

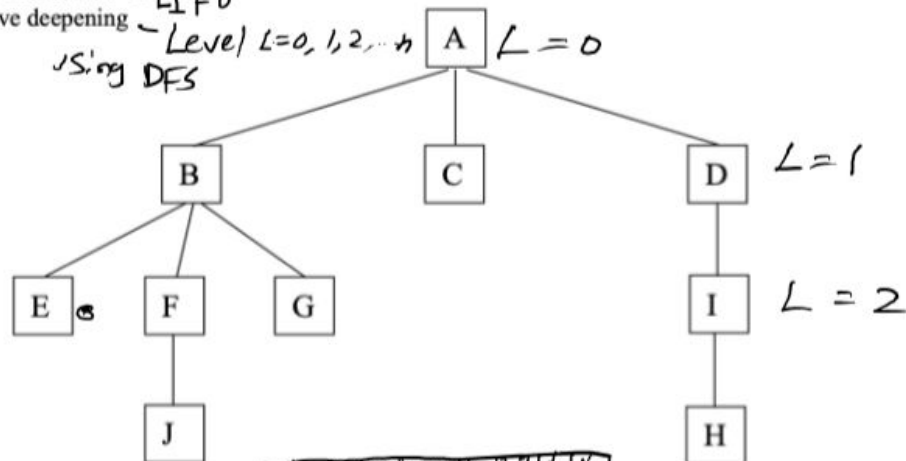
- 1) In what order would the following algorithms visit the nodes of the search tree below? You can assume that all operators have the same cost. (For clarity, "visit" means dequeue from the queuing structure). Hint, for one of these algorithms, we would dequeue 'A' more than once.

A) Breadth first search - level by level (FIFO)

B) Depth first search - LIFO

C) Iterative deepening

using DFS  
Level  $L=0, 1, 2, \dots$



A) A, B, C, D, E, F, G, I, J, H

B) A, B, E, F, J, G, C, D, I, H

C) A, A, B, C, D, A, B, E, F, G, C, D, I, A, B, E, F, J, G, C, D, I, H

- 2) Suppose we need to optimally solve a problem using blind search, for which the goal node is known to be at a depth of exactly 17 (i.e.  $d = 17$ ). What algorithm would you use, and why?

Depth-limited search b/c we know the exact depth.  
It's complete. We have knowledge of depth.

3) Suppose we need to optimally solve a problem using blind search, for which the goal node is known to be at a depth of no more than 29 (i.e.  $d \leq 29$ ). What algorithm would you use, and why?

Iterative deepening b/c Depth-Limited is

- complete  
but not  
optimal



Does this mean L is too big  
so we'll waste time?

yes!

$\leq$  to  $2^9$ , so Depth would not  
be optimal, w/ iterative  
we could find it before  $2^9$ .  
Hence, more optimal.

4) What is the *diameter* of a search problem? You could answer with a single English sentence.

The diameter of a problem is the depth of the  
longest solution or the worst case.

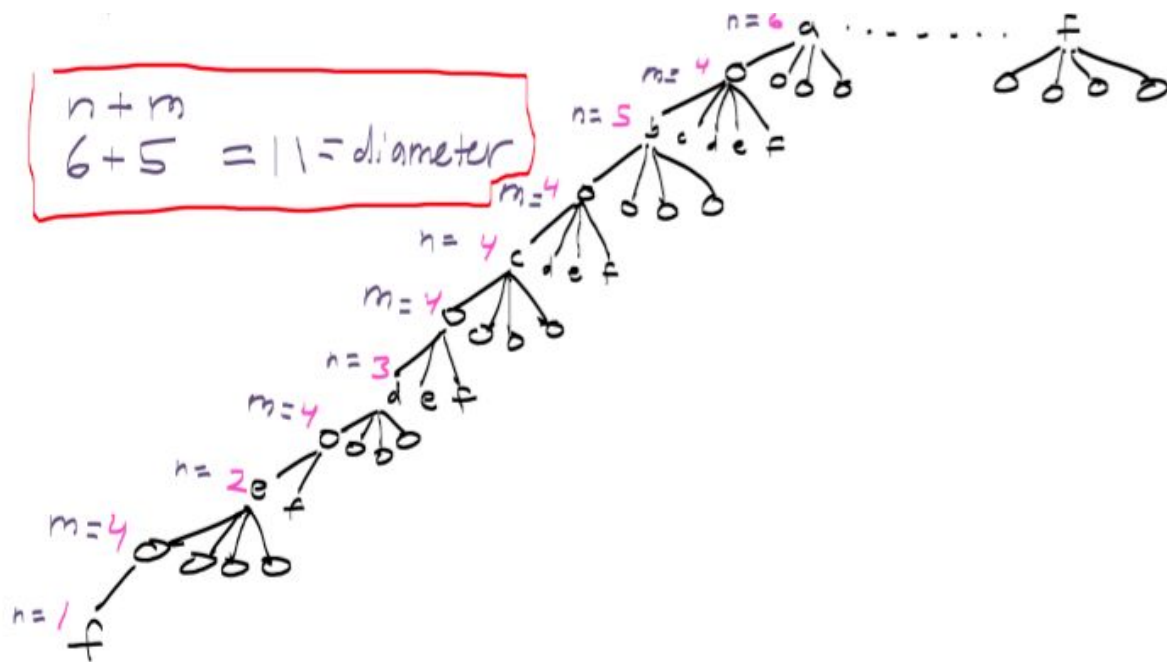
5) What is the diameter of the **countdown numbers game**? (in general, not just the game I show below as an example).  
Justify your answer with two or three English sentences,

[https://www.youtube.com/watch?v=\\_JQYYz92-Uk&ab\\_channel=RussellBabidge](https://www.youtube.com/watch?v=_JQYYz92-Uk&ab_channel=RussellBabidge)

5) There are 4 operators (+, -, \*, /)

There are 6 numbers a, b, c, d, e, f  
We are asked to find the diameter.

No repeats and we do not have to use all the  
numbers. But since we are finding the diameter  
we are using all 6 numbers. So we take each  
number possible and expand each by the #  
of operators.



6) Explain the difference between *optimality* and *completeness* for search (one or two sentences)

Completeness is the technique guaranteed to find an answer while optimality is technique used to find the best answer.

7) Suppose we are trying to solve the *Ballyfermot-by-Bike* problem. The branching factor is **17**, the only solution is known to be at depth **22**. You solve it two ways, Breadth First Search and Iterative Deepening.

- What was the greatest number of nodes in the queue when doing Breadth First Search?
- What was the greatest number of nodes in the queue when doing Iterative Deepening?

7) BFS - with BFS we know that

- Complete? Yes.
- Optimal? Yes.
- Time Complexity:  $O(b^d)$  ← **Bad News**
- Space Complexity:  $O(b^d)$ , note that every node in the fringe is kept in the queue.

bottle neck

• here the branching factor is  $b=17$

• the solution is depth  $d=22$

• It asks for the greatest # of nodes, so

here asking for space complexity  $O(b^d) = O(17^{22}) = 1.17456288 \times 10^{27}$  nodes for BFS

## Iterative Deepening

- - Complete? Yes
  - Optimal? Yes
  - Time Complexity:  $O(b^d)$ , where  $d$  is the depth of the solution.
  - Space Complexity:  $O(bd)$ , where  $d$  is the depth of the solution.

*completeness of Breadth first s  
low space complexity of Depth*

•  $O(bd) = O(17 \cdot 22) = 374$  nodes for iterative deepening.