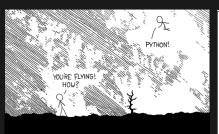
### **Machine Learning**

Lecture Zero - October 1st, 2019

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I LEARNED IT LAST NIGHT! EVERYTHING IS SO SIMPLE!

HELLO WORLD IS JUST print "Hello, world!" I DUNNO...
DYNAMIC TYPING?
WHITESPACE?

COME JOIN US!
PROGRAMMING
IS FUN AGAIN!
IT'S A WHOLE
NEW WORLD

UP HERE!

BUT HOW ARE

YOU FLYING?

I JUST TYPED import antigravity

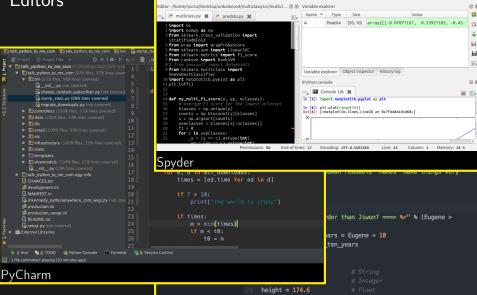
THAT'S IT?

... I ALSO SAMPLED EVERYTHING IN THE MEDICINE CABINET FOR COMPARISON.

BUT I THINK THIS

18 THE PYTHON.

## Editors



▶ ➡ ➡ À Å

\_

22 is\_cool = True # Boolean
23 food\_he\_ate = ["yogurt", "rice", "bulgogi", "rice", "soup"] #
function\_example.py 13:11 UTF-8 Python 19 3 updates

Atom 1/58

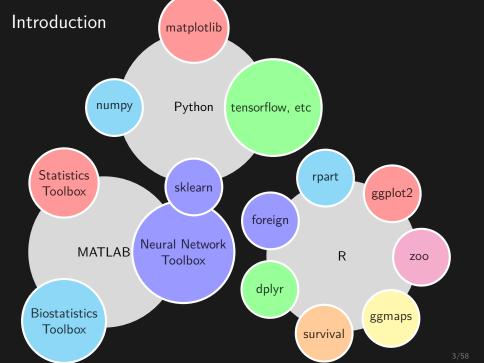
## Agenda

Theory	Practice
~Introduction~	
Numpy	Implement Euclidean distance
Cycles/functions	K-means algorithm
File handling	Use a real dataset
Matplotlib	Plots
Classes/modules	<del></del>
Scikit-learn	Use its k-means
$Keras {+} TF$	Demo

 $\sim$ Finishing touches $\sim$ 



## Introduction



#### Introduction

- Furthermore, Python is a general purpose language
  - It is used in everything from user interfaces to web servers
  - $\circ\,$  Linear algebra is  $\boldsymbol{not}$  a primary citizen

# Introduction: Syntax Python

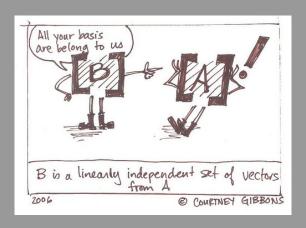
```
1 def is_prime(n):
2  for m in range(2, n):
3    if n % m == 0:
4    return False
5  return True
```

#### **MATLAB**

```
1 function ret = is_prime(n)
2  ret = true;
3  for m=1:(n-1)
4   if mod(n, m) == 0
5    ret = false;
6   break
7  end
8  end
9  end
```

Warning: In Python you **must** properly indent your code.

## NumPy: linear algebra package



### NumPy

The de-facto package for linear algebra is numpy.

Usually, it is shortened to np:

```
1 import numpy as np
```

NumPy features two main structures:

- np.ndarray array of multiple dimensions
- np.matrix matrix (two dimensions)

Why ever use np.matrix when np.ndarray supports two dimensions?

#### NumPy vs MATLAB

Summary of NumPy for MATLAB users <sup>1 2</sup>

MATLAB	NumPy
size(a)	a.shape
a(1:5,:)	a[0:5,:] or a[0:5] or a[:5]
a(end-4:end,:)	a[-5:]
a.'	a.transpose() or a.T
a * b	a.dot(b)
a .* b	a * b

The main conceptual difference is that Numpy supports **arithmetic broadcasting.** That is, you can do the following element-wise multiplication: (6,3) \* (6,1). It automatically assumes you want to multiply by column. In MATLAB, you would have to use bsxfun(@times,r,A) or first use repmat().

https://docs.scipy.org/doc/numpy-dev/user/numpy-for-matlab-users.html

<sup>2</sup>http://mathesaurus.sourceforge.net/matlab-numpy.html

## NumPy Example

Create 
$$B_{ij} = \begin{cases} 5, & \text{if } A_{ij} > 1 \\ 0, & \text{otherwise.} \end{cases}$$

#### Suggestions:

$$B = (A > 1) * 5$$

```
B = np.asarray(
  [[5 if aij > 1 else 0 for aij in ai] for
ai in A])
```

It is probably a good idea to finish this off with:

B = B.astype(np.int8)

to save memory!

#### **API**

#### Python Lists

- 1. Create a list -1 = [1, 5, 2]
- **2.** Access item 1[1]
- **3.** Modify item -1[1] = 7
- **4.** Add item 1.append(8), 1 += [9, 10]

#### NumPy

- 1. Create ndarray from list np.array()
- Create ndarray of zeros/ones np.zeros(), np.ones()
- **3.** Sample Uniform(0,1) np.rand, np.random.random()
- **4.** Sample Normal(0,1) np.randn, np.random.normal()
- **5.** Horizontal concatenation np.vstack(), np.c\_[]
- **6.** Vertical concatenation np.hstack(), np.r\_[]
- 7. Any concatenation np.concatenate(list, axis)

## Project: Implement Euclidean distance

Get the project files on https://github.com/jtrpinto/ml2018.

- 1. Implement a function called euclidean\_distance(a, b)
  - $\circ$  Given two vectors **a** and **b**, computes the square-root of the squared difference between the two vectors
  - $o d = ||x_1 x_2||_2$
  - o TIP: you might want to use vectorisation!
- 2. Use it for the two example vectors given in the script

$$v1 = [1.1, 2.5, 4.4, 0.1, 2.3, 3.4]$$
  
 $v2 = [2.0, 2.2, 1.0, 1.0, 2.5, 3.4]$ 

Possibly useful functions:

np.random.randn, np.mean, np.std, np.sqrt, np.square, np.linalg.norm

## Project: Implement Euclidean distance (solution)

```
2 def euclidean_distance(a, b):
      distance = np.sqrt(np.sum(np.square(a - b)))
      return distance
8 \text{ v1} = \text{np.array}([1.1, 2.5, 4.4, 0.1, 2.3, 3.4])
9 \text{ v2} = \text{np.array}([2.0, 2.2, 1.0, 1.0, 2.5, 3.4])
12 dist = euclidean distance(v1, v2)
14 print ('Distance between v1 and v2: ', dist) # (For these vectors
```

## **Cycles & Functions**

#### Loops

Python has some interesting functions that can help you in loops.

You will probably use these functions a lot in your loops: range, enumerate and zip.

## List Comprehension and Functools

#### List comprehension

#### Functools

 $\circ$  List comprehension is considered the most Pythonic approach.

#### o But...



## Project: Implement the k-means algorithm

Given data  $X_{ij}$ , the user first defines K clusters.

#### The algorithm:

- 1. Random cluster centroids are selected randomly using the MacQueen method:
- 2. Each observation is assigned the closest cluster:

$$\circ c_i(t+1) = \arg\min_k \|x_i - \tilde{c}_k\|_2$$

**3.** Compute the new centroid of each cluster (using the Euclidean distance you implemented before):

$$\circ \ \forall k, j : \tilde{c}_{kj} = \frac{1}{\sum_{i=1}^{N} \mathbb{1}_{c_{i}=k}} \sum_{i=1}^{N} \mathbb{1}_{c_{i}=k} X_{ij}$$

**4.** Repeat steps 2-3 for a set number of iterations.

Please place this inside a kmeans:  $\mathbb{Z}, \mathbb{R}^{N \times M} \to \mathbb{Z}^N$  function, which maps K and X to its respective clusters.

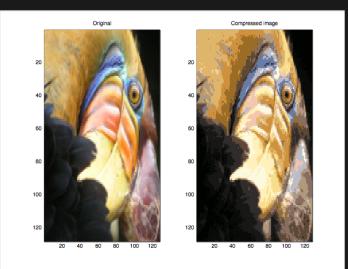
Note: you can also implement a convergence condition that stops the loop as soon as the clusters stabilise.

## Project: Implement the k-means algorithm (solution)

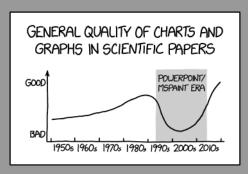
```
1 def k means(X, k=3, n iterations=10):
     for ii in range(n_iterations):
         for index in range(X.shape[0]):
             distance = [euclidean_distance(X[index], cc) for cc
                 in centroidsl
             membership[index] = np.argmin(distance)
         for cc in range(k):
             centroids[cc] = np.mean(X[membership == cc], axis=0)
```

## Kmeans: usage example

K-means can be used for e.g. image compression... 24 (8  $\times$  3) bits  $\rightarrow$  k=64 (6 bits)



## Matplotlib





I'M NOT YOUR
BOYFRIEND!
/ YOU TOTALLY ARE.
I'M CASUALLY
DATING A NUMBER
OF PEOPLE.

BUT YOU SPEND TNICE AS MUCH TIME WITH ME AS WITH ANYONE ELSE. I'M A CLEAR OUTUER.



YOUR MATH IS IRREFUTABLE.

FACE IT—IM
YOUR STATISTICALLY
SIGNIFICANT OTHER



#### Matplotlib

The *de-facto* package for plotting graphics in python is matplotlib.

Matplotlib contains an API<sup>3</sup> called pyplot that is inspired in MATLAB.

See: http://matplotlib.org/1.4.3/api/pyplot\_api.html

<sup>&</sup>lt;sup>3</sup>API = Application Programmer's Interface

#### Matplotlib

#### Example using synthetically created data:

```
1 from matplotlib.pyplot as plt
2 from sklearn.datasets import make_blobs
3 X, y = make_blobs(centers=3)
```

```
1 plt.scatter(X[y == 0, 0], X[y == 0, 1], color='red')
2 plt.scatter(X[y == 1, 0], X[y == 1, 1], color='green')
3 plt.scatter(X[y == 2, 0], X[y == 2, 1], color='blue')
4 plt.show()
```

#### OR

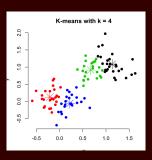
```
1 colors = ['red', 'green', 'blue']
2 plt.scatter(X[:, 0], X[:, 1], color=[colors[_y] for _y in y])
3 plt.show()
```

#### OR

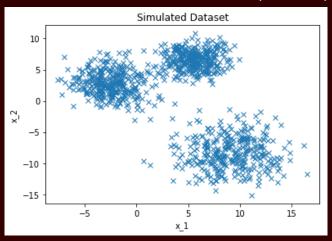
```
1 colors = plt.cm.rainbow(np.linspace(0, 1, 3))
2 plt.scatter(X[:, 0], X[:, 1], color=colors[y])
3 plt.show()
```

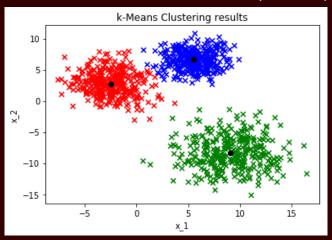
### Project: k-Means in a simulated dataset

- 1. Use matplotlib to plot the simulated dataset
- **2.** Use the implemented k-Means function to **cluster the dataset** (note: use k = 3)
- **3.** Use matplotlib again, to **plot the k-Means clustering result** (use a different color for the points of each cluster)
- **4.** At last, try to **plot the movement of the centroids** over the iterations

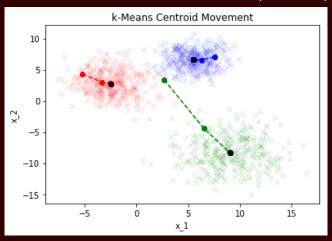


```
2 X, _ = additional_stuff.simulated_dataset()
6 pl.plot(X[:,0], X[:,1], 'x')
8 pl.title('Simulated Dataset')
9 pl.xlabel('x_1')
10 pl.ylabel('x_2')
11 pl.show()
14 membership, centroids, centroids_history = k_means(X, k=3)
```





```
3 pl.scatter(X[:, 0], X[:, 1], marker='x', alpha=0.1, color=[colors
     [int(_y)] for _y in membership])
5 pl.plot(centroids_history[:,0,0], centroids_history[:,0,1], '--',
      marker='o', color='red')
6 pl.plot(centroids_history[:,1,0], centroids_history[:,1,1], '--',
      marker='o', color='green')
7 pl.plot(centroids_history[:,2,0], centroids_history[:,2,1], '--',
      marker='o', color='blue')
9 pl.plot(centroids[:,0], centroids[:,1], 'o', color='black')
11 pl.title('k-Means Centroid Movement')
12 pl.xlabel('x_1')
13 pl.ylabel('x_2')
14 pl.show()
```



## File Handling

### Open files using Numpy

Open a CSV file and add some random noise.

```
import numpy as np
d = np.loadtxt('file.csv', [np.float64, np.float64, np.int8],
delimiter=',', skiprows=1)
X = d[:, :-1]
y = d[:, -1]
```

## Open files using Numpy

Open a CSV file and add some random noise.

```
limport numpy as np
delimiter=',', skiprows=1)
X = d[:, :-1]
y = d[:, -1]
```

By default numpy always works with np.float64. But you may want to change dtype when opening a CSV file or creating a vector in order to use less memory. The following types are available:

```
np.int 8, 16, 32 and 64 bits
np.uint 8, 16, 32 and 64 bits
np.float 16, 32 and 64 bits
np.complex 64 and 128 bits
```

Complex numbers are represented using two 32-bits or 64-bits floats.

By default numpy always works with np.float64. If you work with GPUs, it's a good idea to convert everything to 32-bits.

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## Open images using Scikit-image

```
1 from skimage.io import imread
2 img = imread('filename.png')
3
4 print(img.shape)
5# (512, 512, 3) # if color (RGB)
```

#### **Pandas**

If you are used to R data.frame then you are going to miss things like accessing columns by column name.

There is a widely used data-frame package for Python called pandas.

(This package is particularly useful when dealing with time series because it supports a lot of timeseries functionality we are not going to cover.)

#### Opening is faster than numpy...

```
1 import pandas as pd
2 df = pd.read_csv('titanic.csv')
3 df = pd.read_excel('a.xlsx')
4
5 df.groupby('gender').mean()
6# age height
7# gender
8# female 53.870850 158.201459
9# male 53.491803 158.971695
10
11 df.to_csv('blabla.csv')
12 df.to_excel('blabla.xlsx')
```

#### Indexing

```
1 df['nome-coluna']
2
3 df.loc['nome-linha']
4 df.ix[5] # nro linha
5 df.ix[:, 5] # linha, coluna
```

#### Save Session

There are two ways to save your session/variables to a file:

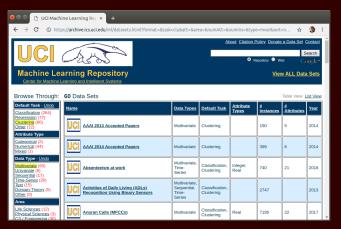
- np.save: numpy binary format
- pickle: binary file (python version-specific)
- json: text file (universal)

#### Pickle is the native Python approach:

```
1 import pickle
2 pickle.dump(d, open('save.pickle', 'wb'))
3# and then you can just load it again:
4 d = pickle.load(open('save.pickle', 'rb'))
```

### Project: Use a real dataset

We are going to use the Iris dataset from "UCI Machine Learning"



It includes 150 samples of flowers of three classes (iris-setosa, iris-versicolor, iris-virginica) and includes measurements of sepal width and length and petal width and length.

## Project: Use a real dataset

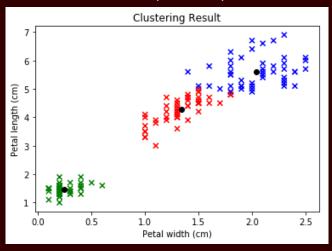
#### Tasks:

- Open 'iris.txt' using pandas read\_csv() function;
- **2. Check the dataset** using Spyder's Variable Explorer;
- 3. Make a numpy array with just two features of the dataset;
- **4.** Use k-means to cluster the dataset (use k = 3);
- 5. Encode the labels and print the mutual information score;
- **6.** Use matplotlib to **plot the results**.

## Project: Use a real dataset (solution)

```
3 data = pd.read_csv('iris.txt')
6 X = np.array(data[['petal width', 'petal length']])
9 membership, centroids, _ = k_means(X, k=3)
15 colors = ['red', 'green', 'blue']
16 pl.scatter(X[:, 0], X[:, 1], marker='x', color=[colors[int(_y)]
      for _y in membership])
17 pl.plot(centroids[:,0], centroids[:,1], 'o', color='black')
18 pl.title('Clustering Result')
19 pl.xlabel('Petal width (cm)')
20 pl.ylabel('Petal length (cm)')
21 pl.show()
```

## Project: Use a real dataset (solution)



## Project: Use an image

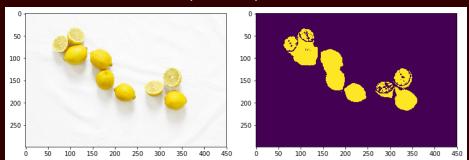
#### Tasks:

- Open the image 'lemons.jpg' using scikit-image io.imread() function;
- 2. Visualise the image using matplotlib imshow() function;
- **3.** Change the shape from  $(w,h,c) \rightarrow (w \times h,c)$  with numpy's reshape() function;
- 4. Use k-means on the reshaped image;
- **5.** Reshape the k-means result back:  $(w \times h, c) \rightarrow (w, h, c)$ ;
- **6. Visualise the result** using the imshow() function;
- 7. Save the result using scikit-image: io.imsave(filename, image).

## Project: Use an image (solution)

```
2 image = io.imread('lemons.jpg')
5 pl.imshow(image)
6 pl.show()
10 image_reshaped=image.reshape((image.shape[0]*image.shape[1], 3))
13 membership, _ , _ = k_means(image_reshaped, k=2)
16 result = membership.reshape((image.shape[0], image.shape[1]))
17 pl.imshow(result)
18 pl.show()
21 io.imsave('result.jpg', result)
```

## Project: Use an image (solution)



## Classes & Modules

#### Classes

```
1 class Animal:
2   def talk(self):
3     raise NotImplementedError('Implement me')
4
5 class Cat(Animal):
6   def talk(self):
7     print("Miau")
8
9 class Human(Animal):
10   def talk(self):
11     print("Bla bla")
12
13 Cat().talk() # what is the output?
```

#### Two notes:

- Python is very dynamic: there are no formal contracts like abstract methods
- in Python, the reference to the object itself is passed explicitly

#### Modules

Different ways to access a module:

```
•1 import fib
2 fib.whatever()

•1 from fib import whatever
2 whatever()

•1 from fib import *
2 whatever()

(import everything into your namespace — usually not recommended)
```

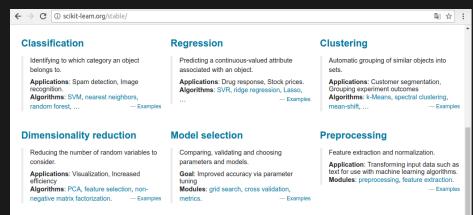
Inside each directory, you must may have a \_\_init\_\_.py file where you can put initialization code.

## Scikit-learn



#### Scikit-learn

#### Scikit-learn has literally everything!



## Scikit-learn interface

Estimator:	Implements the fit method to learn from data.
	For Supervised Learning:
	<pre>1 estimator = estimatorObj.fit(data, labels)</pre>
	and Unsupervised Learning:
	<pre>1 estimator = estimatorObj.fit(data)</pre>
Predictor:	l labels = predictorObj.predict(data)
	May implement predict_proba to return the
	degree of certainty.
Transformer:	Filters or modifies the data:
	new_data = transformerObj.transform(data)
Model:	Measures goodness of fit:
	score = modelObj.score(data, labels)

## Project: Apply K-means with sklearn

#### Tasks:

- Find the sklearn documentation for the K-means algorithms;
- 2. Go to the code you have previously written for the Iris dataset and substitute your k-means function by the KMeans object of sklearn. You should:
  - **2.1** Create the object.
  - **2.2** Estimate the parameters with the data (fit(.)).
  - **2.3** For each sample predict the assigned cluster (predict(.)).
- 3. Plot and check you have obtained an equivalent result.

## Project: Apply K-means with sklearn

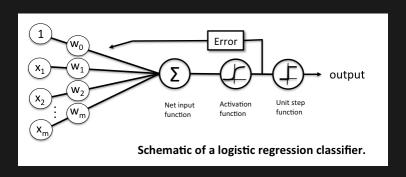
#### Tasks:

- Find the sklearn documentation for the K-means algorithms;
- **2.** Go to the code you have previously written for the Iris dataset and substitute your k-means function by the KMeans object of sklearn. You should:
  - **2.1** Create the KMeans object.
  - **2.2** Estimate the parameters with the data (fit(.)).
  - **2.3** For each sample predict the assigned cluster (predict(.)).
- 3. Plot and check you have obtained an equivalent result.

#### Solution:

```
from sklearn.cluster import KMeans as kmeans
model = kmeans(n_clusters=3)
model.fit(X)
membership = model.predict(X)
centroids = model.cluster_centers_
```

## Classification with Logistic Regression



## Project: Apply Logistic Regression for Classification

We now focus on the problem of categorizing data.

- 1. Find the sklearn documentation for the K-means algorithms;
- 2. Split the data into training and testing.
- **3.** Create the LogisticRegression object and estimate the parameters with the training data.
- **4.** Obtain the accuracy of the model in the training and testing data (score(.)).

#### Further exercises:

- **5.** Run the same code again. Did you obtain the same result?
- **6.** Try the same exercise with another classifier.

Useful functions: train\_test\_split, LogisticRegression, fit, score 44/58

# Project: Apply Logistic Regression for Classification (solution)

#### Solution:

```
from sklearn.linear_model import LogisticRegression
X_train, X_test, y_train, y_test = train_test_split(X, y)
logreg = LogisticRegression()
logreg.fit(X_train, y_train)

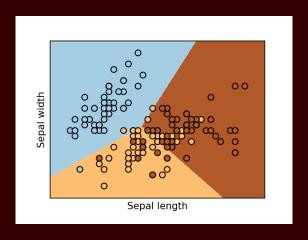
print("Train set: ", logreg.score(X_train, y_train))
print("Test set: ", logreg.score(X_test, y_test))
```

Note: If you want to obtain the same exact results you need to remove the randomness in the process. Some common sources of variation are the train and test split and the initial parameters of the logistic regression.

Note: Because different classifiers have the same interface, we can simply substitute the 3rd line by another model. In this way we can quickly estimate the performance of multiple models for any machine learning problem we want to solve.

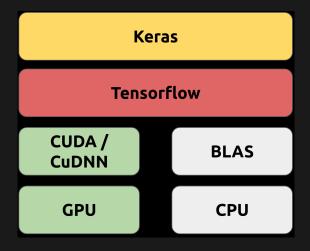
### Plotting the Feature Space

Using the provided function  $(plot_fs())$  plot the feature space. This function might be useful for other projects!



## Keras & TensorFlow

### Keras & TensorFlow



#### Keras

Keras is a high-level neural networks API.

Models in Keras (and Tensorflow) are defined as a graph of operations which transform the data from the input to the output. The simplest possible model in Keras is a **Sequential** which represents a linear stack of operations. We construct the model by adding layers:

```
from keras.layers import Dense
from keras.models import Sequential
model = keras.Sequential()
model.add(Dense(64, activation='relu', input_dim=100))
model.add(Dense(10, activation='softmax'))
```

After creating the model we need to compile it before we start the training process.

#### Keras

After a Keras model is compiled its interface is similar to models in sklearn:

## Sklearn Keras

Fit the training data:

```
1 model.fit 1 model.fit
```

Predict the output for input data:

```
1 model.predict 1 model.predict
```

Evaluate the performance for input data:

```
1 model.score 1 model.evaluate
```

## Logistic Regression in Keras

A Logistic Regression classifier can easily be implemented in Keras as a one layer neural network. For :

Note that although we are doing logistic regression the structure and optimization of this model is different from the sklearn's logistic regression. More on this will be explained on the lecture about logistic regression.

## Project: Implement Logistic Regression in Keras

We now focus on the problem of categorizing data.

- 1. Find the keras documentation for the sequential model;
- **2.** Go to the code you have previously written for classification of the Iris dataset and substitute the sklearn implementation of the logistic regression by your own keras implementation.
- **3.** Fit the training data and obtain the accuracy for the train and test data.
- **4.** Obtain a plot of the feature space (use plot\_fs())

#### When to use sklearn vs Keras

Keras is used to work with neural networks. It allows faster training due to using GPU accelaration. Generally, if you are working with Deep Learning models you will be using Keras or a similar module. For traditional machine learning algorithms you use sklearn.

In this course sklearn will be more useful.

#### MNIST in Keras Demo

An example where modules like keras are used often: Image Recognition with Convolutional Neural Networks.

```
model = Sequential()
model.add(Conv2D(32, kernel\_size=(3, 3),
     activation='relu'.input shape=
     input shape))
model.add(Conv2D(64, (3, 3), activation='
     relu'))
model.add(MaxPooling2D(pool_size=(2, 2)))
model.add(Dropout(0.25))
model.add(Flatten())
model.add(Dense(128, activation='relu'))
model . add ( Dropout (0.5))
model.add(Dense(num classes, activation='
     softmax'))
model.compile(loss=keras.losses.
     categorical crossentropy, optimizer=
     keras.optimizers.Adadelta(), metrics
     =['accuracy'])
model.fit(x_train, y_train,
      batch_size=batch_size,
      epochs=epochs.
      verbose=1,
      validation_data=(x_test, y_test))
score = model.evaluate(x_test, y_test,
     verbose=0)
```

```
3471956218
89125006398
6701636188
3779466123
1598365783
15983658899
3196858899
370948543
```

Logistic Regression: 81% CNN: 99%

## **Finishing Touches**

#### **Pointers**



#### References

In programming languages when calling a function, there are two possible behaviors:

- pass by value (or copy)
- pass by reference

Python uses what some people like to call 'pass-by-object-reference'. Everything is an object and the reference to the object is copied (not the object itself).

```
1 def fn(b):
2  print(id(b))
3  print(a is b)
4 a = []
5 print(id(a))
6 fn(a)
```

#### Output:

```
1 139663236727240
2 139663236727240
3 True
```

#### References

```
1 a = [1,2,3]
2 b = a
3 b[1] = 7
4 print(a)
```

What is the value of a?

```
1 a = [1,2,3]
2 b = a
3 b = [1,7,3]
4 print(a)
```

What is the value of a?

```
1 a = 2
2 b += 5
3 print(a)
```

What is the value of a?

## Python2 vs Python3

Python2 will be discontinued in 2020. The major differences are that:

- In Python3, functions like range() are generators/iterators, while in Python2 they are lists. In most use cases, this will make no difference to you.
- In Python3, strings are codified in Unicode by default. This makes it
  nicer to work with when using, for instance, Portuguese characters like
  ç or á.
- Probably the when you'll notice the most is that in Python2 print 'Hello World' was valid. In Python3, you need to use parenthesis, print('Hello World')
- There are many other small ones. **Most importantly, not all** packages are yet compatible with Python3. (Though 99% are.)

## Python Implementations

There are several implementations of the Python language:

#### CPython

- $\circ \ \boxed{\mathsf{source\ code}} \xrightarrow{\mathsf{is\ compiled\ to}} \boxed{\mathsf{bytecode}} \to \mathsf{execute}$
- CPython is the most popular implementation of Python, and is developed by the Python Foundation
- o This is the implementation people *mean* when they say Python

#### PyPy

- $\circ \ \boxed{\mathsf{source\ code}} \to \boxed{\mathsf{bytecode}} \to \mathsf{execute} \leftrightarrow \boxed{\mathsf{machine\ code}}$
- o This is also a very popular and highly supported implementation
- Faster; this is how Java and MATLAB work

#### Jython

- $\circ \ \boxed{\mathsf{source\ code}} \to \boxed{\mathsf{Java\ bytecode}}$
- $\circ$  The Java interpretor: bytecode  $\rightarrow$  execute  $\leftrightarrow$  machine code
- It outsources work to Java

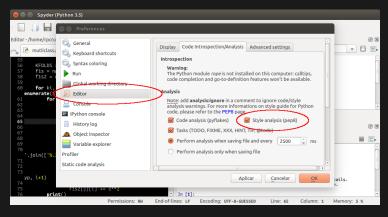
#### PEP8

Using a pretty style makes reading your code much easier.

In Python, there is a coding style that is recommended called PEP8.

**Exercise:** Enable code style checking in Spyder and fix the errors.

Under the Preferences window:





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