$$\frac{\partial z}{\partial t} = \left(\frac{\partial}{\partial t}(x+y)\right)y + (x+y)\frac{\partial y}{\partial t}$$
$$= \left(\frac{\partial x}{\partial t} + \frac{\partial y}{\partial t}\right)y + (x+y)\frac{\partial y}{\partial t}$$

Z = (x+y)y

$$= \left(y \frac{dx}{dt} + y \frac{dy}{dt}\right) + \left(x + y\right) \frac{dy}{dt}$$

$$= y \frac{dx}{dt} + (x+2y) \frac{dy}{dt}$$
$$dz = y dx + (x+2y) dy$$