

DATE OF PROBLEM STUDY

Fall 2019

PROJ. OR STUDY NO

SUBJECT

CISC 483-683 Assignment 2 Answers

WORKS

$$1. a) \text{ Entropy overall} = -\frac{15}{22} \log\left(\frac{15}{22}\right) - \frac{5}{22} \log\left(\frac{5}{22}\right) - \frac{2}{22} \log\left(\frac{2}{22}\right)$$

$$= 1.177$$

$$\text{Info Gain (Split AGE)} = 1.177 - \frac{7}{22}(\text{entropy old}) - \frac{10}{22}(\text{entropy med}) - \frac{5}{22}(\text{entropy young})$$

$$= 1.177 - \frac{7}{22}(0) - \frac{10}{22}(1) - \frac{5}{22}(.971)$$

$$= .502$$

$$\text{Info Gain (Split Hair)} = 1.177 - \frac{5}{22}(\text{entropy short}) - \frac{11}{22}(\text{entropy med}) - \frac{4}{22}(\text{entropy long}) - \frac{2}{22}(\text{entropy horrid})$$

$$= 1.177 - \frac{5}{22}(.371) - \frac{11}{22}(.946) - \frac{4}{22}(.811) - \frac{2}{22}(0)$$

$$= .245$$

$$\text{Info Gain (Split UPKEEP)} = 1.177 - \frac{4}{22}(\text{entropy low}) - \frac{6}{22}(\text{entropy med}) - \frac{3}{22}(\text{entropy high}) - \frac{9}{22}(\text{ent tremendous})$$

$$= 1.177 - \frac{4}{22}(.811) - \frac{6}{22}(1.46) - \frac{3}{22}(0) - \frac{9}{22}(.918)$$

$$= 1.177 - .921 = .256$$

$$\text{Info Gain (Split SHOTS)} = 1.177 - \frac{5}{22}(\text{entropy all}) - \frac{11}{22}(\text{entropy some}) - \frac{6}{22}(\text{entropy none})$$

$$= 1.177 - \frac{5}{22}(.971) - \frac{11}{22}(1.435) - \frac{6}{22}(0)$$

$$= 1.177 - .938 = .239$$

So Split on AGE



Let's look at the young branch with 5 instances

$$\text{Entropy} = .971$$

$$\text{Info Gain (Split Hair)} = .971 - \frac{3}{5}(\text{entropy short}) - 0(\text{entropy med}) - \frac{2}{5}(\text{entropy long}) - 0(\text{entropy horrid})$$

$$= .971 - \frac{3}{5}(.918) - \frac{2}{5}(1)$$

$$= .020$$

$$\text{Info Gain (Split UPKEEP)} = .971 - \frac{2}{5}(\text{entropy low}) - \frac{2}{5}(\text{entropy med}) - \frac{1}{5}(\text{entropy high}) - 0(\text{entropy tremendous})$$

$$= .971 - \frac{2}{5}(0) - \frac{2}{5}(0) - \frac{1}{5}(0) - 0$$

$$= .971$$

$$\text{Info Gain (Split SHOTS)} = .971 - \frac{3}{5}(\text{entropy none}) - \frac{2}{5}(\text{entropy some}) - 0$$

$$= .971 - \frac{3}{5}(0) - \frac{2}{5}(0) - 0$$

$$= .971$$

So Split on either UPKEEP or SHOTS

I'll split on UPKEEP but you could split on SHOTS

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Now look at the med branch with 10 instances

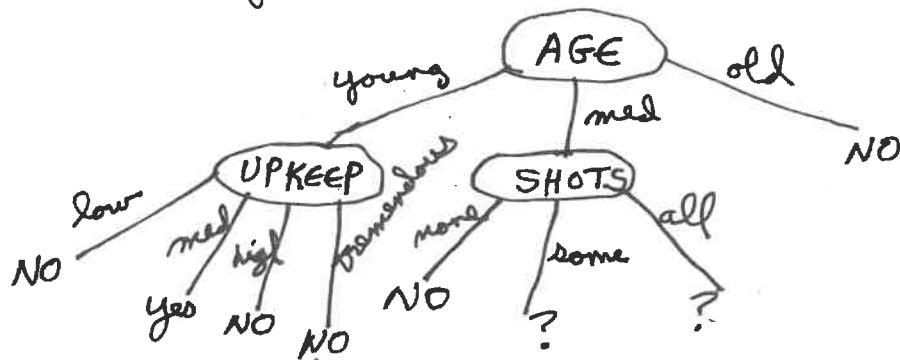
Entropy =

$$\begin{aligned} \text{Info Gain}(\text{Split HAIR}) &= 1.0 - \frac{2}{10}(\text{entropy short}) - \frac{6}{10}(\text{entropy med}) \\ &\quad - 0(\text{entropy long}) - \frac{2}{10}(\text{entropy horrid}) \\ &= 1.0 - \frac{2}{10}(1) - \frac{6}{10}(.918) - 0 - \frac{2}{10}(0) \\ &= 1 - .751 \\ &= .249 \end{aligned}$$

$$\begin{aligned} \text{Info Gain}(\text{Split UPKEEP}) &= 1.0 - \frac{1}{10}(\text{entropy low}) - \frac{2}{10}(\text{entropy med}) \\ &\quad - 0(\text{entropy high}) - \frac{7}{10}(\text{entropy tremendous}) \\ &= 1.0 - \frac{1}{10}(0) - \frac{2}{10}(1) - \frac{7}{10}(.985) \\ &= .110 \end{aligned}$$

$$\begin{aligned} \text{Info Gain}(\text{Split SHOTS}) &= 1.0 - \frac{3}{10}(\text{entropy all}) - \frac{4}{10}(\text{entropy some}) \\ &\quad - \frac{3}{10}(\text{entropy none}) \\ &= 1.0 - \frac{3}{10}(.918) - \frac{4}{10}(.811) - \frac{3}{10}(0) \\ &= .4 \end{aligned}$$

So split on SHOTS



gotten from
majority class
at UPKEEP node

Still need to work on the two ? above
Let's look at the branch labelled SHOTS = some

Entropy = .811

$$\begin{aligned} \text{Info Gain}(\text{Split UPKEEP}) &= .811 - \frac{1}{4}(\text{entropy low}) - 0(\text{entropy med}) \\ &\quad - 0(\text{entropy high}) - \frac{3}{4}(\text{entropy trem}) \\ &= .811 - 0 - 0 - 0 - \frac{3}{4}(.918) \\ &= .122 \end{aligned}$$

$$\begin{aligned} \text{Info Gain}(\text{Split HAIR}) &= .811 - 0(\text{entropy short}) - \frac{3}{4}(\text{entropy med}) \\ &\quad - 0(\text{entropy high}) - \frac{1}{4}(\text{entropy horrid}) \\ &= .811 - 0 - \frac{3}{4}(0) - 0 - \frac{1}{4}(0) = .811 \end{aligned}$$

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WORK

So we split on HAIR

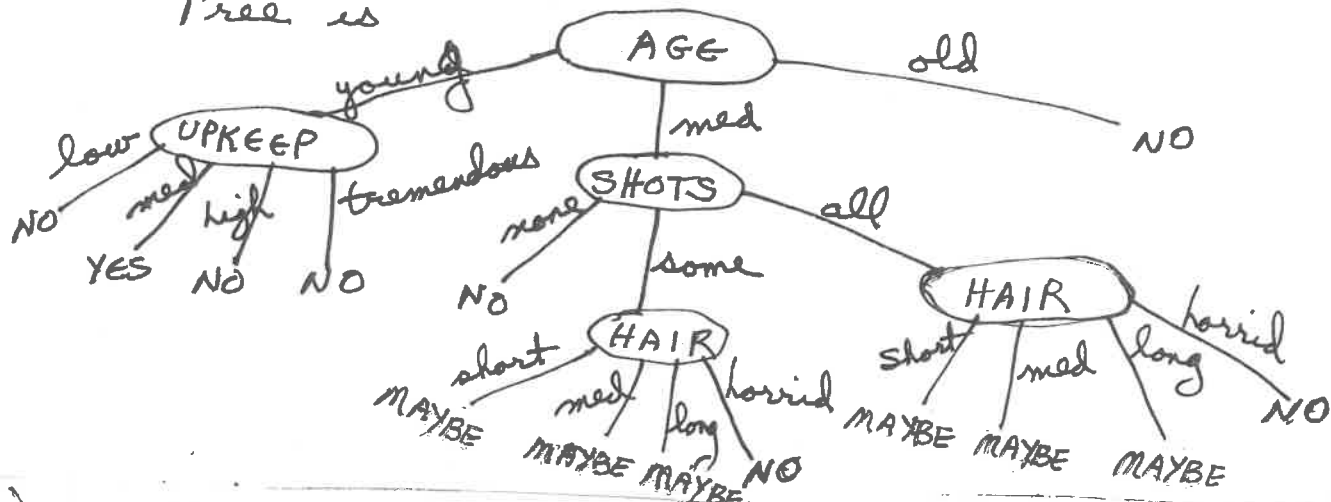
Now let's look at the branch labelled SHOTS=all
entropy = .918

$$\begin{aligned} \text{Info Gain (Split UPKEEP)} &= .918 - 0(\text{entropy low}) - \frac{1}{3}(\text{entropy med}) \\ &\quad - 0(\text{entropy high}) - \frac{2}{3}(\text{entropy tremendous}) \\ &= .918 - 0 - \frac{1}{3}(0) - 0 - \frac{2}{3}(1) \\ &= .251 \end{aligned}$$

$$\text{Info Gain (Split HAIR)} = .918 - 0 = .918$$

So split on HAIR

Tree is



b) Accuracy on test data
for the above tree is $9/11 \approx 82\%$
(the second and 10th instances are incorrectly classified)

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0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30

1C) Consider three possible binary splits on SHOTS

A. {none}, {some, all}

B. {some}, {none, all}

C. {all}, {none, some}

$$\begin{aligned} \text{Gini}(\{ \text{none} \}, \{ \text{some}, \text{all} \}) &= \frac{6}{22}(1-1) + \frac{16}{22} \left(1 - \left(\frac{2}{16} \right) \left(\frac{2}{16} \right) - \left(\frac{5}{16} \right) \left(\frac{5}{16} \right) - \frac{9}{16} \cdot \frac{9}{16} \right) \\ &= \frac{6}{22}(0) + \frac{16}{22} (1 - .016 - .098 - .316) \\ &= \frac{16}{22} (.570) \\ &= .415 \end{aligned}$$

$$\begin{aligned} \text{Gini}(\{ \text{some} \}, \{ \text{none}, \text{all} \}) &= \frac{11}{22} \left[1 - \frac{2}{11} \cdot \frac{2}{11} - \frac{3}{11} \cdot \frac{3}{11} - \frac{6}{11} \cdot \frac{6}{11} \right] \\ &\quad + \frac{11}{22} \left[1 - 0 - \frac{8}{11} \cdot \frac{8}{11} - \frac{9}{11} \cdot \frac{9}{11} \right] \\ &= .297 + .149 \\ &= .446 \end{aligned}$$

$$\begin{aligned} \text{Gini}(\{ \text{all} \}, \{ \text{some}, \text{none} \}) &= \frac{5}{22} \left[1 - 0 - \frac{2}{5} \cdot \frac{2}{5} - \frac{3}{5} \cdot \frac{3}{5} \right] \\ &\quad + \frac{17}{22} \left[1 - \frac{2}{17} \cdot \frac{2}{17} - \frac{3}{17} \cdot \frac{3}{17} - \frac{12}{17} \cdot \frac{12}{17} \right] \\ &= .109 + .353 \\ &= .462 \end{aligned}$$

So the best partition for SHOTS
is {none}, {some, all}