

5.

Exercício 5.1

a)

```
f[x_, y_, z_] = x^2 + 2 y^2 + 3 z^2; ponto = {1, 1, 1};
```

```
f@@ponto
```

```
6
```

```
Gradf[x_, y_, z_] = Grad[f[x, y, z], {x, y, z}]
```

```
{2 x, 4 y, 6 z}
```

Reta normal

$$y = -1 + 2x$$

$$z = -2 + 3x$$

Plano tangente

$$z = \frac{1}{3} (6 - x - 2y)$$

b)

```
f[x_, y_, z_] = x y z^2; ponto = {1, 1, 1};
```

```
f@@ponto
```

```
1
```

$$\text{Gradf}[x_, y_, z_] = \text{Grad}[f[x, y, z], \{x, y, z\}]$$

$$\{y z^2, x z^2, 2 x y z\}$$

Reta normal

$$\begin{aligned} y &= x \\ z &= -1 + 2x \end{aligned}$$

Plano tangente

$$z = \frac{1}{2} (4 - x - y)$$

c)

$$f[x_, y_, z_] = x^2 + 3 y^3 + \text{Sin}[x y] - z; \text{ponto} = \{1, 0, 1\};$$

$$f @ \text{ponto}$$

$$0$$

$$\text{Gradf}[x_, y_, z_] = \text{Grad}[f[x, y, z], \{x, y, z\}]$$

$$\{2x + y \cos[xy], 9y^2 + x \cos[xy], -1\}$$

Reta normal

$$\begin{aligned} y &= \frac{1}{2} (-1 + x) \\ z &= \frac{3}{2} - \frac{x}{2} \end{aligned}$$

Plano tangente

$$z = -1 + 2x + y$$

d)

$$f[x_, y_, z_] = \text{Exp}[x y z]; \text{ponto} = \{1, 1, 0\};$$

`f @@ ponto`

1

`Gradf[x_, y_, z_] = Grad[f[x, y, z], {x, y, z}]`

$\{e^{xyz} yz, e^{xyz} xz, e^{xyz} xy\}$

Reta normal

$$x = 1$$

$$y = 1$$

Plano tangente

$$z = 0$$

Exercício 5.2

a)

`f[x_, y_, z_] = x^3 + x y z; ponto = {2, 2, 1};`

`f @@ ponto`

12

`Gradf[x_, y_, z_] = Grad[f[x, y, z], {x, y, z}]`

$\{3x^2 + yz, xz, xy\}$

Reta normal

$$y = \frac{12 + x}{7}$$

$$z = \frac{3}{7} + \frac{2x}{7}$$

Plano tangente

$$z = \frac{1}{2} (18 - 7x - y)$$

b)

Não

Exercício 5.3

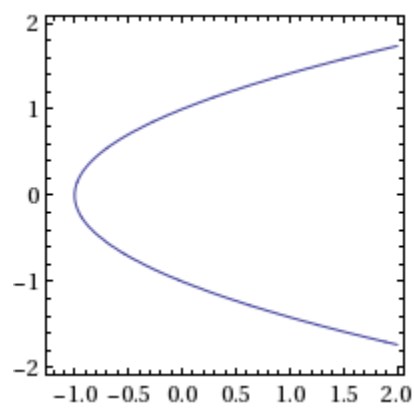
a)

$$f[x, y] = x - y^2; A = \{-1, 0\};$$

$$f @ A$$

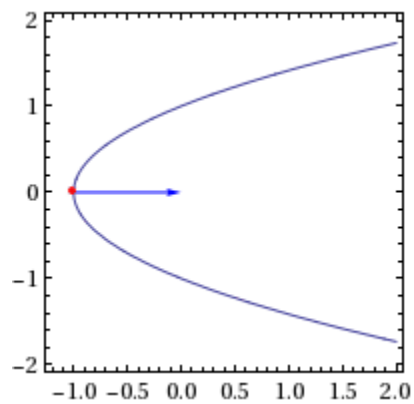
$$-1$$

$$x = -1 + y^2$$



b)

$$\{1, -2y\}$$



c)

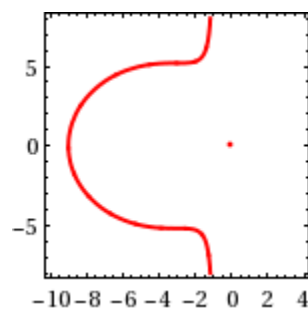
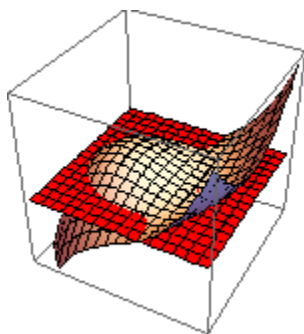
$$z = x$$

Exercício 5.4

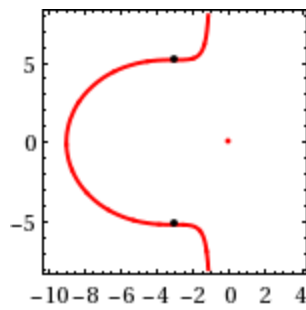
$$f[x_, y_] = x (x^2 + y^2) + 9 x^2 + y^2;$$

$$\text{Grad}[f[x, y], \{x, y\}]$$

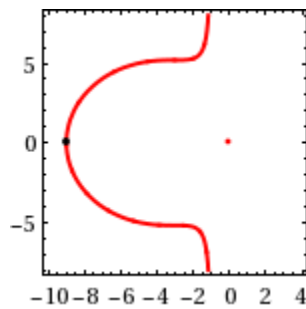
$$\{18x + 3x^2 + y^2, 2y + 2xy\}$$



$$\left\{ \left\{ -3, -3\sqrt{3} \right\}, \left\{ -3, 3\sqrt{3} \right\} \right\}$$



$$\{ \{-9, 0\} \}$$



Exercício 5.5

$$\left\{ \{0, 1\}, \left\{ \frac{2}{3}, -\frac{1}{3} \right\} \right\}$$

Exercício 5.6

$$\left\{ \left\{ \frac{2}{3}, -\frac{4}{3} \right\}, \{2, 0\} \right\}$$

Exercício 5.7

$$f[x_, y_, z_] = x^2 + y^2 + z^2;$$

$$z = \frac{5+y}{2}$$

e

$$x = \frac{5 - y}{2}$$

Exercício 5.8

$$\nabla f(P) \cdot e_1 < 0; \nabla f(Q) \cdot e_2 > 0$$

Created with the Wolfram Language