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completeness of semimartingale convergence

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Theorem. *Let $(\Omega, \mathcal{F}, (\mathcal{F}_t)_{t \in \mathbb{R}_+}, \mathbb{P})$ be a filtered probability space. Then, the space of semimartingales \mathcal{S} forms a <http://planetmath.org/Completecomplete> topological vector space under the semimartingale topology.*

That is, semimartingale convergence is a <http://planetmath.org/TopologicalVectorSpaceve> topology and, for any sequence $X^n \in \mathcal{S}$ such that $X^n - X^m \rightarrow 0$ as $m, n \rightarrow \infty$ then there exists an $X \in \mathcal{S}$ with $X^n \rightarrow X$.