



MURANG'A UNIVERSITY OF TECHNOLOGY

SCHOOL OF PURE AND APPLIED SCIENCE

DEPARTMENT OF APPLIED SCIENCE

UNIVERSITY ORDINARY EXAMINATION

2017/2018 ACADEMIC YEAR

**FIRST YEAR FIRST SEMESTER EXAMINATION FOR BACHELOR OF
SCIENCE IN ORGANIC CHEMISTRY**

AMM102 – MATHEMATICS FOR SCIENCE

DURATION: 2 HOURS

DATE: 13TH DECEMBER 2017

TIME: 9.00AM – 11.00AM

Instructions to Candidates:

1. Answer **Question 1** and **Any Other Two** questions.
2. Mobile phones are not allowed in the examination room.
3. You are not allowed to write on this examination question paper.

SECTION A (Compulsory)

QUESTION ONE (30 Marks)

- a) The roots of the equation $3x^2 + 4x - 5 = 0$ are α, β . Find the values of

$$\frac{1}{\alpha} + \frac{1}{\beta} \text{ and } \alpha^2 + \beta^2 \quad (4 \text{ Marks})$$

- b) The quadratic function

$f(x) = a(x - h)^2 + k$ $a \neq 0$ is in standard form. Rewrite the function $f(x) = 3x^2 - 12x + 17$ in standard form giving the values of k . (3 Marks)

- c) A mixed football team containing 6 men and 5 women is to be chosen from 9 men and 7 women. In how many can this be done? (3 Marks)

- d) The sum of a number of consecutive terms of an arithmetic progression is $-19\frac{1}{2}$, the first term is $16\frac{1}{2}$ and the common difference is -3. Find the number of terms. (3 Marks)

- e) In triangle XYZ, XY=3.5, YZ=4.5 and ZX=6.5. Calculate the size of angle Y. (3 Marks)

- f) Determine the mean absolute deviation of the following distribution. (4 Marks)

Length (cm)	25-29	30-34	35-39	40-44	45-49
Frequency	5	12	25	11	7

- g) A bag A contains 6 white and 4 blue balls while B contains 5 white and 3 blue balls. If one ball is drawn from each bag, find the probability that;

i. Both are white

ii. Both are blue

iii. One is blue and one is white. (6 Marks)

- h) Solve the equation $\log_x^2 + 48\log_2 x = 14$ (4 Marks)

SECTION B (Answer any two questions)

QUESTION TWO (20 Marks)

- a) Without using tables or a calculator, simplify;

$$3\cos^2 45^\circ \cos 42^\circ + \tan^2 60^\circ \sin 48^\circ - 9\cos 60^\circ \cos 42^\circ \quad (4 \text{ marks})$$

- b) Solve the equation $3^x \cdot 7^{2x+1} = 37$ correct to three significant figures. (4 Marks)

- c) Find the sum of the following series;

$$\sum_{r=4}^{16} \left(5 - \frac{r}{4} \right) \quad (4 \text{ marks})$$

- d) Graph the quadratic function $x^2 + 6x + 8$ in general form. (8 Marks)

QUESTION THREE (20 Marks)

- a) Calculate the variance and standard deviation of the distribution given below. (7 Marks)

Volume (cm ³)	40-44	45-49	50-54	55-59	60-64
Frequency	8	20	45	25	2

- b) Given the expansion $(2 + 3x)^8$. Find

- The coefficient of x^4
- Sixth term of the expansion (4 Marks)

- c) A basket contains 3 oranges and 7 mangoes. A boy picked two fruits at random, one at a time without replacement. What is the probability that;

- Both were mangoes
- That one was an orange and one a mango
- That there was at least one mango (6 Marks)

- d) A number is chosen at random from the numbers 1,2,3,...,30. Find the probability that it is;

- Divisible by both 3 and 4 (1 Mark)

- ii. Divisible by 4, given that it is divisible by 3 (2 Marks)

QUESTION FOUR (20 Marks)

- a) Solve the equation $3 \cos 2\theta + \sin \theta = 1$ for $0 \leq \theta \leq 360$ (4 Marks)
- b) Show that $2\sin 75^\circ \cos 45^\circ = \frac{\sqrt{3}+1}{2}$ (3 Mark)
- c) Factorise the expression $6x^3 - 17x^2 - 4x + 3$ and hence solve the cubic equation
- $$6x^3 - 17x^2 - 4x + 3 = 0 \quad (4 \text{ Marks})$$
- d) Obtain the expansion of $(1 + x - 2x^2)^8$ upto the term x^3 (4 Marks)
- e) How many even numbers greater than 50,000 can be formed with the digits 3,4,5,6,7,0 without repetitions. (5 Marks)

QUESTION FIVE (20 Marks)

- a) A woman makes a single deposit of Sh. 1,600 in an account which pays compound interest at a rate of 6% p.a.
- i. How much was the investment worth after twelve years? (2 Marks)
- ii. After how many years will the investment be worth three times its value? (3 Marks)
- b) Find the smallest number of terms of the geometrical progression $8 + 24 + 72 + \dots$ that will give a total greater than 6000000. (5 Marks)
- c) Without using tables or calculators, determine the value of x if;
- $$x = \frac{\log 75 + \log 9 + \log 5}{\log 5 + \log 45} \quad (3 \text{ Marks})$$
- d) Solve the triangle PQR given $p=6.05\text{cm}$, $q=3.65\text{cm}$ and $R=37.5^\circ$ (4 Marks)
- e) Express $\frac{11}{4} \sqrt[3]{\left(\frac{5}{7}\right)}$ in the form $\sqrt[3]{\frac{p}{q}}$ where p or q are integers. (3 Marks)