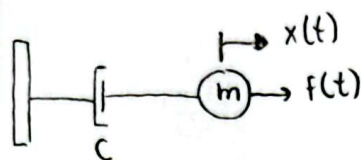


Tutorial 6

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1) Sistema Massa-Amortecedor



$$m\ddot{x}(t) + c\dot{x}(t) = f(t) = f_0 \delta(t)$$

$$m s^2 X(s) + c s X(s) = F_0(s) = f_0/s$$

$$X(s) = \frac{F_0(s)}{m s^2 + c s} \rightarrow \text{função de transferência}$$

$$2) Y(s) = \frac{f_0}{s(m s + c)} \cdot \frac{1}{s} = \frac{f_0}{s^2(m s + c)}$$

$$3) m\ddot{y}(t) + k y(t) = f(t)$$

$$m s^2 X(s) + k X(s) = F(s)$$

$$X(s) = \frac{F(s)}{m s^2 + k}$$

$$4) x_0(t) = \frac{F_0}{a} \left[1 - e^{-\zeta \omega_n t} \left(\cos(\omega_d t) + \frac{\zeta \omega_n}{\omega_d} \sin(\omega_d t) \right) \right]$$

$\zeta = 0$ sem amortecimento

$$x_0(t) = \frac{F_0}{a} [1 - \cos(\omega_n t)]$$

$$\omega_n = \sqrt{\frac{k}{m}} = \sqrt{\frac{100 \text{ N/m}}{1 \text{ Kg}}} = 10 \text{ rad/s}$$

$$\omega_d = \omega_n$$

$$x_0(t) = \frac{10}{100} [1 - \cos(10t)]$$

$$x_0(t) = 0,1 [1 - \cos(10t)]$$

As expressões são equivalentes, os gráficos serão idênticos.