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Martingale criterion (continuous time)

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**Theorem 1.** *Let  $X$  be a local martingale. Then  $X$  is a continuous martingale iff the set  $\{X_\tau : \tau \text{ stopping time}, \tau \leq c\}$  is uniformly integrable for each  $c \geq 0$ .*