

Allen B. Downey

The Little Book of Semaphores

Version 2.2.1

UNDERSTANDING SEMAPHORES AND LEARNING HOW TO APPLY THEM

Allen B. Downey

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http://www.greenteapress.com/semaphores/LittleBookOfSemaphores.pdf

3.7.1 Reusable barrier non-solution (3.7.1a.rebarrier_nonsol.pml)

\$ cat -n 3.7.1a.rebarrier_nonsol.pml | expand The Little Book of Semaphores (2.2.1) 1 2 by A. Downey 3 4 Chapter 3. Basic synchronization patterns 5 3.7 Reusable barrier 6 3.7.1 Reusable barrier non-solution 7 8 9 vk, 2017 */ 10 11 #define THREADS 3 /* value for threads number */ 12 #define N /* value for barrier limit */ 13 3 14 15 #define wait(sem) atomic { sem > 0; sem-- } #define signal(sem) sem++ 16 17 18 byte count=0, mutex=1, turnstile=0 /* turnstile is locked */ 19

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3.7.1 Reusable barrier non-solution (3.7.1a.rebarrier_nonsol.pml)

```
proctype Th(byte i) {
20
21
        byte temp
22
23
    rendezvous:
24
        do
25
            wait(mutex)
        ::
                 temp=count
26
27
                 count=temp+1
28
            signal(mutex)
29
            if
30
             :: count == N ->
                 signal(turnstile)
31
32
             :: else
33
            fi
            wait(turnstile)
34
            printf("Th(%d): count = %d\n",i,count)
35
36
            signal(turnstile)
```

3.7.1 Reusable barrier non-solution (3.7.1a.rebarrier_nonsol.pml)

```
critical:
37
38
            wait(mutex)
39
                 temp=count
40
                 count=temp-1
41
            signal(mutex)
42
            if
             :: count == 0 ->
43
                wait(turnstile)
44
45
             :: else
            fi
46
47
            break /* one only iteration */
        od
48
49
    }
50
```

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3.7.1 Reusable barrier non-solution (3.7.1a.rebarrier_nonsol.pml)

```
$ spin 3.7.1a.rebarrier nonsol.pml | expand
                  Th(3): count = 3
              Th(2): count = 3
          Th(1): count = 3
      turnstile = 0
4 processes created
$ spin 3.7.1a.rebarrier_nonsol.pml | expand
          Th(1): count = 3
                  Th(3): count = 3
              Th(2): count = 2
      turnstile = 0
4 processes created
$ spin 3.7.1a.rebarrier_nonsol.pml | expand
                  Th(3): count = 3
              Th(2): count = 3
          Th(1): count = 1
      turnstile = 0
4 processes created
```

3.7.1 Reusable barrier non-solution (3.7.1b.rebarrier_nonsol.pml)

```
51
    init {
52
        byte i
53
54
        atomic {
55
            for (i: 1 .. THREADS) {
56
                 run Th(i)
57
58
        }
59
        _nr_pr == 1 ->
            assert(turnstile == 0)
60
            printf("turnstile = %d\n",turnstile)
61
   }
62
```

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3.7.1 Reusable barrier non-solution (3.7.1b.rebarrier_nonsol.pml)

```
$ spin 3.7.1b.rebarrier nonsol.pml | expand
                  Th(3): count = 3
              Th(2): count = 2
          Th(1): count = 2
      turnstile = 0
4 processes created
$ spin 3.7.1b.rebarrier_nonsol.pml | expand
              Th(2): count = 3
                  Th(3): count = 3
          Th(1): count = 3
spin: 3.7.1b.rebarrier_nonsol.pml:60, Error: assertion violated
spin: text of failed assertion: assert((turnstile==0))
#processes: 1
                count = 0
                mutex = 1
                turnstile = 1
        proc 0 (:init::1) 3.7.1b.rebarrier nonsol.pml:60 (state 12)
 76:
4 processes created
```

3.7.1 Reusable barrier non-solution (3.7.1c.rebarrier_nonsol.pml)

```
51
    init {
52
        byte i
53
54
        atomic {
55
             for (i: 1 .. THREADS) {
56
                 run Th(i)
57
58
        }
59
        _nr_pr == 1 ->
             assert(turnstile < 3)</pre>
60
             printf("turnstile = %d\n",turnstile)
61
   }
62
```

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3.7.1 Reusable barrier non-solution (3.7.1c.rebarrier_nonsol.pml)

```
$ spin 3.7.1c.rebarrier nonsol.pml | expand
pan:1: invalid end state (at depth 55)
pan: wrote 3.7.1c.rebarrier_nonsol.pml.trail
(Spin Version 6.4.6 -- 2 December 2016)
Warning: Search not completed
        + Partial Order Reduction
Full statespace search for:
        never claim
                                - (none specified)
        assertion violations
        cvcle checks
                                - (disabled by -DSAFETY)
        invalid end states
State-vector 48 byte, depth reached 61, errors: 1
       66 states, stored
        5 states, matched
       71 transitions (= stored+matched)
       12 atomic steps
                        0 (resolved)
hash conflicts:
. . .
```

3.7.1 Reusable barrier non-solution (3.7.1c.rebarrier_nonsol.pml)

```
$ spin -t -p -g -l 3.7.1c.rebarrier_nonsol.pml | expand
Starting Th with pid 1 ...
Starting Th with pid 2 ...
Starting Th with pid 3 ...
        proc 1 (Th:1) 3.7.1c.rebarrier_nonsol.pml:30 (state 7) [((count==3))]
 29:
        proc 1 (Th:1) 3.7.1c.rebarrier_nonsol.pml:31 (state 8) [turnstile = (turnstile+1)]
38: proc 3 terminates
              Th(2): count = 2
          Th(1): count = 1
 54: proc 2 terminates
 55:
        proc 1 (Th:1) 3.7.1c.rebarrier_nonsol.pml:41 (state 22)
                                                                        [mutex = (mutex+1)]
                mutex = 1
        proc 1 (Th:1) 3.7.1c.rebarrier_nonsol.pml:43 (state 23)
                                                                        [((count==0))]
spin: trail ends after 56 steps
#processes: 2
                                                                      1 process blocked!
                count = 0
                                                                      2 processes blocked?
                mutex = 1
                                                                      All 3 processes blocked?
                turnstile = 0
        proc 1 (Th:1) 3.7.1c.rebarrier_nonsol.pml:44 (state 26)
        proc 0 (:init::1) 3.7.1c.rebarrier nonsol.pml:59 (state 11)
 56:
4 processes created
```

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3.7.1 Reusable barrier non-solution (3.7.1c.rebarrier_nonsol.pml)

```
$ spin -run (-E)3.7.1c.rebarrier_nonsol.pml | expand
(Spin Version 6.4.6 -- 2 December 2016)
        + Partial Order Reduction
Full statespace search for:
        never claim
                                 (none specified)
        assertion violations
                                 - (disabled by -DSAFETY)
        cycle checks
        invalid end states
                                 - (disabled by -E flag)
State-vector 48 byte, depth reached 63, errors: 0
    16071 states, stored
    20784 states, matched
    36855 transitions (= stored+matched)
       12 atomic steps
hash conflicts:
                        7 (resolved)
. . .
```

3.7.3 Reusable barrier non-solution (3.7.3a.rebarrier_nonsol.pml)

\$ cat -n 3.7.3a.rebarrier_nonsol.pml | expand The Little Book of Semaphores (2.2.1) 1 2 by A. Downey 3 4 Chapter 3. Basic synchronization patterns 5 3.7 Reusable barrier 6 3.7.3 Reusable barrier non-solution #2 7 8 9 vk, 2017 */ 10 11 #define THREADS 3 /* value for threads number */ 12 /* value for barrier limit */ #define N 3 13 14 15 #define wait(sem) atomic { sem > 0; sem-- } #define signal(sem) sem++ 16 17 18 byte count=0, mutex=1, turnstile=0 /* turnstile is locked */ 19

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3.7.3 Reusable barrier non-solution (3.7.3a.rebarrier_nonsol.pml)

```
proctype Th(byte i) {
20
21
        byte temp
22
23
    rendezvous:
24
        do
25
            wait(mutex)
        ::
                temp=count
26
27
                 count=temp+1
28
            if
29
            :: count == N -> /* may be true for one thread only */
                 signal(turnstile)
30
            :: else
31
32
            fi
            signal(mutex)
33
34
            wait(turnstile)
35
36
            signal(turnstile)
            printf("Th(%d): count = %d, turnstile = %d\n",
37
                    i,count,turnstile)
```

3.7.3 Reusable barrier non-solution (3.7.3a.rebarrier_nonsol.pml)

```
critical:
38
            wait(mutex)
39
40
                temp=count
41
                count=temp-1
            if
42
            :: count == 0 \rightarrow /* may be true for one threads only */
43
                wait(turnstile) /* leave turnstile locked */
44
45
            :: else
            fi
46
47
            signal(mutex)
            break /* one only iteration */
48
49
        od
50
   }
51
```

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3.7.3 Reusable barrier non-solution (3.7.3a.rebarrier_nonsol.pml)

```
init {
52
        byte i
53
54
55
        atomic {
            for (i: 1 .. THREADS) {
56
57
                run Th(i)
58
            }
59
        _nr_pr == 1 ->
60
            assert(turnstile == 0)
61
            printf("turnstile = %d\n",turnstile)
62
   }
63
```

3.7.3 Reusable barrier non-solution (3.7.3a.rebarrier_nonsol.pml)

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3.7.3 Reusable barrier non-solution (3.7.3a.rebarrier_nonsol.pml)

```
$ spin 3.7.3a.rebarrier nonsol.pml | expand
              Th(2): count = 3, turnstile = 1
          Th(1): count = 3, turnstile = 1
                  Th(3): count = 2, turnstile = 1
      turnstile = 0
4 processes created
$ spin 3.7.3a.rebarrier_nonsol.pml | expand
                  Th(3): count = 3, turnstile = 1
          Th(1): count = 3, turnstile = 0
              Th(2): count = 3. turnstile = 1
      turnstile = 0
4 processes created
$ spin 3.7.3a.rebarrier_nonsol.pml | expand
                  Th(3): count = 3, turnstile = 0
              Th(2): count = 3, turnstile = 0
          Th(1): count = 1, turnstile = 0
      turnstile = 0
4 processes created
```

3.7.3 Reusable barrier non-solution (3.7.3b.rebarrier_nonsol.pml)

```
$ cat -n 3.7.3b.rebarrier_nonsol.pml | expand
            The Little Book of Semaphores (2.2.1)
            by A. Downey
     2
     3
     4
            Chapter 3. Basic synchronization patterns
     5
     6
            3.7 Reusable barrier
     7
            3.7.3 Reusable barrier non-solution #2
     8
     9
            vk, 2017
        */
    10
    11
       #define THREADS 3 /* value for threads number */
    12
                            /* value for barrier limit */
       #define N
    13
    14
       #define wait(sem) atomic { sem > 0; sem-- }
    15
       #define signal(sem) sem++
    16
    17
       byte count=0, mutex=1, turnstile=0 /* turnstile is locked */
    18
    19
        byte loop[THREADS+1]=1
        bool sameloop=true
    20
```

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3.7.3 Reusable barrier non-solution (3.7.3b.rebarrier_nonsol.pml)

```
22
    proctype Th(byte i) {
23
        byte temp, j
24
25
    rendezvous:
26
        do
27
            wait(mutex)
        ::
                temp=count
28
29
                 count=temp+1
            if
30
31
            :: count == N -> /* may be true for one thread only */
                 signal(turnstile)
32
            :: else
33
34
            fi
            signal(mutex)
35
36
37
            wait(turnstile)
38
            signal(turnstile)
            printf("Th(%d): loop %d\n",i,loop[i])
39
40
```

3.7.3 Reusable barrier non-solution (3.7.3b.rebarrier_nonsol.pml)

```
critical:
41
42
            atomic {
43
                 for (j: 1 .. N-1) {
                     sameloop = sameloop && (loop[j] == loop[j+1])
44
45
                 assert(sameloop)
46
            }
47
48
            wait(mutex)
49
50
                 temp=count
51
                 count=temp-1
            if
52
            :: count == 0 \rightarrow /* may be true for one threads only */
53
                wait(turnstile) /* leave turnstile locked */
54
             :: else
55
56
            fi
57
            signal(mutex)
58
```

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3.7.3 Reusable barrier non-solution (3.7.3b.rebarrier_nonsol.pml)

```
if
59
60
             :: loop[i] == 2 ->
                 break
61
             :: else ->
62
                 loop[i]++
63
             fi
64
        od
65
66
    }
67
    init {
68
        byte i
69
70
71
        atomic {
             for (i: 1 .. THREADS) {
72
73
                 run Th(i)
74
             }
75
        }
        _nr_pr == 1 ->
76
             assert(turnstile == 0)
77
             printf("turnstile = %d\n",turnstile)
78
79
    }
```

3.7.3 Reusable barrier non-solution (3.7.3b.rebarrier_nonsol.pml)

```
$ spin 3.7.3b.rebarrier_nonsol.pml | expand
          Th(1): loop 1
              Th(2): loop 1
                  Th(3): loop 1
          Th(1): loop 2
spin: 3.7.3b.rebarrier nonsol.pml:46, Error: assertion violated
spin: text of failed assertion: assert(sameloop)
#processes: 4
                count = 1
                mutex = 0
                turnstile = 1
                loop[0] = 1
                loop[1] = 2
                loop[2] = 2
                loop[3] = 1
                sameloop = 0
              3 (Th:1) 3.7.3b.rebarrier_nonsol.pml:52 (state 38)
128:
        ргос
        proc 2 (Th:1) 3.7.3b.rebarrier_nonsol.pml:26 (state 47)
128:
        proc 1 (Th:1) 3.7.3b.rebarrier_nonsol.pml:46 (state 26)
128:
              0 (:init::1) 3.7.3b.rebarrier nonsol.pml:76 (state 11)
128:
        ргос
4 processes created
```

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3.7.5 Reusable barrier solution (3.7.5.rebarrier.pml)

```
$ cat -n 3.7.5.rebarrier.pml | expand
       /* The Little Book of Semaphores (2.2.1)
     2
            by A. Downey
     3
     4
            Chapter 3. Basic synchronization patterns
     5
     6
            3.7 Reusable barrier
     7
            3.7.5 Reusable barrier solution
     8
    9
           vk, 2017
    10
        */
    11
       #define THREADS 3 /* value for threads number */
    12
                            /* value for barrier limit */
    13
       #define N 3
    14
       #define wait(sem) atomic { sem > 0; sem-- }
    15
       #define signal(sem) sem++
    16
    17
       byte count=0, mutex=1, turnstile=0, turnstile2=1
    18
        byte loop[THREADS+1]=1
    19
    20
       bool sameloop=true
    21
```

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3.7.5 Reusable barrier solution (3.7.5.rebarrier.pml)

```
proctype Th(byte i) {
22
23
         byte temp, j
24
25
    rendezvous:
26
         do
27
         ::
              wait(mutex)
28
                   temp=count
29
                   count=temp+1
              if
30
              :: count == N ->
31
                  wait(turnstile2)  /* lock the second */
signal(turnstile)  /* unlock the first */
32
33
34
35
              fi
              signal(mutex)
36
37
38
              wait(turnstile)
                                          /* first turnstile */
              signal(turnstile)
39
40
              printf("Th(%d): loop %d\n",i,loop[i])
41
```

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3.7.5 Reusable barrier solution (3.7.5.rebarrier.pml)

```
critical:
42
43
            atomic {
                for (j: 1 .. N-1) {
44
                    sameloop = sameloop && (loop[j] == loop[j+1])
45
46
47
                assert(sameloop)
            }
48
49
50
            wait(mutex)
51
                temp=count
52
                count=temp-1
53
            if
54
            :: count == 0 ->
                wait(turnstile) /* lock the first */
55
                signal(turnstile2) /* unlock the second */
56
57
            :: else
58
            fi
59
            signal(mutex)
60
            wait(turnstile2)
                                   /* second turnstile */
61
62
            signal(turnstile2)
```

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3.7.5 Reusable barrier solution (3.7.5.rebarrier.pml)

```
if
63
64
             :: loop[i] == 3 ->
                 break
65
             :: else ->
66
67
                 loop[i]++
68
             fi
69
        od
    }
70
71
    init {
72
73
        byte i
74
75
        atomic {
             for (i: 1 .. THREADS) {
76
77
                 run Th(i)
78
             }
79
        _nr_pr == 1 ->
80
             assert(turnstile == 0)
81
82
             assert(turnstile2 == 1)
83
```

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3.7.5 Reusable barrier solution (3.7.5.rebarrier.pml)

```
$ spin 3.7.5.rebarrier.pml | expand
          Th(1): loop 1
                  Th(3): loop 1
              Th(2): loop 1
              Th(2): loop 2
                  Th(3): loop 2
          Th(1): loop 2
              Th(2): loop 3
          Th(1): loop 3
                  Th(3): loop 3
4 processes created
$ spin -run 3.7.5.rebarrier.pml | expand
(Spin Version 6.4.6 -- 2 December 2016)
        + Partial Order Reduction
Full statespace search for:
        never claim
                                (none specified)
        assertion violations
                                - (disabled by -DSAFETY)
        cycle checks
        invalid end states
State-vector 48 byte, depth reached 236, errors: 0
```

3.7.6 Preloaded turnstile (3.7.6.rebarrier_preloaded.pml)

```
$ cat -n 3.7.6.rebarrier_preloaded.pml | expand
       /* The Little Book of Semaphores (2.2.1)
     2
            by A. Downey
     3
     4
            Chapter 3. Basic synchronization patterns
     5
     6
            3.7 Reusable barrier
     7
            3.7.6 Preloaded turnstile
     8
    9
           vk, 2017
        */
    10
    11
       #define THREADS 3 /* value for threads number */
    12
                            /* value for barrier limit */
       #define N 3
    13
    14
       #define wait(sem) atomic { sem > 0; sem-- }
    15
       #define signal(sem) sem++
    16
    17
       #define signalN(sem,NN) for (j: 1 .. NN) { sem++ } /* no atomic */
    18
    19
       byte count=0, mutex=1, turnstile=0, turnstile2=0
    20
       byte loop[THREADS+1]=1
        bool sameloop=true
    21
```

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3.7.6 Preloaded turnstile (3.7.6.rebarrier_preloaded.pml)

```
. . .
   22
   23
        proctype Th(byte i) {
            byte temp, j
   24
   25
        rendezvous:
   26
   27
            do
                wait(mutex)
   28
            ::
   29
                    temp=count
   30
                    count=temp+1
                if
   31
   32
                :: count == N ->
                    signalN(turnstile,N) /* unlock the first */
   33
   34
                :: else
                fi
   35
                signal(mutex)
   36
   37
   38
                wait(turnstile)
                                        /* first turnstile */
                printf("Th(%d): loop %d\n",i,loop[i])
   39
   40
```

3.7.6 Preloaded turnstile (3.7.6.rebarrier_preloaded.pml)

```
critical:
41
42
            atomic {
43
                for (j: 1 .. N-1) {
                    sameloop = sameloop && (loop[j] == loop[j+1])
44
45
46
                assert(sameloop)
            }
47
48
            wait(mutex)
49
50
                temp=count
51
                count=temp-1
            if
52
53
            :: count == 0 ->
                signalN(turnstile2,N) /* unlock the second */
54
55
            :: else
56
            fi
            signal(mutex)
57
58
59
            wait(turnstile2) /* second turnstile */
```

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3.7.6 Preloaded turnstile (3.7.6.rebarrier_preloaded.pml)

```
if
60
61
             :: loop[i] == 3 ->
                 break
62
             :: else ->
63
                 loop[i]++
64
             fi
65
        od
66
    }
67
68
    init {
69
        byte i
70
71
72
        atomic {
             for (i: 1 .. THREADS) {
73
74
                 run Th(i)
75
             }
76
        }
        _nr_pr == 1 ->
77
             assert(turnstile == 0)
78
             assert(turnstile2 == 0)
79
    }
80
```

3.7.6 Preloaded turnstile (3.7.6.rebarrier_preloaded.pml)

```
$ spin -run 3.7.6.rebarrier_preloaded.pml | expand
(Spin Version 6.4.6 -- 2 December 2016)
        + Partial Order Reduction
Full statespace search for:
                                 - (none specified)
        never claim
        assertion violations

    (disabled by -DSAFETY)

        cycle checks
        invalid end states
State-vector 48 byte, depth reached 272, errors: 0
$ spin 3.7.6.rebarrier_preloaded.pml | expand
              Th(2): loop 1
          Th(1): loop 1
                  Th(3): loop 1
          Th(1): loop 2
                  Th(3): loop 2
              Th(2): loop 2
                  Th(3): loop 3
          Th(1): loop 3
              Th(2): loop 3
4 processes created
```

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3.7.7 Barrier objects (3.7.7.barrier_object.pml)

```
$ cat -n 3.7.7.barrier_object.pml | expand
     1
       /* The Little Book of Semaphores (2.2.1)
     2
            by A. Downey
     3
     4
            Chapter 3. Basic synchronization patterns
     5
     6
            3.7 Reusable barrier
     7
            3.7.7 Barrier objects
     8
     9
            vk, 2017
        */
    10
    11
    12
       #include "Semaphore.h"
       #include "Barrier.h"
    13
    14
       #define THREADS 3 /* value for threads number */
    15
                            /* value for barrier limit */
       #define N 3
    16
    17
    18
       Semaphore mutex=1
    19
       Barrier barrier
    20
        byte loop[THREADS+1]=1
    21
    22
        unsigned group: 31 = 0
    23
```

```
proctype Th(byte i) {
24
25
        do
26
        ::
            printf("Th(%d): loop %d\n",i,loop[i])
27
28
    rendezvous:
29
            bar_wait(barrier)
30
    critical:
31
            group=group*10+loop[i]
            assert(group==1 || group==11 || group==111 ||
32
                    group==1112 || group==11122 || group==111222 ||
33
                    group==1112223 || group==11122233 || group==111222333)
34
            printf("Th(%d): loop %d passed with %d\n",i,loop[i],group)
35
36
            if
37
            :: loop[i] == 3 ->
38
39
                 break
            :: else ->
40
                 loop[i]++
41
            fi
42
43
        od
44
    }
45
```

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3.7.7 Barrier objects (3.7.7.barrier_object.pml)

```
init {
46
47
        byte i
48
49
        bar init(barrier,N)
50
51
        atomic {
52
            for (i: 1 .. THREADS) {
                 run Th(i)
53
54
55
        }
56
        _nr_pr == 1 ->
            assert(barrier._turnstile == 0)
57
             assert(barrier._turnstile2 == 0)
58
59
    }
```

```
$ cat -n Semaphore.h | expand
     1
     2
                            byte
        #define Semaphore
     3
        #define wait(sem)
     4
                                 atomic { sem > 0; sem-- }
        #define signal(sem)
     5
                                 sem++
        #define signalN(sem,NN) for (_i: 1 .. NN) { sem++ } /* no atomic */
     7
     8
        byte _i=0
     9
```

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3.7.7 Barrier objects (3.7.7.barrier_object.pml)

```
$ cat -n Barrier.h | expand
     1
     2
        typedef Barrier {
            byte
     3
                       _n
                       _count
     4
            byte
     5
            Semaphore mutex
            Semaphore _turnstile
     6
            Semaphore _turnstile2
     7
     8
     9
    10
        inline bar_init(bar,n) {
            bar._n
    11
                             = n
            bar._count
    12
    13
            bar._mutex
            bar._turnstile = 0
    14
            bar._turnstile2 = 0
    15
    16
        }
    17
```

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```
inline bar_phase1(bar) {
18
        wait(bar._mutex)
19
                             /* atomic here */
20
            bar. count++
21
            if
22
             :: bar._count == bar._n ->
23
                 signalN(bar._turnstile,bar._n)
24
25
            fi
        signal(bar._mutex)
26
        wait(bar._turnstile)
27
28
    }
29
```

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3.7.7 Barrier objects (3.7.7.barrier_object.pml)

```
inline bar_phase2(bar) {
30
        wait(bar._mutex)
31
            bar._count-- /* atomic here */
32
            if
33
            :: bar. count == 0 ->
34
                signalN(bar._turnstile2,bar._n)
35
            :: else
36
            fi
37
38
        signal(bar._mutex)
        wait(bar._turnstile2)
39
40
    }
41
    inline bar_wait(bar) {
42
        bar_phase1(bar)
43
        bar_phase2(bar)
44
45
    }
46
```

\$ spin (-T) 3.7.7.barrier_object.pml | expand Th(1): loop 1 Th(2): loop 1 Th(3): loop 1 Th(2): loop 1 passed with 1 Th(1): loop 1 passed with 11 Th(2): loop 2 Th(3): loop 1 passed with 111 Th(1): loop 2 Th(3): loop 2 Th(1): loop 2 passed with 11122 Th(2): loop 2 passed with 11122 Th(2): loop 3 Th(3): loop 2 passed with 111222 Th(1): loop 3 Th(3): loop 3 Th(2): loop 3 passed with 1112223 Th(1): loop 3 passed with 11122233 Th(3): loop 3 passed with 111222333 4 processes created INF646 Métodos Formales VK, 2017 - The Little Book of Semaphores 41 3.7.7 Barrier objects (3.7.7.barrier_object.pml)

3.8.4 Exclusive queue (3.8.4a.exclusive_queue.pml)

\$ cat -n 3.8.4a.exclusive_queue.pml | expand The Little Book of Semaphores (2.2.1) by A. Downey 2 3 4 Chapter 3. Basic synchronization patterns 5 6 3.8 Queue 7 3.8.4 Exclusive queue solution 8 9 vk, 2017 */ 10 11 #include "Semaphore.h" 12 13 #define N 6 14 15 Semaphore mutex=1, leaderQueue=0, followerQueue=0, rendezvous=0 16 17 byte leaders=0, followers=0 18

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3.8.4 Exclusive queue (3.8.4a.exclusive_queue.pml)

```
proctype Leader(byte i) {
19
20
        wait(mutex)
        if
21
        :: followers > 0 ->
22
23
             followers - -
             signal(followerQueue)
24
25
        :: else ->
            leaders++
26
            signal(mutex)
27
            wait(leaderQueue)
28
29
        fi
30
31
    dance:
        printf("leader %d: to dance\n",i)
32
        wait(rendezvous)
33
        printf("leader %d: dancing\n",i)
34
35
        signal(mutex)
36
    }
37
```

3.8.4 Exclusive queue (3.8.4a.exclusive_queue.pml)

```
proctype Follower(byte i) {
38
        wait(mutex)
39
        if
40
        :: leaders > 0 ->
41
42
            leaders--
43
            signal(leaderQueue)
        :: else ->
44
            followers++
45
            signal(mutex)
46
47
            wait(followerQueue)
48
        fi
49
50
    dance:
        atomic {
51
            signal(rendezvous)
52
            printf("follower %d: dancing\n",i)
53
54
        }
    }
55
56
```

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3.8.4 Exclusive queue (3.8.4a.exclusive_queue.pml)

```
init {
57
        byte i
58
59
        atomic {
60
61
             for (i: 1 .. N) {
62
                 if
63
                 :: i % 2 -> run Leader(i)
                 :: else -> run Follower(i)
64
65
                 fi
            }
66
67
        }
    }
68
```

3.8.4 Exclusive queue (3.8.4a.exclusive_queue.pml)

```
$ spin -T 3.8.4a.exclusive_queue.pml | expand
follower 2: dancing
leader 1: to dance
leader 1: dancing
follower 6: dancing
leader 3: to dance
leader 3: dancing
follower 4: dancing
leader 5: to dance
leader 5: dancing
7 processes created
$ spin -T 3.8.4a.exclusive_queue.pml | expand
follower 2: dancing
leader 5: to dance
leader 5: dancing
leader 3: to dance
follower 6: dancing
leader 3: dancing
leader 1: to dance
follower 4: dancing
leader 1: dancing
7 processes created
                                                                         47
```

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3.8.4 Exclusive queue (3.8.4b.exclusive_queue.pml)

```
proctype Leader(byte i) {
19
        wait(mutex)
20
21
        if
        :: followers > 0 ->
22
23
            followers--
24
            assert(followerQueue == 0)
25
            signal(followerQueue)
        :: else ->
26
            leaders++
27
            signal(mutex)
28
29
            wait(leaderQueue)
30
        fi
31
32
    dance:
        printf("leader %d: to dance\n",i)
33
        wait(rendezvous)
34
        printf("leader %d: dancing\n",i)
35
        signal(mutex)
36
37
    }
38
```

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3.8.4 Exclusive queue (3.8.4b.exclusive_queue.pml)

```
proctype Follower(byte i) {
39
        wait(mutex)
40
        if
41
        :: leaders > 0 ->
42
43
            leaders--
44
            assert(leaderQueue == 0)
            signal(leaderQueue)
45
        :: else ->
46
            followers++
47
            signal(mutex)
48
49
            wait(followerQueue)
        fi
50
51
52
    dance:
        atomic {
53
            signal(rendezvous)
54
            printf("follower %d: dancing\n",i)
55
56
        }
57
    }
58
```

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3.8.4 Exclusive queue (3.8.4b.exclusive_queue.pml)

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3.8.4 Exclusive queue (3.8.4c.exclusive_queue.pml)

\$ cat -n 3.8.4c.exclusive_queue.pml | expand

The Little Book of Semaphores (2.2.1) 2 by A. Downey 3 4 Chapter 3. Basic synchronization patterns 5 6 3.8 Oueue 7 3.8.4 Exclusive queue solution 8 9 vk, 2017 */ 10 11 #include "Semaphore.h" 12 13 #define N(5) 14 15 Semaphore mutex=1, leaderQueue=0, followerQueue=0, rendezvous=0 16 byte leaders=0, followers=0 17 18

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3.8.4 Exclusive queue (3.8.4c.exclusive_queue.pml)

3.8.4 Exclusive queue (3.8.4c.exclusive_queue.pml)

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3.8.4 Exclusive queue (3.8.4d.exclusive_queue.pml)

\$ cat -n 3.8.4d.exclusive_queue.pml | expand

```
The Little Book of Semaphores (2.2.1)
 1
 2
        by A. Downey
 3
 4
        Chapter 3. Basic synchronization patterns
 5
 6
        3.8 Oueue
 7
        3.8.4 Exclusive queue solution
 8
9
        vk, 2017
    */
10
11
   #include "Semaphore.h"
12
13
   #define N(6)
14
15
    Semaphore mutex=1, leaderQueue=0, followerQueue=0, rendezvous=0
16
    byte
              leaders=0, followers=0
17
18
```

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3.8.4 Exclusive queue (3.8.4d.exclusive_queue.pml)

```
59
    init {
60
        byte i
61
62
        atomic {
             for (i:(0).. N) {
63
64
                 if
65
                 :: i % 2 -> run Leader(i)
                 :: else -> run Follower(i)
66
                 fi
67
68
             }
69
        }
70
   }
```

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3.8.4 Exclusive queue (3.8.4d.exclusive_queue.pml)

3.8.4 Exclusive queue (3.8.4d.exclusive_queue.pml)

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