

1a) Queremos:

$$\int x^\alpha \sqrt{a^2 x^2 - 1}^\beta dx$$
$$= K \int u^\alpha \sqrt{u^2 - 1}^\beta du$$

Temos:

$$\int x^\alpha \sqrt{a^2 x^2 - 1}^\beta dx \quad \left[\begin{array}{l} u = ax \\ \frac{1}{a} u = x \\ \frac{1}{a} du = dx \end{array} \right]$$
$$= \int \left(\frac{u}{a} \right)^\alpha \sqrt{u^2 - 1}^\beta \cdot \frac{1}{a} du$$
$$= \frac{1}{a^{\alpha+1}} \int u^\alpha \sqrt{u^2 - 1}^\beta du$$

Então:

$$[1A] = \left(\begin{array}{l} \int x^\alpha \sqrt{a^2 x^2 - 1}^\beta dx \quad [u = ax] \\ = \frac{1}{a^{\alpha+1}} \int u^\alpha \sqrt{u^2 - 1}^\beta du \end{array} \right)$$