$$\int_{2}^{6} x^{3} dx$$

indef 
$$\int x^3 dx = \frac{x^4}{4} + C$$

$$\int_{2}^{6} x^{3} dx = \frac{x^{4}}{4} \Big|_{2}^{6} = \frac{6^{4}}{4} - \frac{2^{4}}{4}$$

$$\int_{3}^{12} (5^{x} - 2x) dx$$
indef 
$$\int (5^{x} - 2x) dx = \int_{3}^{x} (5^{x} - 2x) dx = \int_{3}^{x} (5^{x} - 2x) dx = \left( \frac{5^{x}}{4^{x}} - x^{2} \right)_{3}^{12} = \left( \frac{5^{12}}{4^{x}} - 12^{2} \right) - \left( \frac{5^{3}}{4^{3}} - 3^{2} \right)$$

$$\int_{4}^{9} (3^x + \frac{1}{x}) \, dx$$

indef: 
$$\int (3^{x} + \frac{1}{x}) dx = \frac{3^{x}}{\ln 3} + \ln |x| + C$$

$$\int_{4}^{9} \left(3^{x} + \frac{1}{x}\right) dx = \left(\frac{3^{x}}{h_{3}} + \ln(x)\right)_{4}^{9} = \left(\frac{3^{9}}{h_{3}} + \ln|9|\right) - \left(\frac{3^{4}}{h_{3}} + \ln|4|\right)$$

$$\int_{2}^{3} x^{4}(x+8) dx$$

indef 
$$\int x^{4}(x+8) dx = \int x^{5} + 8x^{4} dx = \frac{x^{6}}{6} + 8 \cdot \frac{x^{5}}{5} + C$$

$$\int_{2}^{3} x^{4} (x+8) dx = \left(\frac{x^{6}}{6} + \frac{8x^{5}}{5}\right)^{3}_{2} = \left(\frac{3^{6}}{6} + \frac{8(3)^{5}}{5}\right) - \left(\frac{2^{6}}{6} + \frac{8(2)^{5}}{5}\right)$$