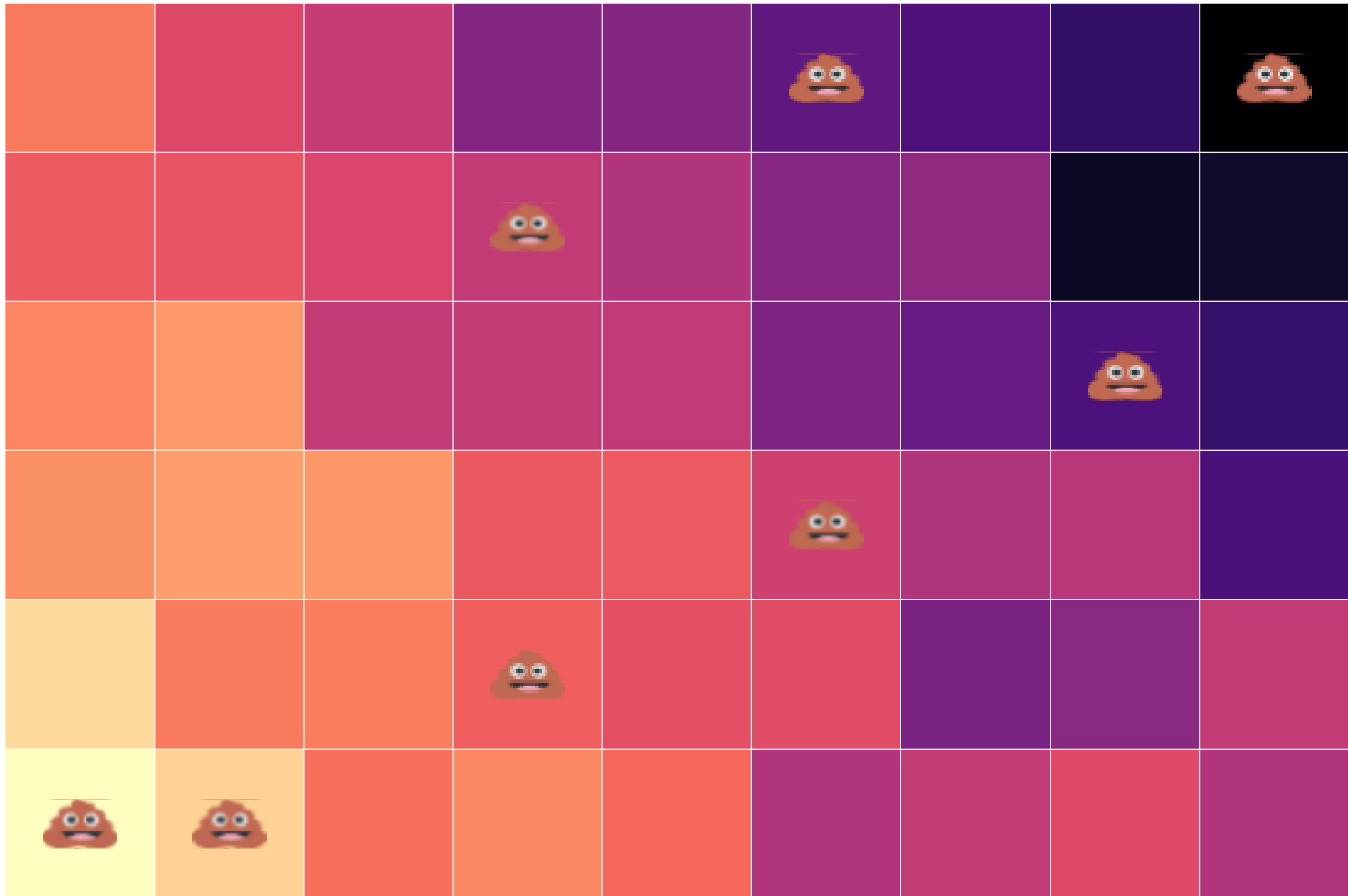
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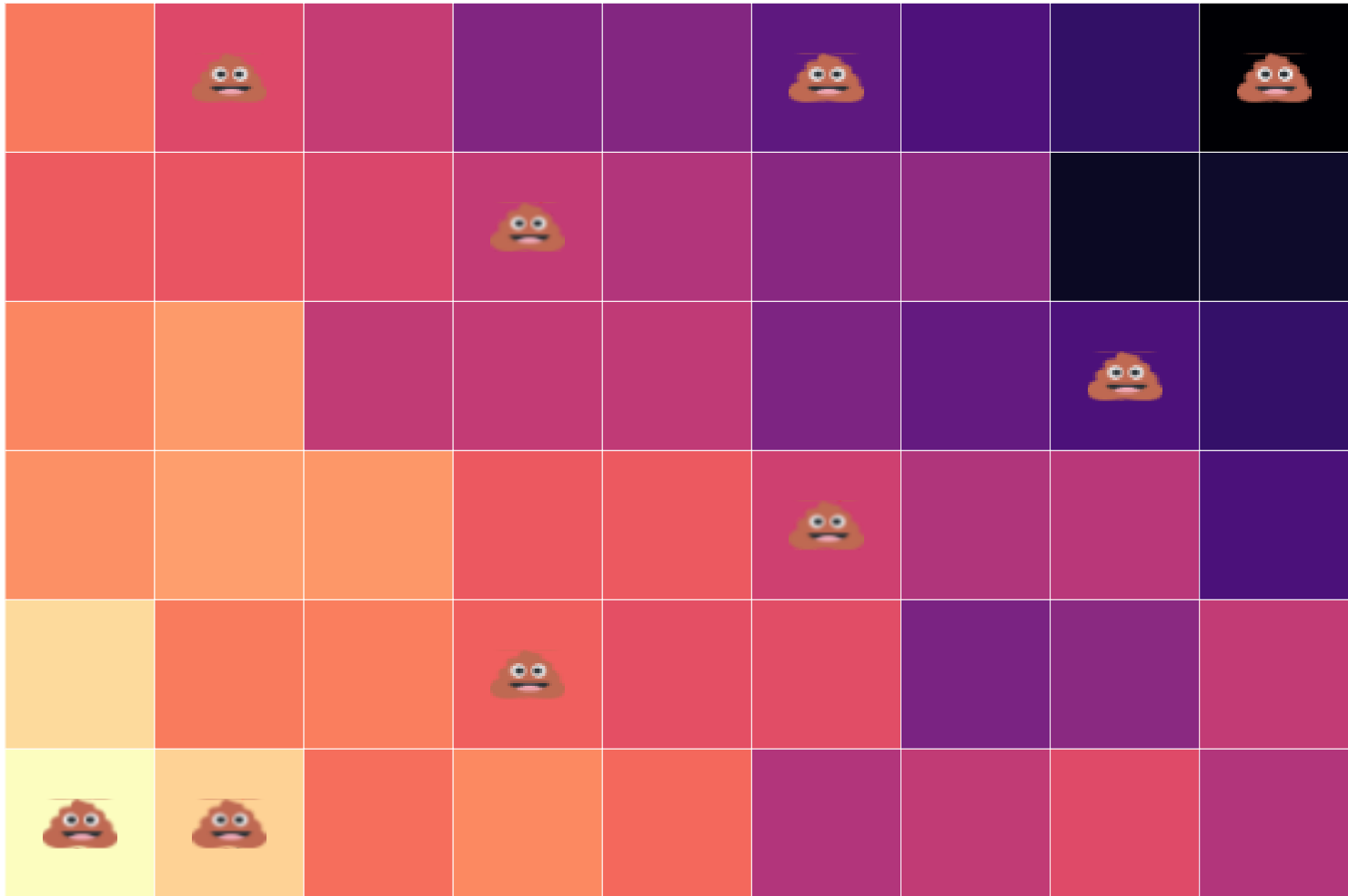
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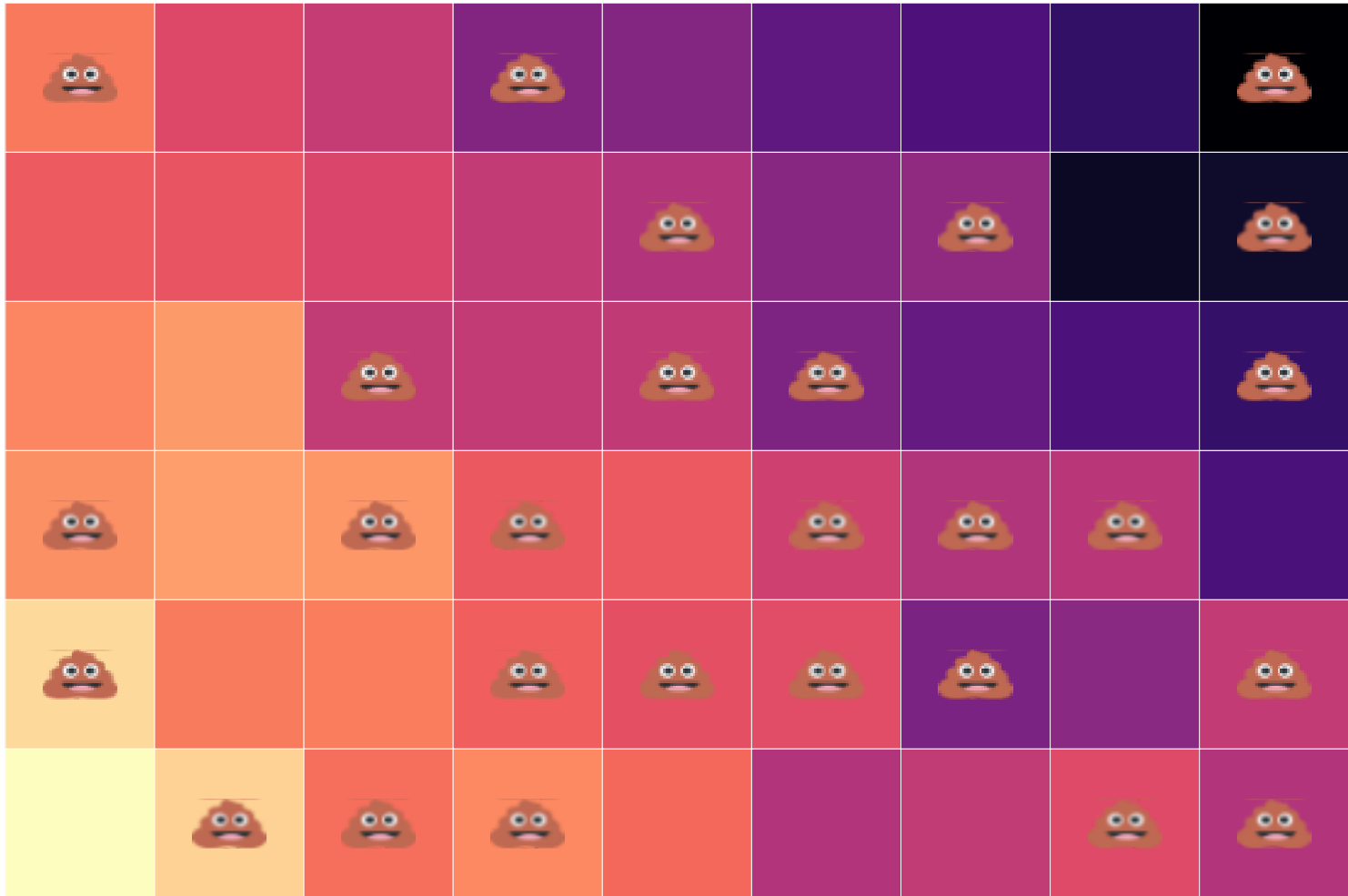
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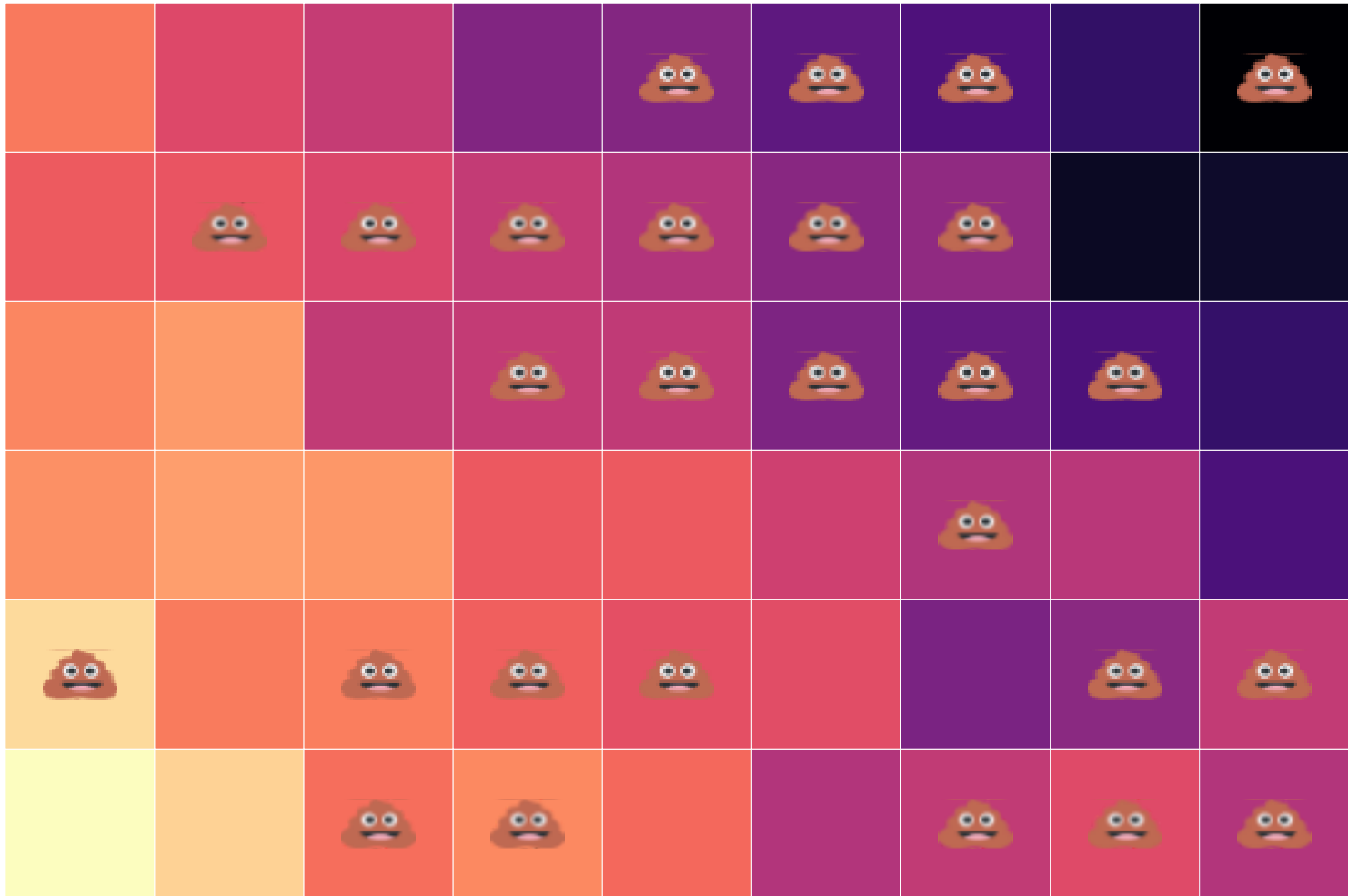
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Example: The causal effect of fertilizer

We can estimate the **causal effect** of fertilizer on crop yield by comparing the average yield in the treatment group (💩) with the control group (no 💩).

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A: On average, **randomly assigning treatment should balance** trt. and control across the other dimensions that affect yield (soil, slope, water).

Causality

Example: Returns to education

Labor economists, policy makers, parents, and students are all interested in the (monetary) *return to education*.

Causality

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Thought experiment:

- Randomly select an individual.
- Give her an additional year of education.
- How much do her earnings increase?

This change in earnings gives the **causal effect** of education on earnings.

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The point (2) above also illustrates the difficulty in learning about educations while *holding all else constant*.

Many important variables have the same challenge—gender, race, income.

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- Admissions **cutoffs**
- **Lottery** enrollment and/or capacity **constraints**

Causality

Real-world experiments

Both examples consider **real experiments** that isolate causal effects.

Characteristics

- **Feasible**—we can actually (potentially) run the experiment.
- **Compare individuals** randomized into treatment against individuals randomized into control.
- **Require "good" randomization** to get *all else equal* (exogeneity).

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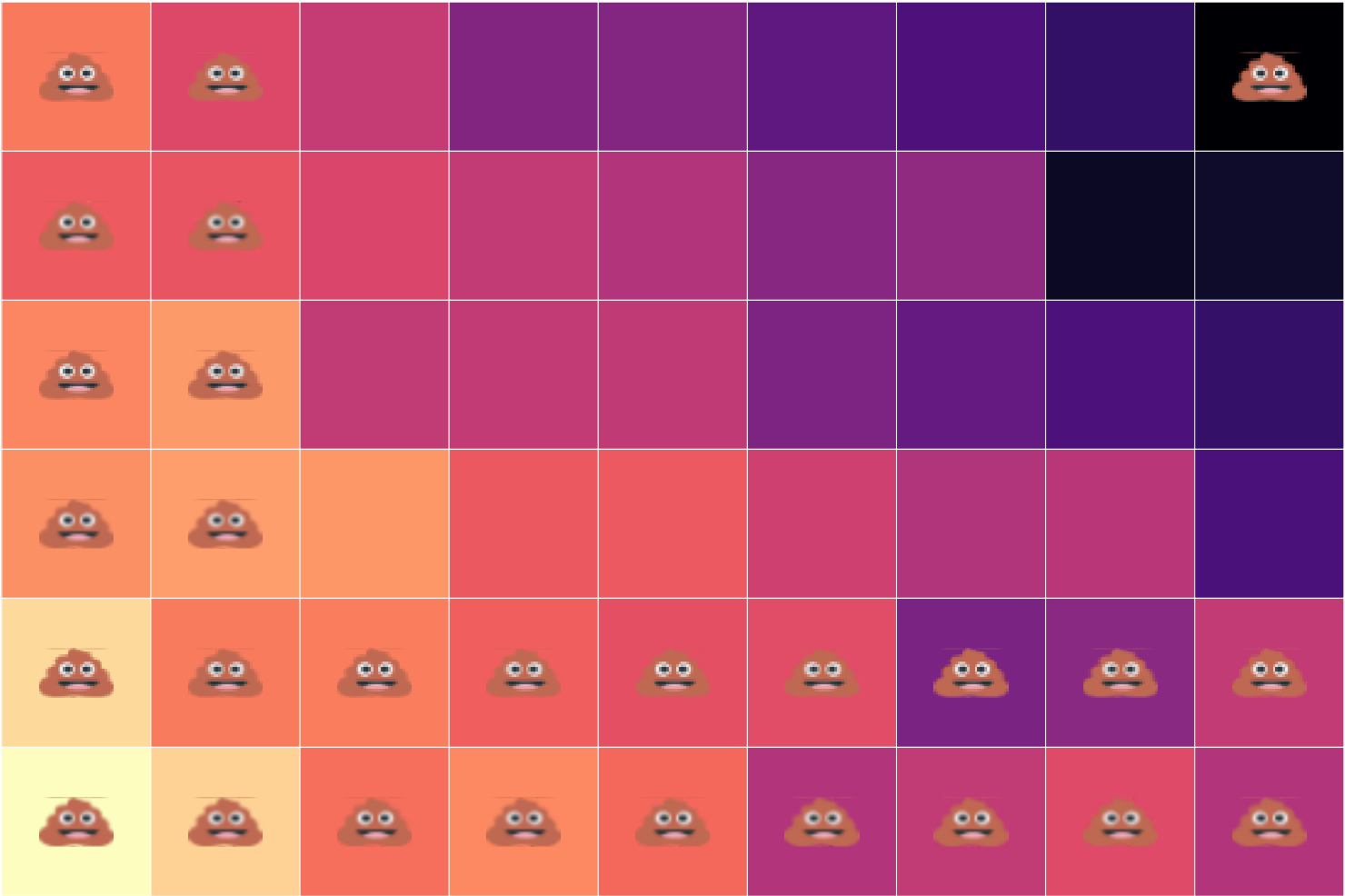
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- **Require "good" randomization** to get *all else equal* (exogeneity).

Note: Your experiment's results are only as good as your randomization.

Unfortunate randomization



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The ideal experiment

The **ideal experiment** would be subtly different.

Rather than comparing units randomized as **treatment** vs. **control**, the ideal experiment would compare treatment and control **for the same, exact unit**.

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This *ideal experiment* is clearly infeasible[†], but it creates nice notation for causality (the Rubin causal model/Neyman potential outcomes framework).

[†] Without (1) God-like abilities and multiple universes or (2) a time machine.

Causality

The ideal experiment

The *ideal* data for 10 people

```
#>      i trt  y1i  y0i
#> 1    1   1 5.01 2.56
#> 2    2   1 8.85 2.53
#> 3    3   1 6.31 2.67
#> 4    4   1 5.97 2.79
#> 5    5   1 7.61 4.34
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Calculate the causal effect of trt.

$$\tau_i = y_{1,i} - y_{0,i}$$

for each individual i .

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#>      i trt  y1i  y0i effect_i
#> 1    1   1 5.01 2.56      2.45
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The mean of τ_i is the

average treatment effect (ATE).

Thus, $\bar{\tau} = 3.82$

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This model highlights the fundamental problem of causal inference.

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#> 10 10   0  NA 1.40
```

We can't observe $y_{1,i}$ and $y_{0,i}$.

But, we do observe

- $y_{1,i}$ for i in 1, 2, 3, 4, 5
- $y_{0,j}$ for j in 6, 7, 8, 9, 10

Causality

The ideal experiment

So a dataset that we actually observe for 6 people will look something like

```
#>      i trt  y1i  y0i
#> 1    1   1 5.01   NA
#> 2    2   1 8.85   NA
#> 3    3   1 6.31   NA
#> 4    4   1 5.97   NA
#> 5    5   1 7.61   NA
#> 6    6   0  NA 4.15
#> 7    7   0  NA 0.56
#> 8    8   0  NA 3.52
#> 9    9   0  NA 4.49
#> 10 10   0  NA 1.40
```

We can't observe $y_{1,i}$ and $y_{0,i}$.

But, we do observe

- $y_{1,i}$ for i in 1, 2, 3, 4, 5
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Q: How do we "fill in" the `NA`s and estimate $\bar{\tau}$?

Causality

Causally estimating the treatment effect

Notation: Let D_i be a binary indicator variable such that

- $D_i = 1$ if individual i is treated.
- $D_i = 0$ if individual i is not treated (*control* group).

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Then, rephrasing the previous slide,

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Q: How can we estimate $\bar{\tau}$ using only $(y_{1,i} | D_i = 1)$ and $(y_{0,i} | D_i = 0)$?

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$$Avg(y_i | D_i = 1) - Avg(y_i | D_i = 0)$$

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Q: When does this simple difference in groups' means provide information on the **causal effect** of the treatment?

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Time for math! 🎉

Causality

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This assumption says that the treatment effect is equal (constant) across all individuals i .

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Note: We defined

$$\tau_i = \tau = y_{1,i} - y_{0,i}$$

which implies

$$y_{1,i} = y_{0,i} + \tau$$

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So our proposed group-difference estimator give us the sum of

1. τ , the **causal, average treatment effect** that we want
2. **Selection bias**: How much trt. and control groups differ (on average).

Next time: Solving selection bias.

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