

EART97051 EDSML

Environmental Data: Week 1. Remote Sensing & Earth Observation



2. Algebraic operations & spectral indices

Dr Philippa J. Mason

Senior Lecturer in Planetary Remote Sensing,
Department of Earth Science & Engineering, Imperial College London, SW7 2AZ, UK
E-mail: p.j.mason@ic.ac.uk

Lecture Plan

1. (Briefly) Reflectance spectroscopy & spectral signatures
2. General formulae for multi-band point operations:
 - Algebraic operations
 - Formulation & uses plus examples
3. Development of spectral indices
 - Formulation & uses plus examples
4. Summary

1. Some background information on reflectance spectroscopy

Causes of spectral behaviour

Physical

- Scattering effects
 - Diffuse and/or specular reflection
 - Volume and/or surface scattering
 - Single and/or multiple scattering
 - Wavelength, particle & surface – dependent
- Refractive index (ratio of the speed of light through one material to that through another)
 - Reflectance, transmission
 - Wavelength-dependent
- Absorption coefficient
 - Chemical composition & mineral crystallography
 - Electronic and/or vibrational processes
 - Wavelength-dependent

Chemical

Sub-atomic processes causing spectral absorption

i. Electronic transitions in VIS & NIR

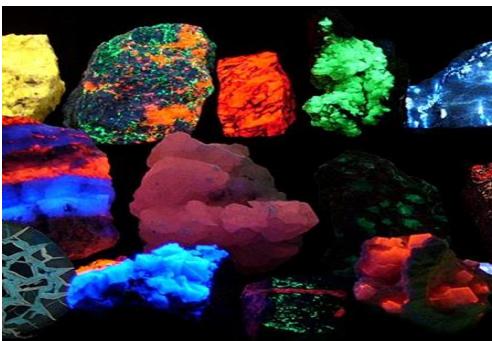
- a) Crystal Field effects (sub-atomic)
- b) Charge Transfer effects (sub-atomic)

ii. Vibrational transitions in SWIR & TIR

- Bond stretch, bending & rotation (molecular)

iii. Fluorescence (UV)

- High energy required – all UV absorbed by atmosphere so we can only do this in laboratory conditions!



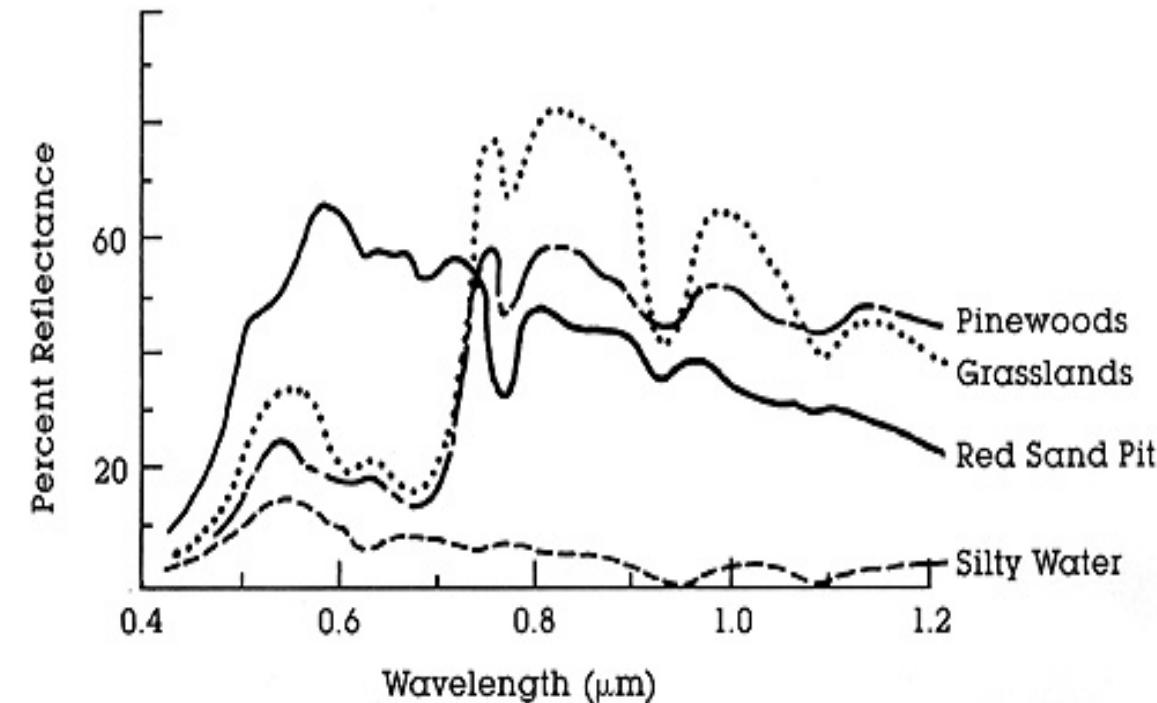
All effects are wavelength dependent

In all cases, absorbed energy is later emitted at longer wavelength than it is absorbed

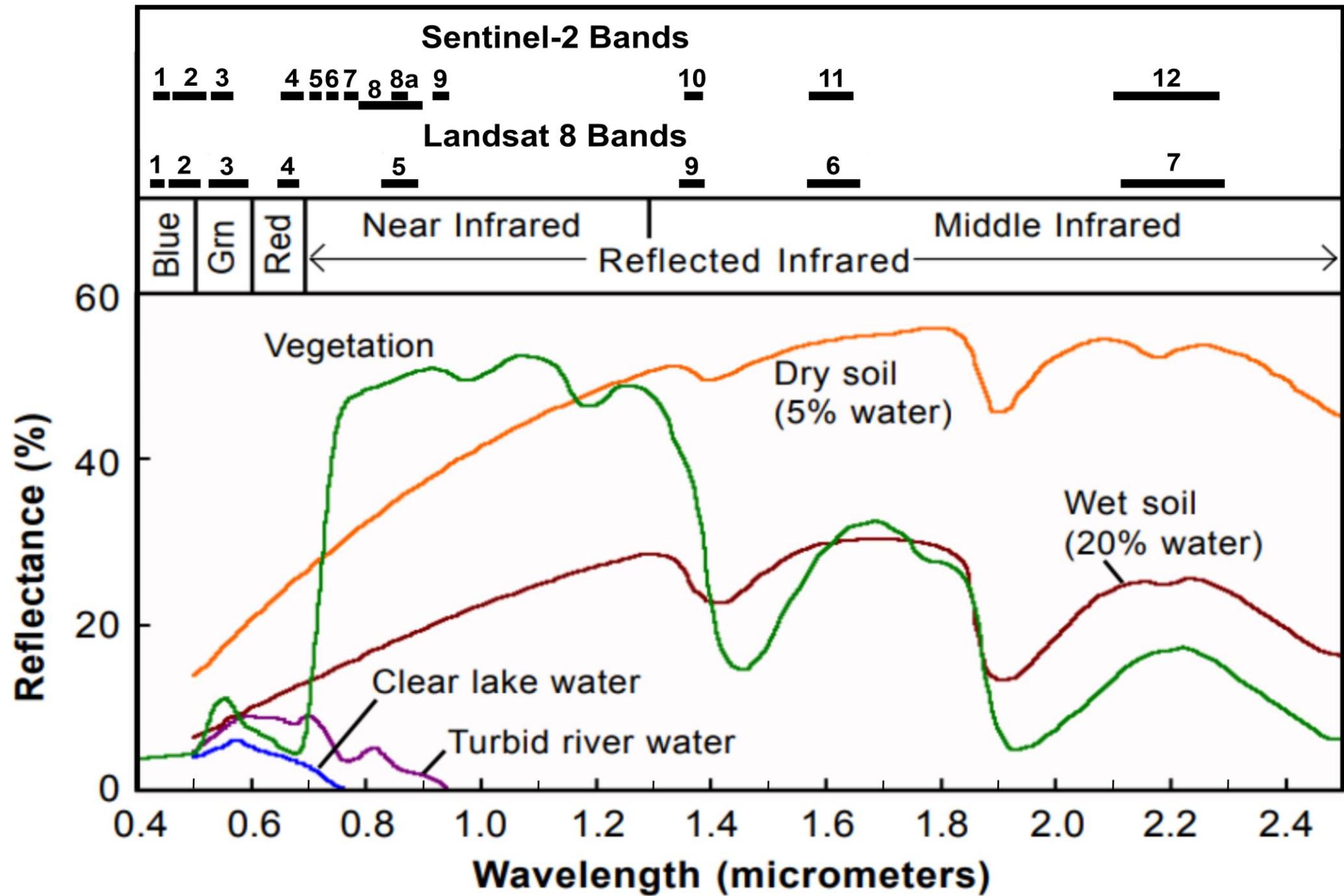
Reflectance spectroscopy how to exploit spectral profiles

1. Three forms of interaction with incident energy (I):
 - Selective **Reflection (R)**, **Absorption (A)** and **Transmittance (T)**
 - Proportions of R, A & T depend on the **wavelength of the energy and the chemistry of the material (and condition of its surface)**.
2. Later photons are **Emitted (E)** from a surface (also wavelength and chemistry dependent)
3. By **measuring the energy reflected (and/or emitted)** by target materials **over a range of wavelengths**, we build up a spectral response or **signature** for a particular target substance
4. By comparing the signatures of different materials we can distinguish between them (where we might not be able to, if we compared them at a single wavelength only)
5. Knowing where to ‘look’ spectrally and understanding the factors which influence the spectral response are critical to correctly identifying/interpreting the contributions of significant different materials to that signature.

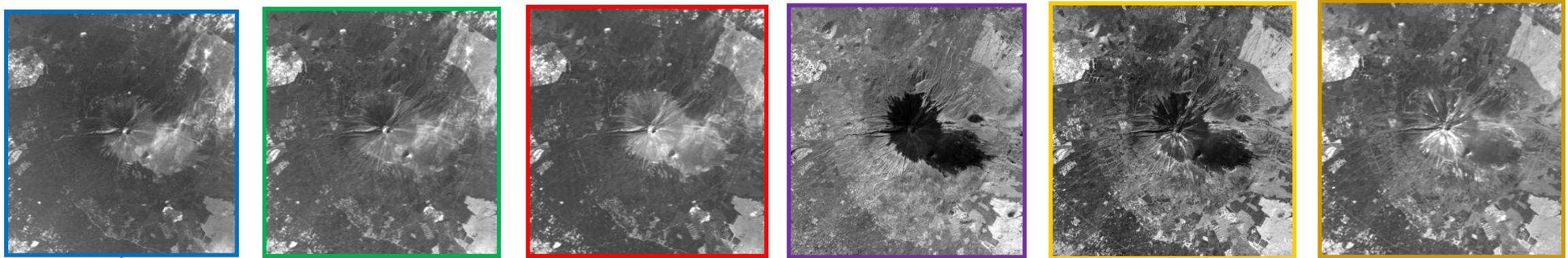
Spectral signatures of the common ground objects



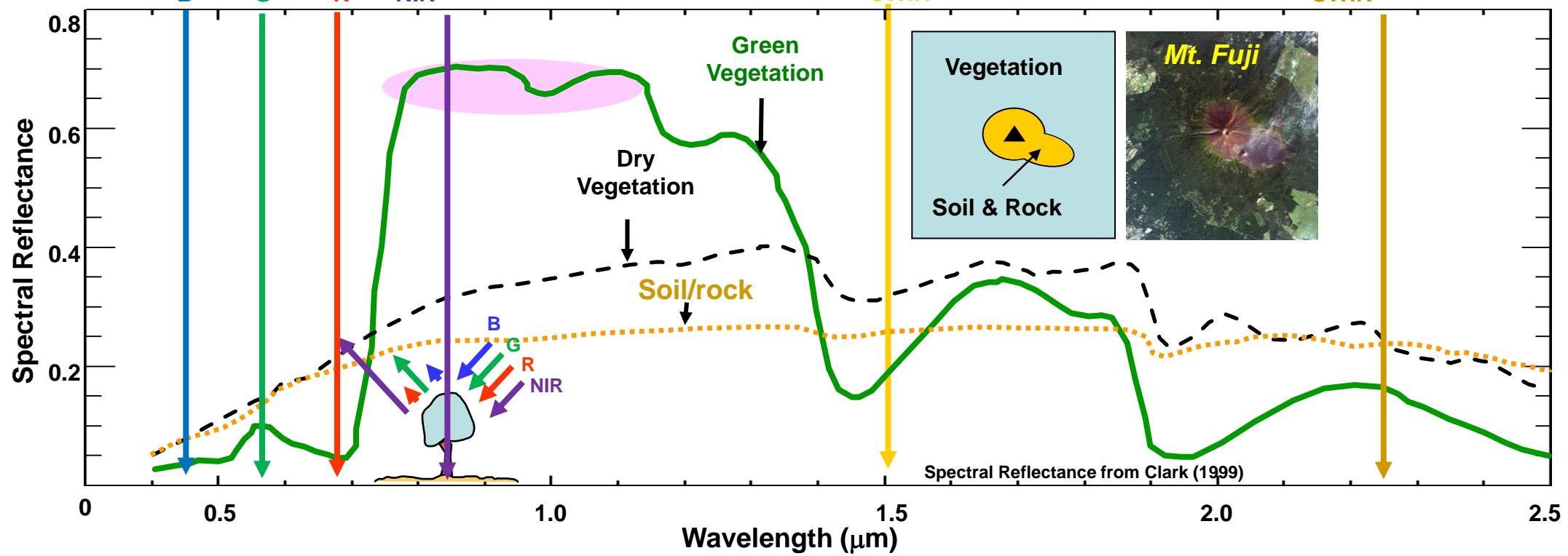
= Fundamental to understanding the appearance of features in multispectral images



Understanding single-band (monochromatic) images of multispectral datasets



Landsat-7 / ETM+ 1 2 3 4 5 6 7

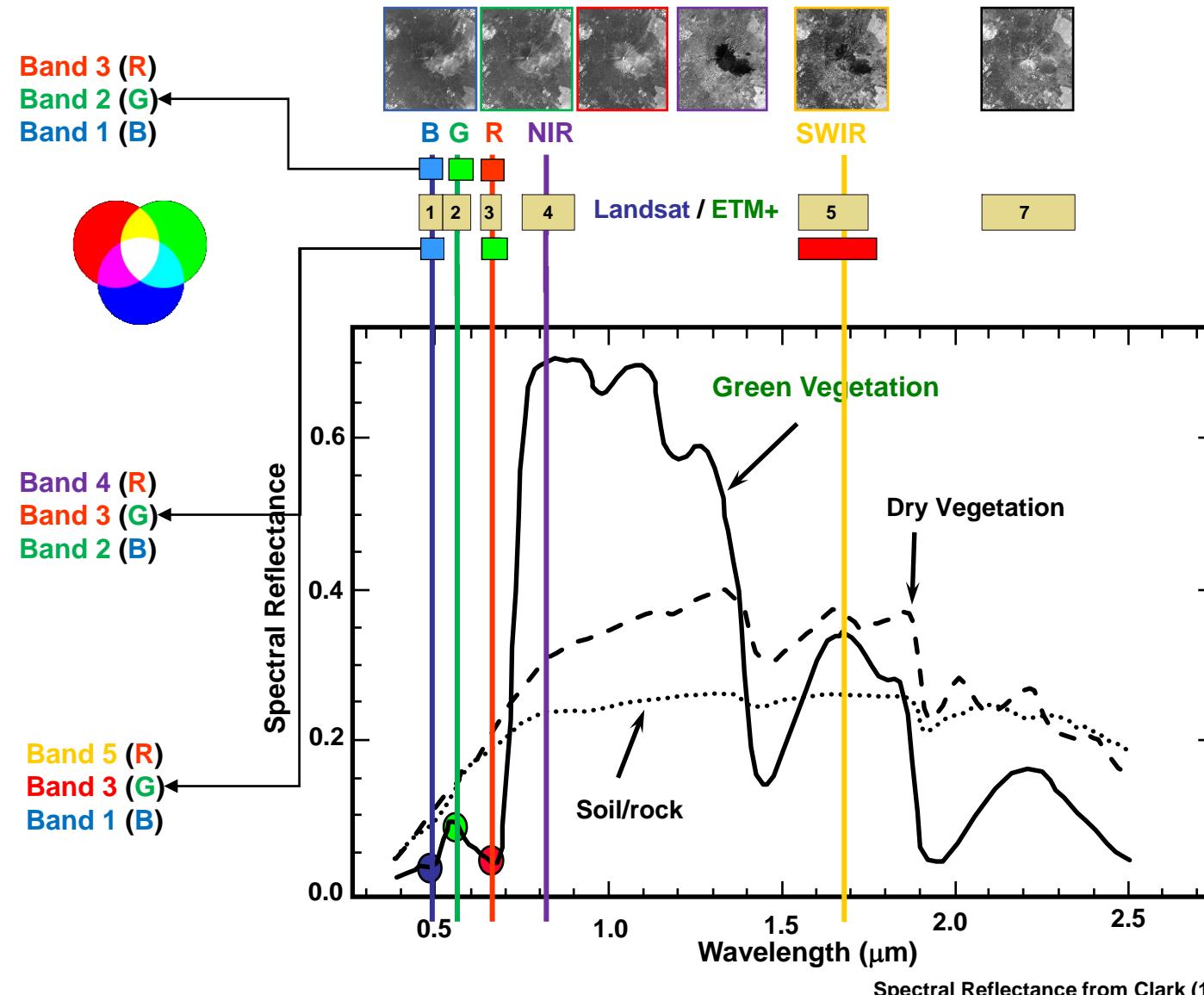


Understanding colour composite images from multispectral datasets

'True Colour' Composite



False Colour Composites



- Multispectral (or 'Broad-band') sensors have a few bands with broad bandwidths defined in microns
- Spectral bands are positioned in atmospheric windows
- Spatial resolutions vary from 10s metres to < 1 m
- Examples: Landsat, Sentinel-2 and most VHR sensors*

[*only WV-3 provides bands beyond VIS-NIR]

2. Algebraic Operations (Multi-band point operations)

- For multi-spectral bands (multi-layer images) algebraic operations, i.e. using the 4 basic arithmetic operations (+, -, ×, ÷), logarithmic, exponential, sin, tan, etc., **can be applied to the DNs of different bands, at each pixel to produce a new image**. Such processing is called an **image algebraic operation**.
- Algebraic operations are performed on each pixel, among DNs of spectral bands (or layers), without involving neighbourhood pixels. They can therefore be considered as **multi-band point operations** defined as:

$$y = f(x_1, x_2, \dots, x_n) \quad \text{where } n \text{ is the number of bands or layers.}$$

- Obviously, all images involved in algebraic operations should be **precisely co-registered**. As the image algebraic operation is entirely pixel-to-pixel based, we can generalise the description in the following sections: let $X_i, i = 1, 2, \dots, n$ represent both the i^{th} band image, and any pixel in the i^{th} band image belongs to an n band image dataset \mathbf{X} , where $X_i \in \mathbf{X}$, and Y is the output image as well as any pixel in the output image.
- NB Unlike contrast enhancement, **algebraic operations are position relevant**; they must be performed on a per-pixel basis.

2.1 Image addition

This operation produces a weighted summation (average) of two or more images:

$$Y = \frac{1}{k} \sum_{i=1}^n w_i X_i$$

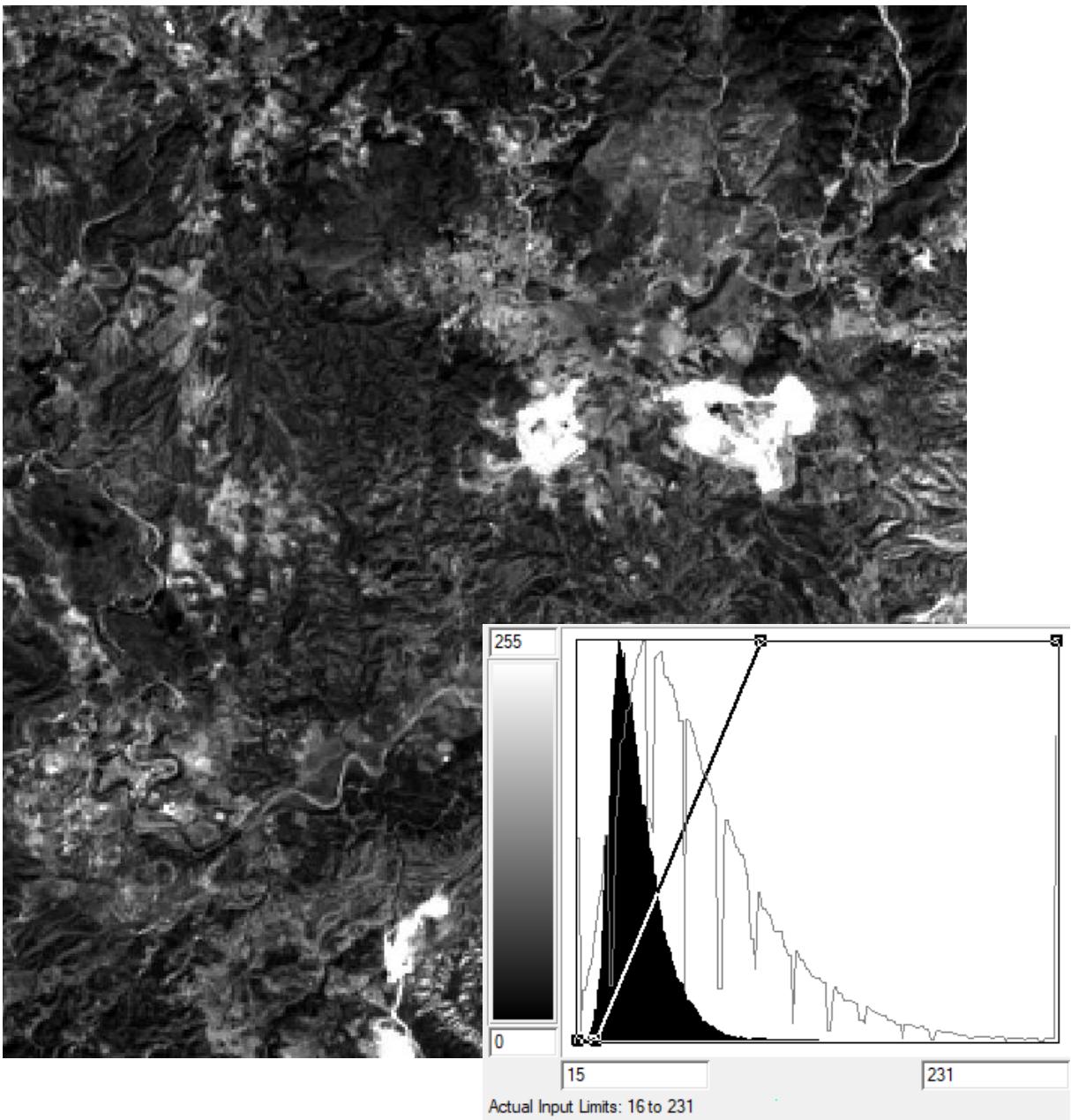
where w_i is the weight of image X_i and k is a scaling factor.

- Important applications of image addition are **noise reduction** and **increasing the signal-to-noise ratio (SNR)**.
- For example, if each image band of an n band multi-spectral image is contaminated by an additive but random noise source, the noise pixels are unlikely to occur at the same positions in each bands and thus a noise pixel DN in band i will be averaged with the non-noise DNs in the other $n-1$ bands.
- As a result, random noise will be largely suppressed. For n duplications of an image each contaminated by a same level of random noise, then the SNR of the summation image of these n duplications is:

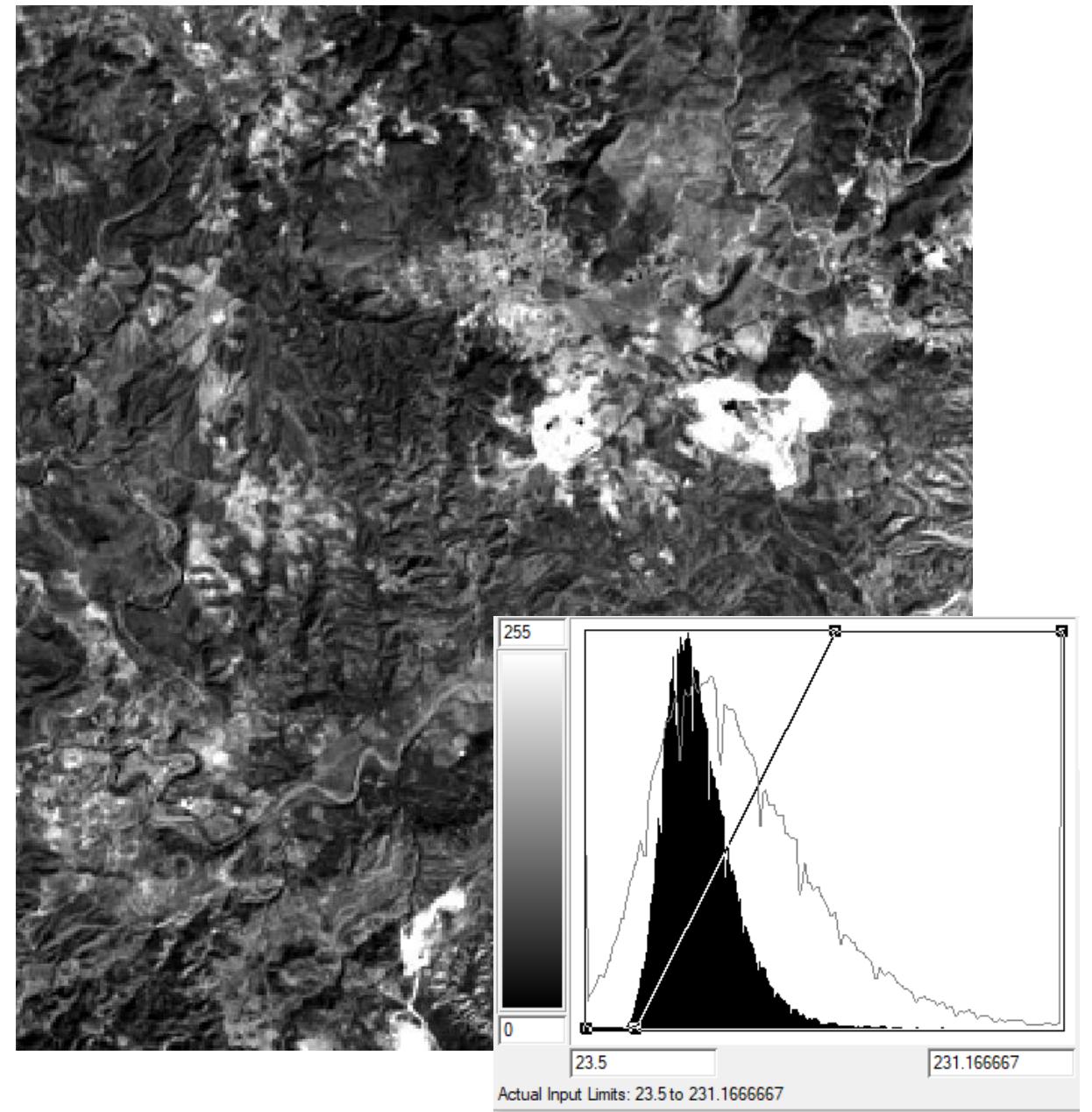
$$SNR_y = \sqrt{n} \cdot SNR_i$$

- This implies that for n -band multi-spectral imagery, the summation of all the bands can increase SNR by about \sqrt{n} times.

Band 1



Weighed summation of bands 1-5 +7

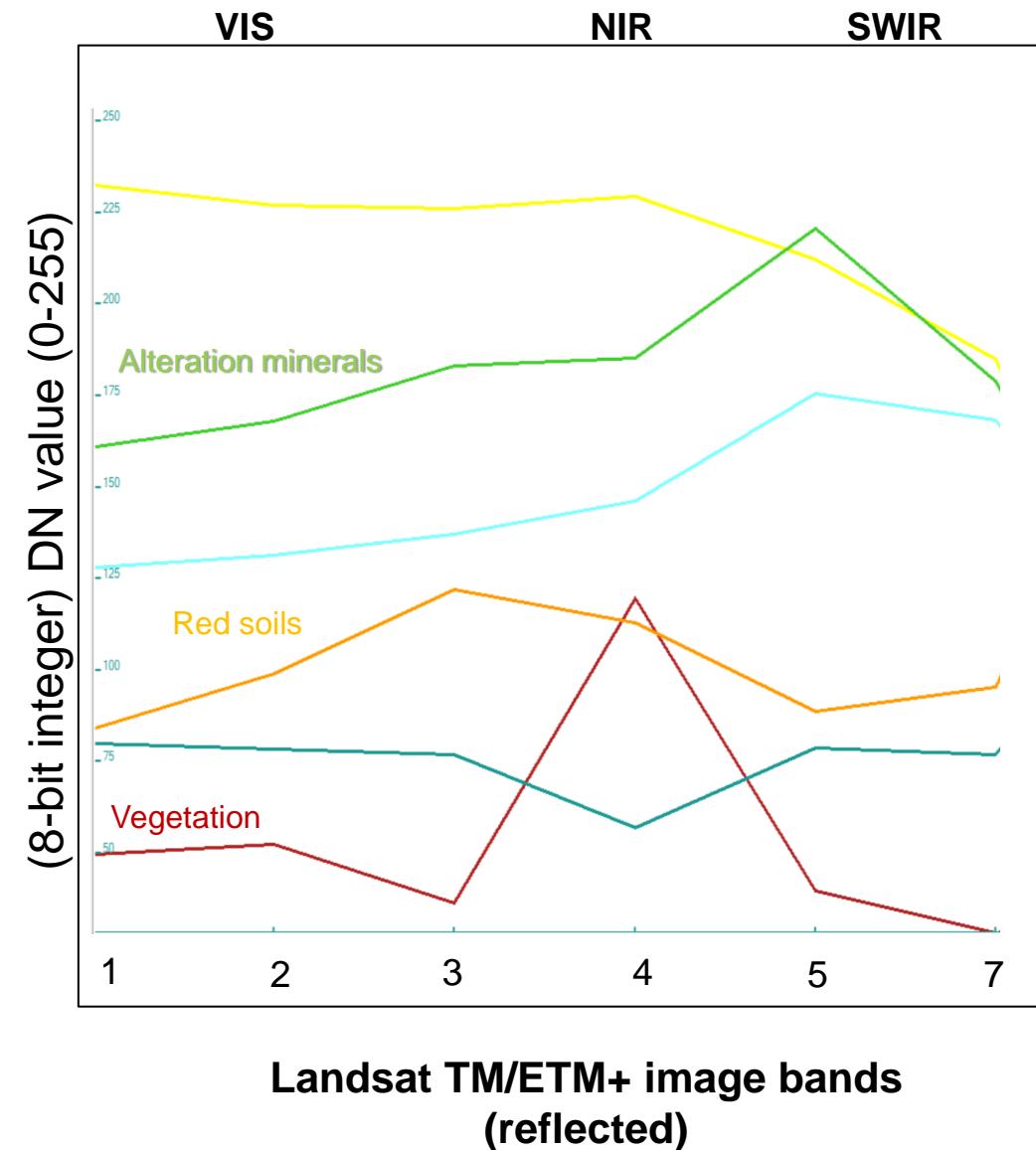


2.2 Image subtraction (Differencing)

Image subtraction produces a difference image from two input images:

$$Y = \frac{1}{k} (w_i X_i - w_j X_j)$$

- The weights w_i and w_j are important to assure a balanced differencing is performed.
 - If the brightness of X_i is significantly higher than that of X_j , for instance, the difference image will be dominated by X_i and the true difference between the two images, per pixel, will not be effectively revealed!
- Subtraction is one of the simplest and most effective techniques for **selective spectral enhancement**. It is also useful for **change detection** and **removal of background illumination bias**.
- In general though, a **subtraction operation reduces the image information and decrease image SNR**.
 - Because image subtraction removes the common features while retaining the random noise in both images.



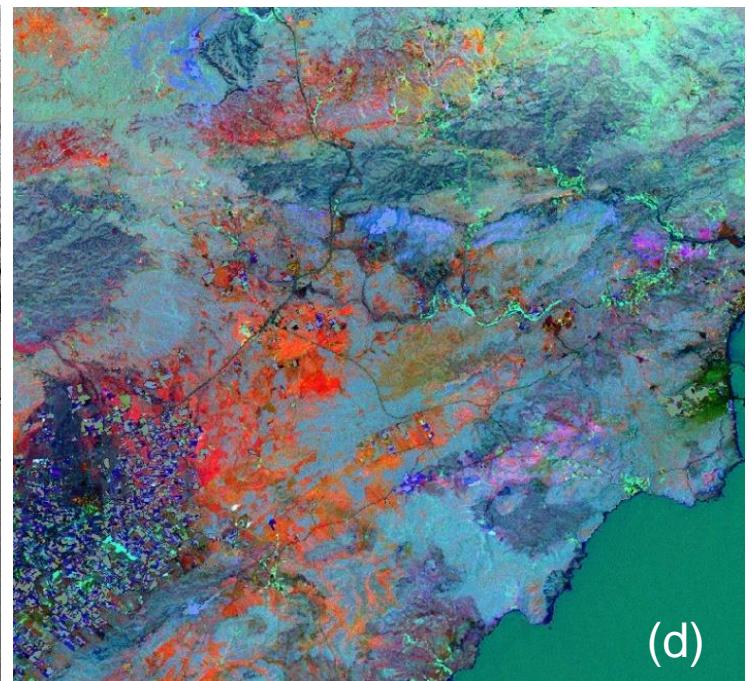
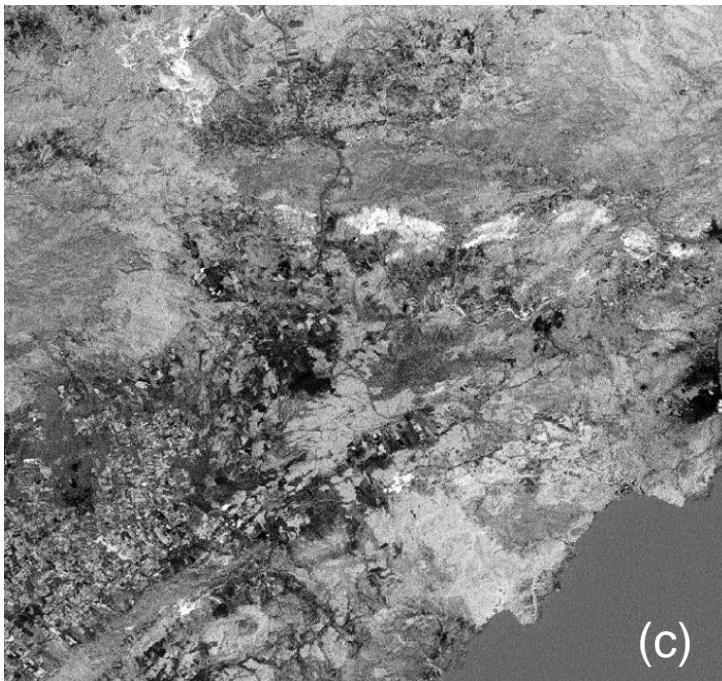
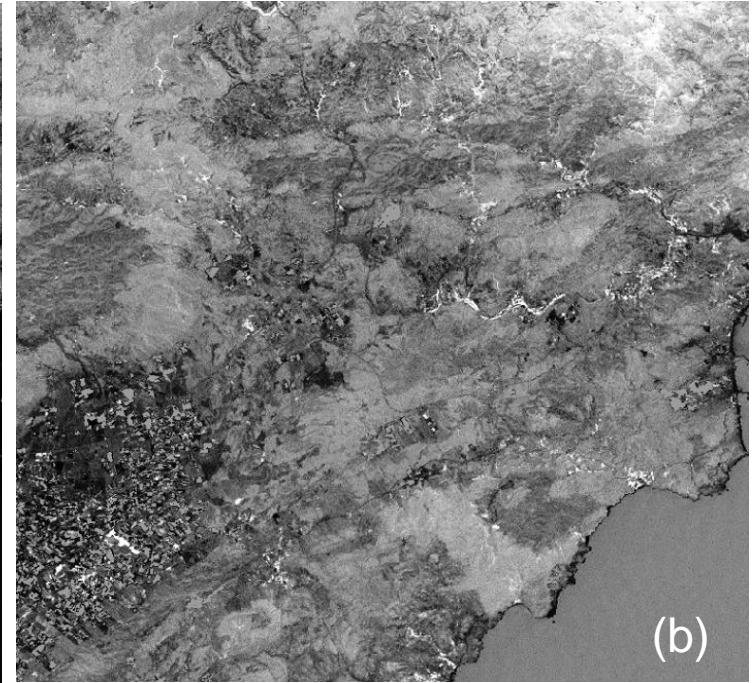
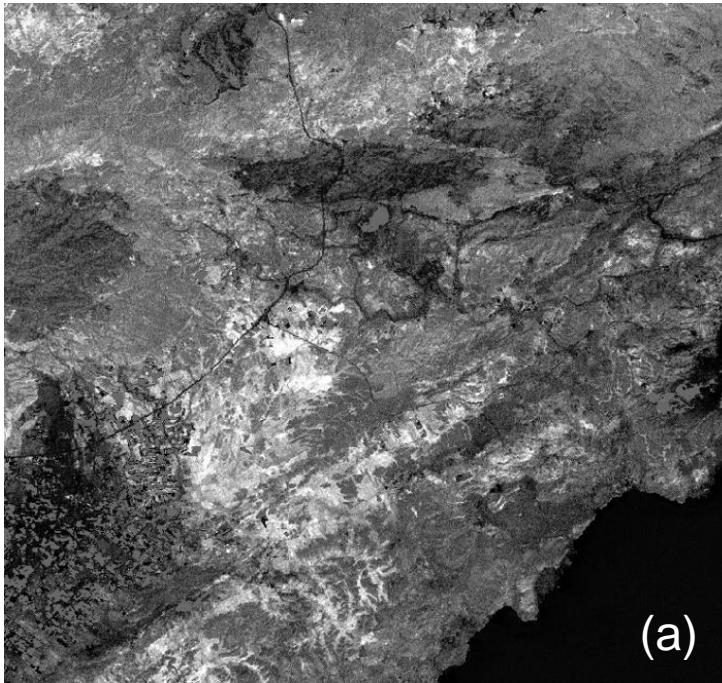
Difference images and colour composite:

- (a) TM3 - TM1 highlights red features often associated with iron oxides.
- (b) TM4 - TM3 detects the diagnostic 'red edge' features of vegetation (chlorophyll).
- (c) TM5 - TM7 enhances hydrated mineral absorption features in SWIR spectral range.

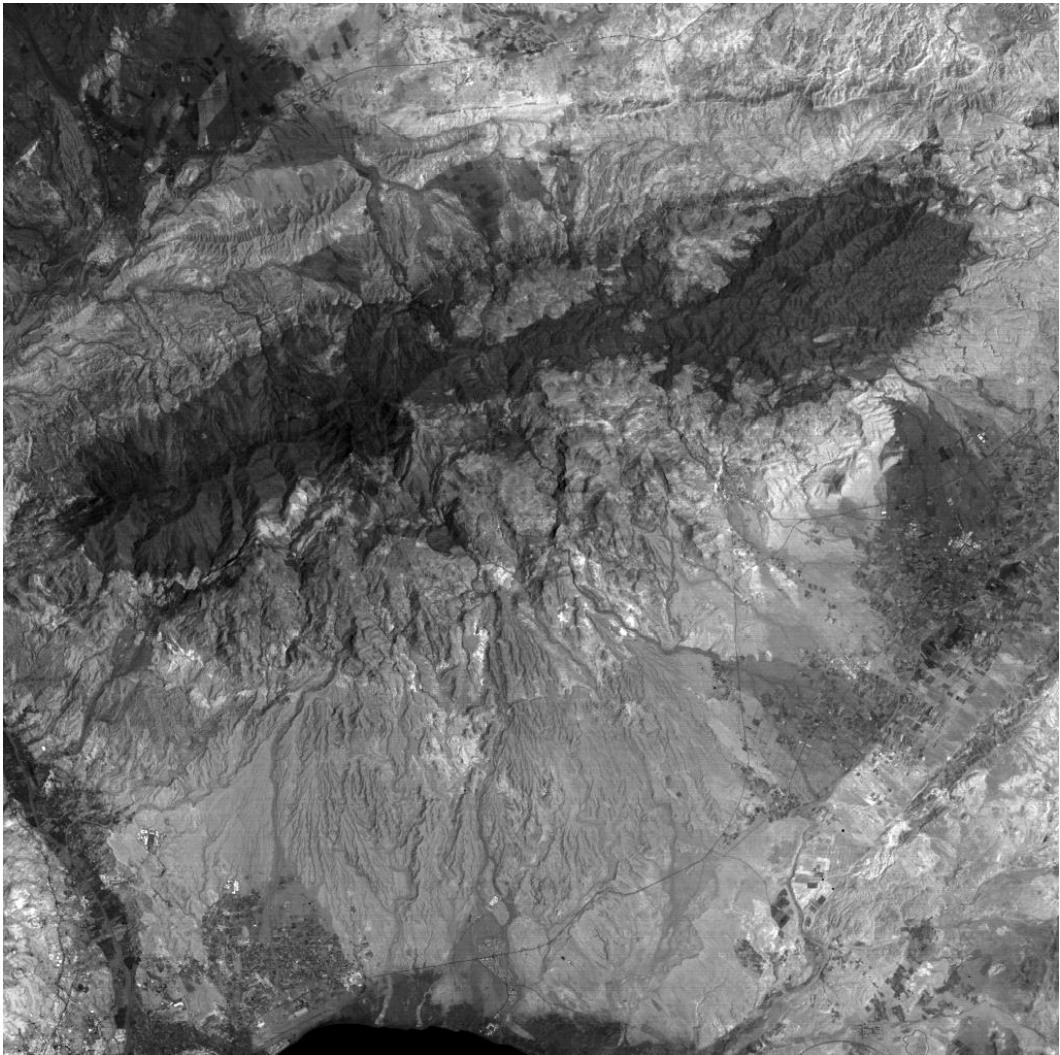
(d) Colour composite of:

- (a) TM3 - TM1 (R),
- (b) TM4 - TM3 (G)
- (c) TM5 - TM7 (B)

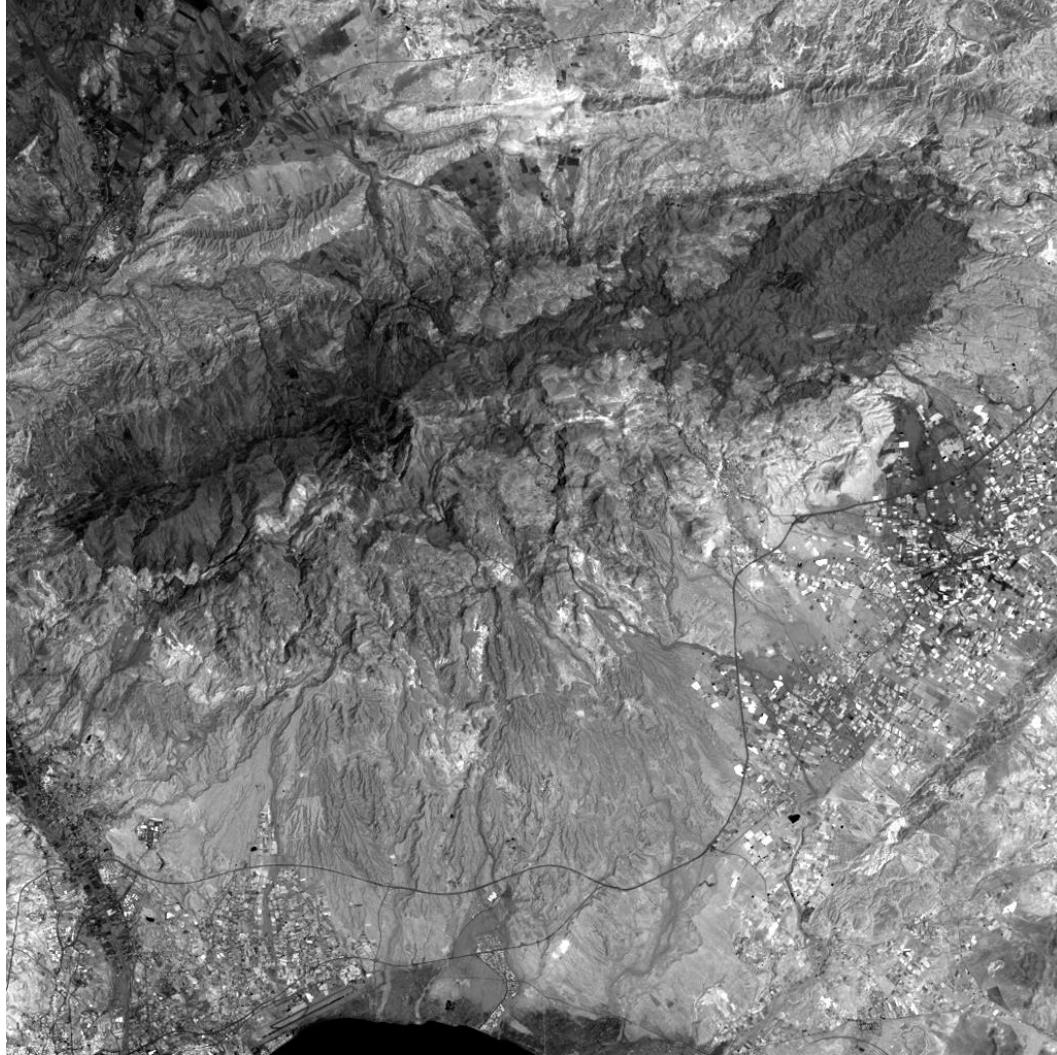
Highlights iron oxide, vegetation and hydrated minerals, in R, G and B colours respectively.



Mapping environmental change by differencing



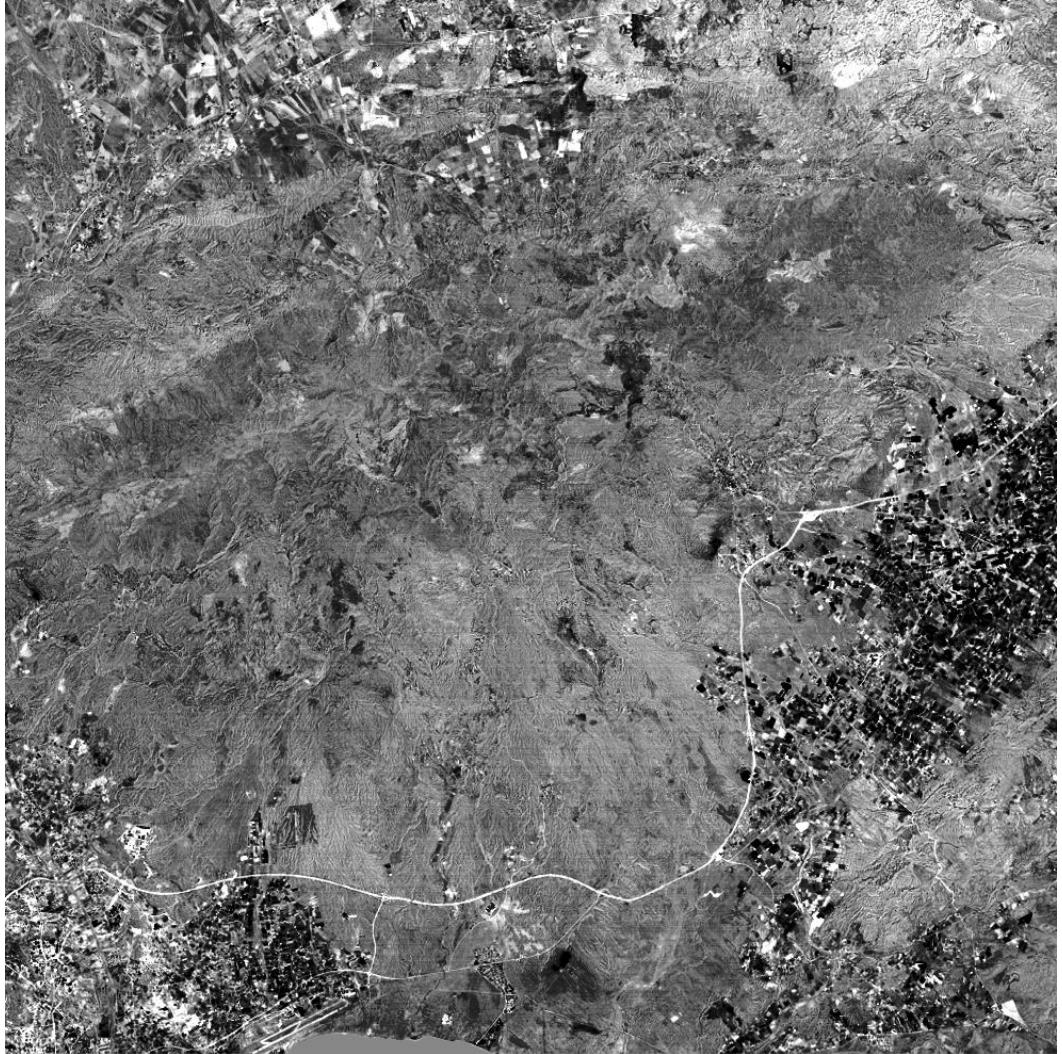
1984 Landsat-4 TM image band 5



1999 Landsat-7 ETM+ image band 5

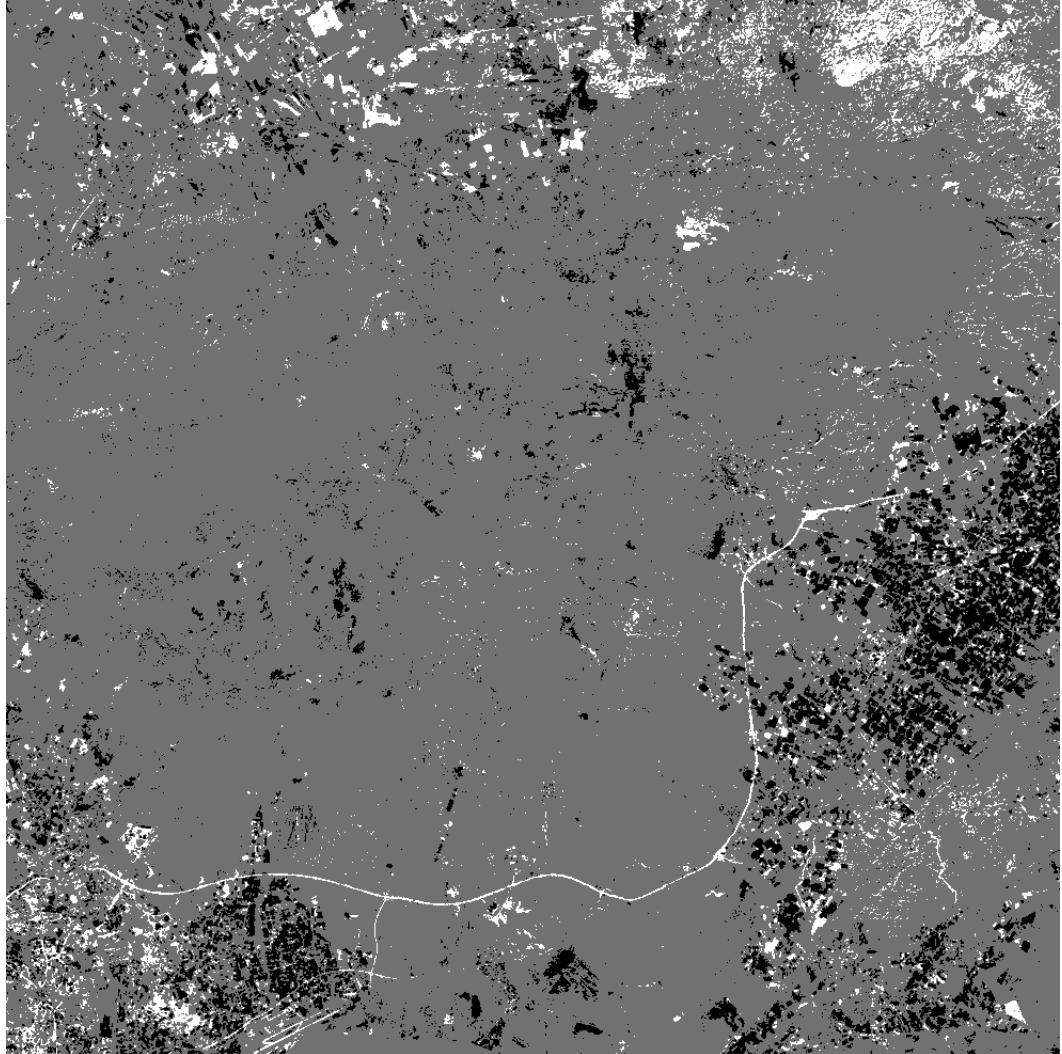
Images have been precisely co-registered on pixel-wise basis – this forces the cancellation of any topographic parallax shift in feature position

Mapping environmental change by differencing



Difference image: 1984 - 1999

Black = features getting brighter from 1984 to 1999; White = features getting darker from 1984 to 1999; Grey = no significant change in brightness.



Thresholded difference image with 3 levels

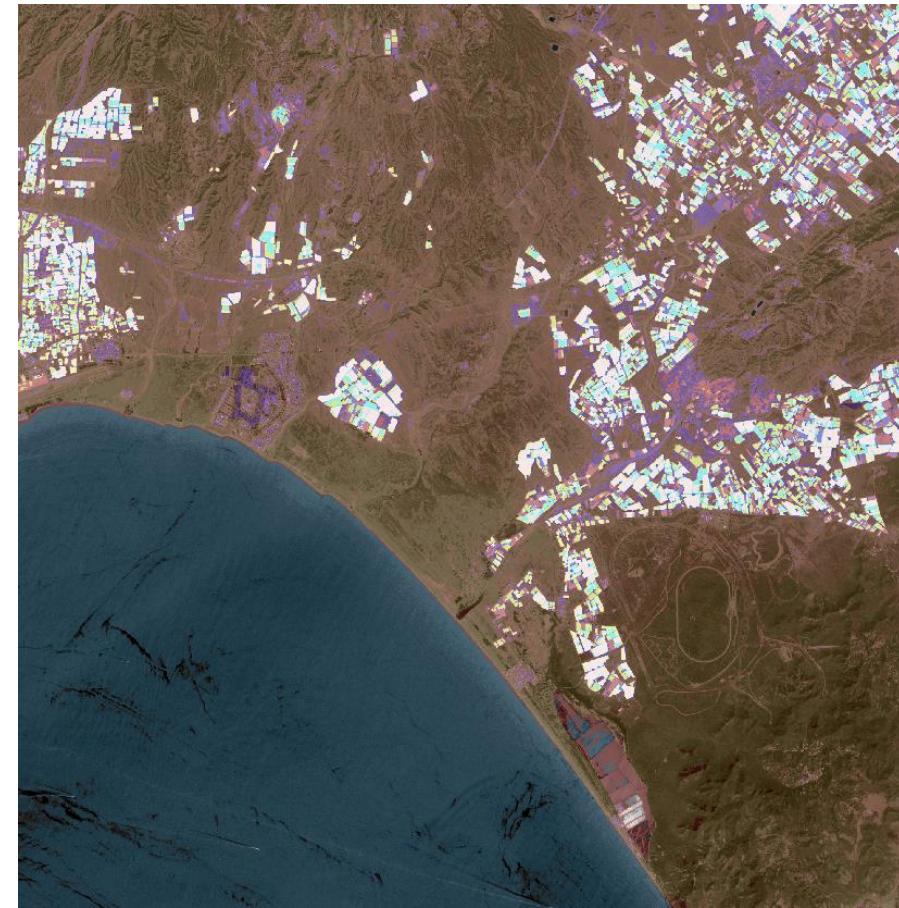
2.3 Image multiplication

$$Y = X_i \cdot X_j$$

- Here image multiplication is performed on each image pixel - band i DN is multiplied by band j DN.
 - NB This is fundamentally different from matrix multiplication
 - remember a digital image is a 2D array, it is **not** a matrix.

Key applications of image multiplication:

- a) **Masking** – e.g. using an image to remove part of another image. For instance, if X_i is a mask image composed of DN values 0 and 1, the pixels in image X_j , which corresponding to 0 in X_i will become 0 (masked or clipped out) and the other DN values remain unchanged in the output image Y .
- This operation can also be done (more efficiently) using a logical operation of a given condition, i.e. *if ... then ... else*
- b) **Modulation** – e.g. using one image to *modulate* another. For instance, topographic shading can be added to a coloured (flat) map or classified image by using a panchromatic image (intensity component) to modulate the three colour components (red, green and blue) of the scanned map or to a pseudocolour classification image as below:



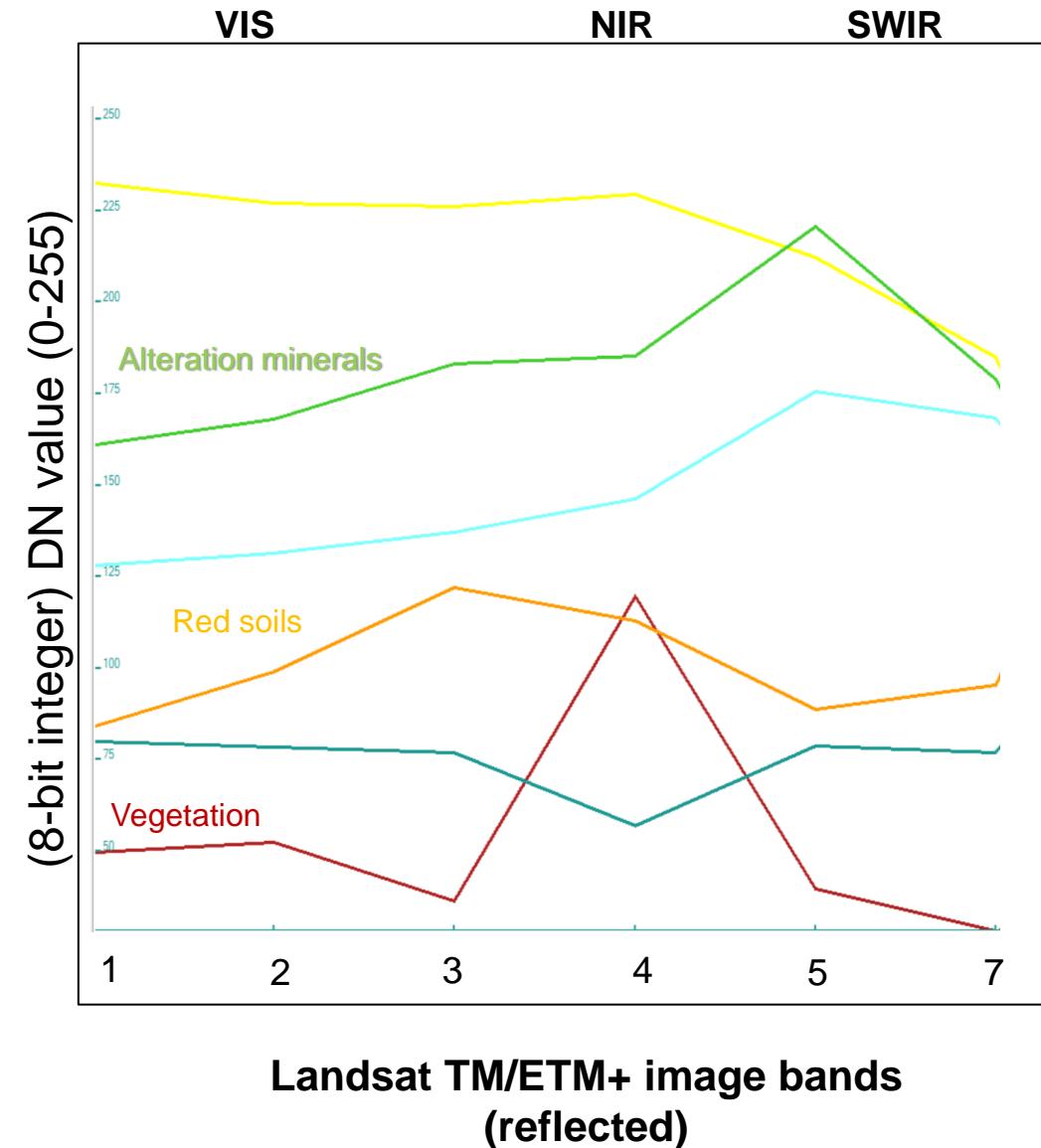
Classification image modulated by intensity of a spectral band – re-introduces some topographic shading.

2.4 Image division (Ratio)

Image division is a very popular technique known as **ratio**. The operation is defined as:

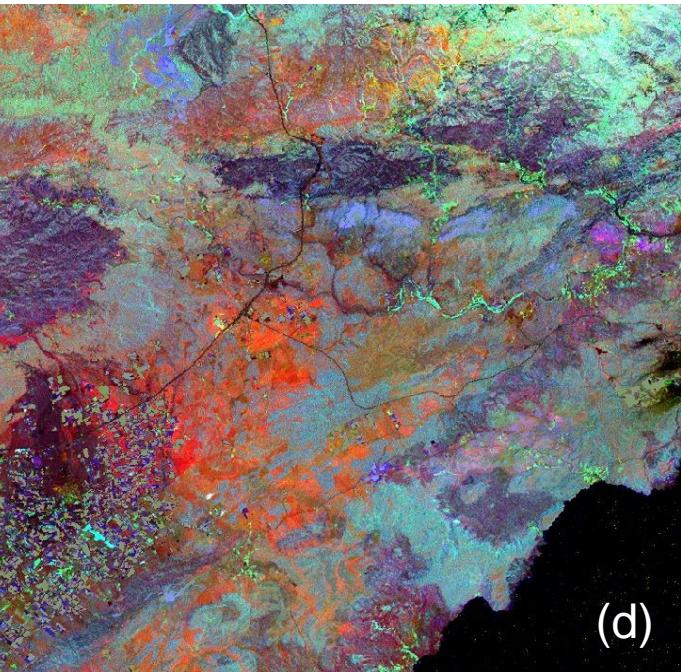
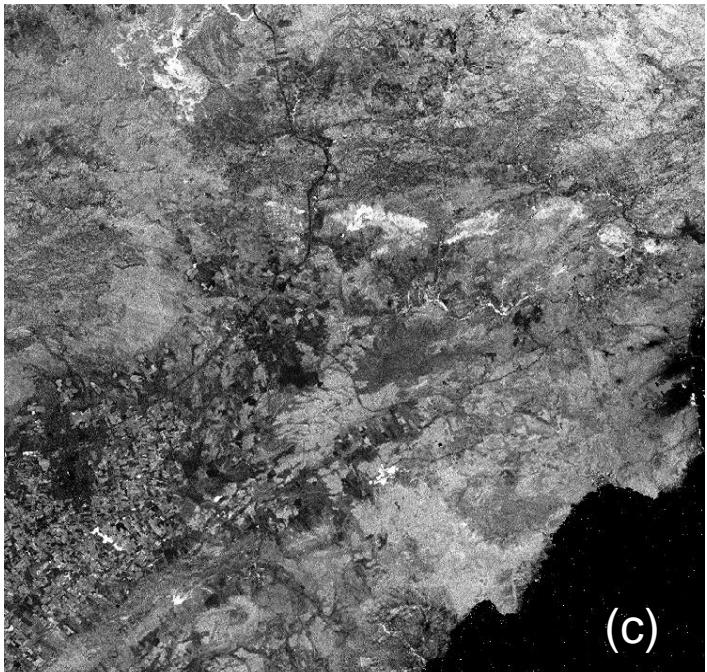
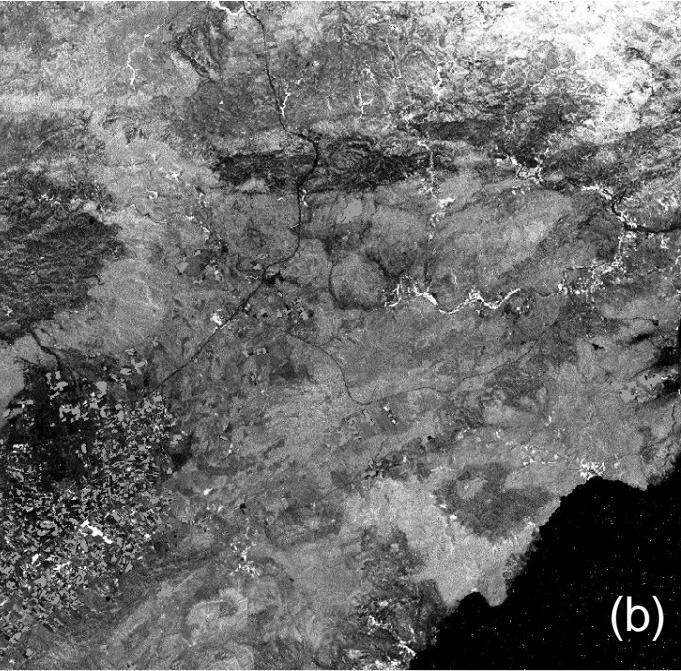
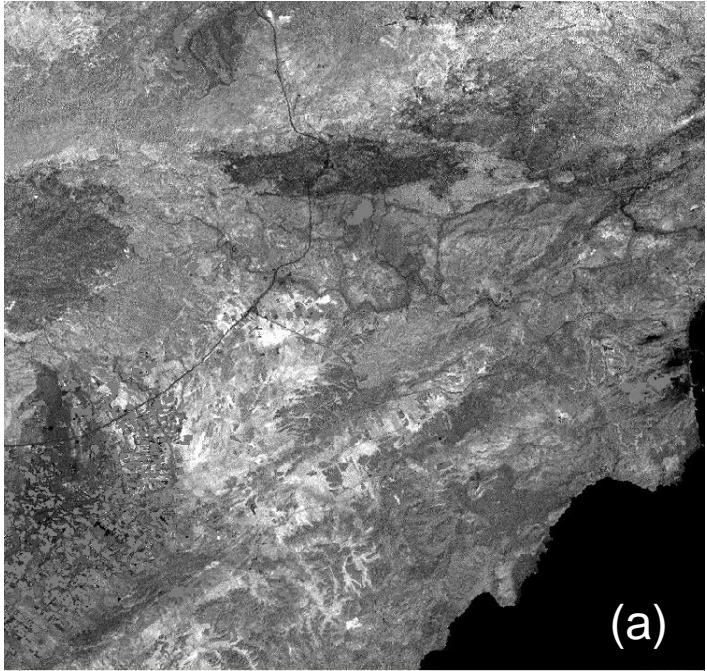
$$Y = \frac{X_i}{X_j}$$

- For processing involving image division, certain protection is usually needed to avoid overflow (where a number is divided by zero).
 - A common trick is to shift up the value range of denominator image by adding 1 to avoid zero.
- The output ratio image Y is an image of real numbers instead of integers.
- NB If both X_i and X_j are 8-bit integer images, the possible output value ranges for Y are 0, $[1/255, 1]$, or $[1, 255]$. The value range $[1/255, 1]$ may contain just as much information as that in the much wider value range $[1, 255]$!
- NB If you then linear stretch the result, you could achieve **significant information loss** because the information recorded in value range $[1/255, 1]$ could be compressed into a very few DN levels. So beware and stretch carefully!



2.4 Image division (Ratio) cont'd

- Ratios are often designed to highlight **particular target features in high value DNs**.
 - Direct stretch of ratio image Y may enhance the target features better, at the cost of losing the information represented by low ratio DNs.
 - Thus it is important to notice that, although ratios TM1/TM3 and TM3/TM1 are reciprocal of each other and contain the same information, they will be different after linear scale contrast enhancement!
- **NB when you design a ratio, make sure the target information has high DN values in the output ratio image (more intuitive).**
- Ratio is very useful for selective enhancement of spectral features. Ratio images derived from different band pairs are often displayed in RGB system to generate ratio colour composites.
 - e.g. a colour composite of TM5/TM7 (blue), TM4/TM3 (green) and TM3/TM1 (red) may highlight clay minerals in blue, vegetation in green and iron oxide in red.
- Many indices, such as Normalised Difference Vegetation Index (NDVI), have been developed based on both differencing and ratio operations.



Ratio images and ratio colour composite:

(a) TM3 / TM1

(b) TM4 / TM3

(c) TM5 / TM7

(d) Ratio colour composite of:

- TM3 / TM1 (R),
- TM4 / TM3 (G)
- TM5 / TM7 (B)

Ratio for suppression of topography

- For a given incident angle of solar radiation, the radiation energy received by an area of land surface **depends on the angle between the land surface and the incident radiation.**
- Therefore, solar illumination on land surface varies with terrain slope and aspect, which causes topographic shadows. The DNs in different spectral bands of a multi-spectral image **are proportional to the solar radiation received by land surface and its spectral reflectance.**
- Let $DN(\lambda)$ represent the digital number of a pixel in an image of spectral band λ , then:

$$DN(\lambda) = \rho(\lambda)E(\lambda)$$

- Where $\rho(\lambda)$ and $E(\lambda)$ are the spectral reflectance and irradiance of spectral band λ . Irradiance is the total solar radiation received at the land surface corresponding to the pixel.

- Suppose a pixel representing a land surface facing the sun ($DN2$) receives n times radiation energy received by another pixel on the land surface facing away from the sun ($DN1$), then the DNs of the two pixels in spectral bands i and j are as below.

Shaded pixel:

$$DN1(i) = \rho(i)E(i) \quad DN1(j) = \rho(j)E(j)$$

Illuminated pixel:

$$DN2(i) = n\rho(i)E(i) \quad DN2(j) = n\rho(j)E(j)$$

Shaded ratio:

$$R1_{i,j} = \frac{DN1(i)}{DN1(j)} = \frac{\rho(i)E(i)}{\rho(j)E(j)}$$

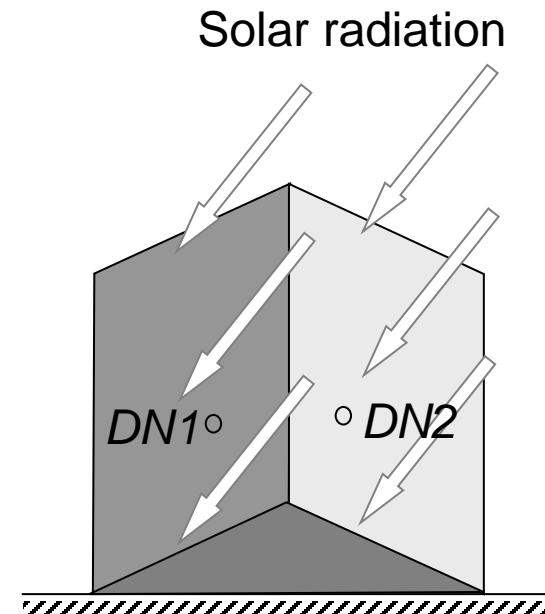
Illuminated ratio:

$$R2_{i,j} = \frac{DN2(i)}{DN2(j)} = \frac{n\rho(i)E(i)}{n\rho(j)E(j)} = \frac{\rho(i)E(i)}{\rho(j)E(j)}$$

Therefore:

$$R1_{i,j} = R2_{i,j}$$

- Result = topographic shading is suppressed by ratio
- Since topography often accounts for more than 90% information of a multi-spectral image, ratio images therefore **reduce SNRs significantly**.



3. Spectral index derivation & supervised enhancement

- **Unlimited combinations** of algebraic operations can be derived using basic arithmetic operations and algebraic functions.
- For a meaningful and effective operation, knowledge of the **spectral properties of the target** is essential.
 - Formulae composed for the enhancement of particular targets are known as **indices or spectral indices**, e.g. the Normalised Difference Vegetation Index (NDVI), or a ***band-depth index*** (e.g. $(b1+b2)/b3$)
 - Spectral indices are guided by physical principles and can therefore be considered a kind of '***supervised enhancement***'.
- Here we briefly introduce a few commonly used spectral indices based on Landsat TM/ETM+ image data.
- You can design your own indices for any given image processing objective, based on the spectral properties of the target.

3.1 Vegetation Indices

- Healthy vegetation has a high reflection peak in near infrared (NIR) and an absorption trough in red (R) because of the spectral properties of chlorophyll.
- If we could see NIR, vegetation would be NIR rather than green (and very bright). This significant difference in brightness between R and NIR bands is called the '**red edge**' that is a unique spectral property making photosynthesising vegetation distinctively different from all other ground objects.
- This diagnostic spectral feature of vegetation can be very effectively enhanced by both differencing and ratio operations.

Vegetation Ratio Index
(VRI):

$$VI = \frac{NIR - \text{Min}(NIR)}{Red - \text{Min}(Red) + 1}$$

Normalised Difference
Vegetation Index (NDVI):

$$NDVI = \frac{NIR - Red}{NIR + Red}$$

Green Normalized
Difference Vegetation

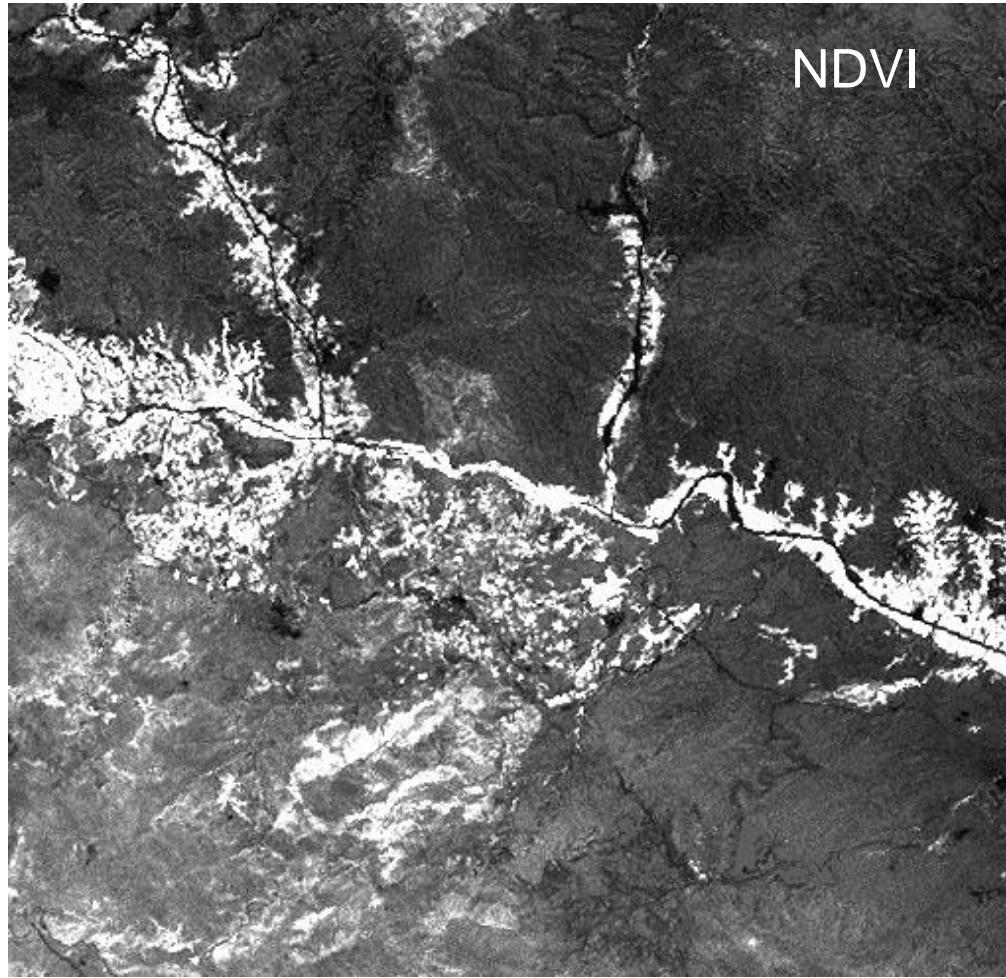
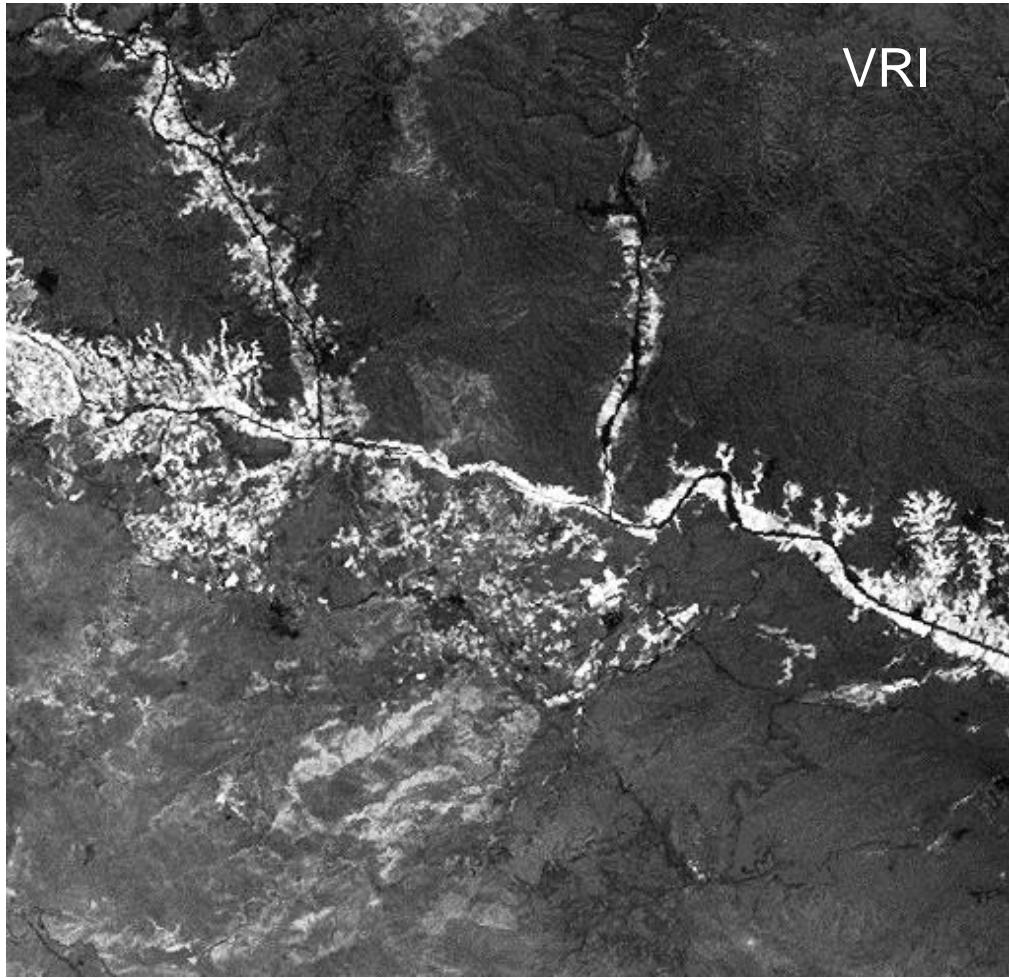
$$NGDVI = \frac{NIR - Green}{NIR + Green}$$

SAVI, (Soil Adjusted
Vegetation Index)

$$SAVI = \frac{(1 + L)(NIR - Red)}{(NIR + Red + L)}$$

where L is a canopy background adjustment factor. An L value of 0.5 has been found to minimize soil brightness variations and eliminate the need for additional calibration.

Vegetation Indices



There are several other variations on the NDVI theme, e.g. **SAVI** (Soil Adjusted Vegetation Index), **NDWI** (Normalised Difference Water Index), **EVI** (Enhanced Vegetation Index, and **NDSI** (Normalised Difference Snow Index)

Other well-known spectral indices

NDWI, (Normalised Difference Water Index)

$$\text{NDWI} = \frac{(X_{nir} - X_{swir})}{(X_{nir} + X_{swir})}$$

$$\text{NDWI} = \frac{(X_{green} - X_{nir})}{(X_{green} + X_{nir})}$$

BI, Brightness Index (of soils)

$$BI = \sqrt{\left(\frac{(X_{red} * X_{red})}{(X_{green} * X_{green})} \right)^2}$$

NDSI, (Normalised Difference Snow Index)

$$NDSI = \frac{(X_{green} - X_{swir})}{(X_{green} + X_{swir})}$$

- Water content in leaves (Gao, 1996).
- In land areas, this also serves as a Normalized Burn Ratio (BNR)
- Water in water bodies (liquid water)



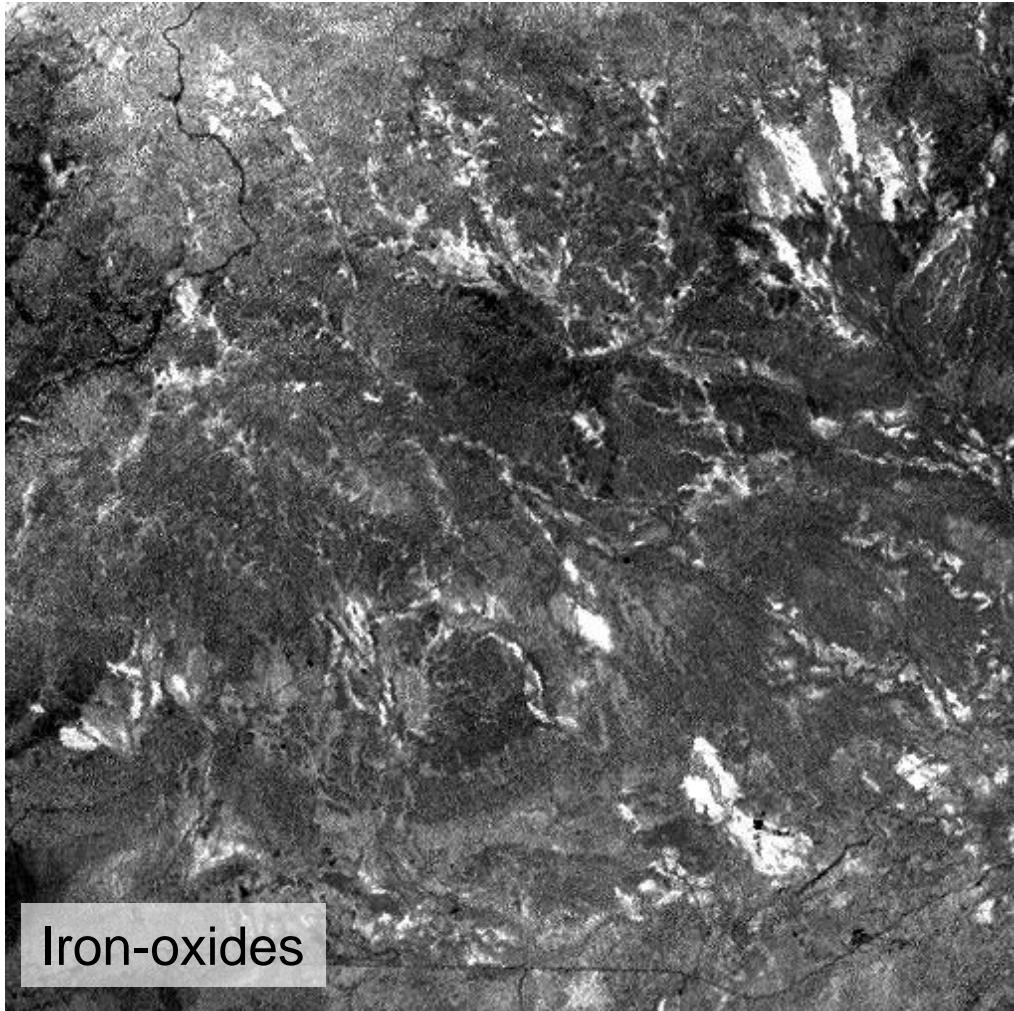
At 1.6 μm, snow absorbs sunlight, and so it appears darker than clouds, so you can distinguish between the two brightest objects affecting image brightness, and remove the ice & snow

3.2 Iron-oxide spectral index

- Iron-oxides are one of the most common and widely spread mineral groups in the natural environment.
- e.g. red or reddish brown soils and rocks: as a result of high reflectance in Red and absorption in Blue parts of the spectrum.
- Red soils are closely associated with natural iron-oxides & hydroxides (weathering) and with hydrothermal alteration
- We can enhance iron-oxides using the ratio between red and blue spectral band images.

$$Y = \frac{Red - \text{Min}(Red)}{Blue - \text{Min}(Blue) + 1}$$

$$Y = \frac{TM\ 3 - \text{Min}(TM\ 3)}{TM\ 1 - \text{Min}(TM\ 1) + 1}$$

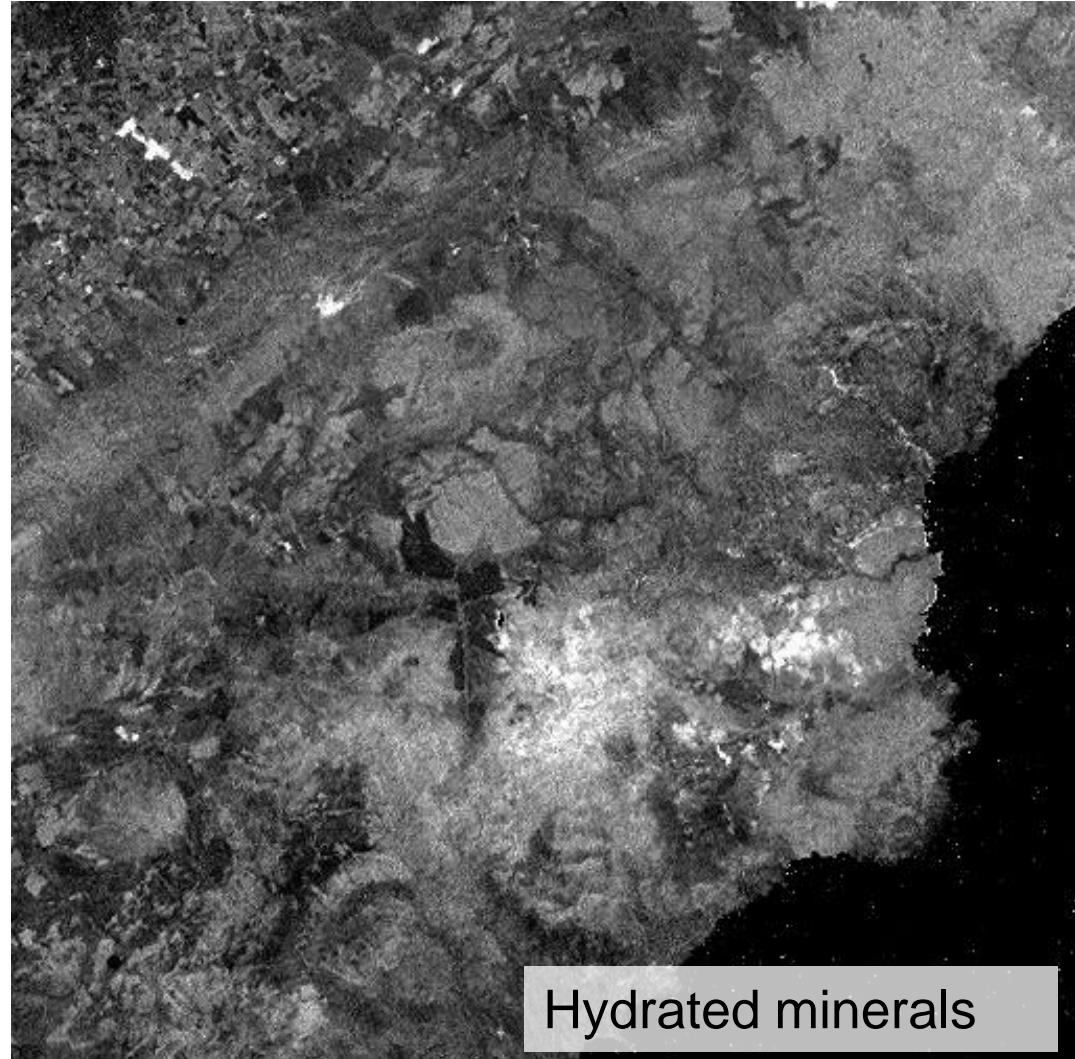


3.3 Hydrated mineral ratio index (OH- present in mineral structure)

- Hydrated minerals are effective indicators of chemical weathering, rock & mineral alteration in the presence of water, which are useful for mineral exploration using remote sensing.
- The typical spectral signature making hydrated minerals different from unaltered rocks is that they all have strong reflectance in SWIR $\sim 1.66 \mu\text{m}$ (corresponding to TM band 5) and strong absorption $\sim 2.2 \mu\text{m}$ (corresponding to TM band 7) – more on this later
- Thus all hydrated minerals can be enhanced by the ratio between these two SWIR bands (TM5 & TM7).

$$Y = \frac{SWIR1 - \text{Min}(SWIR1)}{SWIR2 - \text{Min}(SWIR2) + 1}$$

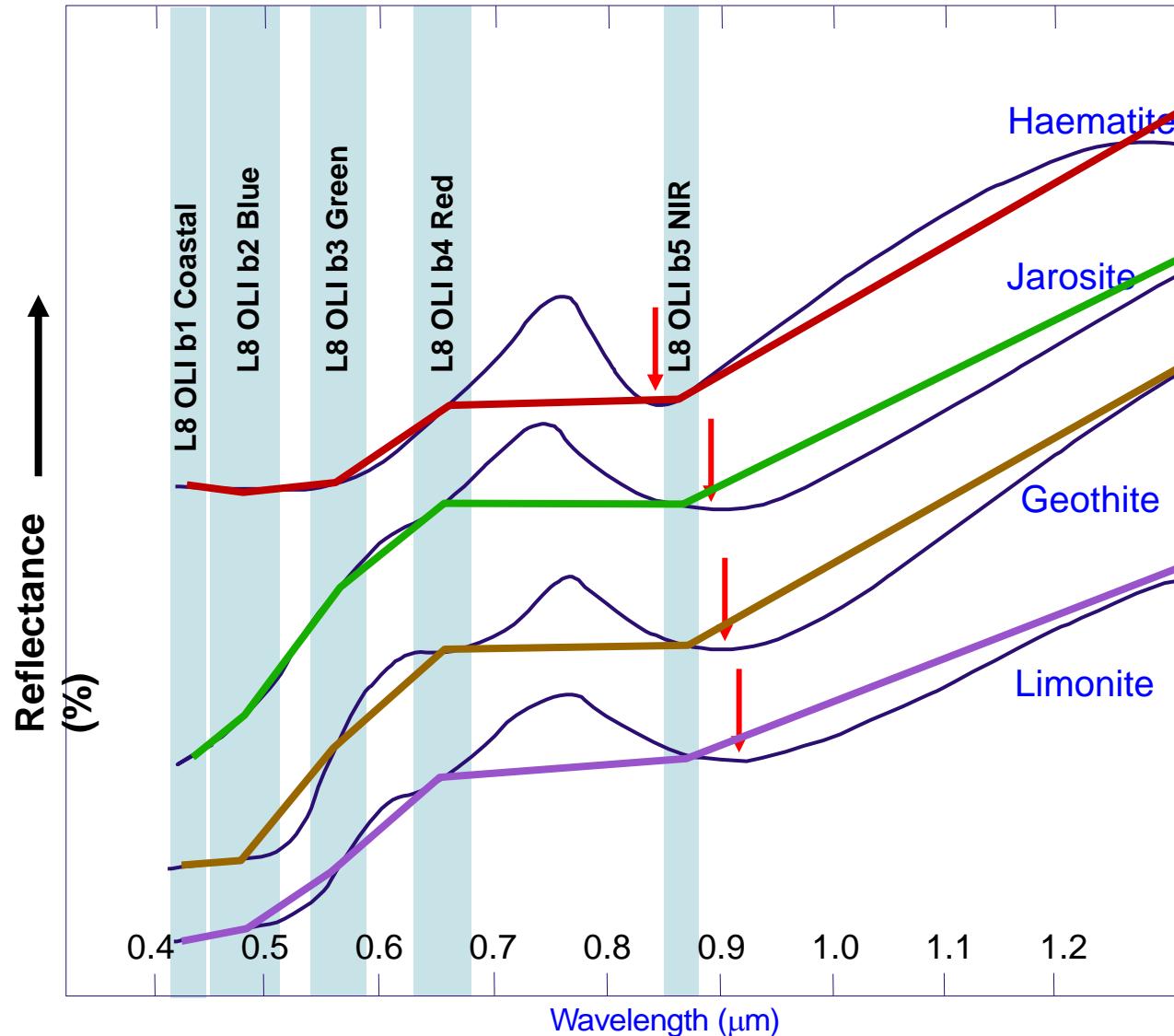
$$Y = \frac{TM5 - \text{Min}(TM5)}{TM7 - \text{Min}(TM7) + 1}$$



Iron oxides/hydroxides spectral indices & Landsat 8 & 9 OLI

Landsat 8 OLI :

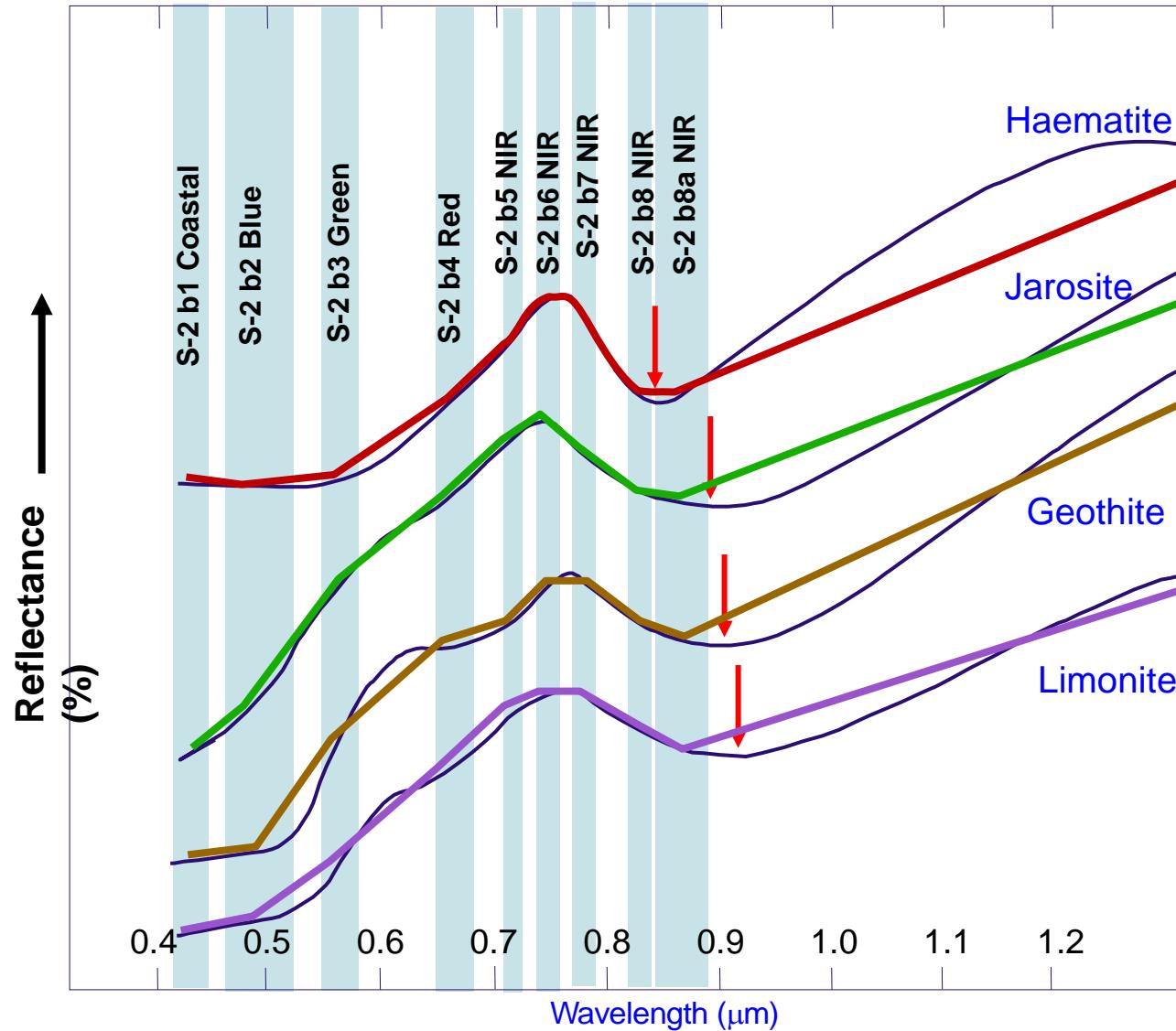
- Band widths are much narrower
- Extra Coastal (new b1) added
- Allows better discrimination (potentially)
- $-(b_1+b_2+b_3)/(i_4+i_5)$ haematite
- b_3/b_2 or b_4/b_2 goethite & jarosite
- B_4/b_1 jarosite (possibly)



Iron oxides/hydroxides spectral indices & Sentinel-2

Sentinel-2:

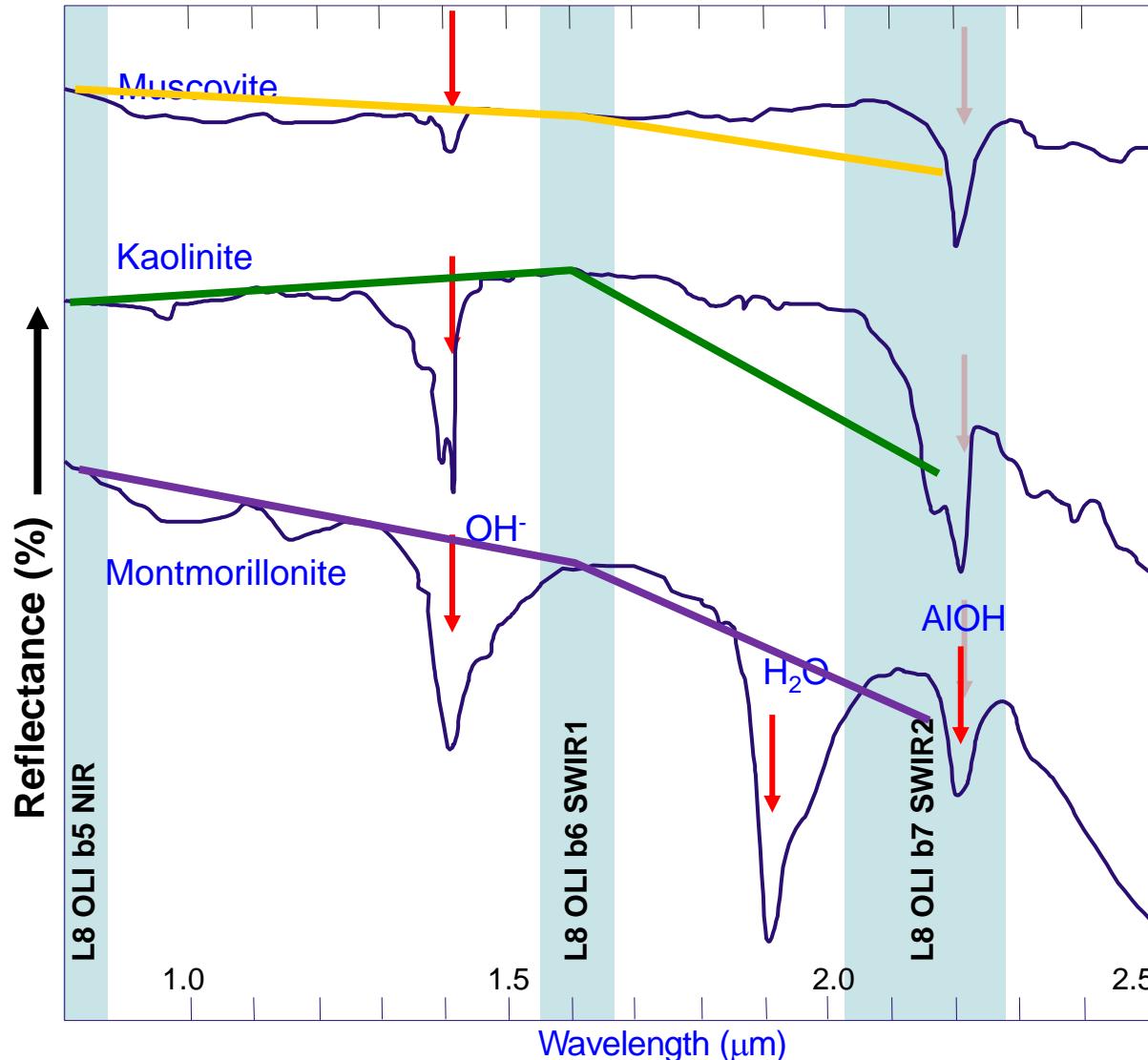
- Similar to Landsat 8
- More VNIR bands and narrower bandwidths
- Allows potentially much better discrimination (and possibly identification)
- Treating STL-2 as a hyperspectral sensor may allow better discrimination/identification



Hydrated minerals spectral indices & Landsat 8 & 9 OLI

Landsat 8 OLI :

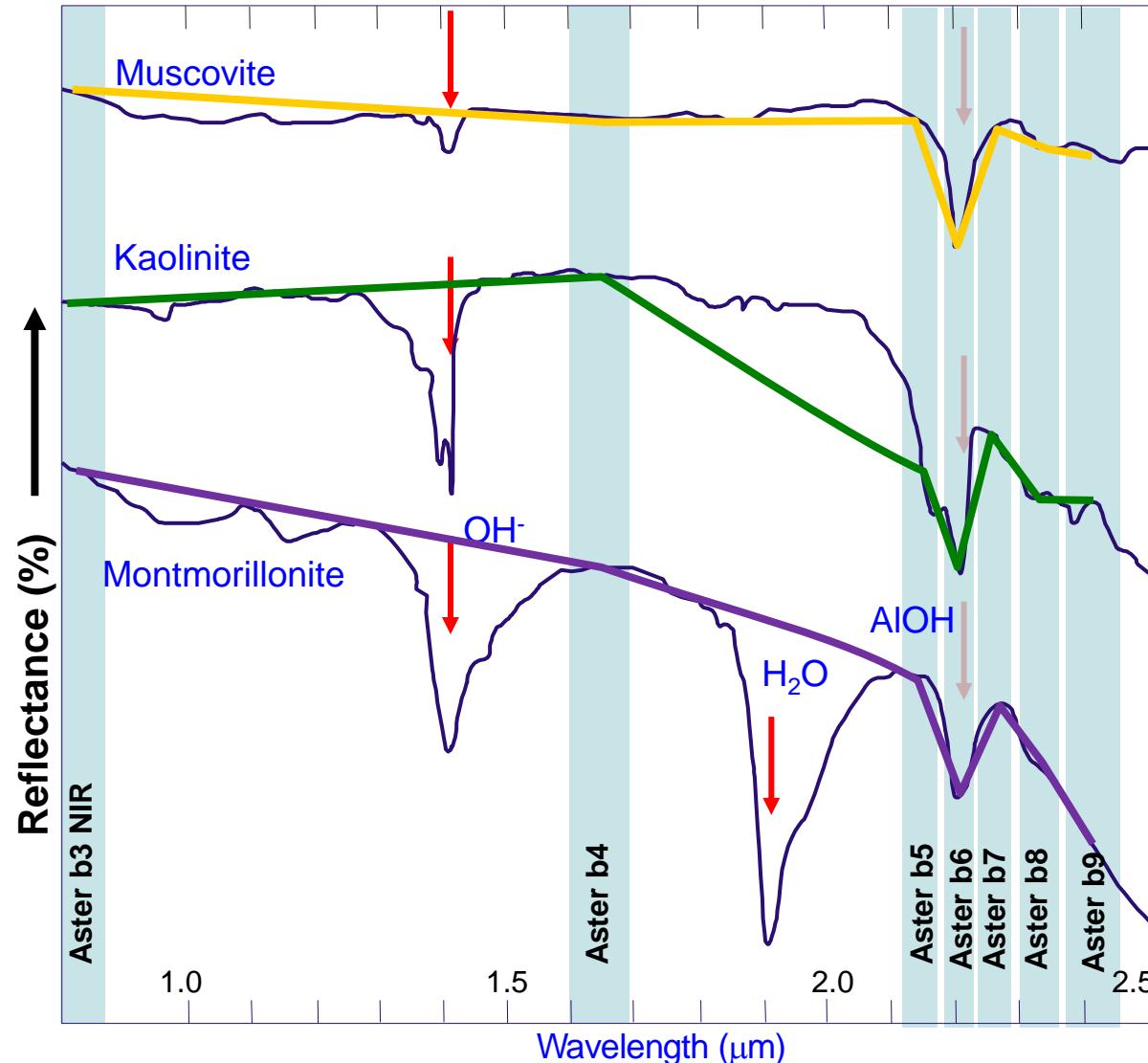
- There are still only 2 SWIR bands....
- Band widths narrower than L5 & 7
- Still only allows discrimination of general clays
- Confusion with carbonates around 2.2 mm region
- Made more tricky if vegetation present



Hydrated minerals spectral indices & ASTER

ASTER with 6 SWIR bands

- Allows discrimination of mineral groups and associations which are important in exploration
- Separable groups include:
 - Kaolinite/alunite & pyrophyllite
 - Muscovite-sericite/illite
 - Biotite/phengite
 - Montmorillonite/smectite
 - Chlorite
- Argillic, advanced argillic, silicic and propylitic alteration styles can be separated



Python resources

For the ultimate guide to spectral indices, try this

- <https://github.com/awesome-spectral-indices/awesome-spectral-indices>

For a set of spectral indices with GUI

- <https://github.com/rander38/Remote-Sensing-Indices-Derivation-Tool>

2.6 Summary

- In this chapter, we learnt simple arithmetic operations between images and discussed their major applications for image spectral enhancement.
- The key point is that all the image algebraic operations are point based and performed among the corresponding pixels in different images without involvement of neighbourhood pixels. We can therefore regard algebraic operations as ***multi-image point operations***.
- A major application of image algebraic operations is for selective enhancement of spectral signatures of particular target materials in a multi-spectral image.
- For this purpose, investigating the spectral properties of these targets is essential to compose effective algebraic operations rather than just ‘having a go’.
- This process, from spectral analysis to composing an algebraic formula, is generally called ***supervised enhancement***. If such a formula is not image scene dependent and can be widely used, it is called an ***index*** image, for instance, NDVI is a well known vegetation index image.

2.7 Revision Questions

1. Why is an image algebraic operations also called a multi-image point operation? Write down the mathematical definition of the multi-image point operation.
2. Why does image addition improves image SNR? Using a stationary camera to take 9 pictures of the same scene under identical illumination conditions and then summing them to then generate an average image, by how many times is the SNR is improved in comparison with any an individual picture?
3. Describe image difference (subtraction) and ratio (division) operations and compare the two techniques in terms of change detection, selective enhancement and processing efficiency.
4. What is the importance of the weights in image subtraction? Suggest the most desirable pre-processing step for image differencing...
5. Why does image differencing decrease the SNR?
6. Describe image multiplication and its major application.
7. Explain the characteristics of the value range of a ratio image. Do you think that two reciprocal ratio images contain the same information when displayed after a linear stretch, and explain why?
8. Using a diagram to describe ratio image as a coordinate transformation from a Cartesian coordinates system to a polar coordinates system.
9. Explain the principle of topographic suppression using image ratio technique.
10. What is the NDVI and how it is designed? Explain the different functionalities of differencing and ratio operations in NDVI.
11. Describe the design and functionality of TM or ETM+ iron oxide and hydrated mineral (incl. clay & gypsum) indices.
12. Try the normalised differencing approach, similar to NDVI, to enhance iron oxide and clay minerals. Compare the results with the corresponding ratio indices and explain why the ratio based indices are more effective for these two minerals?

Working with Earth Observation data using open-source python tools

Make a working environment for your raster processing

You will need to install the following packages (e.g. from conda or conda-forge) since they will be used often:

- [rasterio](#) Reads and writes geospatial raster datasets
- [matplotlib](#) Publication quality figures, images, plots etc
- [pandas](#) Data structures for data analysis, time series, and statistics
- [geopandas](#) Geographic pandas extensions, includes projection between coordinate systems
- [shapely](#) Manipulation and analysis of planar geometric objects. Uses o-s geometry library [GEOS](#)
- [folium](#) For visualising geospatial data
- [gdal \(or libgdal\)](#) Translator library for geospatial data formats (published by Open Source Geospatial Foundation)
- [earthpy](#) Utility functions for the working with spatial data in the Earthpy tutorial set

Installing these may take some time!!

NB We have noticed that descartes=1.1.0 and shapely=1.8.4 and geopandas=0.9.0 will function together, but other versions may not

And for all kinds of ML clustering and classification, there is also Scikit-learn

Working with Earth Observation data using open-source python tools

There could be various reasons why GDAL (Geospatial Data Abstraction Library) might not install properly in JupyterLab. Here are some common issues and potential solutions:

1. Install GDAL: Ensure you are using the correct installation method. You can install GDAL using package managers like **conda** or **pip**.

- **conda install -c conda-forge gdal**
- **pip install gdal**

2.Compatibility: Check for compatibility issues between GDAL, its dependencies, and your JupyterLab environment. Sometimes, there might be conflicts or dependencies that are not compatible with each other. Ensure that the versions you're installing are compatible with your Python version and other packages.

3.System Environment: GDAL might have system-level dependencies that need to be installed separately. Ensure that the necessary system-level dependencies for GDAL are installed on your machine before installing GDAL itself. These dependencies might include libraries like **libgdal**.

4.Permissions: Installation issues may arise due to permission problems. Ensure that you have the necessary permissions to install packages in your JupyterLab environment.

5.Virtual Environments: If you are using virtual environments, make sure you have activated the correct environment where you want to install GDAL. Installations made in one environment won't be accessible from another unless specifically configured.

6.Error Messages: If you encounter any error messages during installation, they can provide valuable information about what went wrong and can help identify the issue and find a solution.

7.Update or Upgrade: Ensure your package manager (conda or pip) is up-to-date and try updating or upgrading it before installing GDAL. Sometimes, older versions of package managers can cause installation issues.

8.Community Forums/Support: If you're still facing issues, consider checking GDAL's community forums, GitHub issues, or other support channels. Users there might have encountered similar problems and could provide guidance or solutions.

Remember, GDAL can be sensitive to system configurations and dependencies, so troubleshooting installation issues might require some trial and error.

Working with Earth Observation data using open-source python tools

Here are two great introductory tutorials on Github called the “Open Source Geoprocessing Tutorial”. Please work on either one. There are instructions for what will be needed., i.e. to clone the github repo in each case since these also hold the tutorial datasets and all the exercises as jupyter notebooks so you can step through each (or DIY).

1. <https://github.com/patrickcgray/open-geo-tutorial?tab=readme-ov-file>

This steps you through the basics of handling raster images (reading, stacking, reshaping), displaying images and histograms, creating and displaying spectral indices, using vector data (points, lines, polygons), and classification (supervised with training data and unsupervised) and, in the second tutorial, deep learning classification approaches (e.g. random forests, k-nearest neighbour, k-means etc) and Principal Component Analysis (PCA) which we will talk about later, as well as classification accuracy assessments.

For some **terrain analysis**, use the following tutorials:

- https://earthpy.readthedocs.io/en/latest/gallery_vignettes/plot_dem_hillshade.html (this is part of the Earthpy tutorial set, which is excellent and comprehensive <https://earthpy.readthedocs.io/en/latest/get-started.html#>)
- <https://www.earthdatascience.org/tutorials/get-slope-aspect-from-digital-elevation-model/>

And on the EarthLab site there is a huge range of tutorials. For **Time-Series analysis**, try this:

- <https://www.earthdatascience.org/courses/use-data-open-source-python/use-time-series-data-in-python/>