$$\int \frac{1}{1+x^2} \, dx$$

Solution

Since the derivative of the arctangent function is $\frac{1}{x^2+1}$, the derivative rule immediately gives the integral:

$$\int \frac{1}{1+x^2} \, dx = \tan^{-1}(x) + C.$$