Solution

$$\int \frac{1}{\sqrt{x^2 + 6x + 9}} \, dx = \int \frac{1}{\sqrt{(x+3)^2}} \, dx$$
$$= \int \frac{1}{x+3} \, dx$$
$$= \ln|x+3| + C$$

using the substitution $u = x + 3$.