$$\frac{dy}{dx} = \frac{f(x)}{g(y)}$$

$$g(y)dy = f(x)dx$$

$$\int g(y)dy = \int f(x)dx$$

$$G(y)+C_1 \qquad F(x)+C_2$$

$$G(y) + C_1 = F(x) + C_2$$

$$G(y) = F(x) + C_2 - C_1$$

$$= F(x) + C_3$$

$$G^{-1}(G(y)) = G^{-1}(F(x) + C_3)$$