



iCyPhy



Model-Based Design of Cyber-Physical Systems

Edward A. Lee

**Design, Modeling, and Architecture of Complex Industrial Systems (COMASIC)
Masters Program**

Université Paris-Saclay

Saclay, France, Jan. 23, 2020



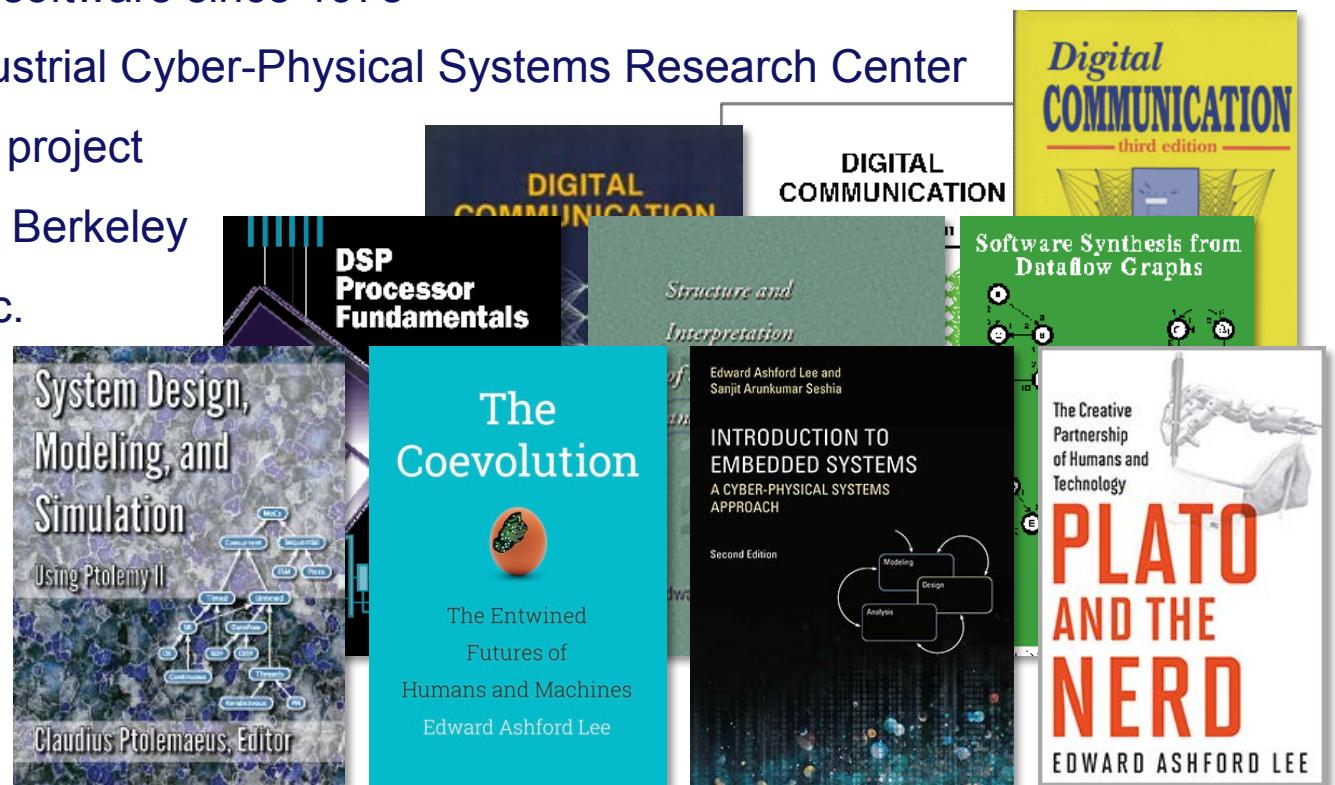
University of California, Berkeley



Introducing Edward A. Lee

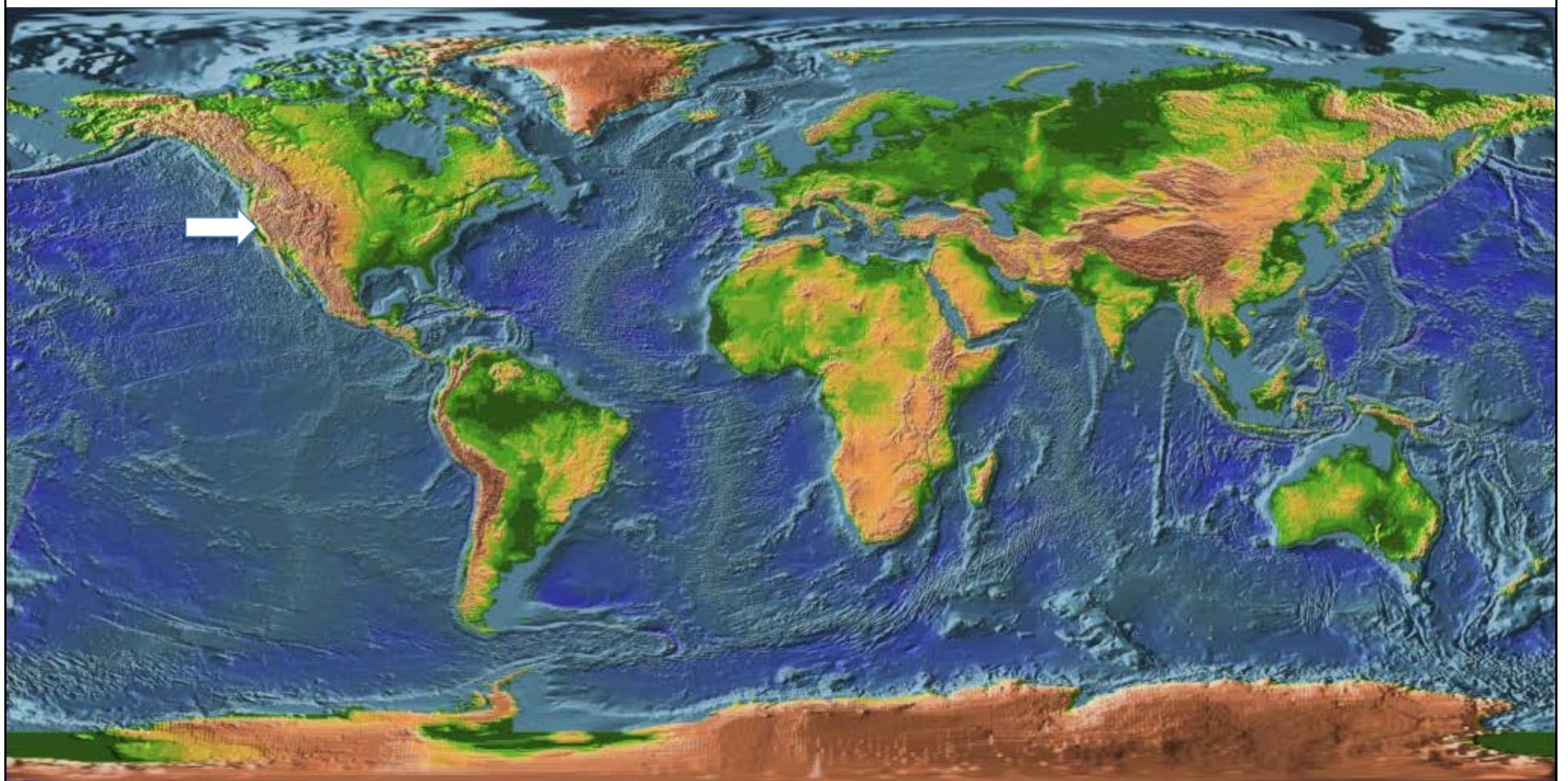
- BS (Yale), SM (MIT), PhD (Berkeley)
- Bell Labs in the early 1980s
- Berkeley EECS faculty since 1986
- Working on embedded software since 1978
- Director of iCyPhy, Industrial Cyber-Physical Systems Research Center
- Director of the Ptolemy project
- Former Chair of EECS, Berkeley
- Co-founder of BDTI, Inc.
- Books...

<http://ptolemy.org/~eal>
eal@berkeley.edu





Location





The University of California at Berkeley





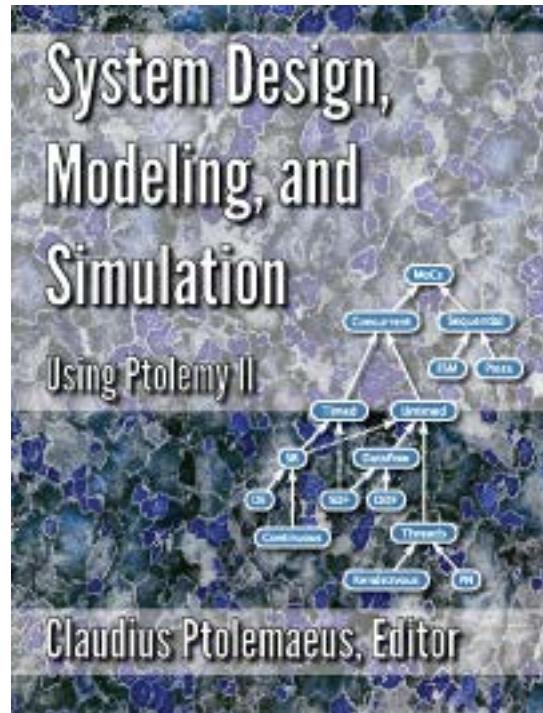
Disclaimer

This is not a survey of the field.

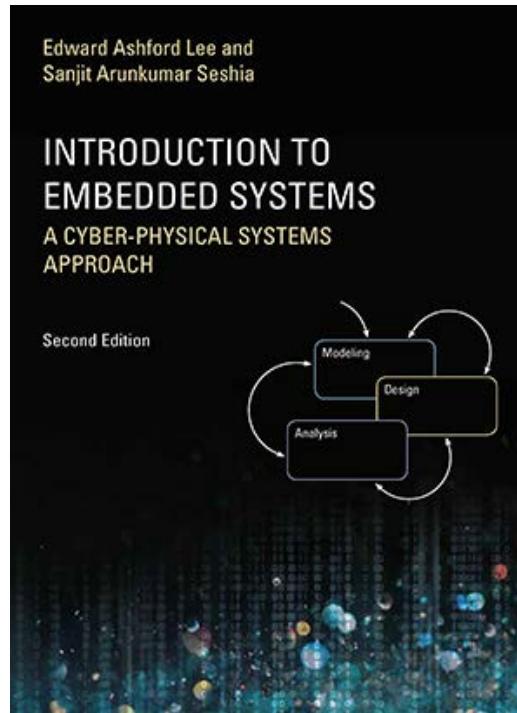
I will give you a narrow Berkeley view with a lot of opinions and personal perspectives.



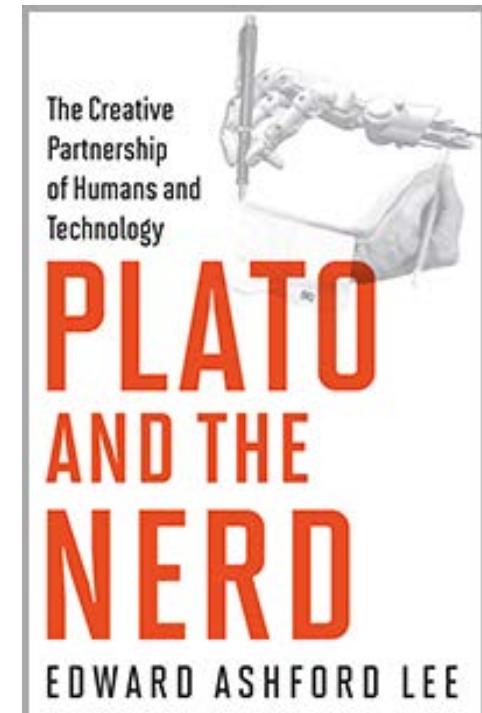
Resources



<http://ptolemy.org/systems>



<http://leeseshia.org>



<http://platoandthenerd.org>



Outline

- Cyber-Physical Systems (CPS)
- Challenges
- Models
- Determinism
- Limits of Determinism
- Abstraction and Refinement
- Time



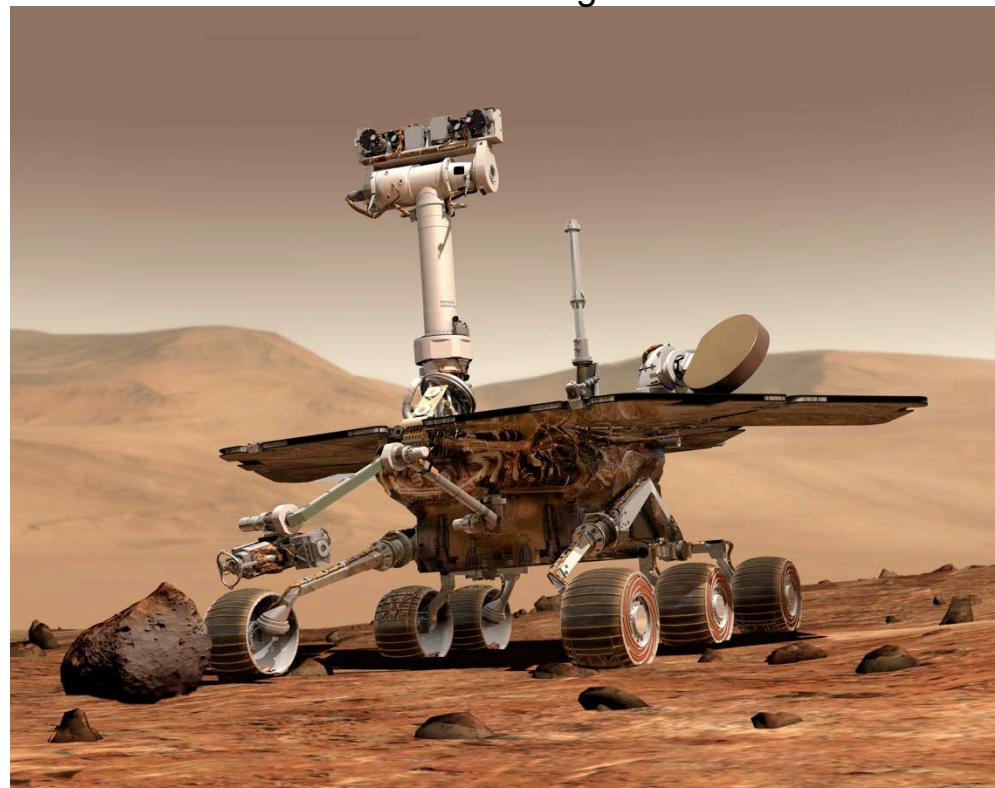
Cyber-Physical Systems

Orchestrating networked computational resources and physical systems.

Roots:

- Term coined around 2006 by Helen Gill at the National Science Foundation in the US.
- **Cyberspace**: attributed William Gibson, who used the term in the novel Neuromancer.
- **Cybernetics**: coined by Norbert Wiener in 1948, to mean the conjunction of control and communication.

Image: Wikimedia Commons





Cyber-Physical Systems

Not just information technology:

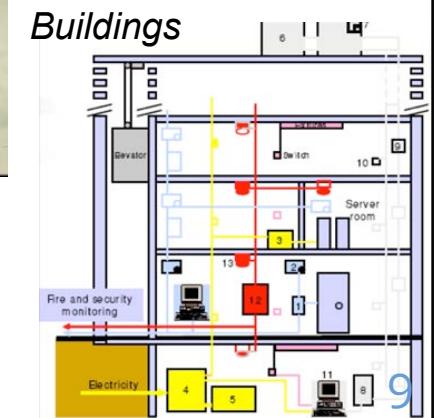
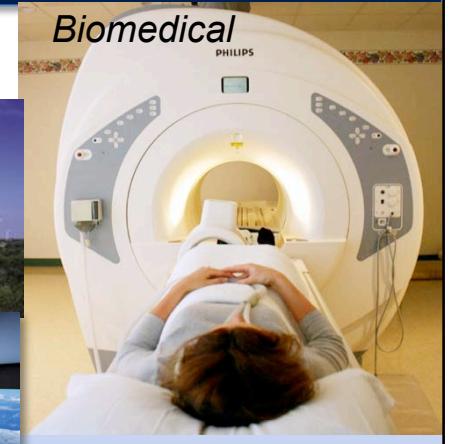
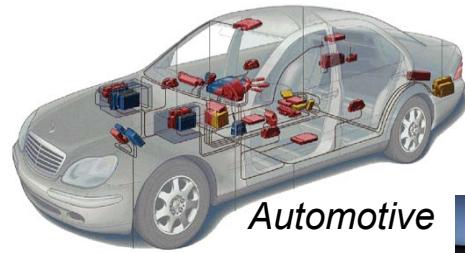
- Cyber + Physical
- Computation + Dynamics
- Security + Safety

Properties:

- Highly dynamic
- Safety critical
- Uncertain environment
- Physically distributed
- Sporadic connectivity
- Resource constrained

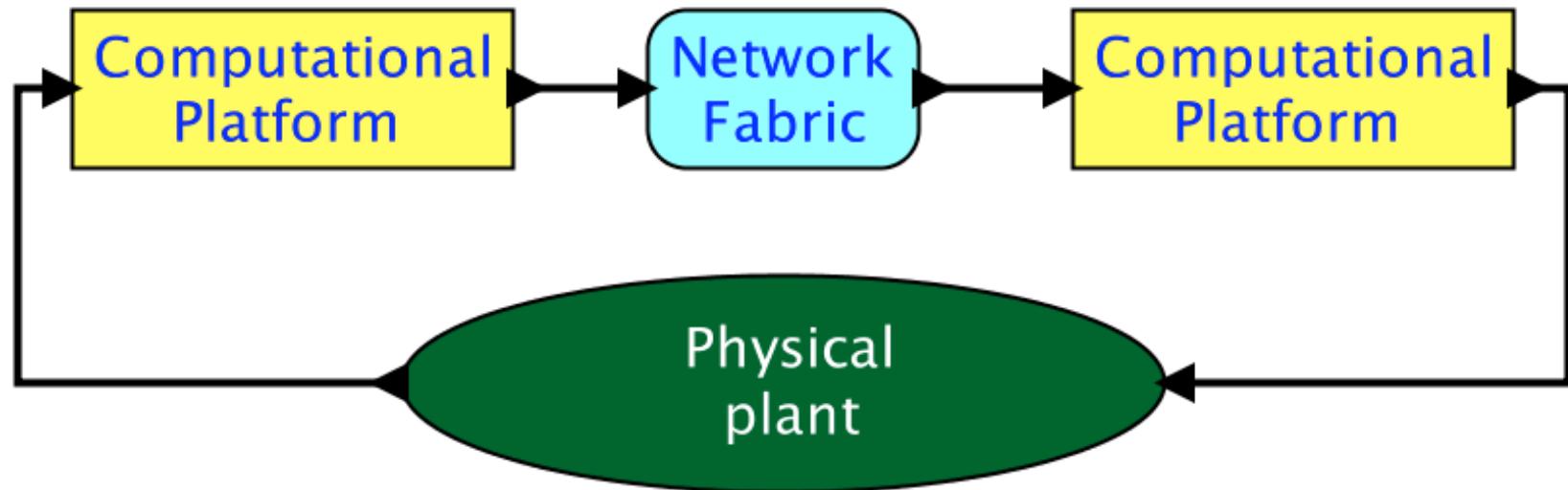
We need engineering **models** and **methodologies** for dependable cyber-physical systems.

Lee, Berkeley





Cyber-Physical Systems Pattern



Often safety critical, real time, and resource constrained.



Example

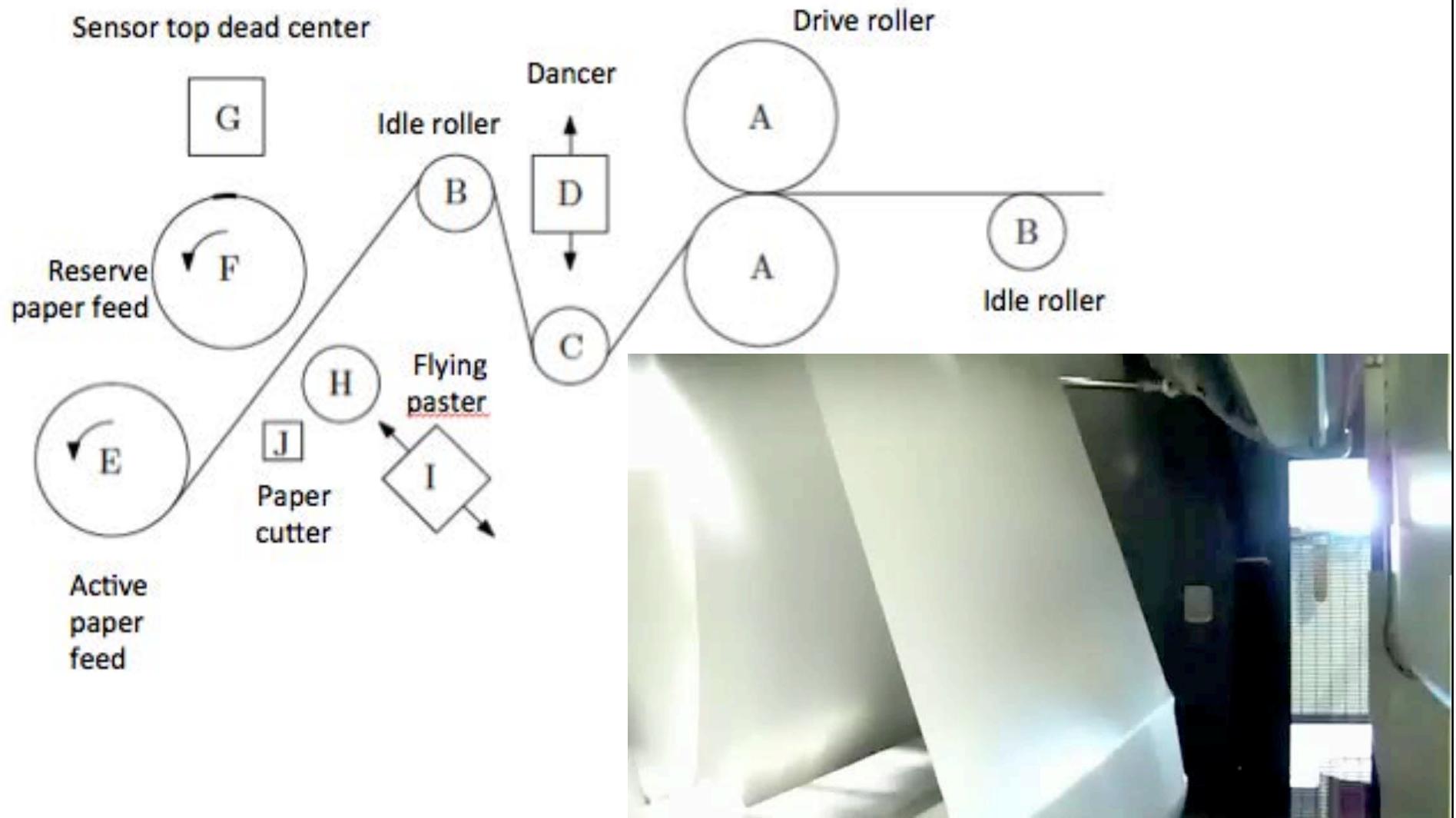
*Hundreds of
microcontrollers
orchestrating depositing
ink and slicing paper
flying through the
machine at 100 km/hr.*

This Bosch Rexroth printing press is a cyber-physical factory using Ethernet and TCP/IP with high-precision clock synchronization (IEEE 1588) on an isolated LAN.





Example – Flying Paster



Source: <http://offsetpressman.blogspot.com/2011/03/how-flying-paster-works.html>



Example – Flying Paster



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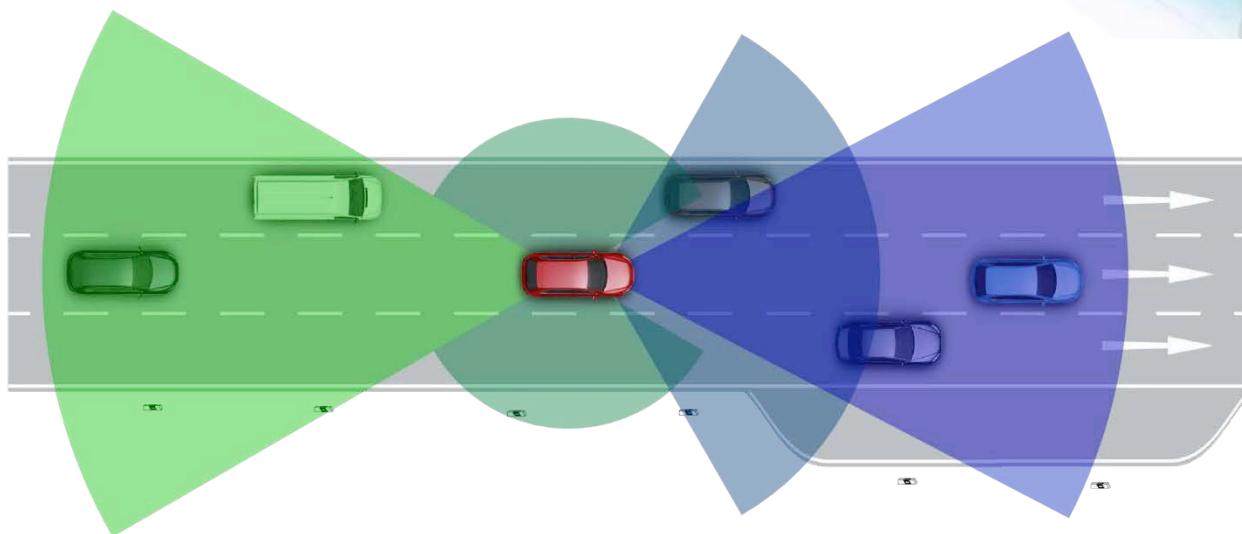
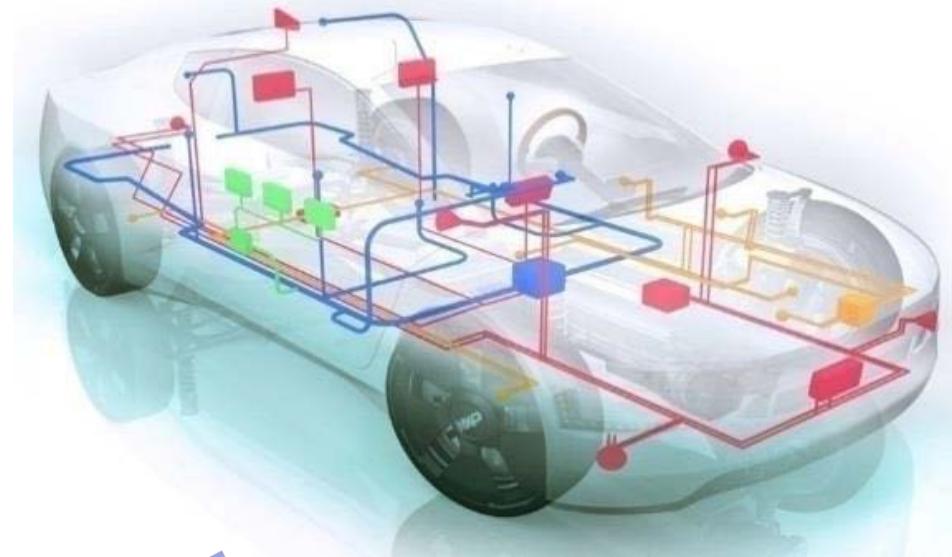
CPS Challenge Problem: *Prevent This*





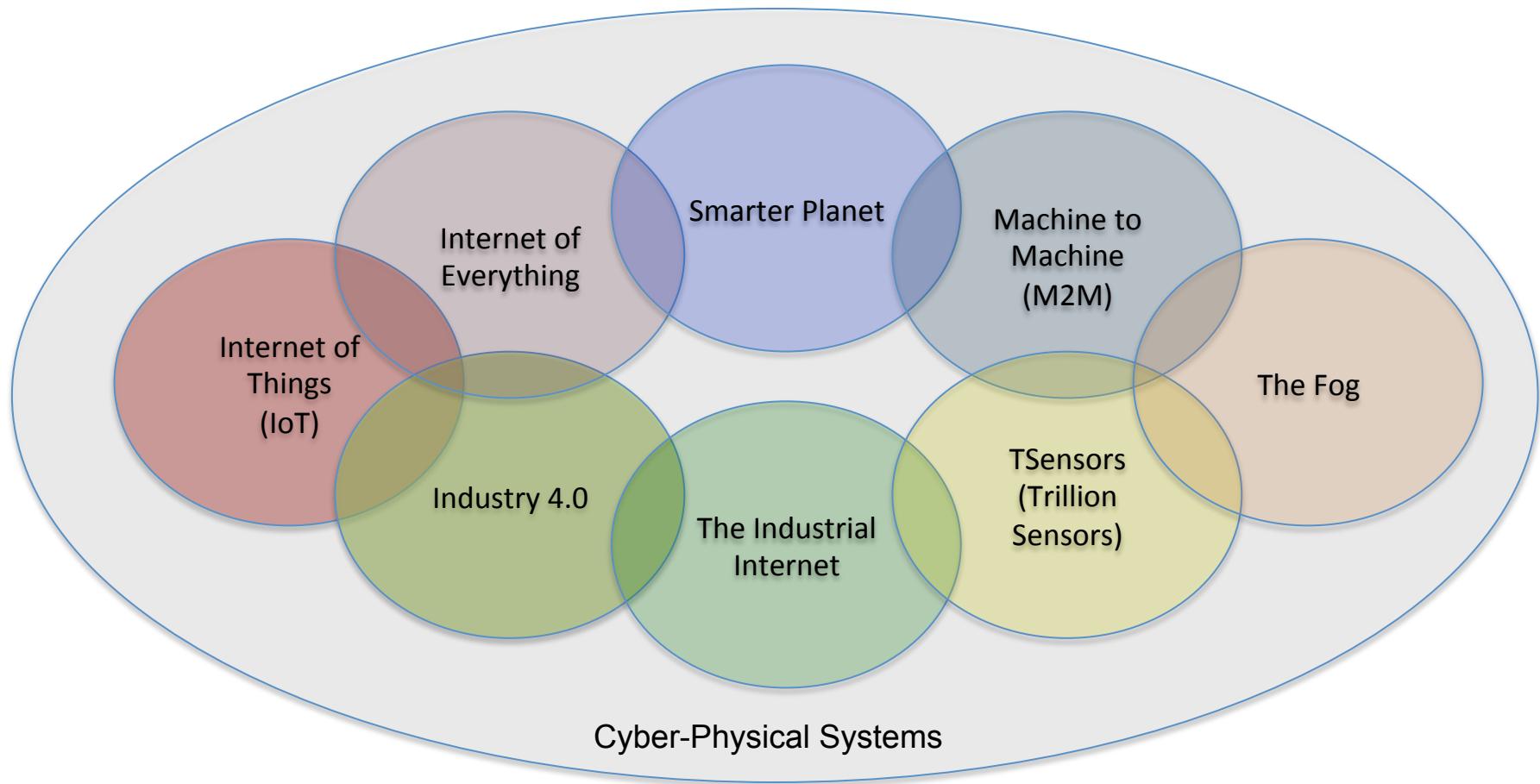
Automotive CPS and Societal Challenges

- Safer Transportation
- Reduced Emissions
- Smart Transportation
- Energy Efficiency
- Climate Change
- Human-Robot Collaboration





CPS-related terms





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- Time



Software Problems





Bad Design



Matt Haughey

@mathowie



Follow

If you need cheering up today, know that using my new IoT bike lock that only works with a phone took me 10min to unlock my bike after lunch



Lee, Berkeley, with thanks to Bjoern Hartmann

My egg tray doesn't like my Wi-Fi network. That may sound like a Mad Lib, but I'm serious. It took me 15 minutes to correctly pair Quirky's \$15 Egg Minder with the iPhone app, which gives you a count of remaining eggs. Yet when I removed eggs from the tray to make breakfast, one of them remained virtually present. I guess you could say the app was... scrambled.





Updates

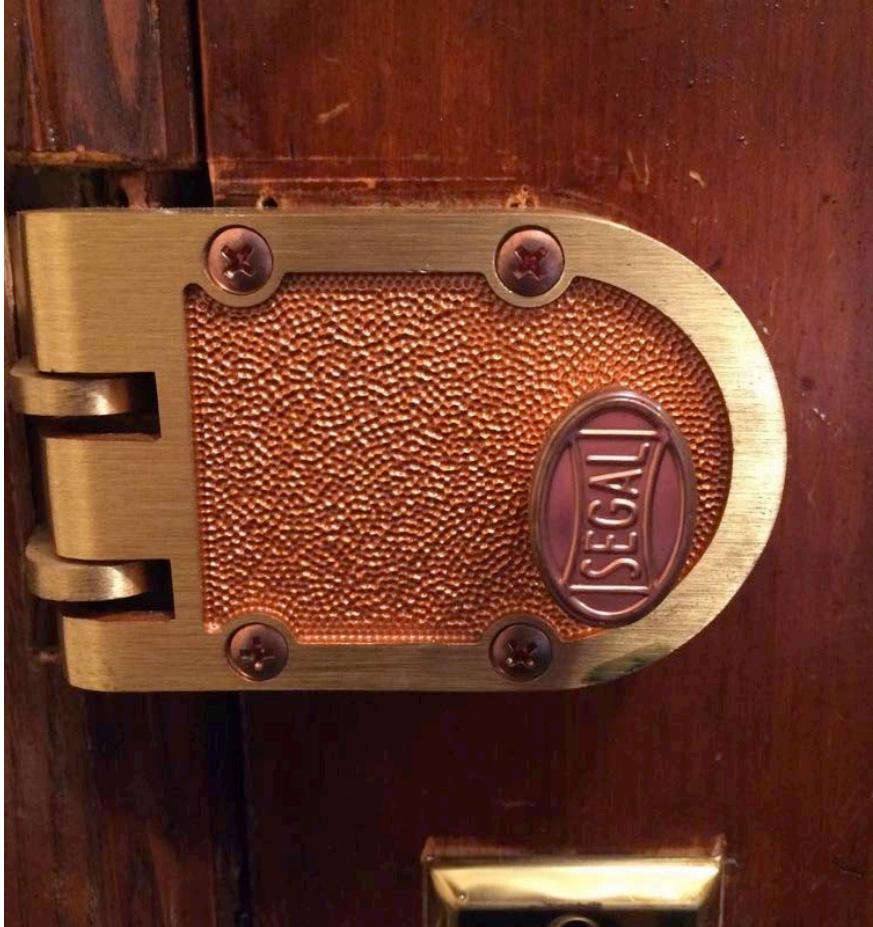


Lightbulb firmware update

“My bulbs are at 7E. I keep getting prompted to update every once in a while. About 70% of the time I get an upgrade failed message. The rest of the time I get the update completed message, but bulbs still show 7E. “

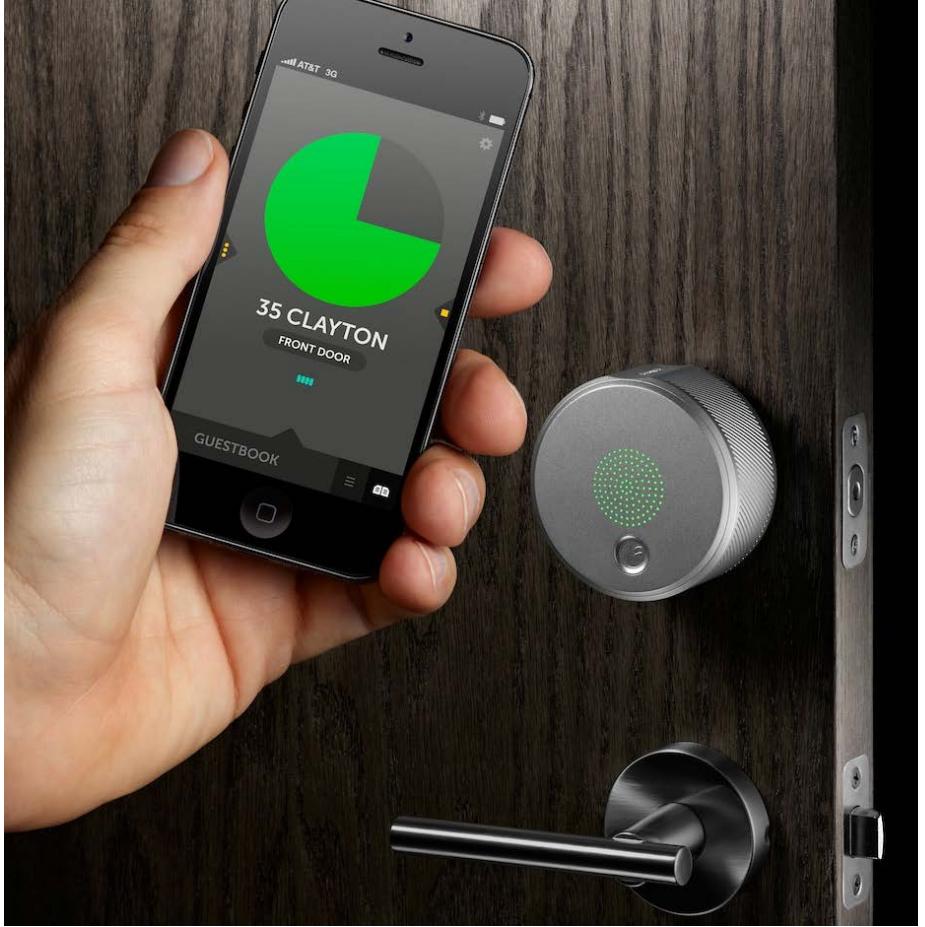


Lifespan



Segal Lock.
Lifespan: ~100 years

Lee, Berkeley, with thanks to Bjoern Hartmann



August Bluetooth Lock.
Lifespan:?



Irreproducible Results



This would eventually become a recurring theme with my thermostat. In the middle of winter it began disconnecting, frequently overnight — even when there was a solid internet connection — and didn't have a backup mode. I'd wake up seeing my own breath, then spend hours rebooting the thermostat, boiler, and router to get it working again. The only way to control the gadget is via the app, so when it breaks you're really screwed.

The thermostat company later released a second version of its device with a wall control to avoid that no-backup-when-app-breaks situation, but it was another \$150 on top of what I'd already spent trying to bring smarts to my heating. Out of frustration, I got it anyway.



Lee, Berkeley, with thanks to Bjoern Hartmann



Problems are not just annoying

NASA's Toyota Study Released by Dept. of Transportation released in 2011 found that Toyota software was “untestable.”

Possible
victim of
unintended
acceleration.





Security Risk

The New York Times

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NEW YORK, SATURDAY, OCTOBER 22, 2016



Lee, Berkeley

New Weapons Used in Attack On the Internet

By NICOLE PERLROTH

SAN FRANCISCO — Major websites were inaccessible to people across wide swaths of the United States on Friday after a company that manages crucial parts of the internet's infrastructure said it was under attack.

Users reported sporadic problems reaching several websites, including Twitter, Netflix, Spotify, Airbnb, Reddit, Etsy, SoundCloud and The New York Times.

The company, Dyn, whose servers monitor and reroute internet traffic, said it began experiencing what security experts called a distributed denial-of-service attack just after 7 a.m. Reports that many sites were inaccessible started on the East Coast, but spread westward in three waves as the day wore on and into the evening.



A Simple Challenge Problem

A software component on a microprocessor in an aircraft door provides two network services:

1. “open”
2. “disarm”

Assume state is closed and armed.

What should it do when it receives a request “open”?



Image by Christopher Doyle from Horley, United Kingdom - A321 Exit Door, CC BY-SA 2.0



A Simple Challenge Problem

A software component on a microprocessor in an aircraft door provides two network services:

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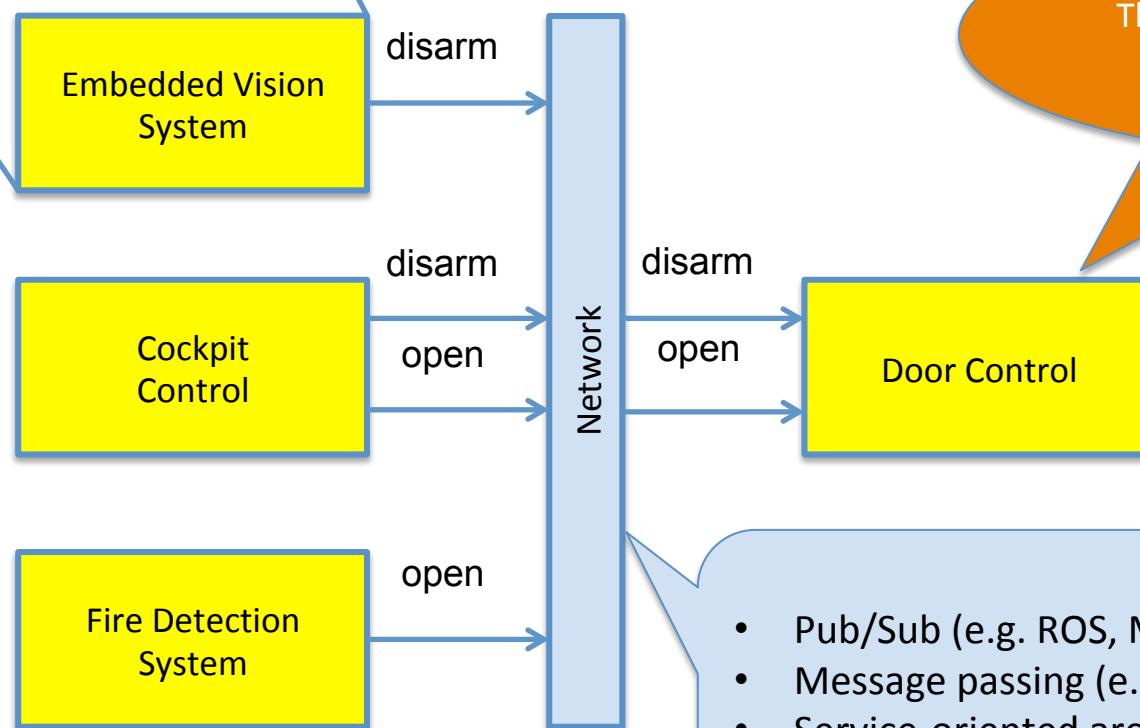


Image from *The Telegraph*, Sept. 9, 2015

Possible Architectures



Realized with an NI



The question: What to do upon receiving “open”?

- Pub/Sub (e.g. ROS, MQTT, Azure, Google Cloud)
- Message passing (e.g. Akka, Erlang)
- Service-oriented architecture (e.g. gRPC)
- Shared memory (e.g. Linda)



Some Solutions (?)

1. Just open the door.

How much to test? How much formal verification? How to constrain the design of other components? The network?

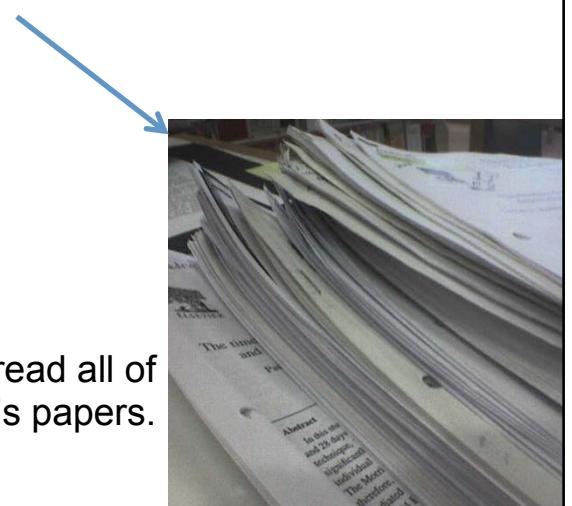
2. Send a message “ok_to_open?” Wait for responses.

How many responses? How long to wait? What if a component has failed and never responds?

3. Wait a while and then open.

How long to wait?

Better go read all of Lamport's papers.





Avionics



What is assurance?

- Software is correct?
- Compiler is correct?
- Microprocessor is correct?

Correct execution of correct software provides little assurance.



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The Kopetz Principle



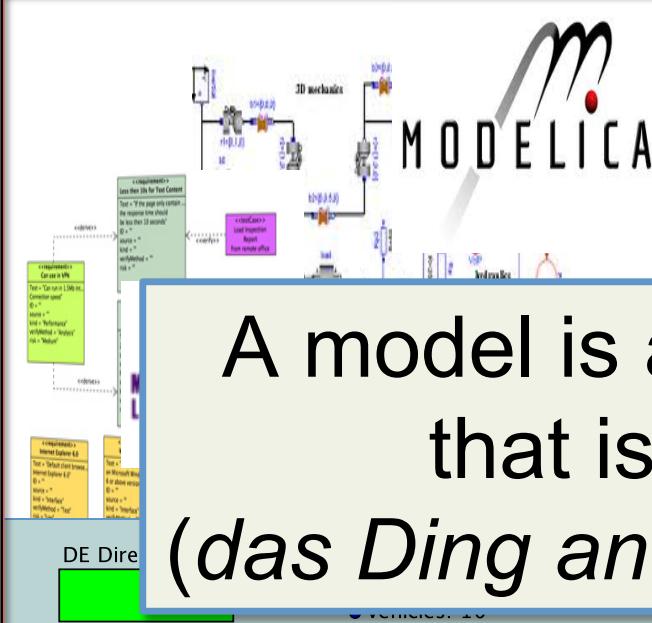
Hermann Kopetz
Professor (Emeritus)
TU Vienna

Many properties that we assert about systems (safety, determinism, timeliness, reliability) are in fact not properties of the system, but rather properties of a *model* of the system.

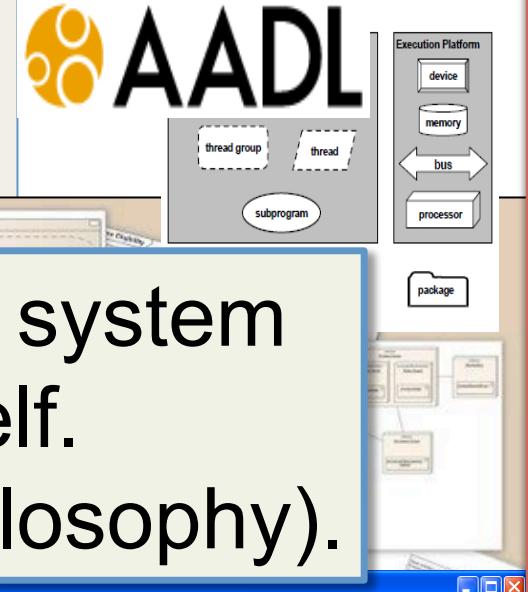
Assurance is about models, not things.



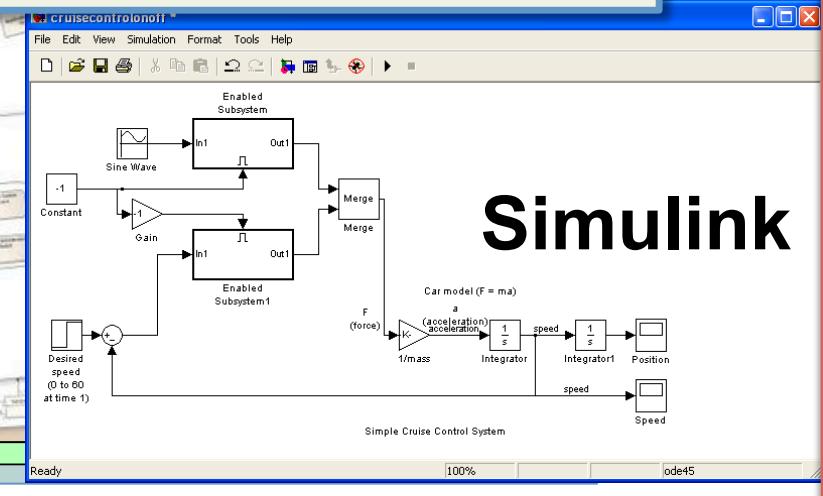
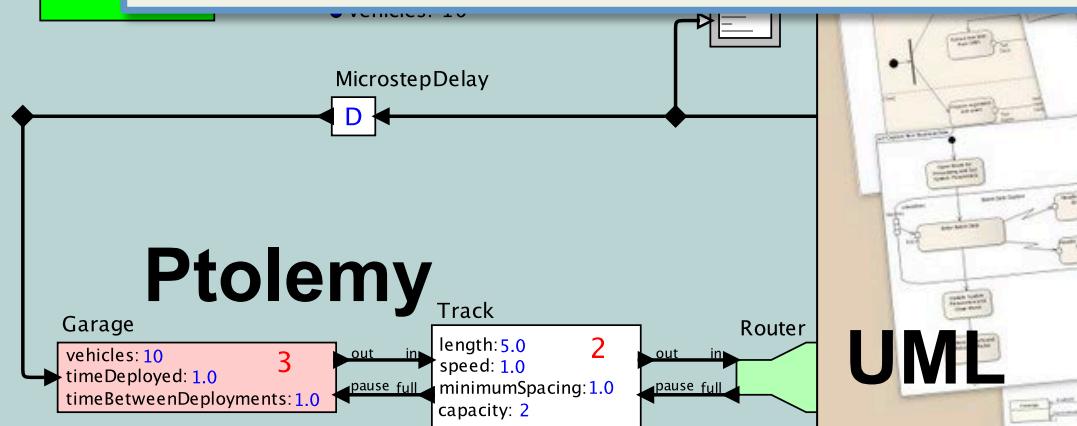
What is a model?



```
// Source code is a model:  
for (int i=0; i<10; i++) {  
    x[i] = a[i]*b[j-i];  
    notify(x[i]);  
}
```



A model is any description of a system
that is not the thing-in-itself.
(das Ding an sich in Kantian philosophy).





Quiz: Is this a Model?

```
1 void foo(int32_t x) {  
2     if (x > 1000) {  
3         x = 1000;  
4     }  
5     if (x > 0) {  
6         x = x + 1000;  
7         if (x < 0) {  
8             panic();  
9         }  
10    }  
11 }
```



The physical system has many properties not represented in the model (e.g. timing, temperature, physical volume).





Purposes of Models

- Describe structure, weight, dimensions, ...
- Describe energy needs, temperatures, ...
- Describe dynamics
- Document a design
- Simulate a behavior
- Verify that conformance with a requirement
- Specify a requirement
- ...



Properties of Models

Formal?

A *formal model* is a model given in a well-defined, machine-readable syntax and can be mechanistically manipulated using well-defined rules to derive properties of the model.

Executable?

An *executable model* is a formal model describing the dynamic behavior of a system where a machine can use the model to simulate that dynamic behavior.

Faithful?

A *faithful model* is a model that reasonably accurately conforms to properties of the thing being modeled.



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Deterministic Models

Single-threaded imperative programs

```
1 void foo(int32_t x) {  
2     if (x > 1000) {  
3         x = 1000;  
4     }  
5     if (x > 0) {  
6         x = x + 1000;  
7         if (x < 0) {  
8             panic();  
9         }  
10    }  
11 }
```

Physical System



Instruction set architecture (ISA)

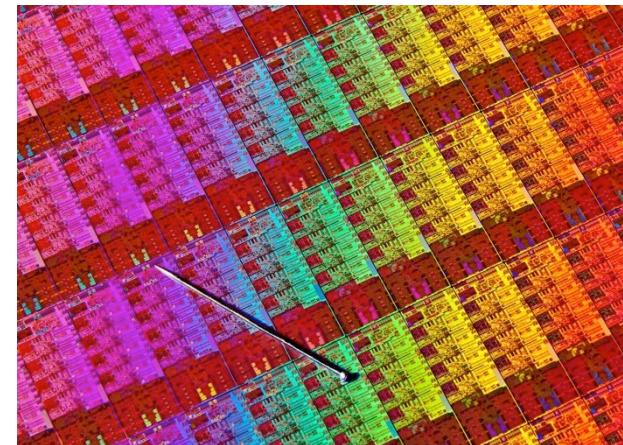
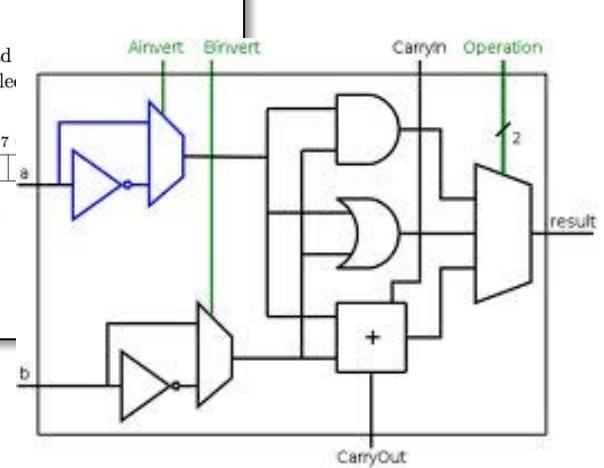
Integer Register-Register Operations

RISC-V defines several arithmetic R-type operations. All operations read as source operands and write the result into register *rd*. The *funct* field sele

31	27 26	22 21	17 16	7
rd	rs1	rs2	funct10	
5	5	5	10	
dest	src1	src2	ADD/SUB/SLT/SLTU	
dest	src1	src2	AND/OR/XOR	
dest	src1	src2	SLL/SRL/SRA	
dest	src1	src2	ADDW/SUBW	
dest	src1	src2	SLLW/SRLW/SRAW	

Waterman, et al., The RISC-V Instruction Set Manual, UCB/EECS-2011-62, 2011

Synchronous digital logic



Images: Wikimedia Commons



Determinism as a Property of Models

A **model** is *deterministic* if, given the initial *state* and the *inputs*, the model defines exactly one *behavior*.



Deterministic models have proven valuable

- They enable testing.
 - Known inputs => known outputs
- Analysis is more tractable.
 - Math: Boolean algebra, calculus, etc.
- Simulation is more useful.
 - One input yields one trace.
- Verification scales better.
 - Much smaller state space.
- More certifiable.
 - What is being certified is clearer.



Some nondeterministic designs are untestable

NASA's Toyota Study (US Dept. of Transportation, 2011) found that Toyota software was “untestable.”

Possible
victim of
unintended
acceleration





Determinism in Physics: Laplace's Demon

Pierre Simon Laplace

Pierre-Simon Laplace (1749–1827).
Portrait by Joan-Baptiste Paulin Guérin, 1838

Lee, Berkeley





Did quantum physics dash this hope?

“At first, it seemed that these hopes for a complete determinism would be dashed by the discovery early in the 20th century that events like the decay of radioactive atoms seemed to take place at random. It was as if God was playing dice, in Einstein’s phrase. **But science snatched victory from the jaws of defeat** by moving the goal posts and redefining what is meant by a complete knowledge of the universe.”

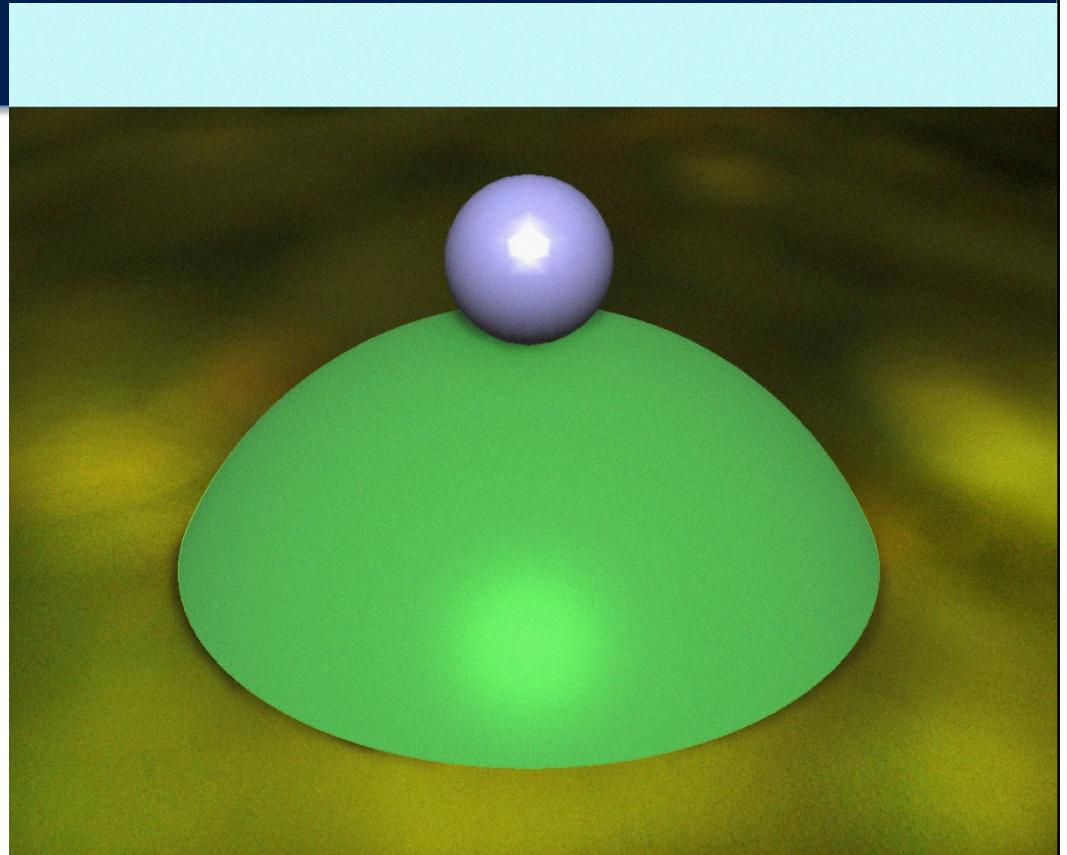
(Stephen Hawking, 2002)





Norton's Hill

Even without quantum physics, Newtonian physics is not deterministic.



Norton, J. D. (2007). Causation as Folk Science. In *Causation, Physics, and the Constitution of Reality*, Oxford, Clarendon Press.

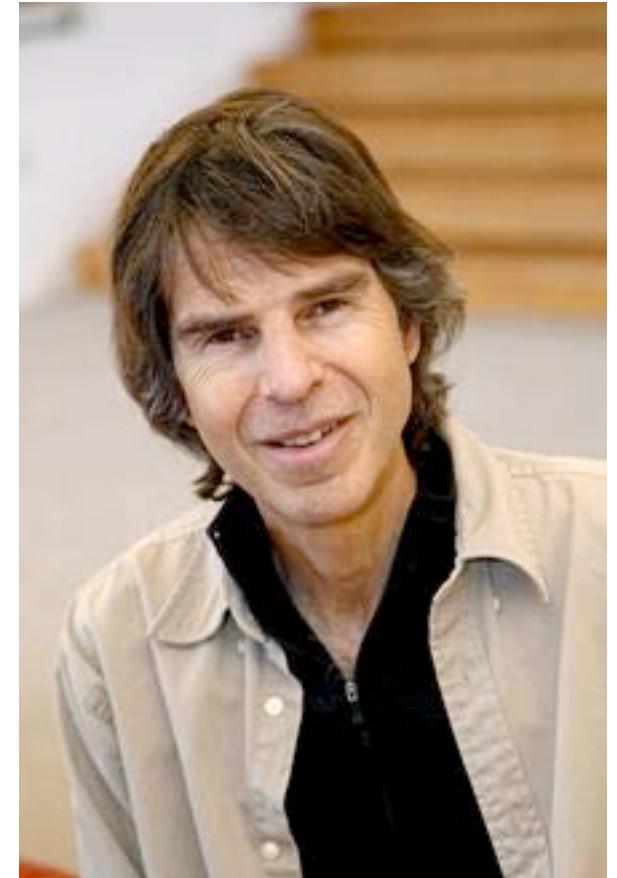
Metastable system that obeys all of Newton's laws but is nondeterministic.



Laplace's Demon cannot exist.

In 2008, David Wolpert proved that
Laplace's demon cannot exist.

His proof relies on the observation
that such a demon, were it to exist,
would have to exist in the very
physical world that it predicts.



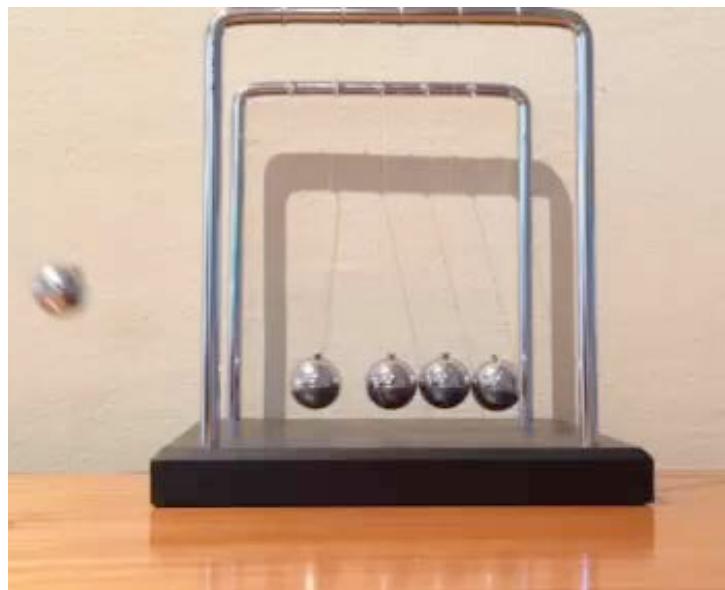
David Wolpert



Determinism is a property of models, not things

$$x(t) = x(0) + \int_0^t v(\tau) d\tau$$
$$v(t) = v(0) + \frac{1}{m} \int_0^t F(\tau) d\tau,$$

Deterministic
model



Deterministic
system?



Determinism as a Property of Models

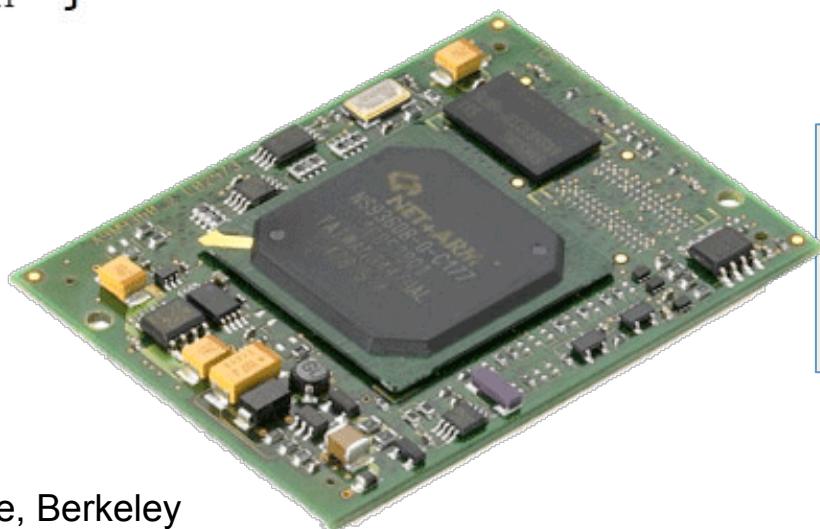
A **model** is *deterministic* if, given the initial *state* and the *inputs*, the model defines exactly one *behavior*.

Our most valuable models are *deterministic*.



Software as a Model

```
1 void foo(int32_t x) {  
2     if (x > 1000) {  
3         x = 1000;  
4     }  
5     if (x > 0) {  
6         x = x + 1000;  
7         if (x < 0) {  
8             panic();  
9         }  
10    }  
11 }
```



This program defines exactly one behavior, given the input x .

The modeling framework defines state, input, and behavior.

The physical system has many properties not represented in the model (e.g. timing, temperature, ...).



Architecture as a Model

Physical System Model



Image: Wikimedia Commons

Integer Register-Register Operations

RISC-V defines several arithmetic R-type operations. All operations read the *rs1* and *rs2* registers as source operands and write the result into register *rd*. The *funct* field selects the type of operation.

31	27 26	22 21	17 16	7 6	0
rd	rs1	rs2	funct10	opcode	
5	5	5	10	7	
dest	src1	src2	ADD/SUB/SLT/SLTU	OP	
dest	src1	src2	AND/OR/XOR	OP	
dest	src1	src2	SLL/SRL/SRA	OP	
dest	src1	src2	ADDW/SUBW	OP-32	
dest	src1	src2	SLLW/SRLW/SRAW	OP-32	

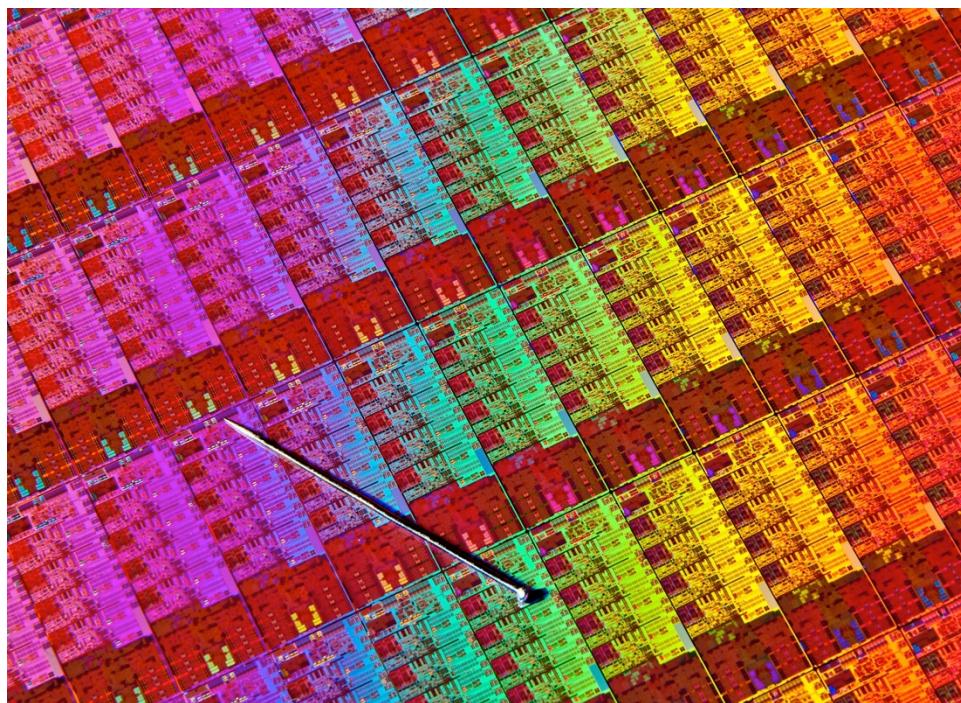
Waterman, et al., The RISC-V Instruction Set Manual,
UCB/EECS-2011-62, 2011

*Instruction Set Architectures (ISAs)
are deterministic models*

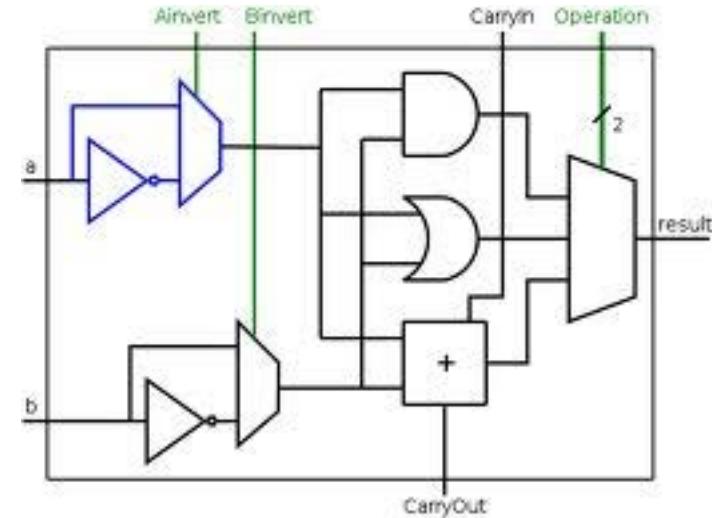


Digital Circuits as Models

Physical System



Model



Synchronous digital logic
is a deterministic model



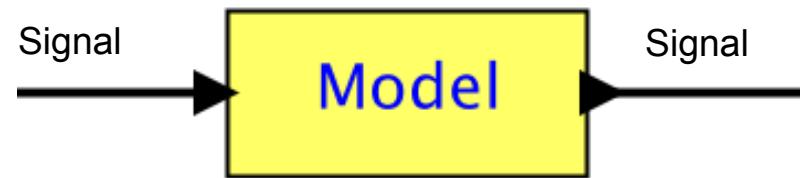
Physical Dynamics as a Model

Physical System



Image: Wikimedia Commons

Model



$$\dot{\mathbf{x}}(t) = \dot{\mathbf{x}}(0) + \frac{1}{M} \int_0^t \mathbf{F}(\tau) d\tau$$

Differential Equations
are deterministic models



CPS combinations of deterministic models are nondeterministic



Lee, Berkeley

Image: Wikimedia Commons

```
1 void initTimer(void) {
2     SysTickPeriodSet(SysCtlClockGet() / 1000);
3     SysTickEnable();
4     SysTickIntEnable();
5 }
6 volatile uint timer_count = 0;
7 void ISR(void) {
8     if(timer_count != 0) {
9         timer_count--;
10    }
11 }
12 int main(void) {
13     SysTickIntRegister(&ISR);
14     .. // other init
15     timer_count = 2000;
16     initTimer();
17     while(timer_count != 0) {
18         ... code to run for 2 seconds
19     }
20     ... // other code
21 }
```



$$\dot{\mathbf{x}}(t) = \dot{\mathbf{x}}(0) + \frac{1}{M} \int_0^t \mathbf{F}(\tau) d\tau$$



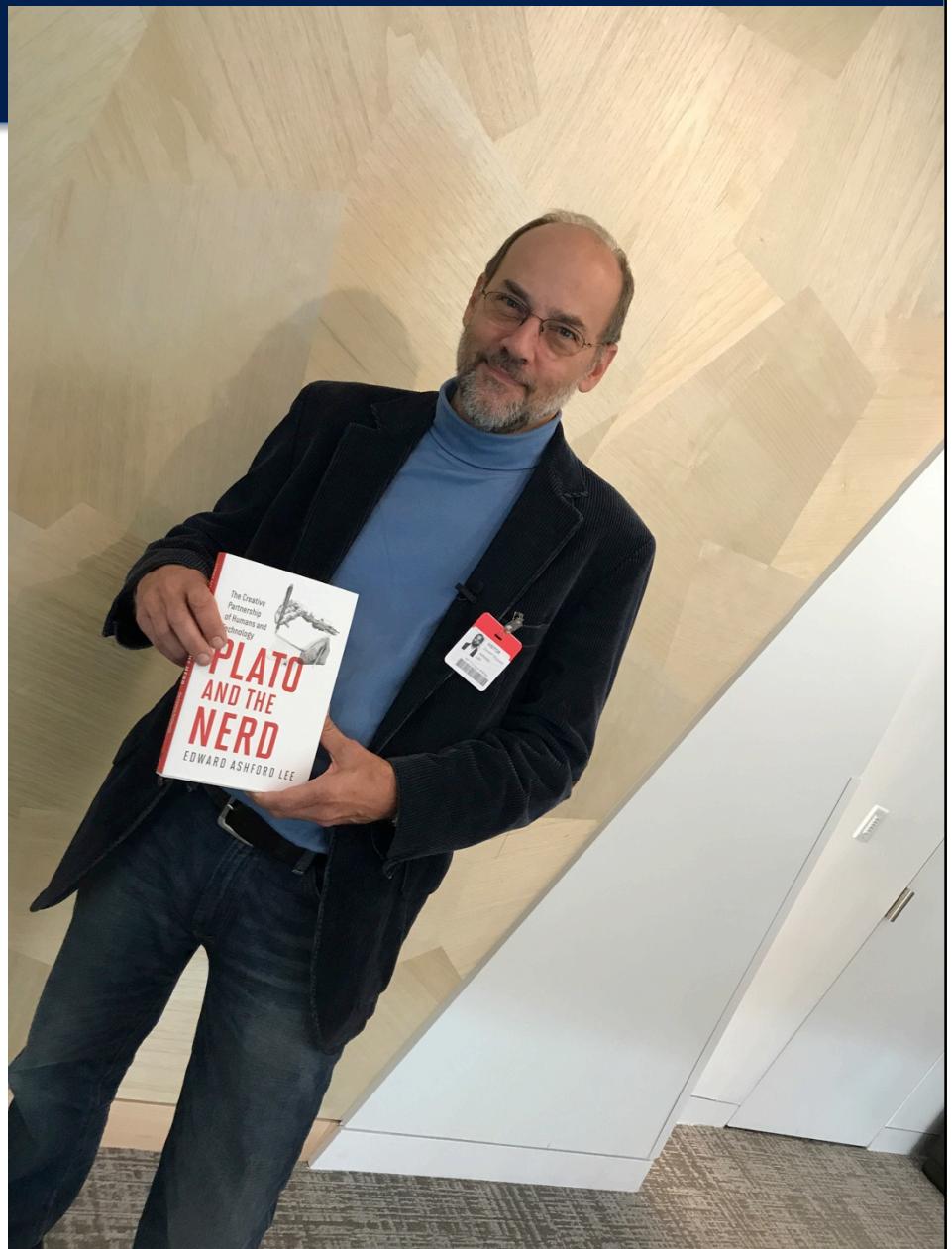
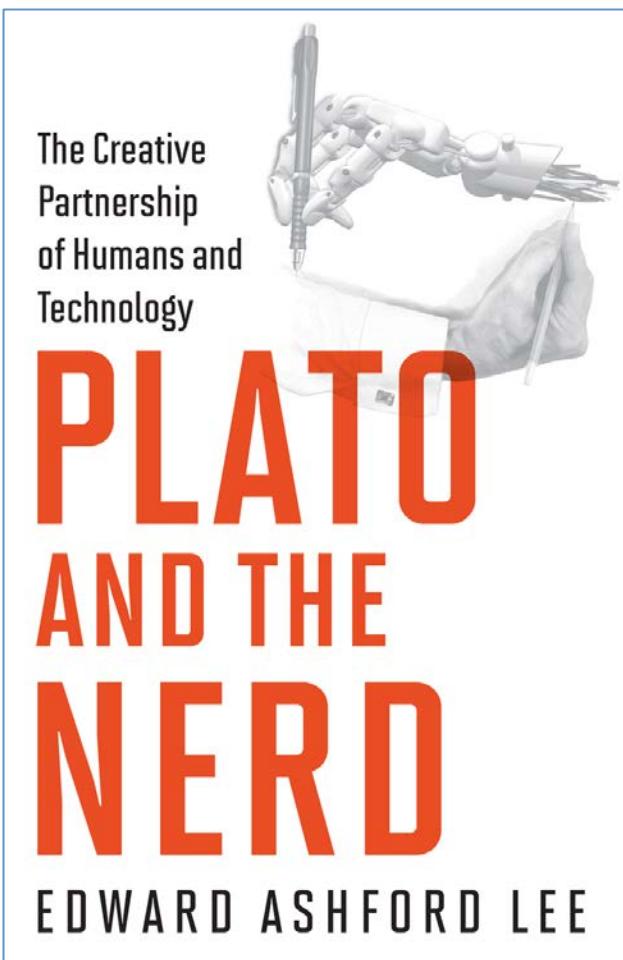
Determinism? What about resilience? Adaptability?

Deterministic models do not eliminate the need for robust, fault-tolerant designs.

In fact, they *enable* such designs, because they make it much clearer what it means to have a fault!



An Epiphany





Two Usage Patterns for Models

- In *science*, the value of a model lies in how well its behavior matches that of the physical system.
- In *engineering*, the value of a *physical system* lies in how well its behavior matches that of the model.

A scientist asks, “Can I make a model for this thing?”

An engineer asks, “Can I make a thing for this model?”

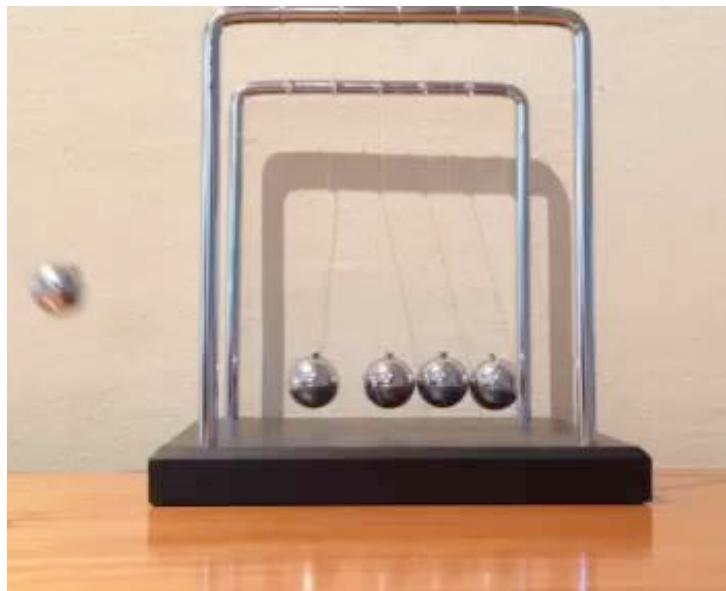


Models vs. Reality

$$x(t) = x(0) + \int_0^t v(\tau) d\tau$$

$$v(t) = v(0) + \frac{1}{m} \int_0^t F(\tau) d\tau.$$

The model



The target
(the thing
being
modeled).

In this example,
the *modeling
framework* is
calculus and
Newton's laws.

Fidelity is how
well the model
and its target
match



A Model

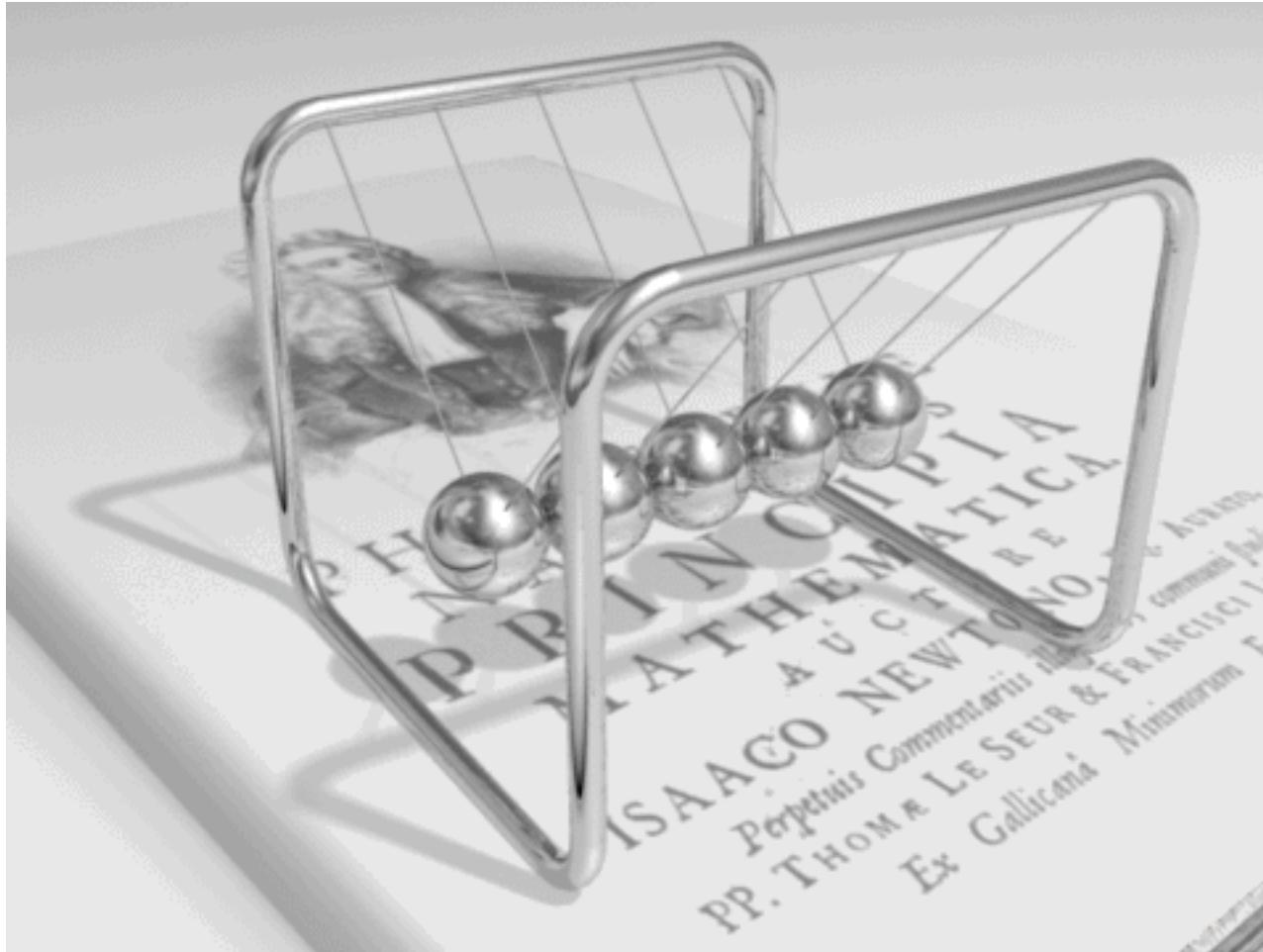
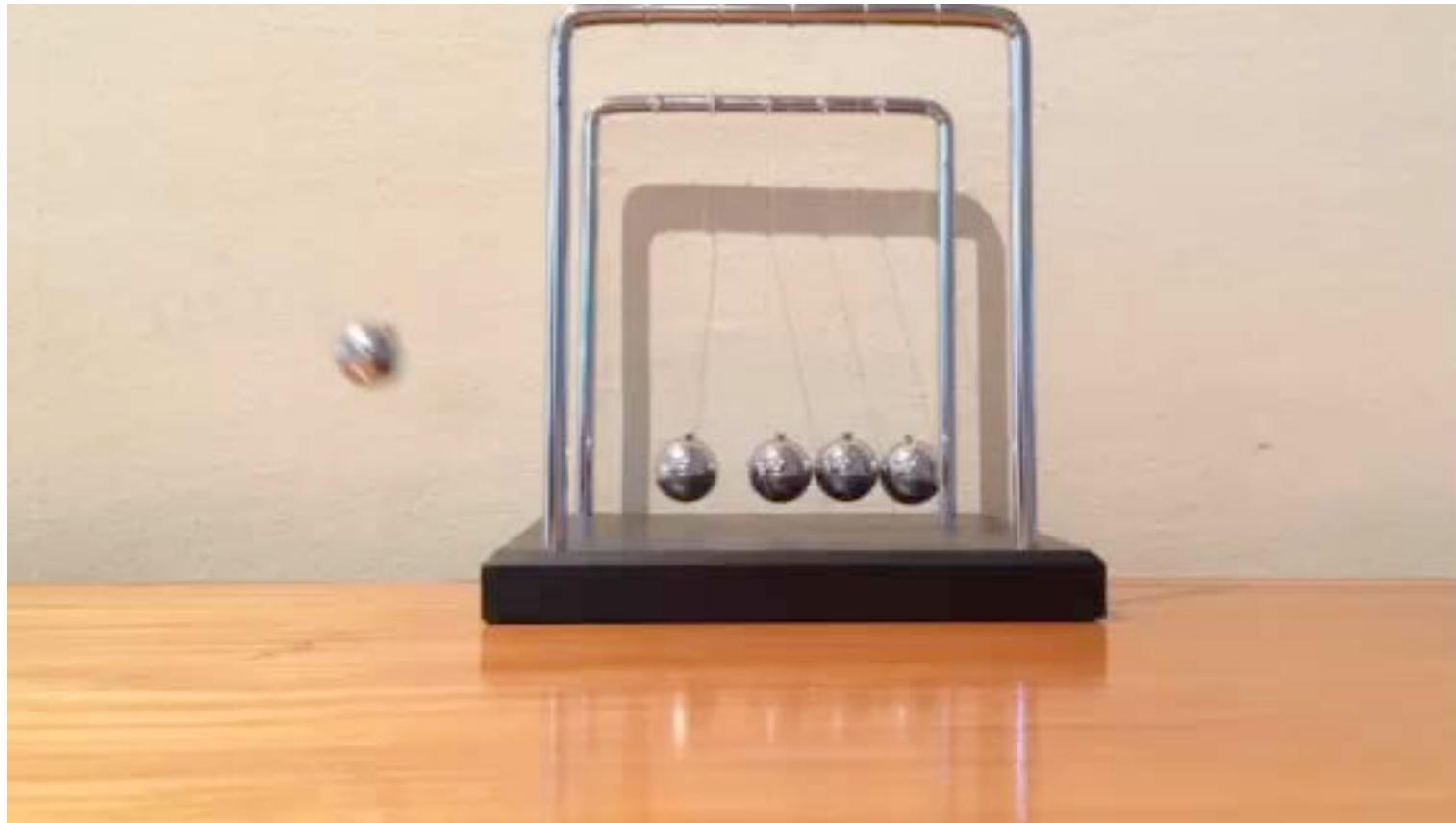


Image by Dominique Toussaint, GNU Free Documentation License, Version 1.2 or later.



A Physical Realization





Model Fidelity

- To a *scientist*, the model is flawed.
- To an *engineer*, the realization is flawed.

To a realist, both are flawed...



Useful Models and Useful Things

“Essentially, all models are wrong,
but some are useful.”

Box, G. E. P. and N. R. Draper, 1987: *Empirical Model-Building and Response Surfaces*. Wiley Series in Probability and Statistics, Wiley.

“Essentially, all system implementations
are wrong, but some are useful.”

Lee and Sirjani, “What good are models,” FACS 2018.



The Value of Simulation

“Simulation is doomed to succeed.”

Could this statement be confusing engineering and scientific models?



Figure 1: Three scenes generated from a single ~20-line SCENIC scenario representing bumper-to-bumper traffic.

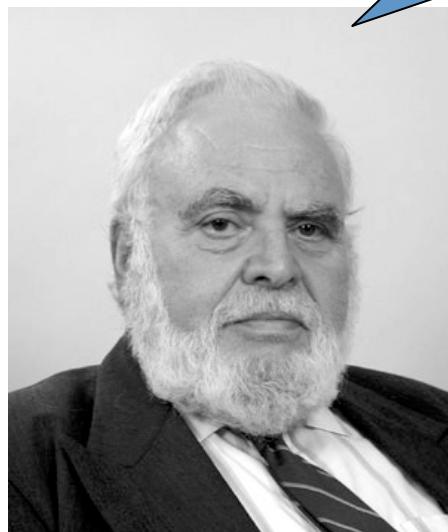
[Fremont, et al., Scenic: Language-Based Scene Generation, Arxiv.org, Sept. 2018]



Engineers often confuse the model with its target

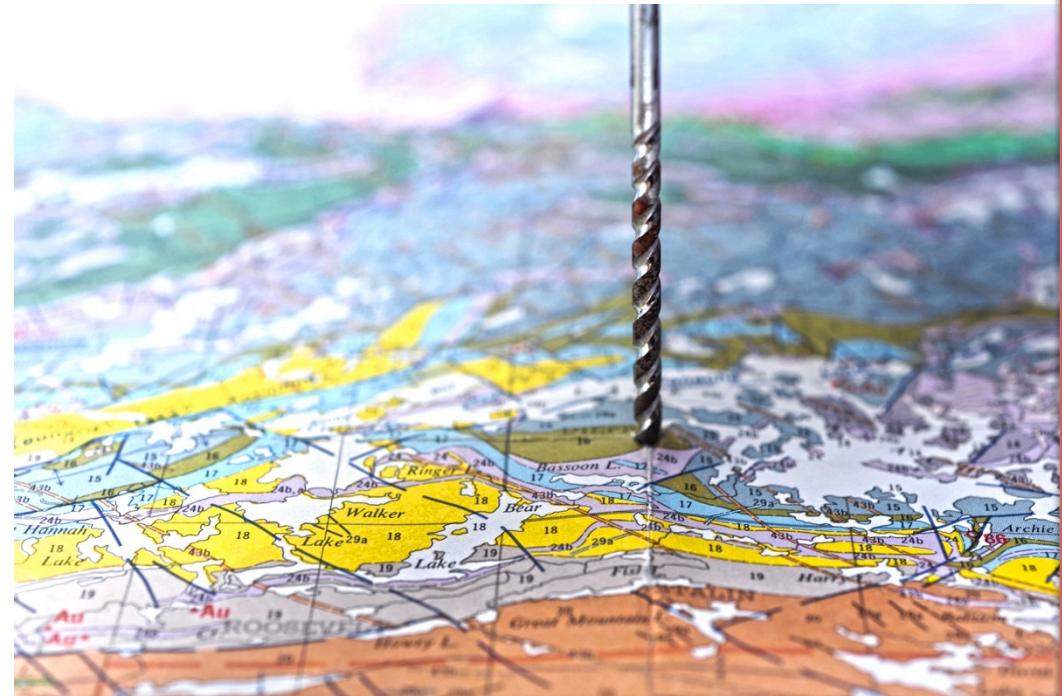
You will never strike oil by
drilling through the map!

But this does not in any way
diminish the value of a map!



Solomon Wolf Golomb

Lee, Berkeley





Model-Based Design of Cyber-Physical Systems

Changing the Question:

Is the question whether we can build models
describing the behavior of cyber-physical systems?

Or

Is the question whether we can make cyber-physical
systems that behave like our models?



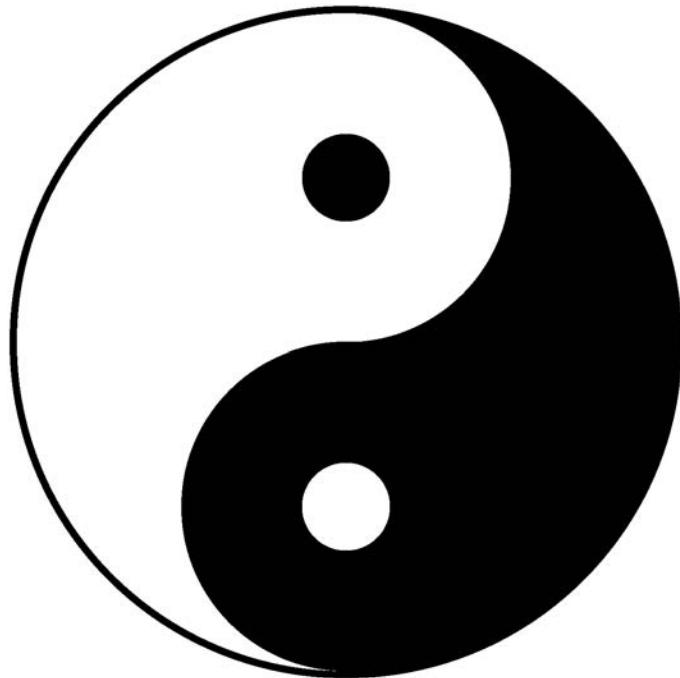
Outline

- Cyber-Physical Systems (CPS)
- Challenges
- Models
- Determinism
- Limits of Determinism
- Abstraction and Refinement
- Time



But...

Determinism has its limits.



- Complexity
- Uncertainty
- Chaos
- Incompleteness



Complexity

- Some systems are too complex for deterministic models.
- Nondeterministic abstractions become useful.

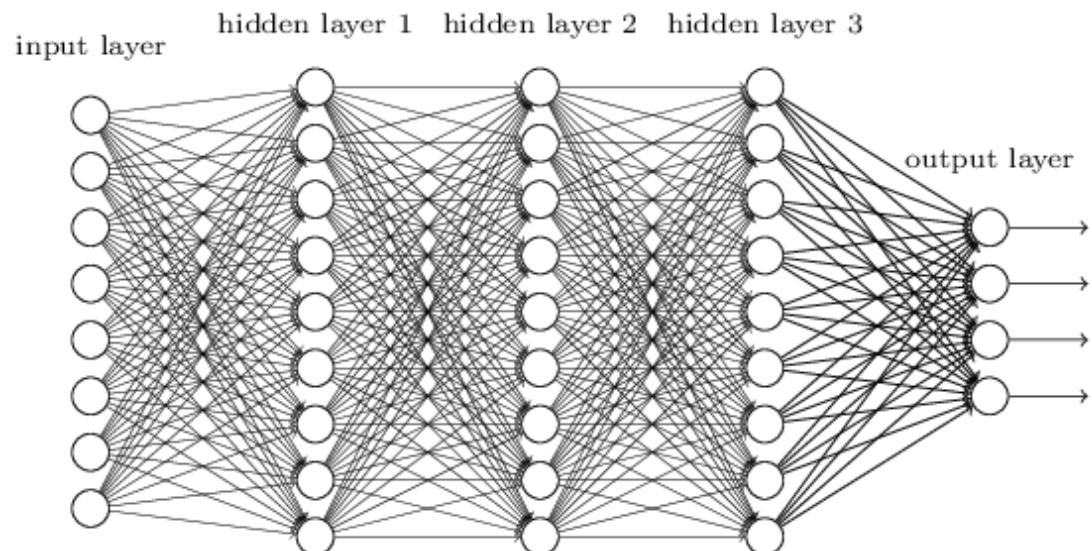


“Iron wing” model of an Airbus A350.



Complexity

- Some systems are too complex for deterministic models.
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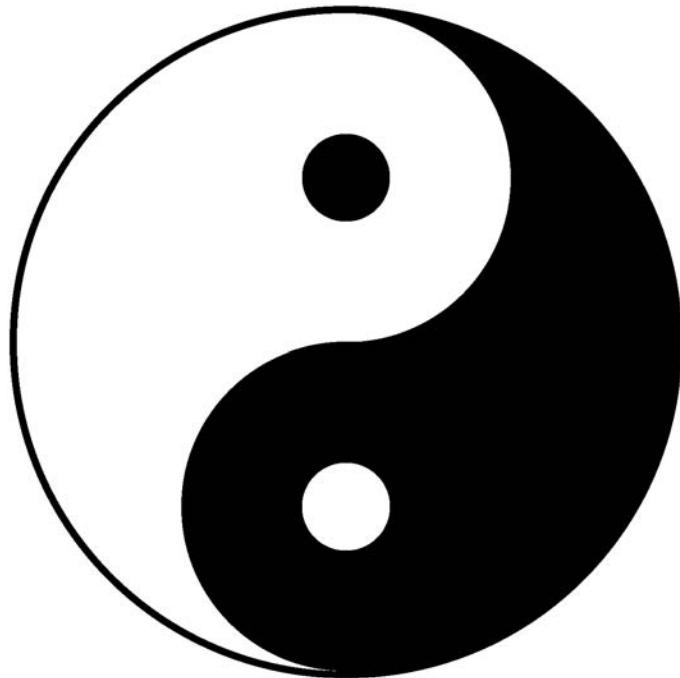


[Deep Learning](#), draft book in preparation, by Yoshua Bengio, Ian Goodfellow, and Aaron Courville.
<http://www.deeplearningbook.org/>



But...

Determinism has its limits.



- Complexity
- Uncertainty
- Chaos
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Uncertainty

- We can't construct deterministic models of what we don't know.
- For this, nondeterminism is useful.
- Bayesian probability (which is mostly due to Laplace) quantifies uncertainty.

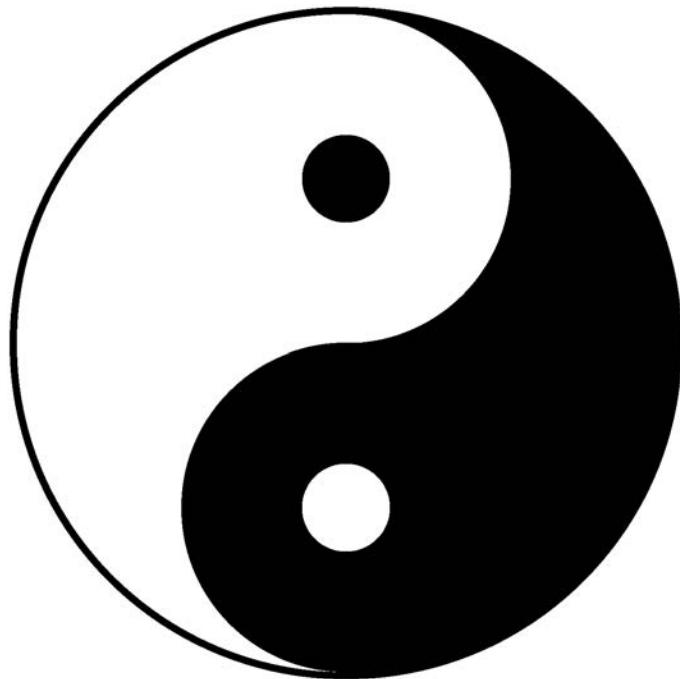


Portrait of Reverend Thomas Bayes (1701 - 1761) that is probably not actually him.



But...

Determinism has its limits.



- Complexity
- Uncertainty
- Chaos
- Incompleteness

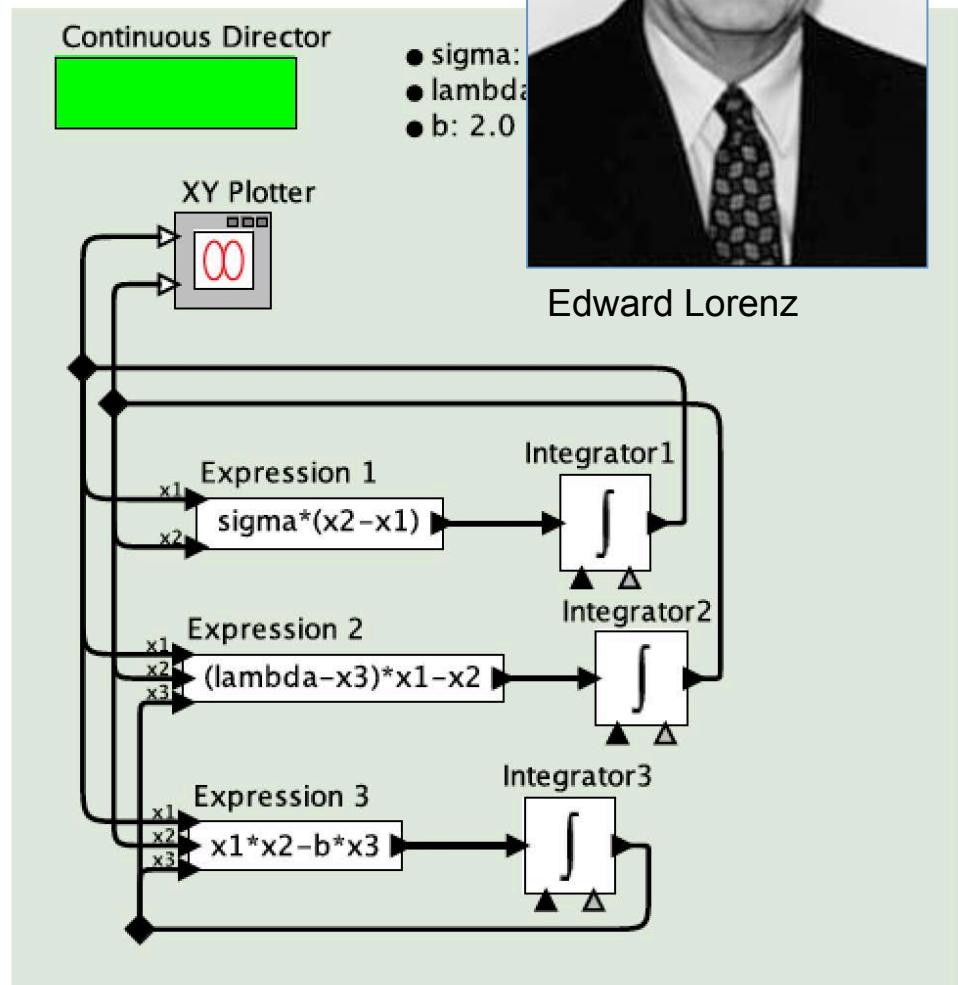


Determinism does not imply predictability

Lorenz attractor:

$$\begin{aligned}\dot{x}_1(t) &= \sigma(x_2(t) - x_1(t)) \\ \dot{x}_2(t) &= (\lambda - x_3(t))x_1(t) - x_2(t) \\ \dot{x}_3(t) &= x_1(t)x_2(t) - bx_3(t)\end{aligned}$$

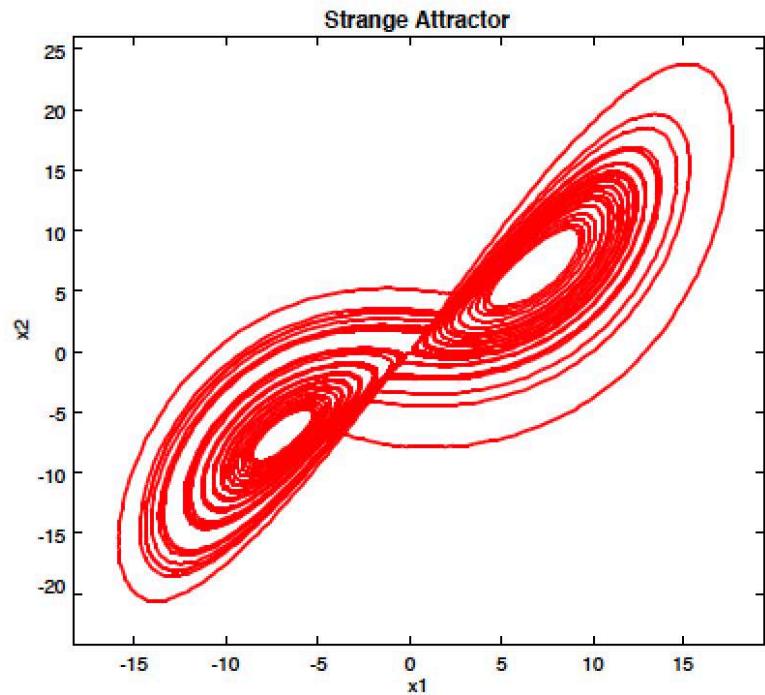
This is a chaotic system, so arbitrarily small perturbations have arbitrarily large consequences.



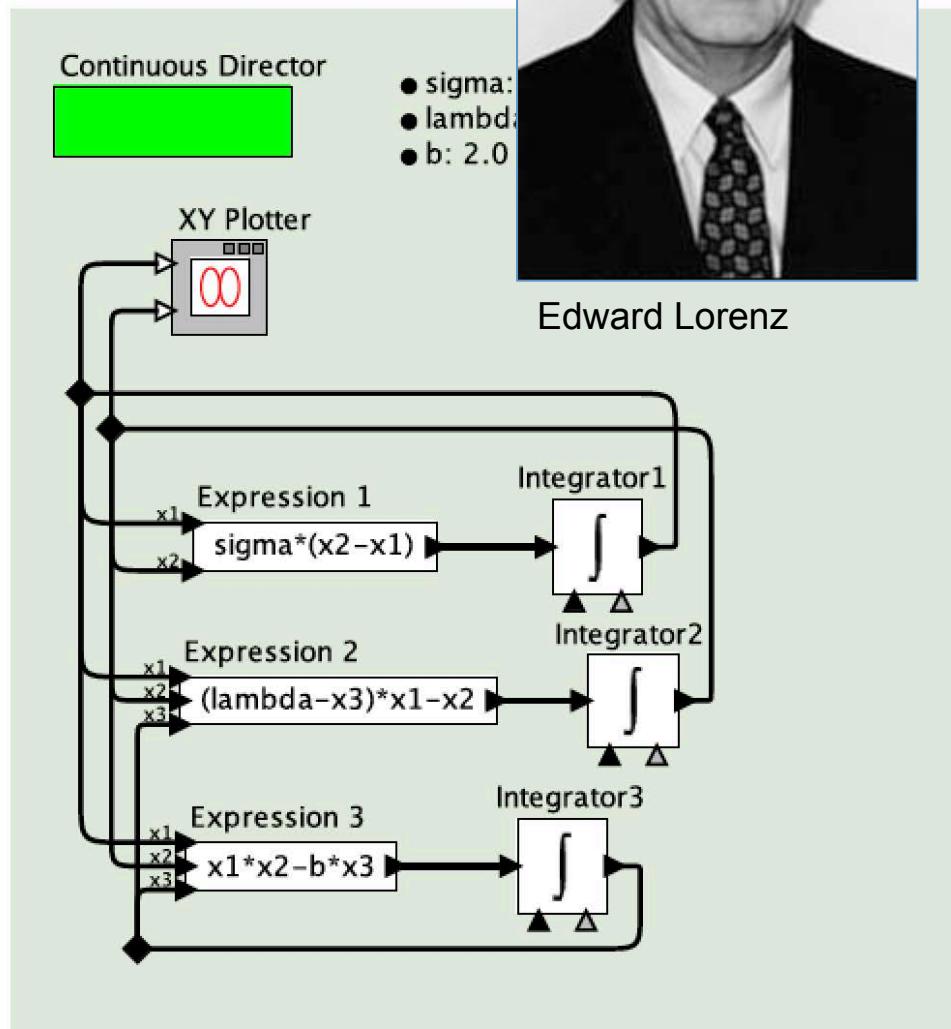


Determinism does not imply predictability

Plot of x_1 vs. x_2 :



The position of a point is not meaningfully predictable even though the system is deterministic.





Determinism does not imply predictability

Deterministic
real-time
scheduling
results in
chaos.

[Thiele and Kumar,
EMSOFT 2015]

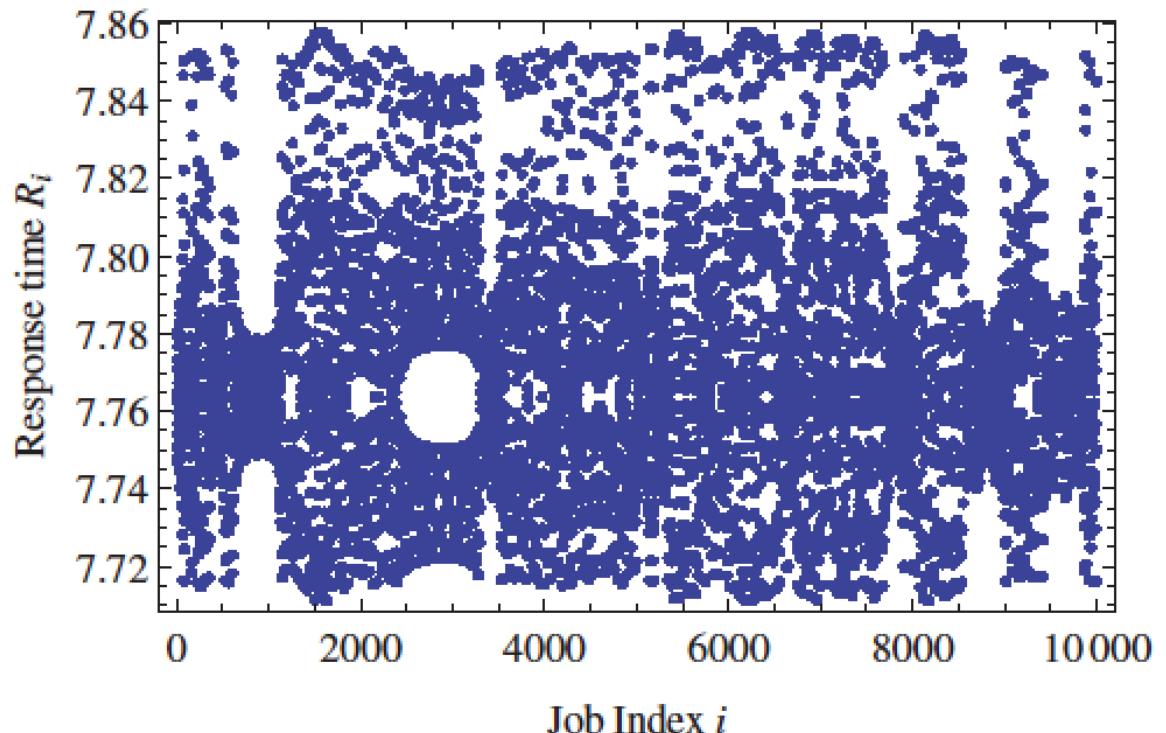
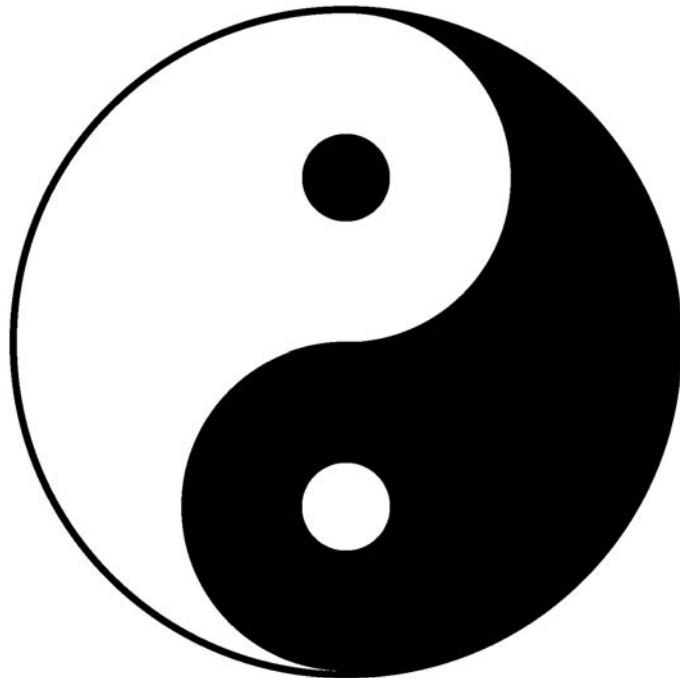


Fig. 15. Response time across jobs for the multi-resource scheduler with $R_s(i - 1) = 7.76$ and $R_s(i - 2) = 7.74$.



But...

Determinism has its limits.



- Complexity
- Uncertainty
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Incompleteness of Determinism

Any set of deterministic models rich enough to encompass Newton's laws plus discrete transitions is incomplete.

Lee, *Fundamental Limits of Cyber-Physical Systems Modeling*, ACM Tr. on CPS, Vol. 1, No. 1, November 2016

Fundamental Limits of Cyber-Physical Systems Modeling

EDWARD A. LEE, EECS Department, UC Berkeley

This article examines the role of modeling in the engineering of cyber-physical systems. It argues that the role that models play in engineering is different from the role they play in science, and that this difference should direct us to use a different class of models, where simplicity and clarity of semantics dominate over accuracy and detail. I argue that determinism in models used for engineering is a valuable property and should be preserved whenever possible, regardless of whether the system being modeled is deterministic. I then identify three classes of fundamental limits on modeling, specifically chaotic behavior, the inability of computers to numerically handle a continuum, and the incompleteness of determinism. The last of these has profound consequences.

CCS Concepts: • Theory of computation → Timed and hybrid models; • Computing methodologies → Modeling methodologies; • Software and its engineering → Domain specific languages

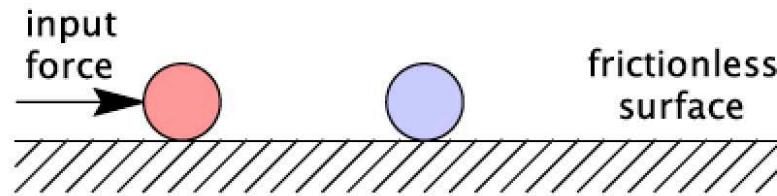
Additional Key Words and Phrases: Chaos, continuums, completeness

ACM Reference Format:

Edward A. Lee. 2016. Fundamental limits of cyber-physical systems modeling. ACM Trans. Cyber-Phys. Syst. 1, 1, Article 3 (November 2016), 26 pages.
DOI: <http://dx.doi.org/10.1145/2912149>



Illustration of the Incompleteness of Determinism



Conservation of momentum:

$$m_1 v'_1 + m_2 v'_2 = m_1 v_1 + m_2 v_2.$$

Conservation of kinetic energy:

$$\frac{m_1(v'_1)^2}{2} + \frac{m_2(v'_2)^2}{2} = \frac{m_1(v_1)^2}{2} + \frac{m_2(v_2)^2}{2}.$$

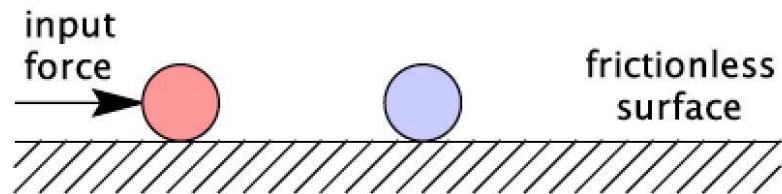
We have two equations and two unknowns, v'_1 and v'_2 .



Illustration of the Incompleteness of Determinism

Quadratic problem has two solutions.

Solution 1: $v'_1 = v_1$, $v'_2 = v_2$
(ignore collision).



Solution 2:

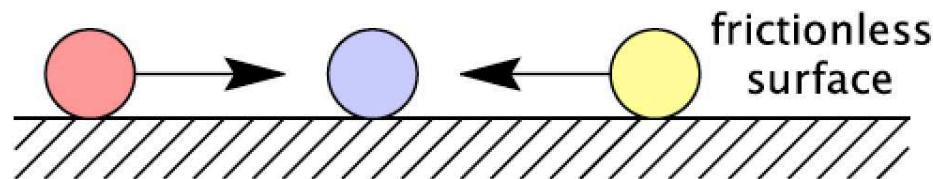
$$v'_1 = \frac{v_1(m_1 - m_2) + 2m_2 v_2}{m_1 + m_2}$$
$$v'_2 = \frac{v_2(m_2 - m_1) + 2m_1 v_1}{m_1 + m_2}.$$

Note that if $m_1 = m_2$, then the two masses simply exchange velocities (Newton's cradle).



Illustration of the Incompleteness of Determinism

Consider this scenario:

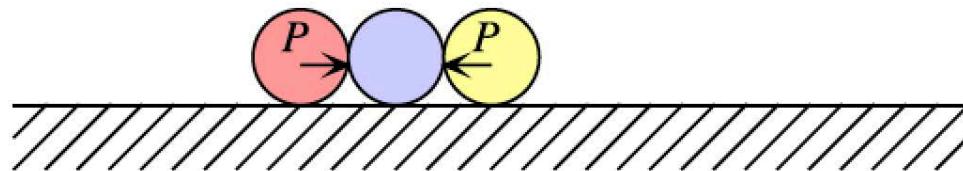


Simultaneous collisions where one collision does not cause the other.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

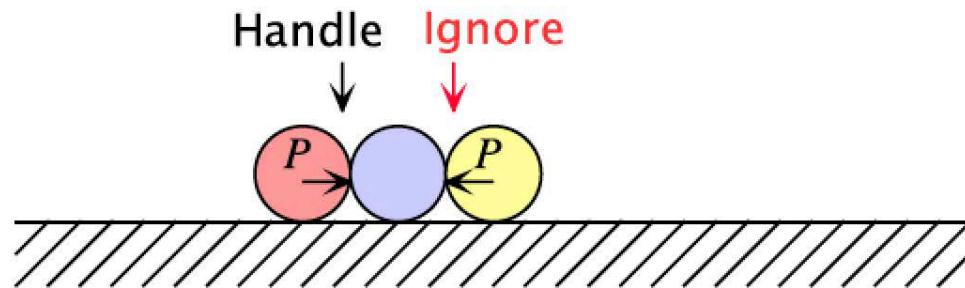


At superdense time $(\tau, 0)$, we have two simultaneous collisions.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

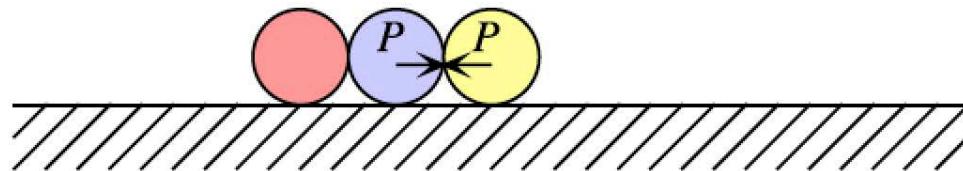


At superdense time $(\tau, 1)$, choose arbitrarily to handle the left collision.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

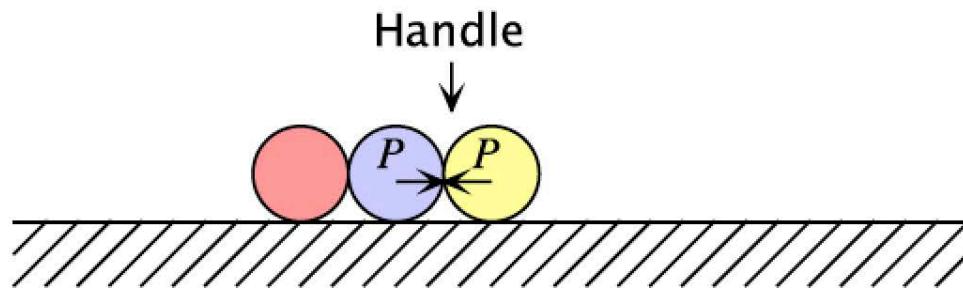


After superdense time $(\tau, 1)$, the momentums are as shown.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

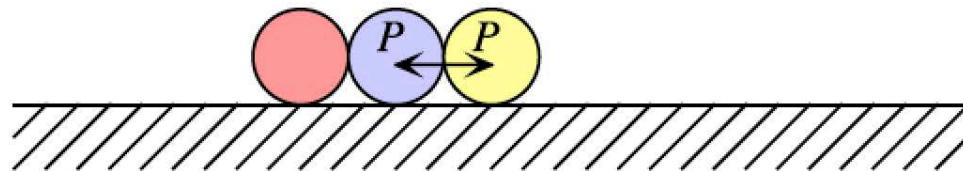


At superdense time $(\tau, 2)$, handle the new collision.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

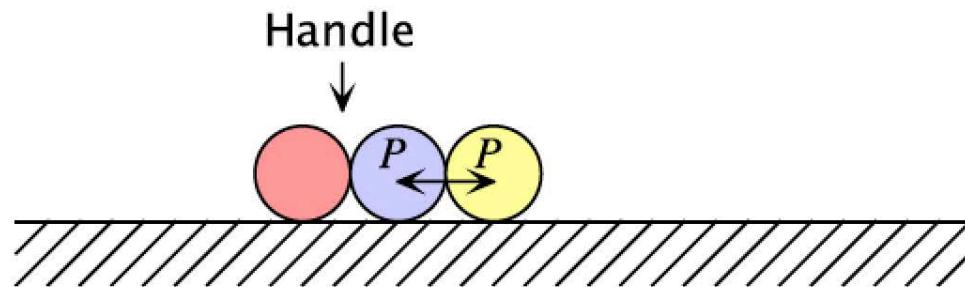


After superdense time $(\tau, 2)$, the momentums are as shown.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

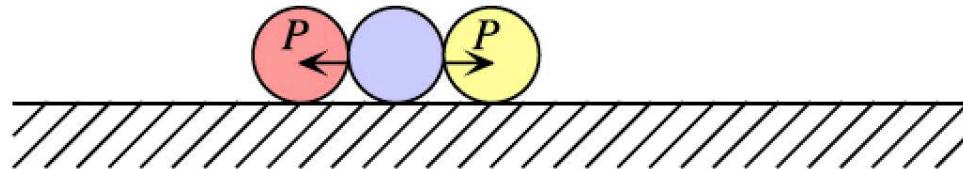


At superdense time $(\tau, 3)$, handle the new collision.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

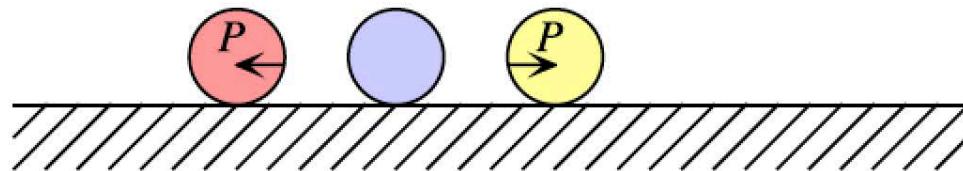


After superdense time $(\tau, 3)$, the momentums are as shown.



Illustration of the Incompleteness of Determinism

One solution: nondeterministic interleaving of the collisions:

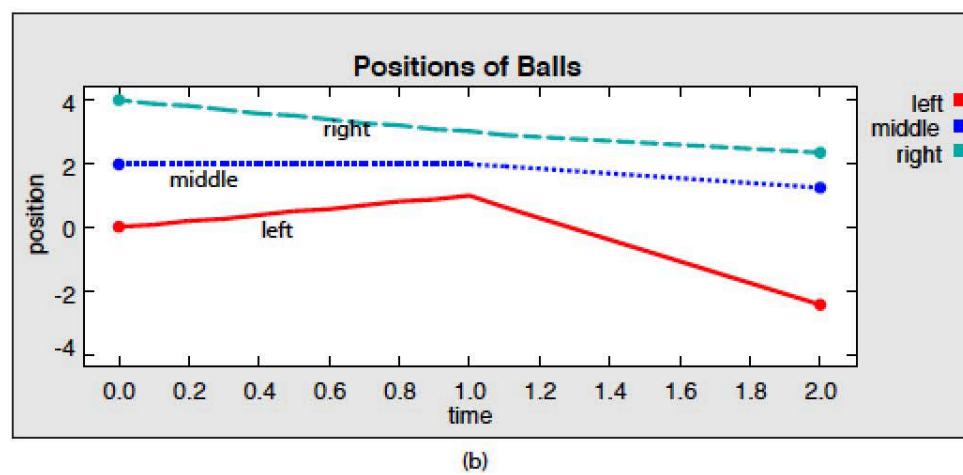
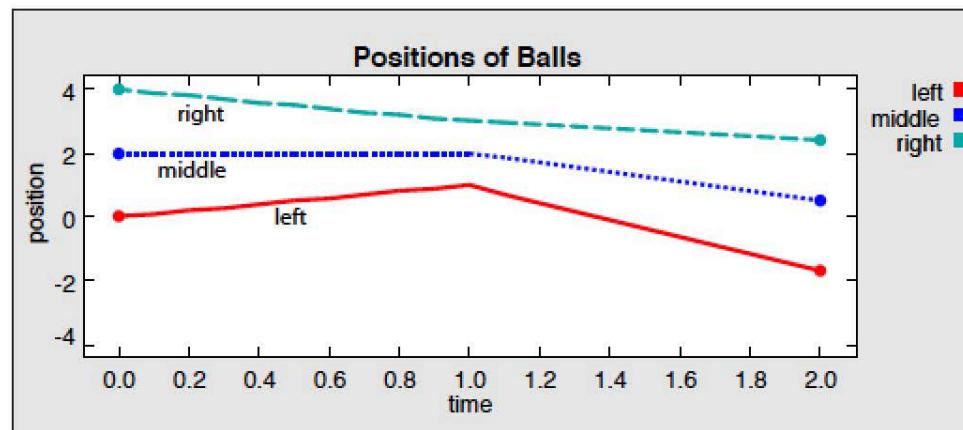


The balls move away at equal speed (if their masses are the same!)



Arbitrary Interleaving Yields Nondeterminism

If the masses are different, the behavior depends on which collision is handled first!

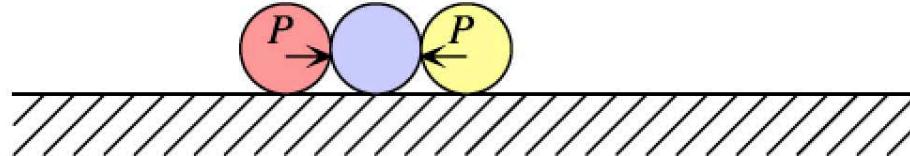




Recall the Heisenberg Uncertainty Principle

We cannot simultaneously know the position and momentum of an object to arbitrary precision.

But the reaction to these collisions depends on knowing position and momentum precisely.

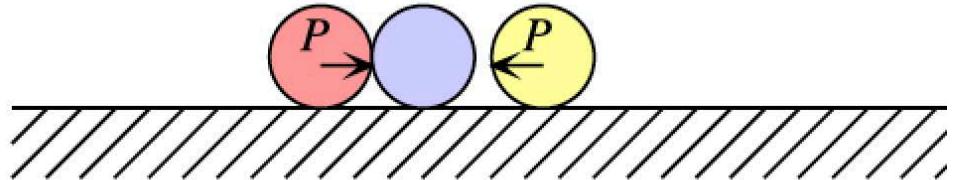




Is Determinism Incomplete?

Let τ be the time between collisions. Consider a sequence of models for $\tau > 0$ where $\tau \rightarrow 0$.

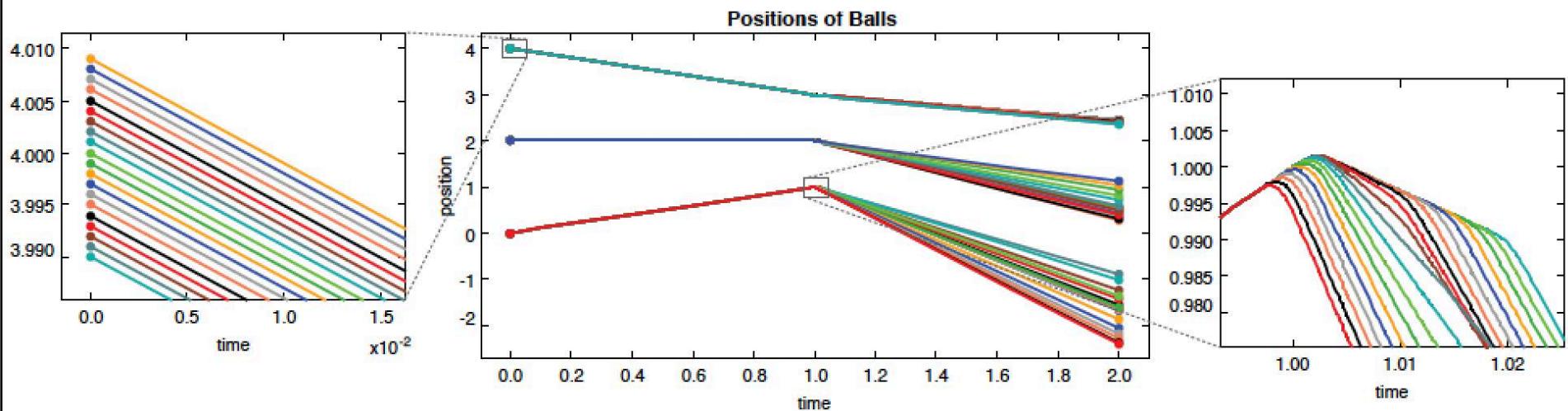
Every model in the sequence is deterministic, but the limit model is not.



- In Lee (2016), I show that this sequence of models is Cauchy, so the space of deterministic models is incomplete (it does not contain its own limit points).
- In Lee (2014), I show that a direct description of this scenario results in a non-constructive model. The nondeterminism arises in making this model constructive.



Rejecting discreteness leads to deterministic chaos



[Lee, ACM Tr. on CPS, 2016]

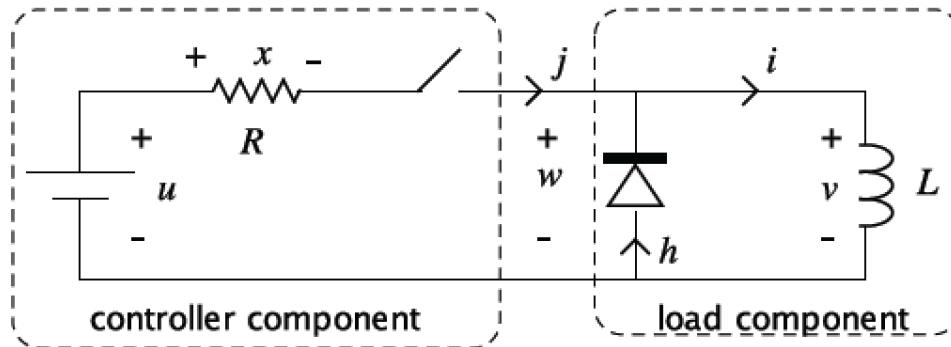
A continuous deterministic model that models collisions as elastic springs is chaotic.



Rejecting discreteness requires rejecting causality

Example from Lee,
“Constructive Models of Discrete and
Continuous Physical Phenomena,” IEEE
Access, 2014

A **flyback diode** is a commonly used circuit that prevents arcing when disconnecting an inductive load (like a motor) from a power source.



When the switch goes from closed to open, the causality and direct feedthrough properties of the two components reverse.

There is no logic that can transition from A causes B to B causes A smoothly without passing through non-constructive models.



Outline

- Cyber-Physical Systems (CPS)
- Challenges
- Models
- Determinism
- Limits of Determinism
- Abstraction and Refinement
- Time



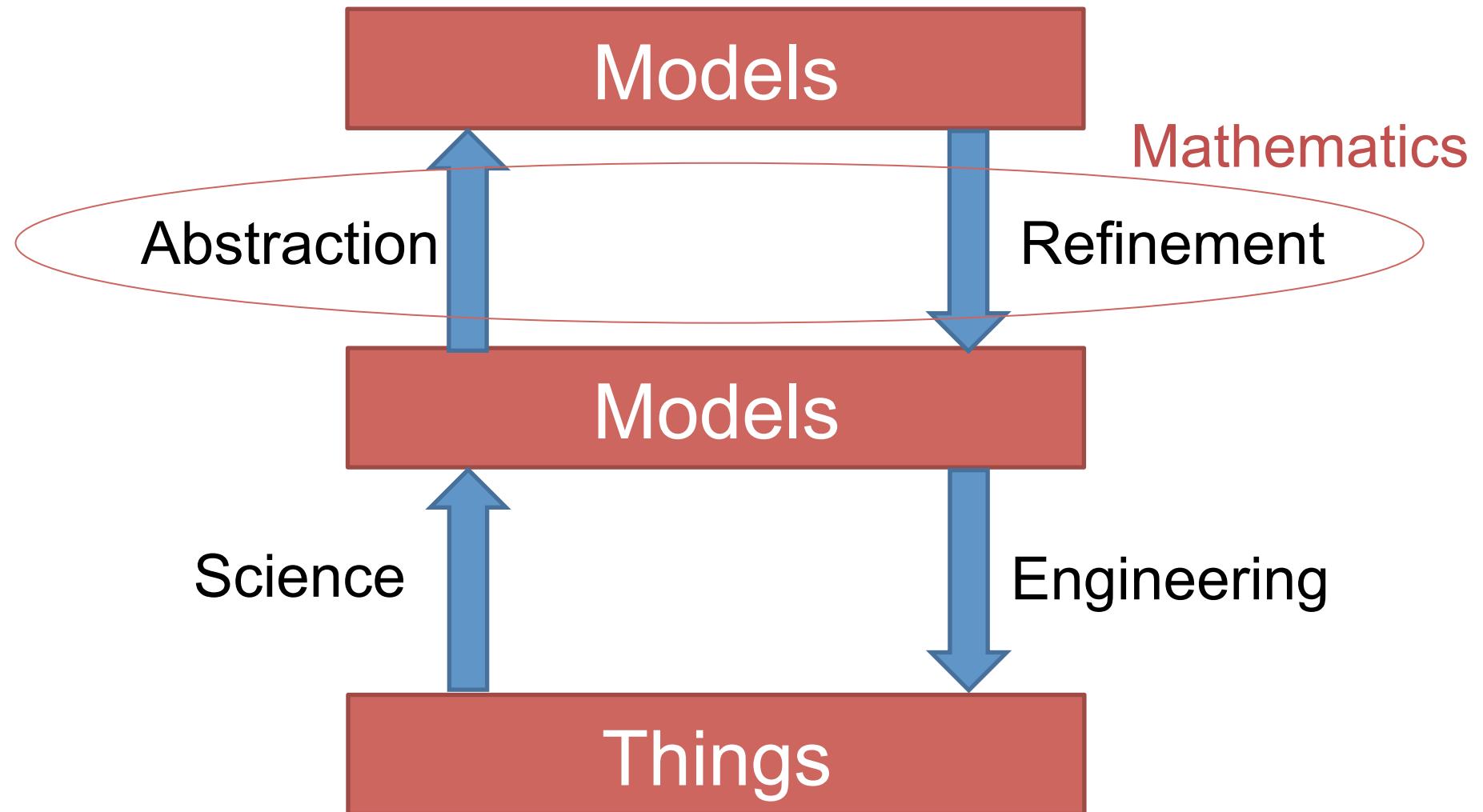
Abstraction and Refinement

- An **abstraction A of B** is **sound** if every *property of interest* that is true for A is also true for B
- If A is a sound abstraction of B, then
B is a **refinement** of A

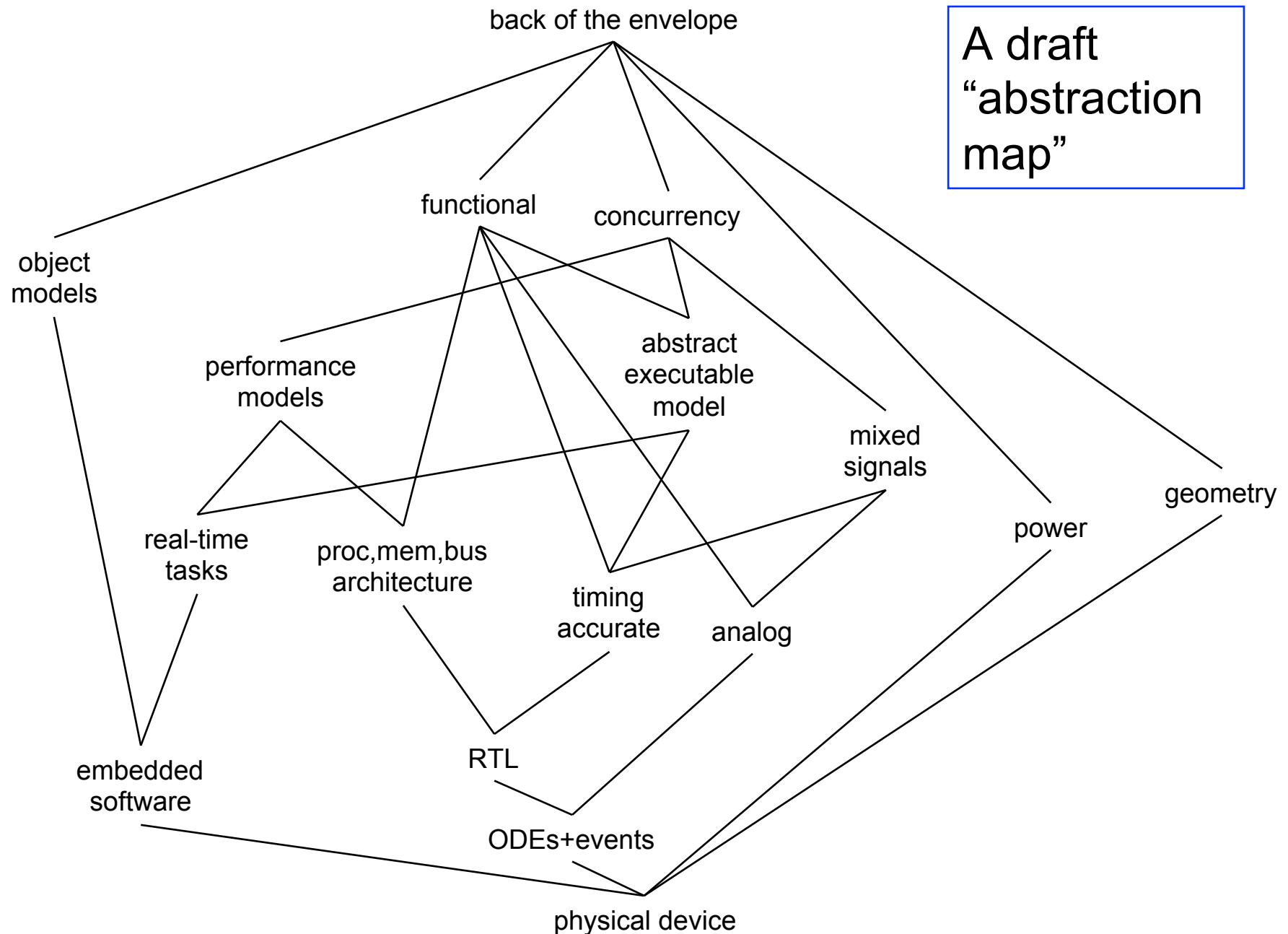
A simulation (of model A) is “doomed to succeed” in that it will not reveal properties of a refinement (B) nor of the thing-in-itself that are not also properties of A.



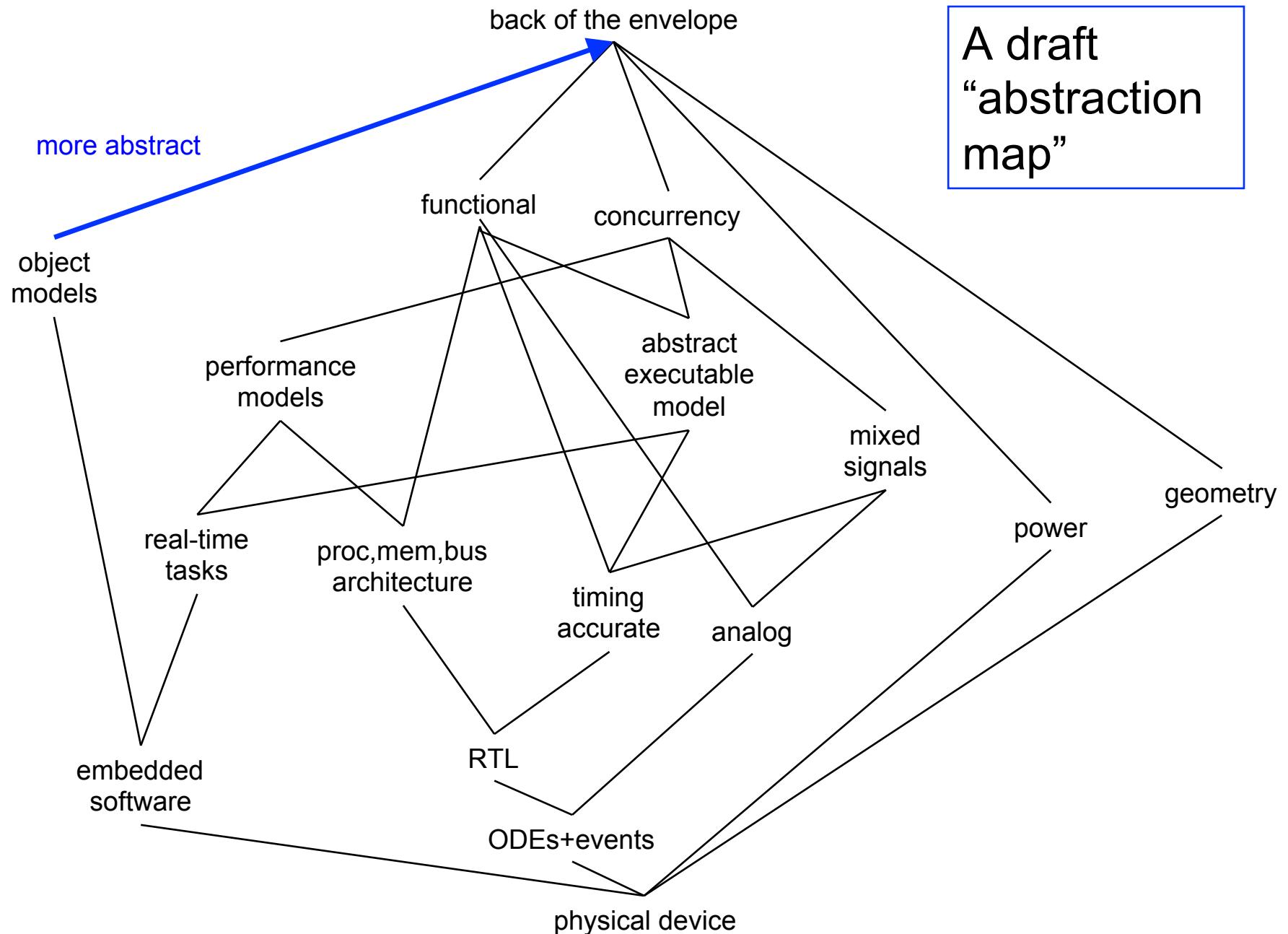
Models and Things (vs. Models and Models)



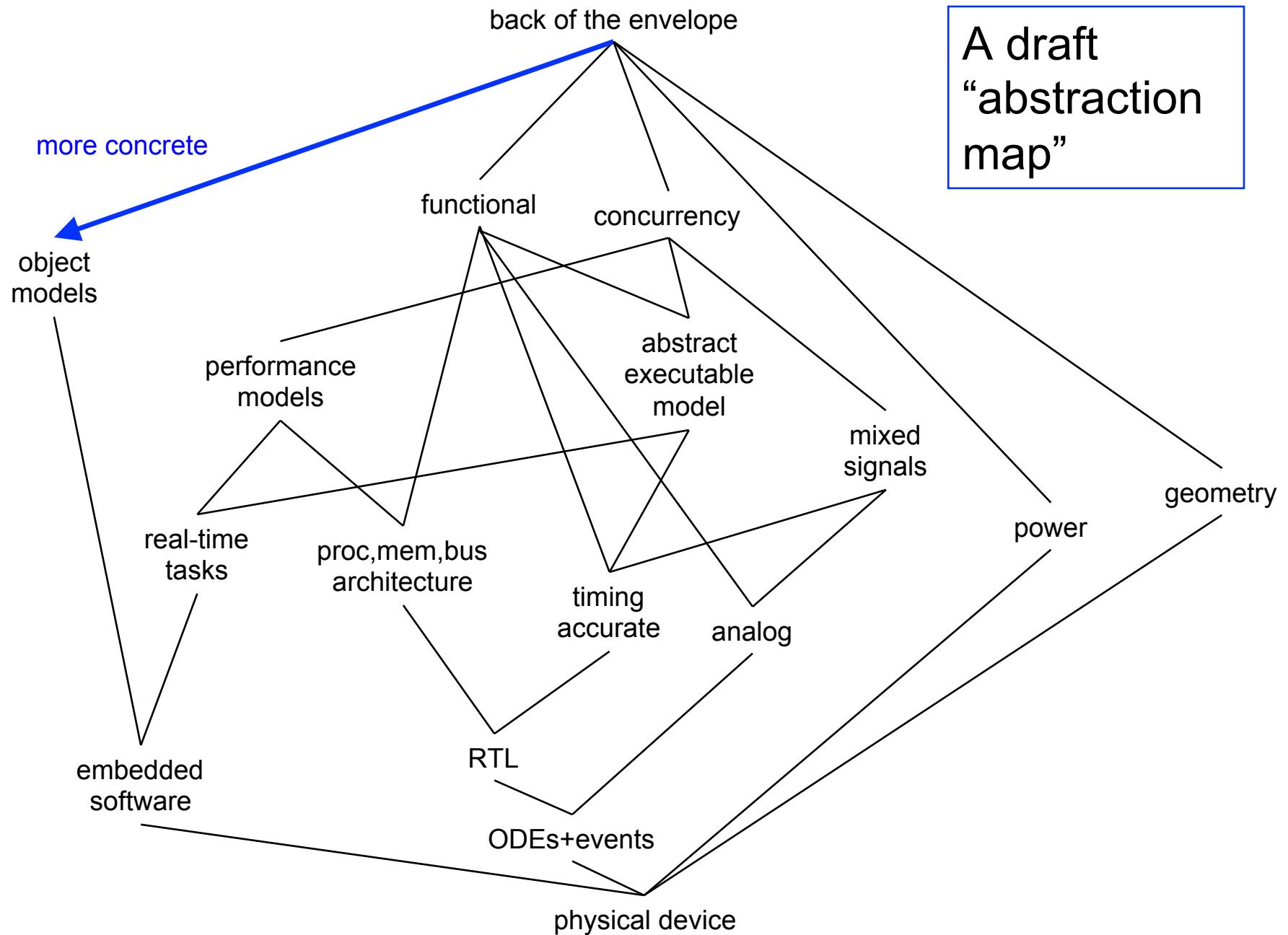
A draft
“abstraction
map”



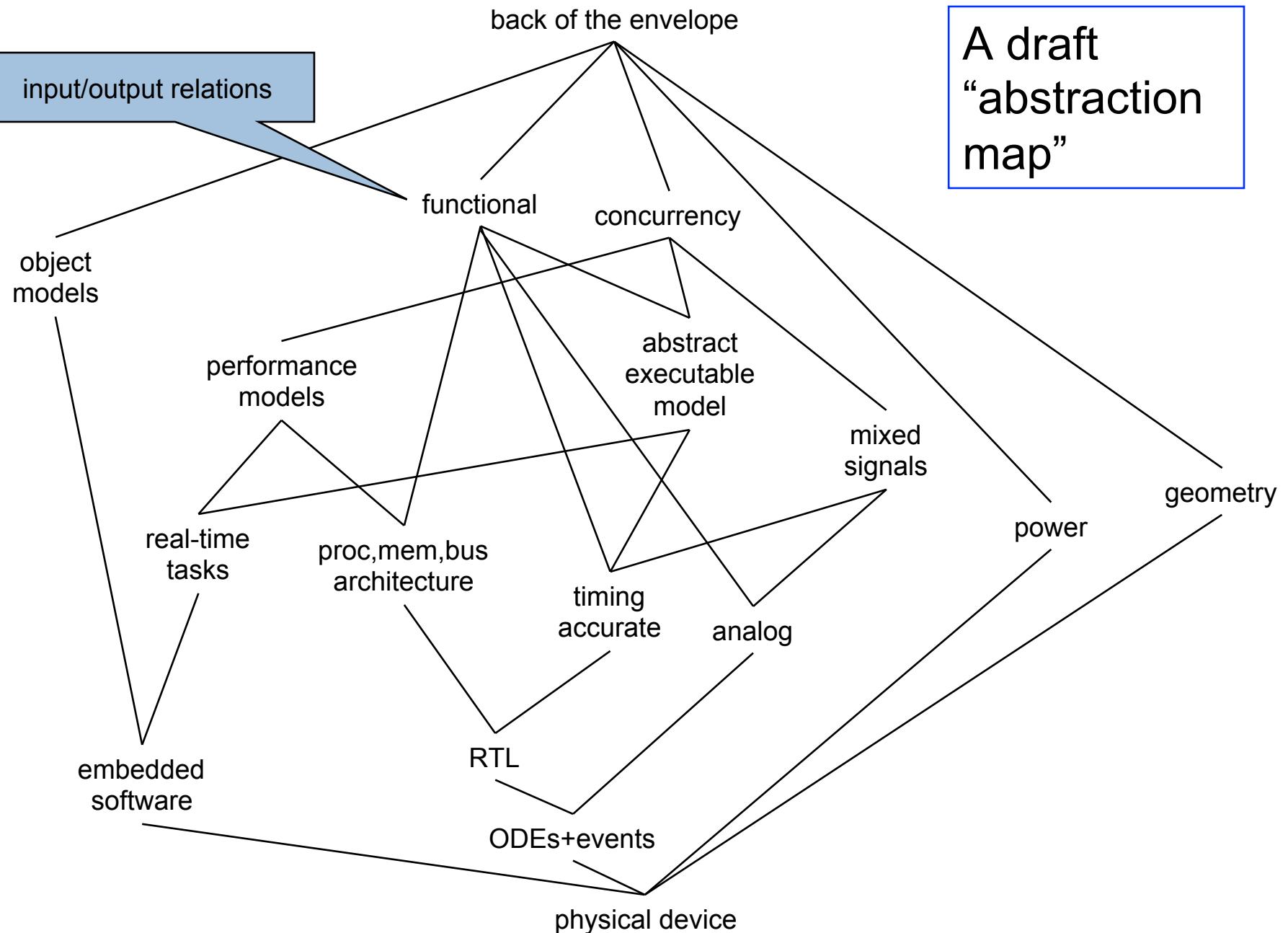
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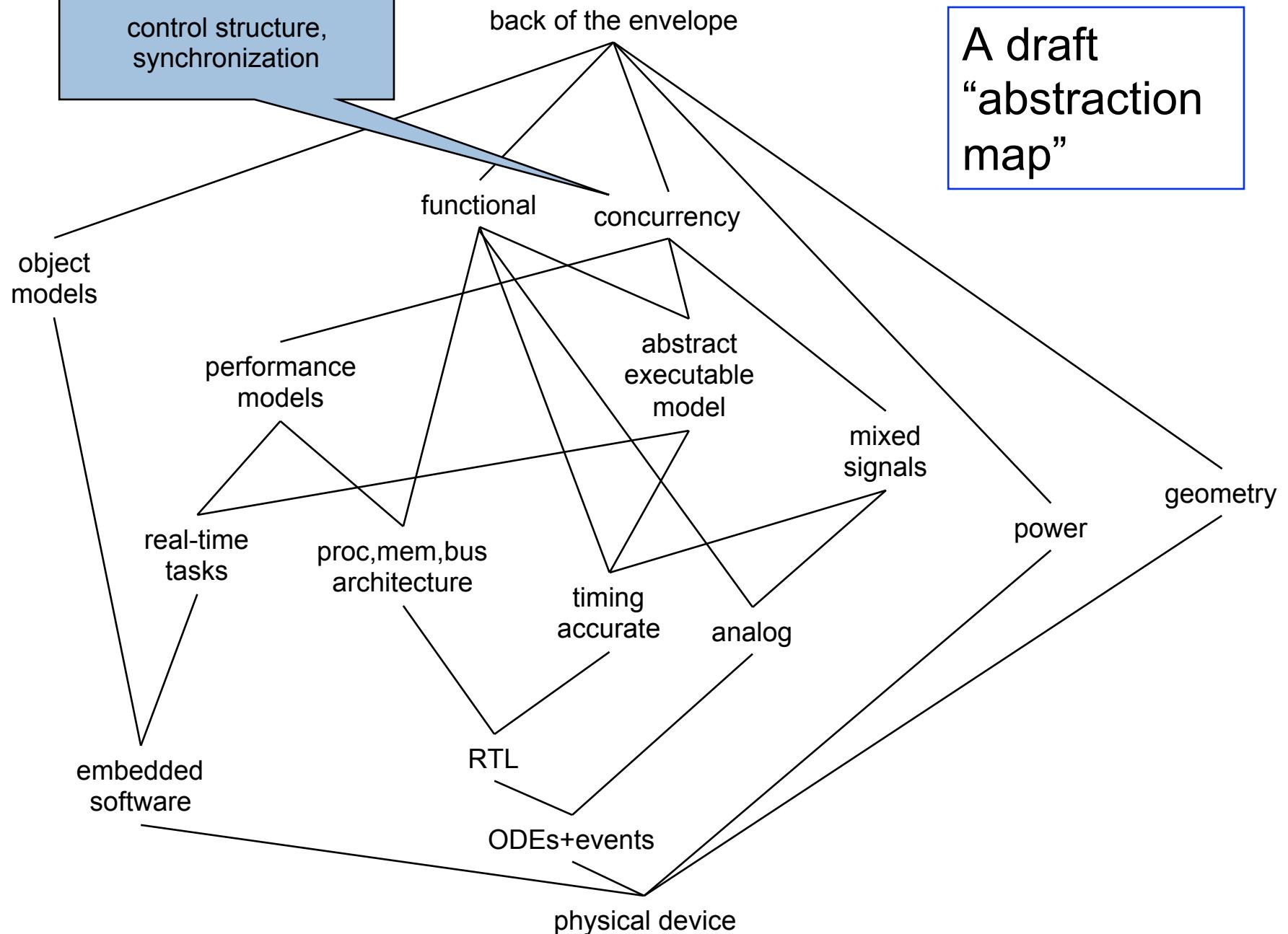
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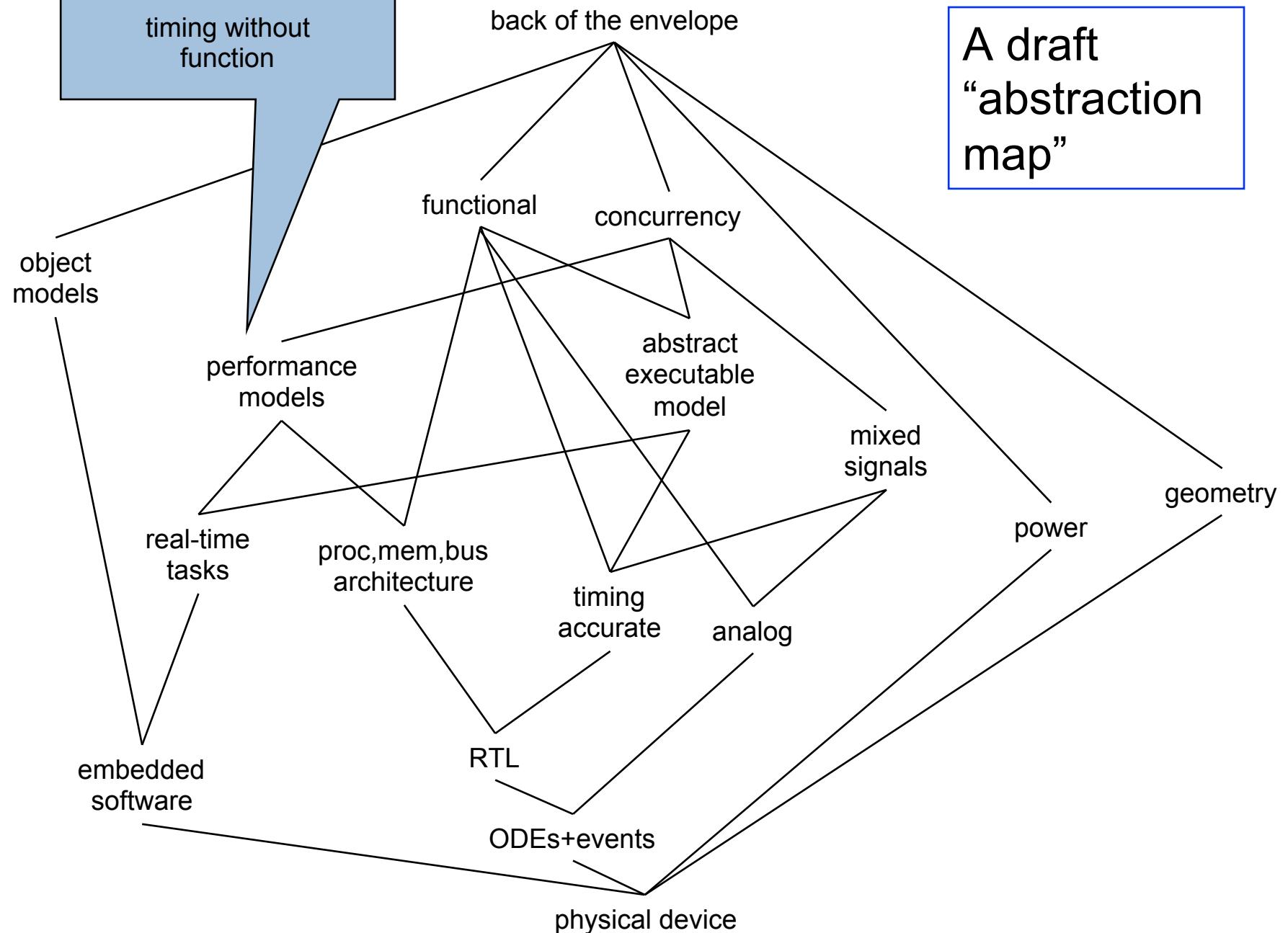
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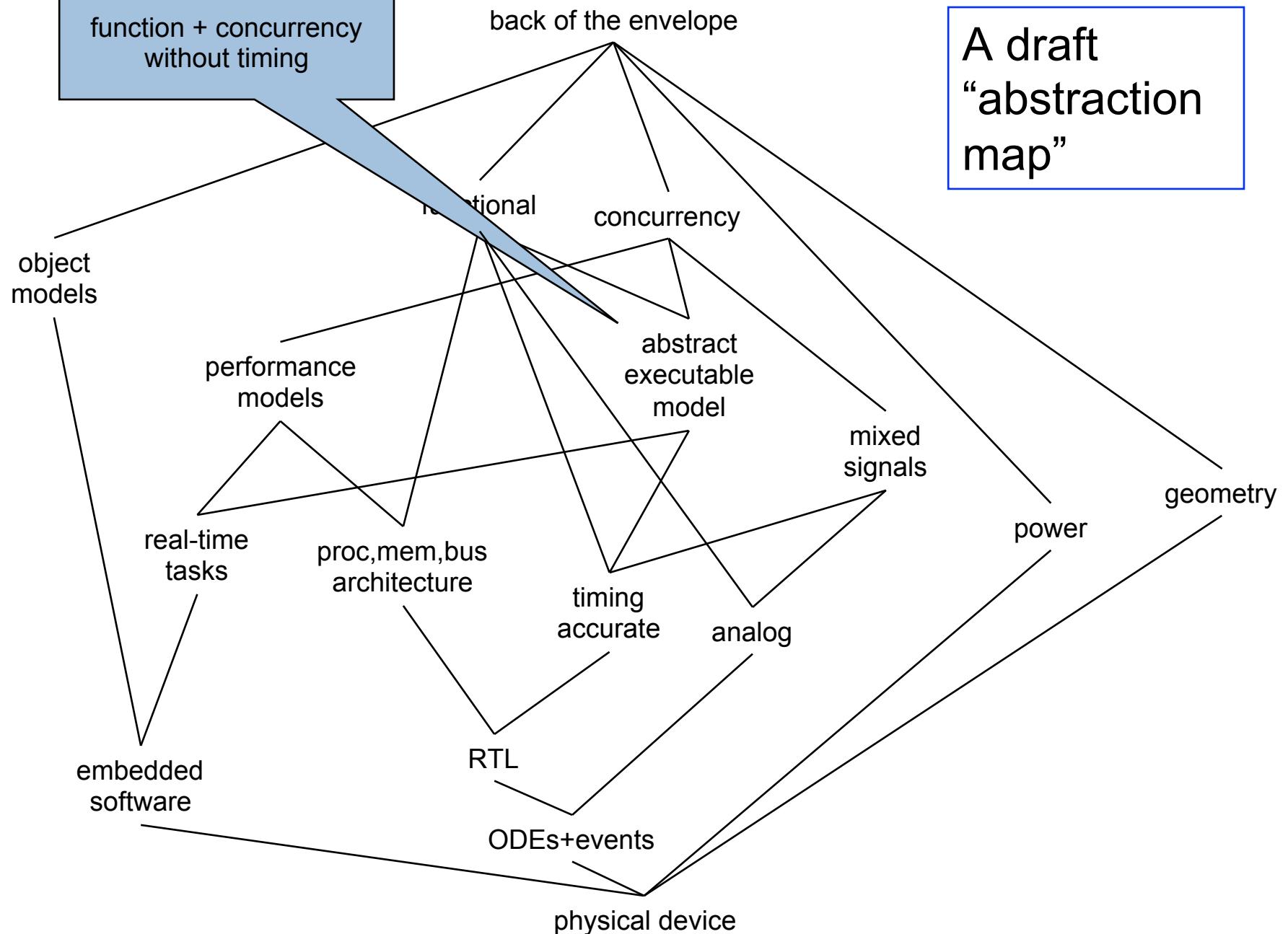
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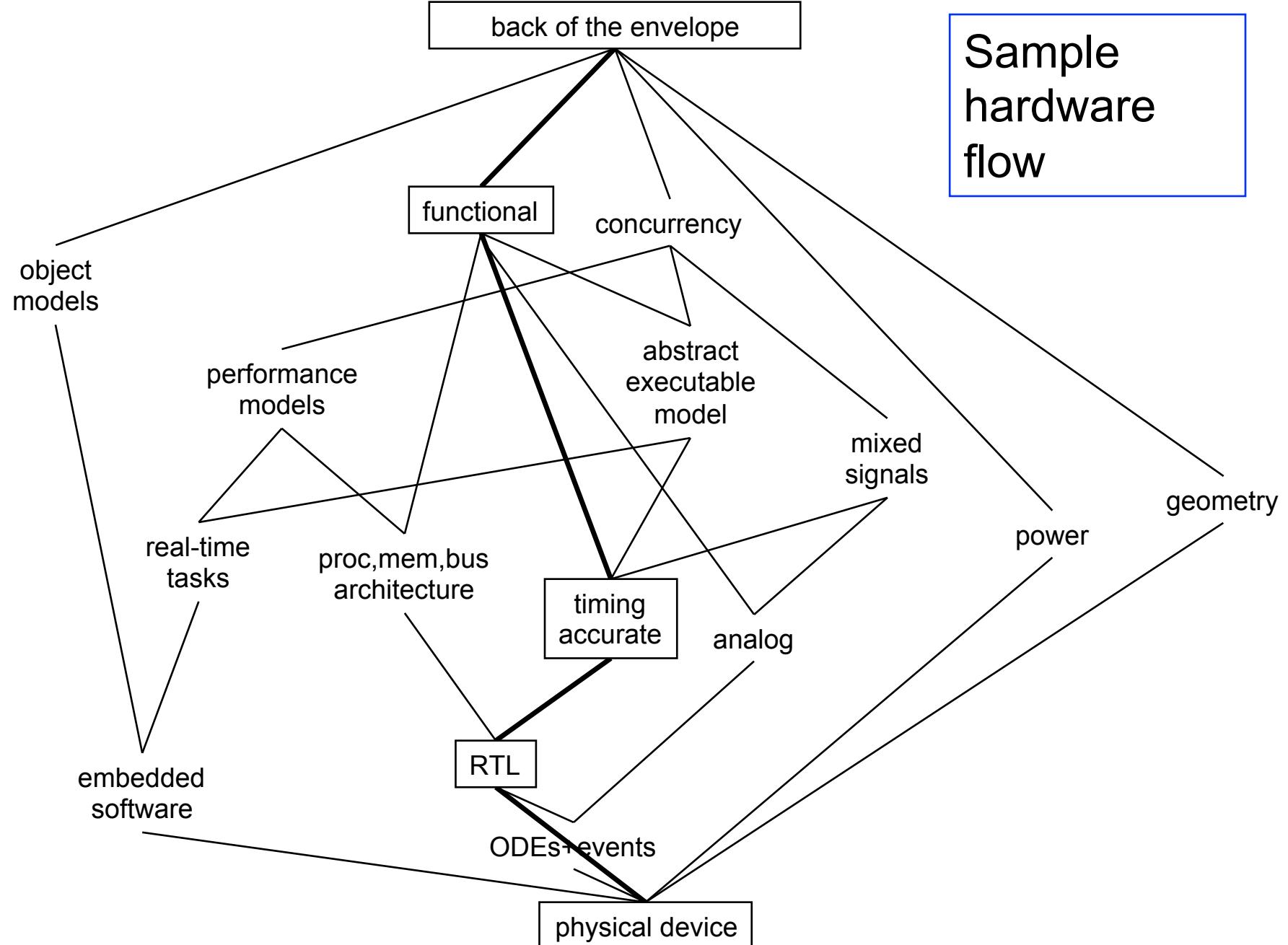


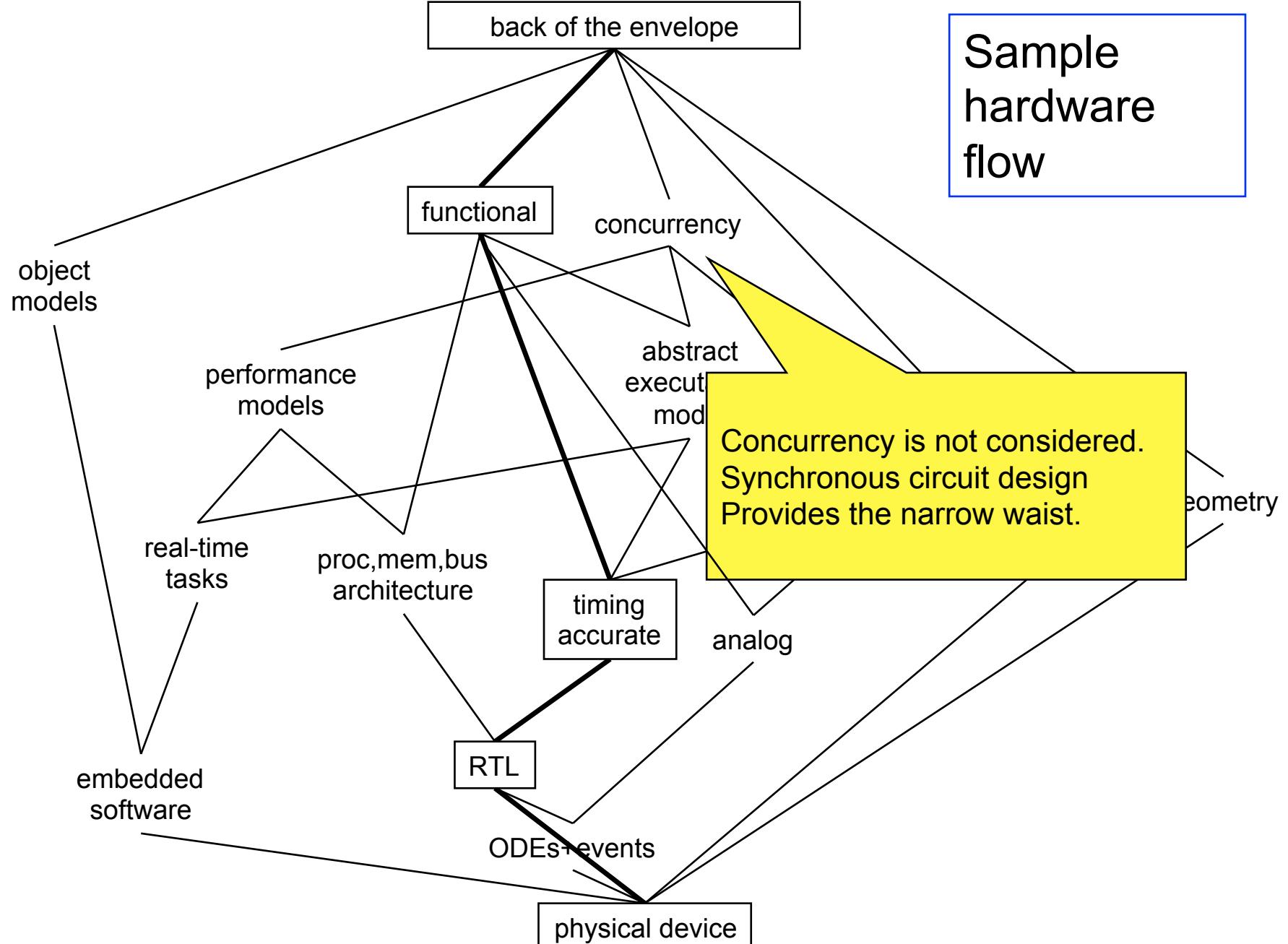
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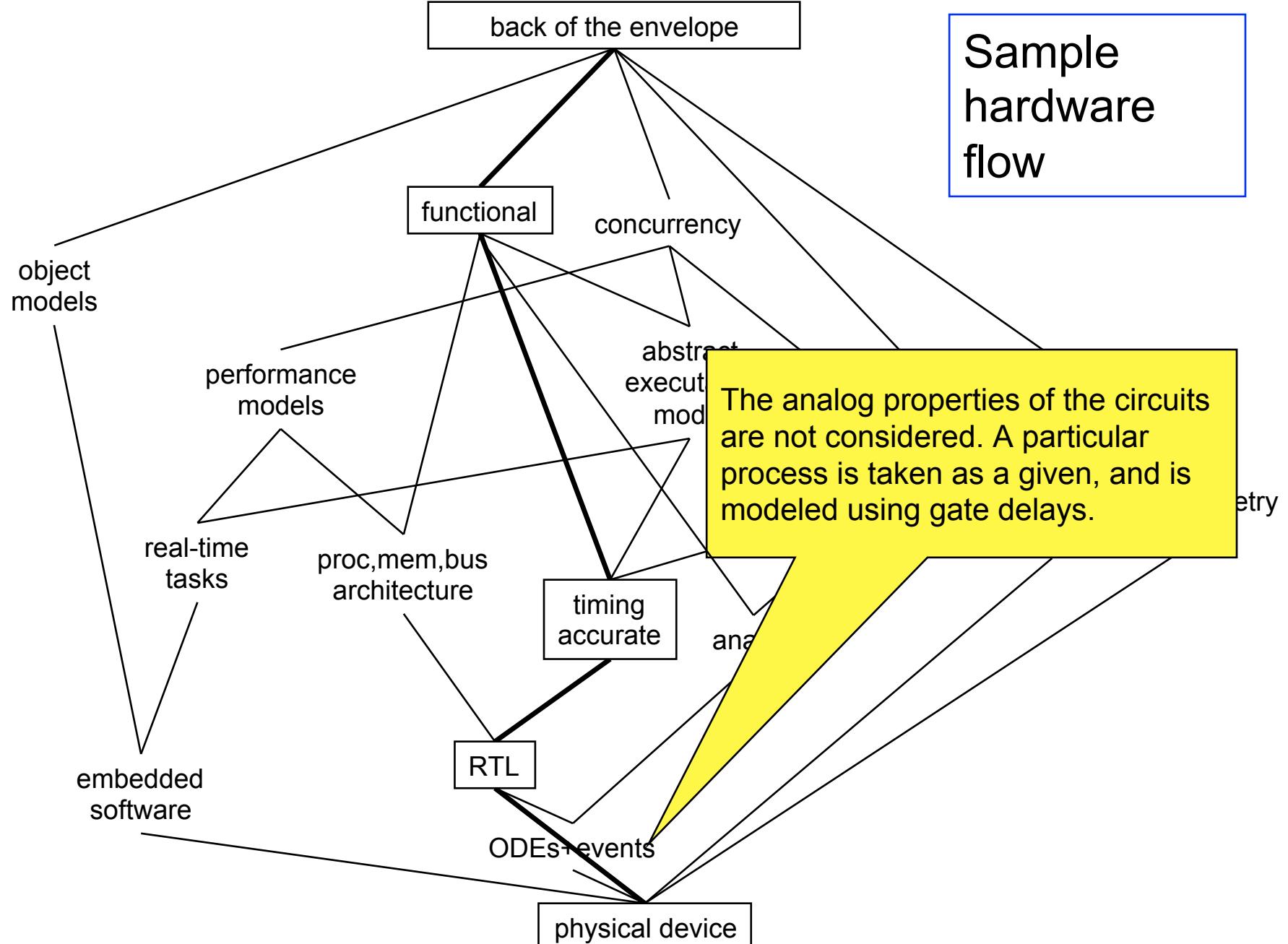


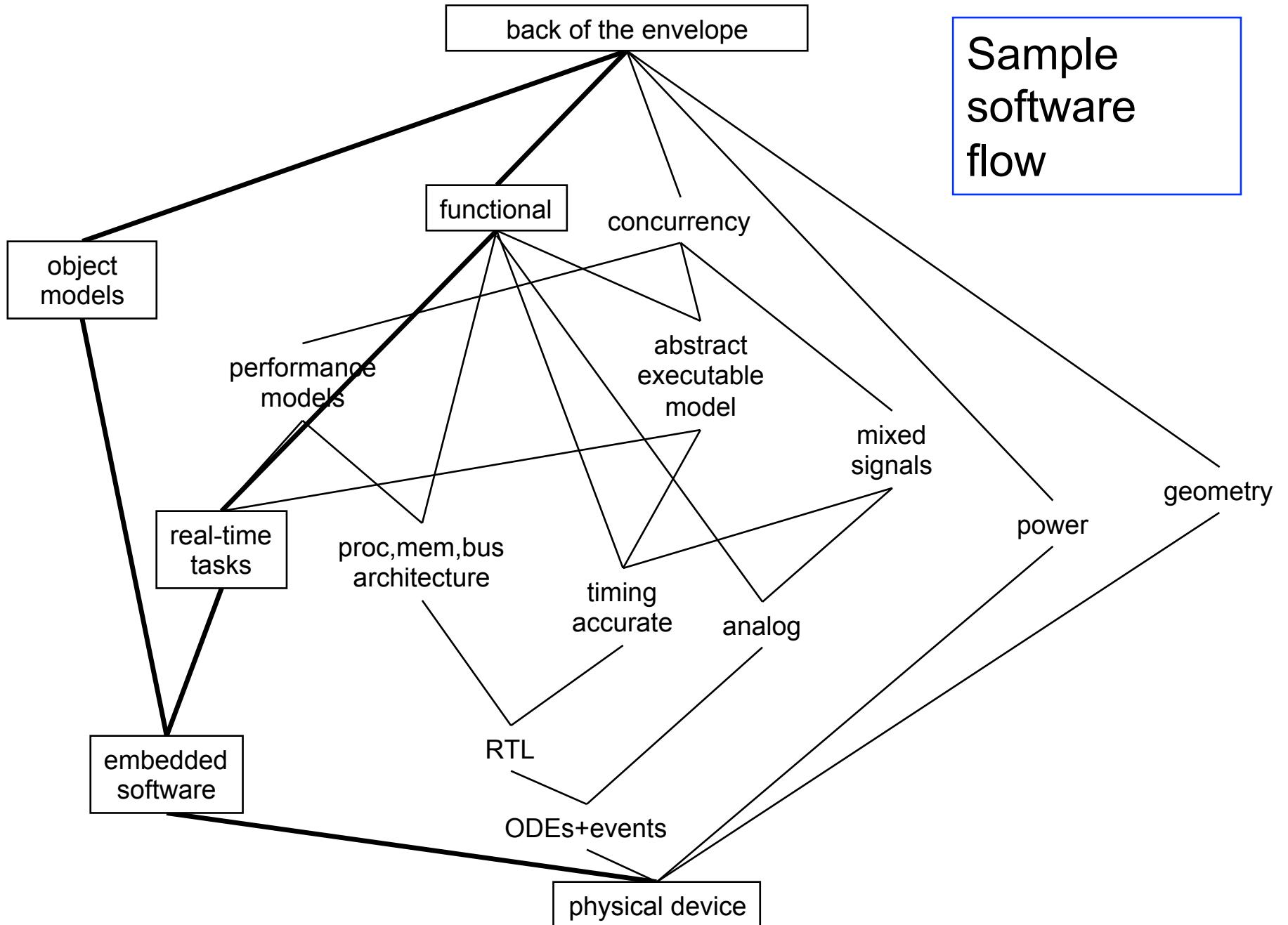
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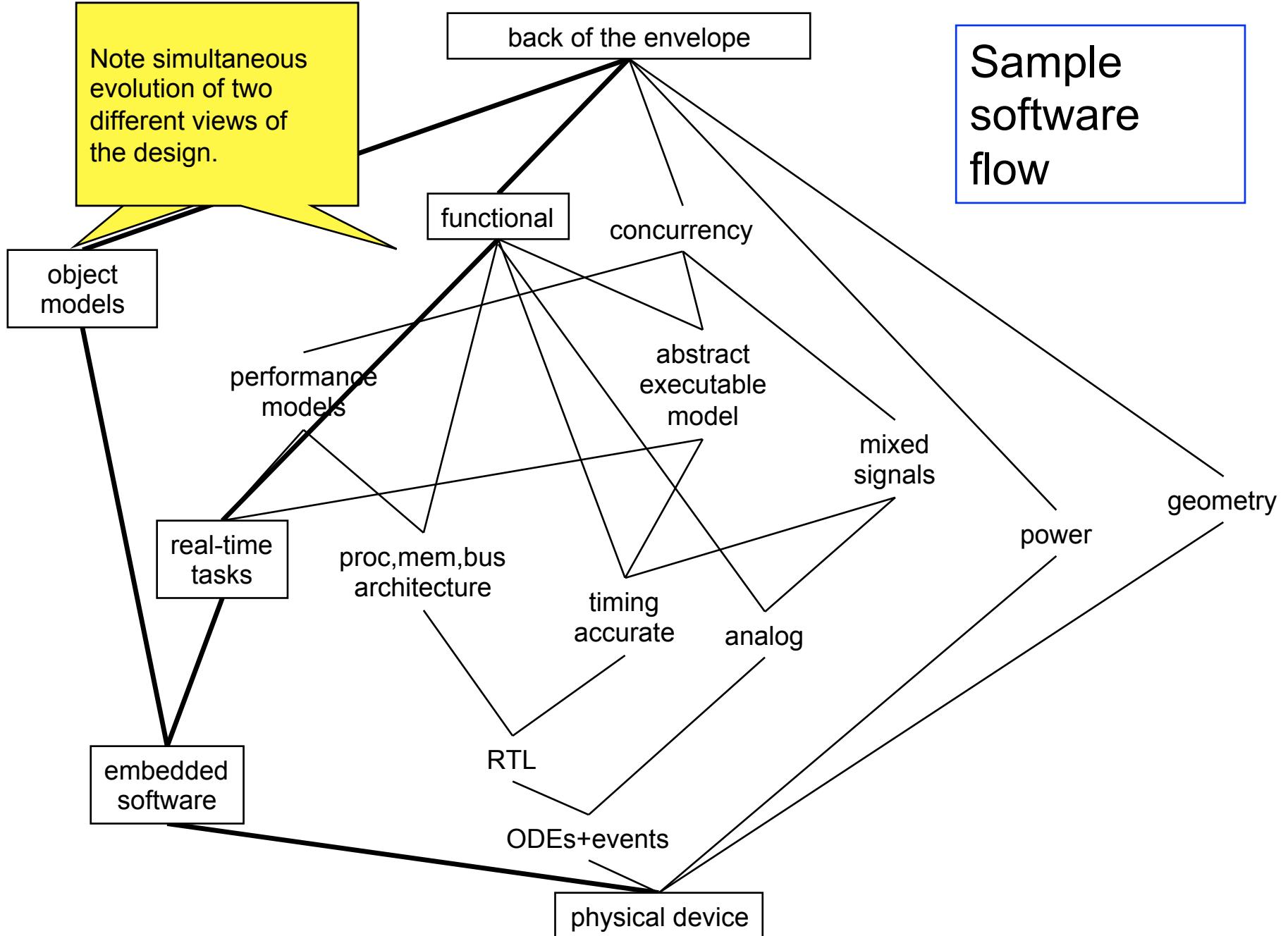


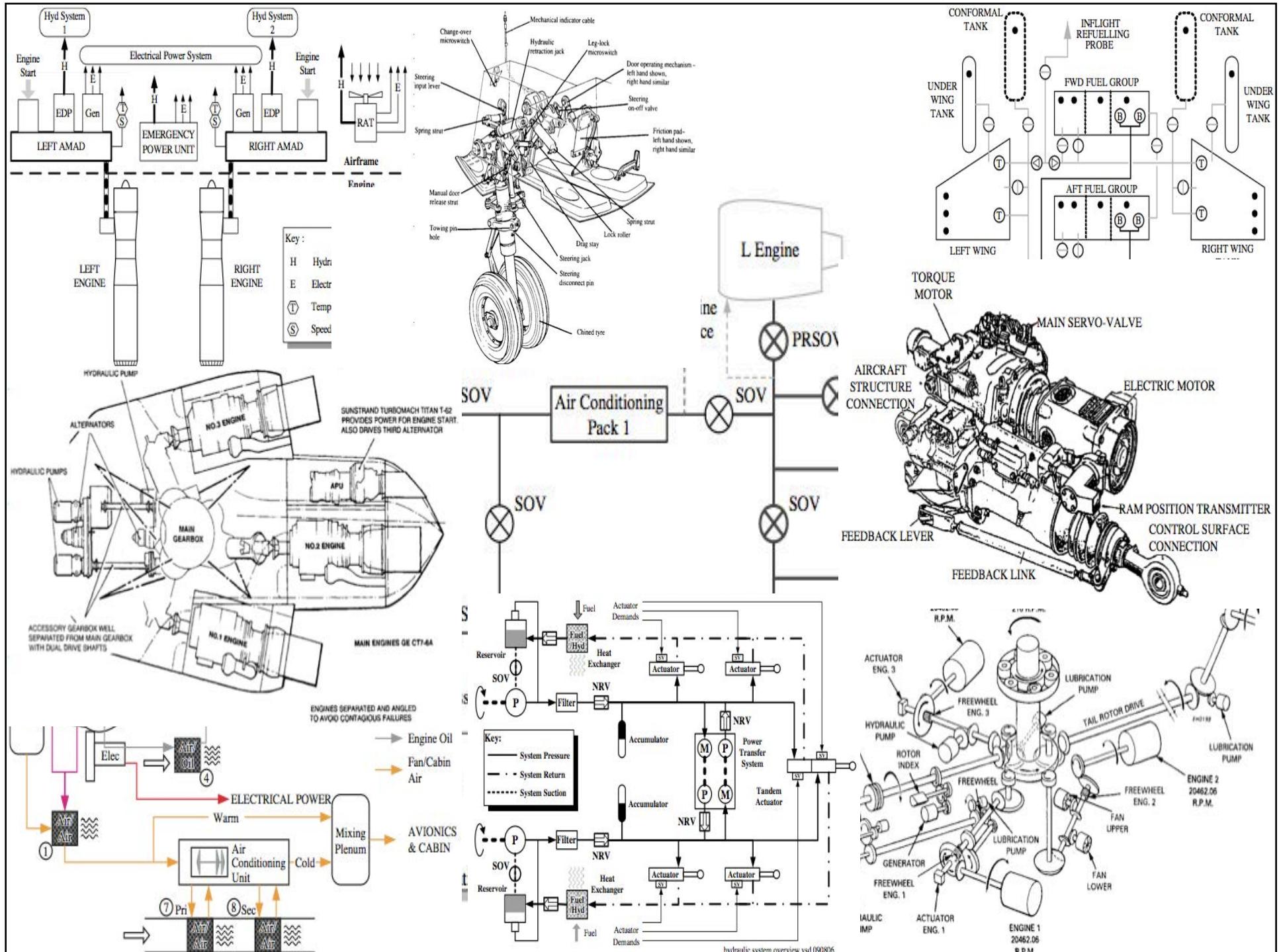




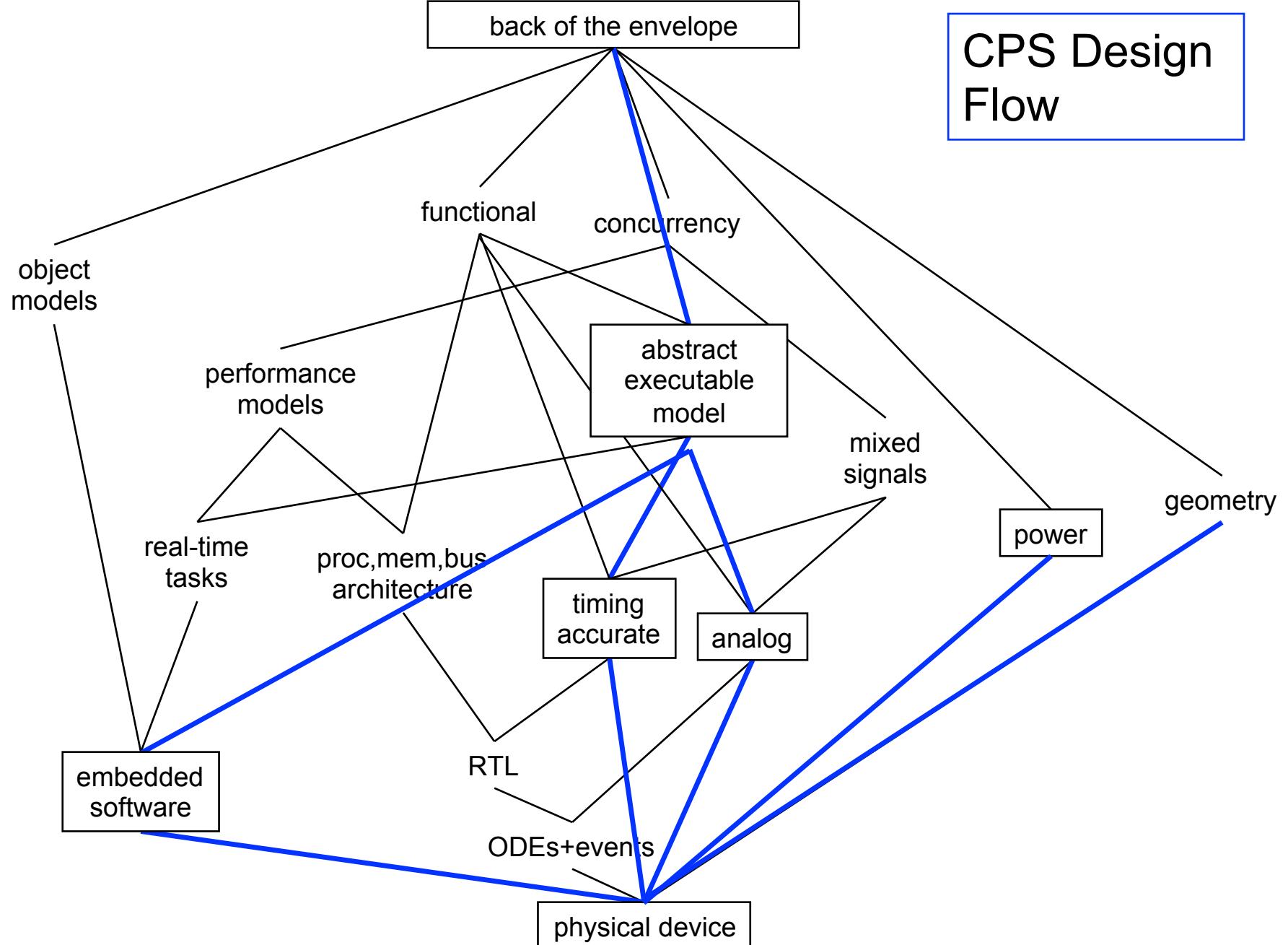




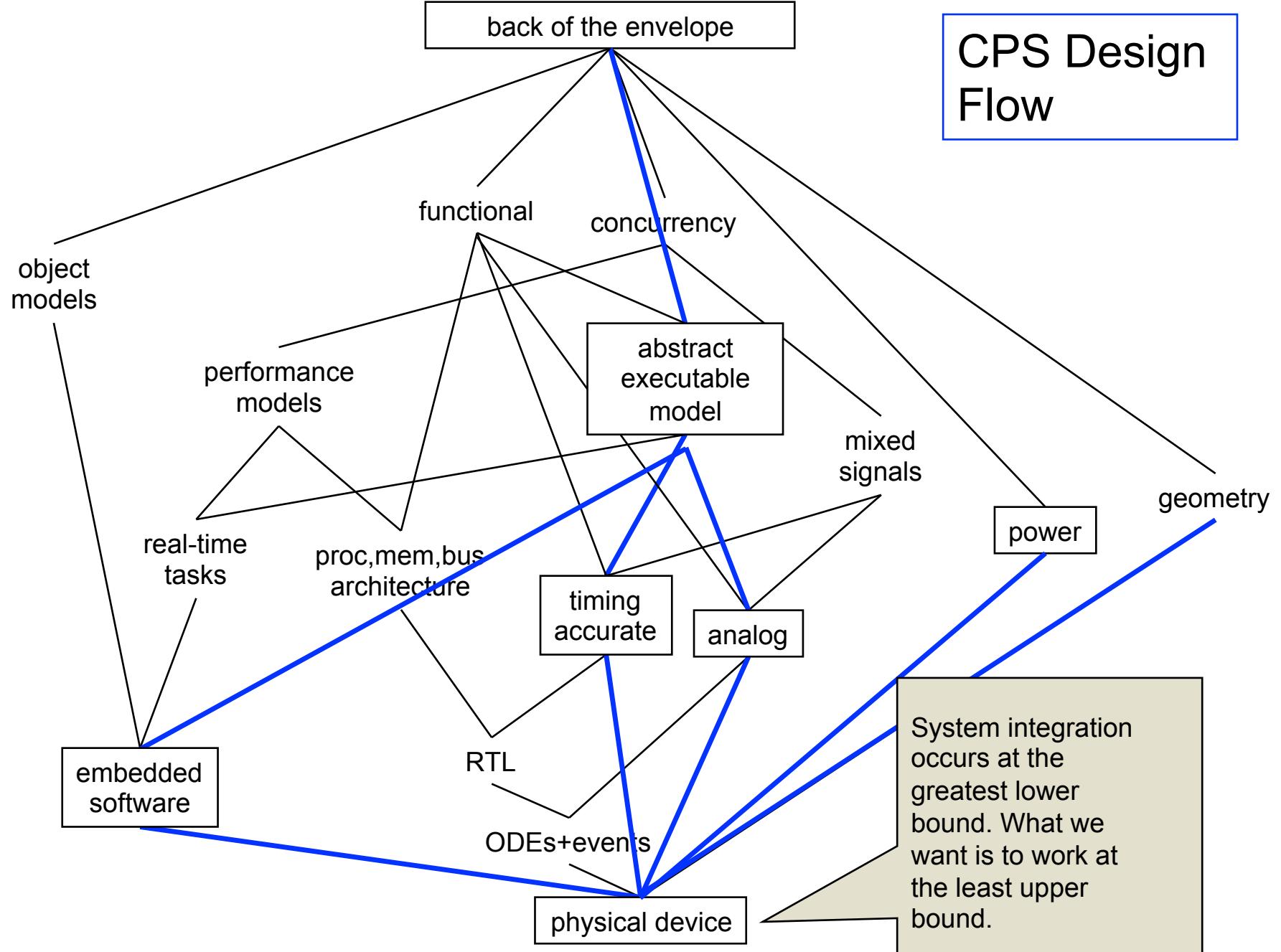




CPS Design Flow



CPS Design Flow





A Story



In “fly by wire” aircraft, computers control the plane, mediating pilot commands.

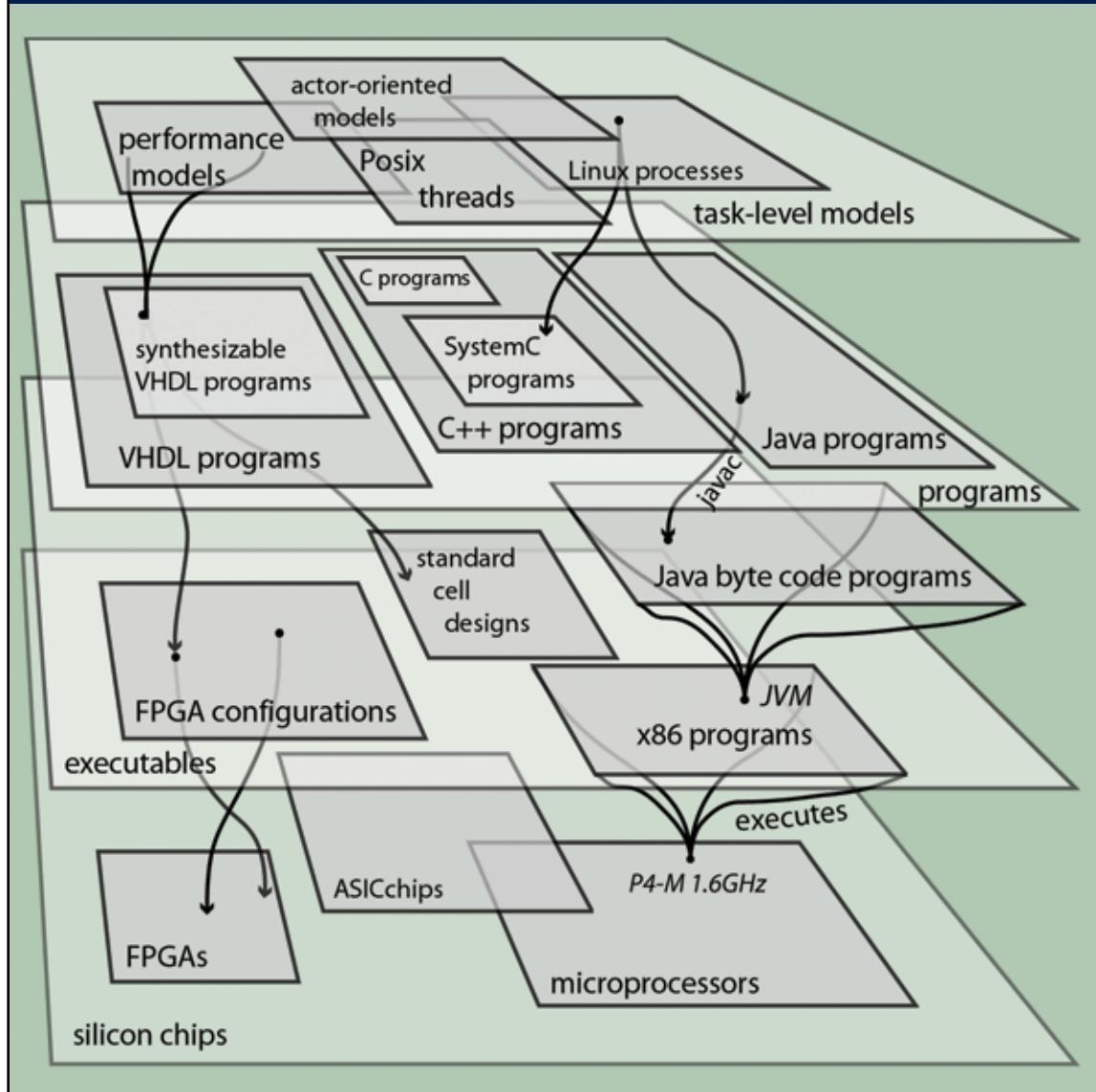


CCA 2.0
Boeing Dreamscape



Abstraction Layers

All of which are models except the bottom



The purpose of an abstraction is to hide details of the implementation below and provide a platform for design from above.



Abstraction Layers

All of which are models except the bottom



Every abstraction layer has failed for the aircraft designer.

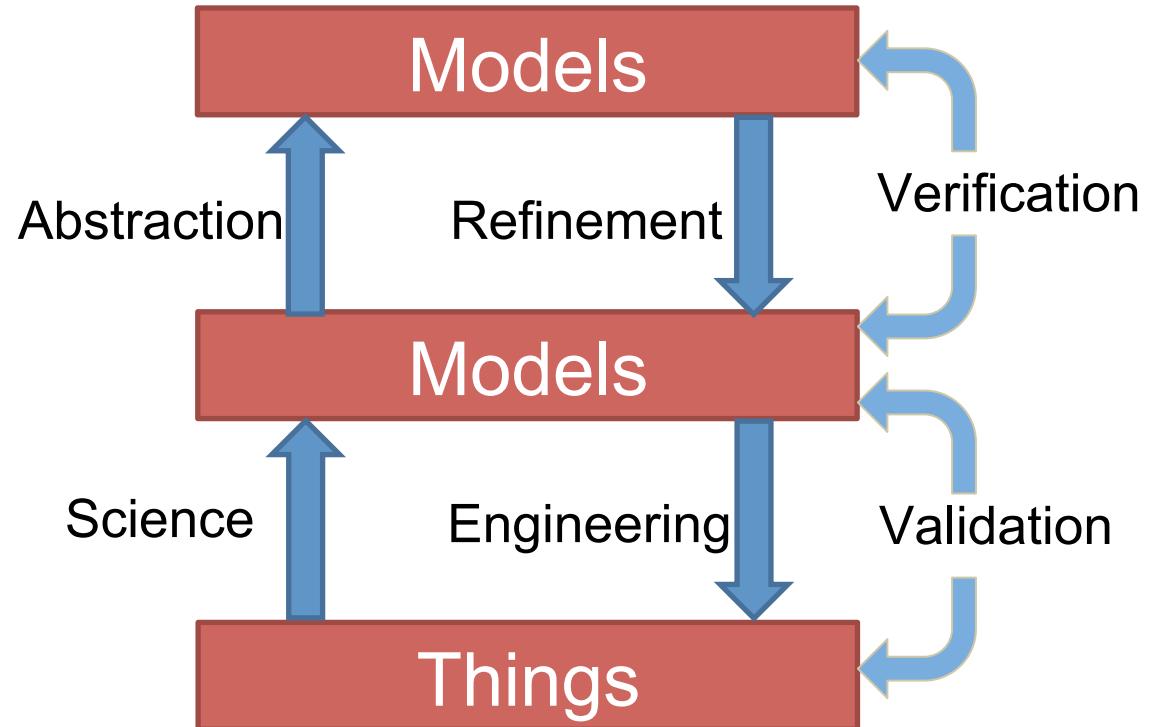
The design *is* the implementation.



Verification and Validation

Per Boehm:

- Am I building the right product? (validation)
- Am I building the product right? (verification)



Formal methods can only address the Verification question.

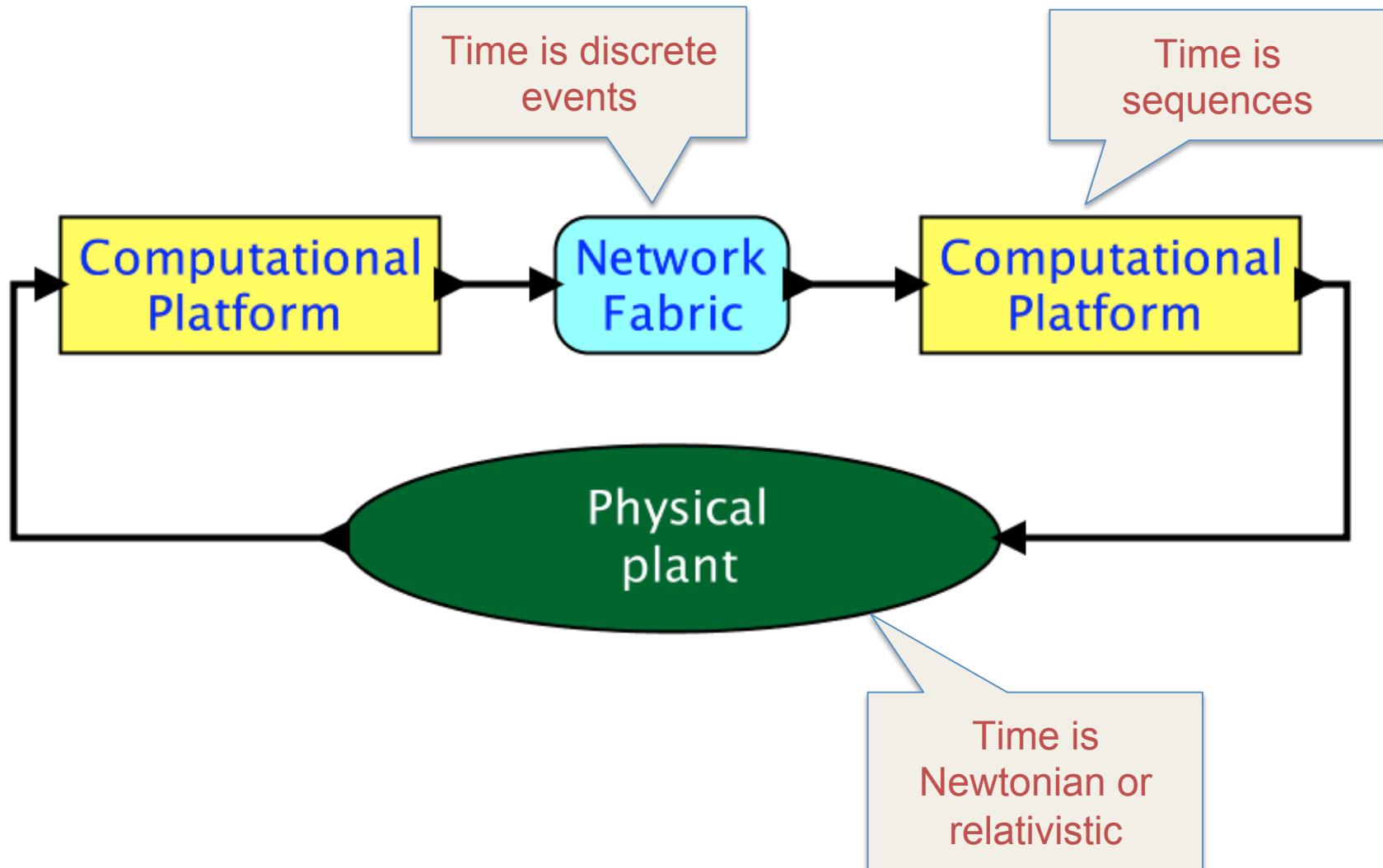


Outline

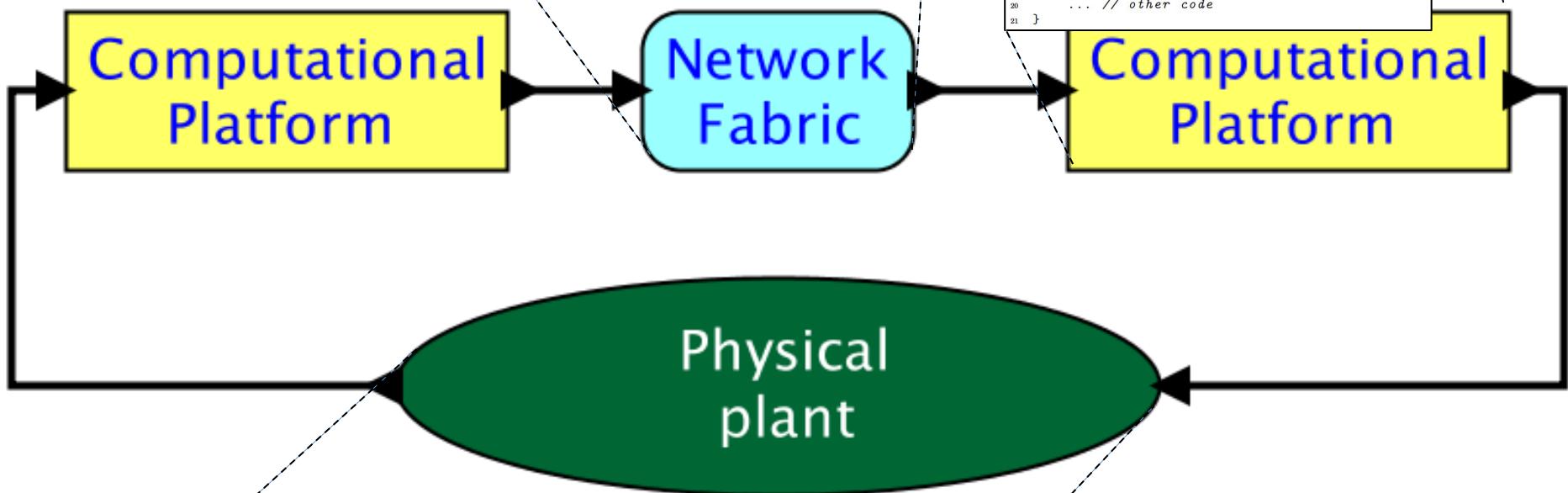
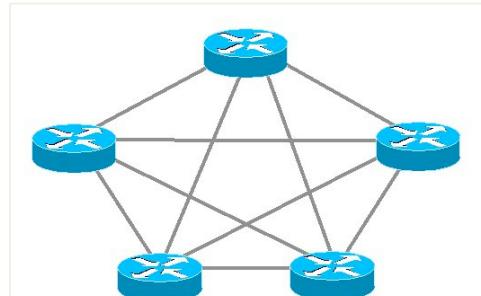
- Cyber-Physical Systems (CPS)
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- Abstraction and Refinement
- Time



Cyber-Physical Systems Pattern



The models are more deterministic than the reality



The modeling languages have disjoint, incompatible semantics

System dynamics
emerges from the
physical realization

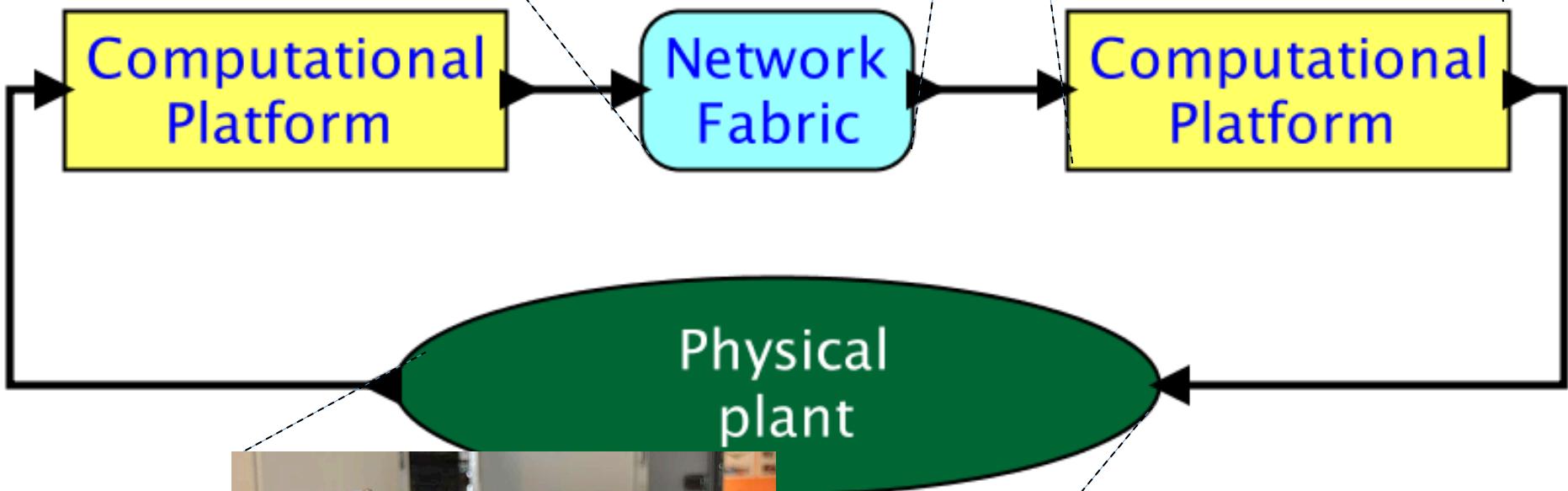
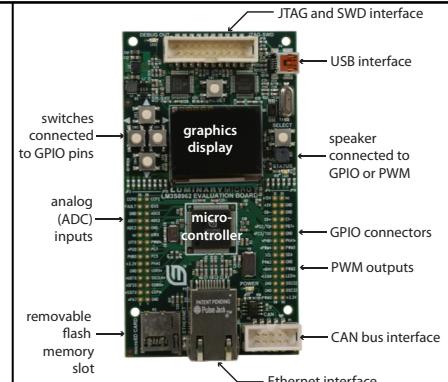
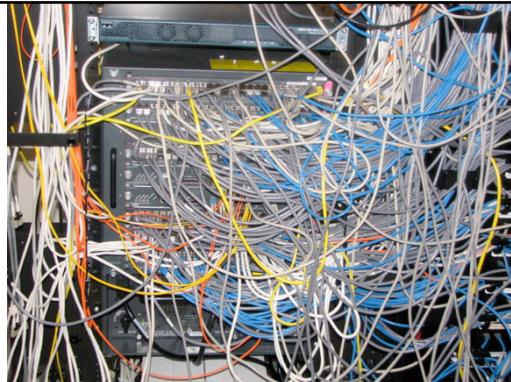
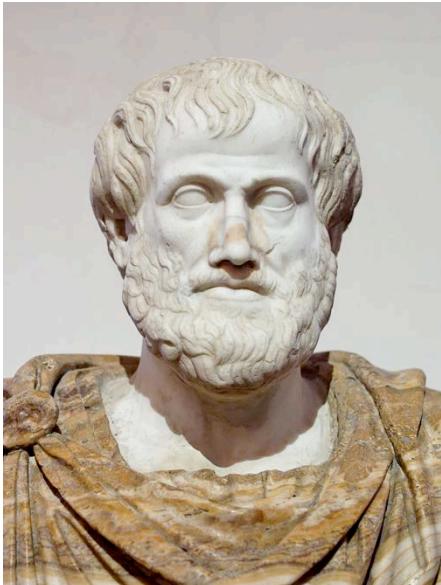


Image: Wikimedia Commons



What is Time?

Change



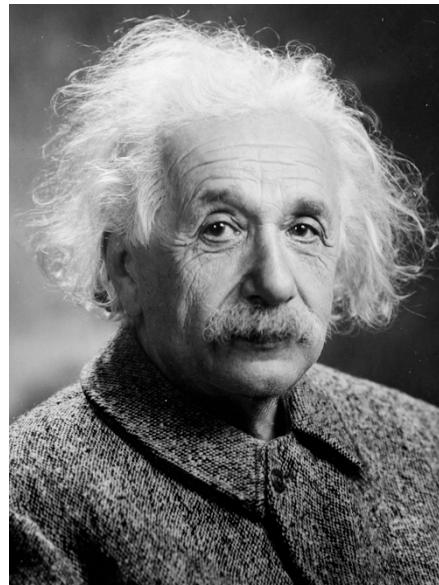
Aristotle

Smooth



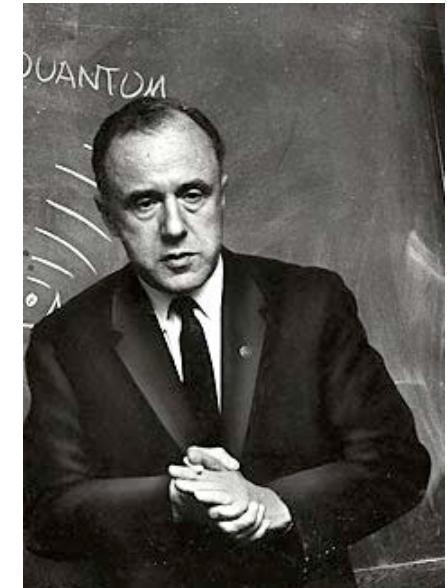
Newton

Relative



Einstein

Discrete



Wheeler



What is Time from a Physics Perspective?

Change?

Uniformly advancing in a continuum?

Arrow of increasing entropy?

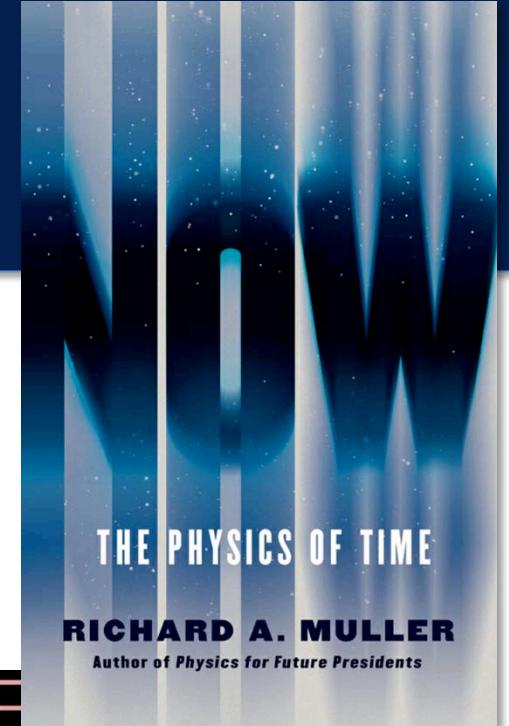
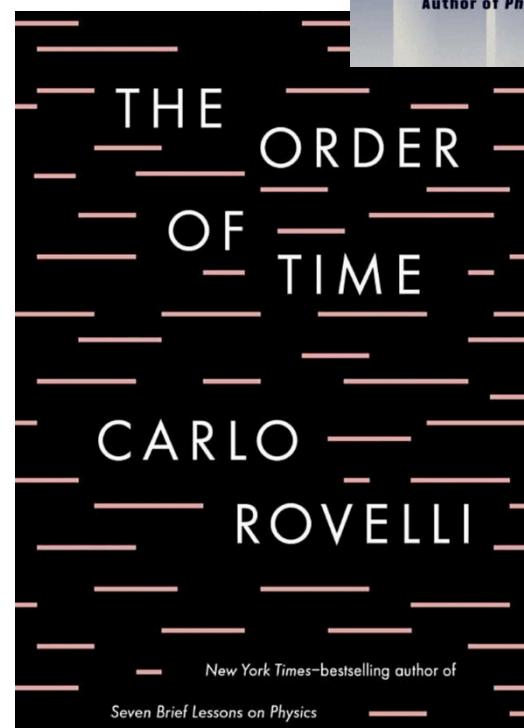
Expansion of space-time?

Discrete or continuous?

Total or partial order?

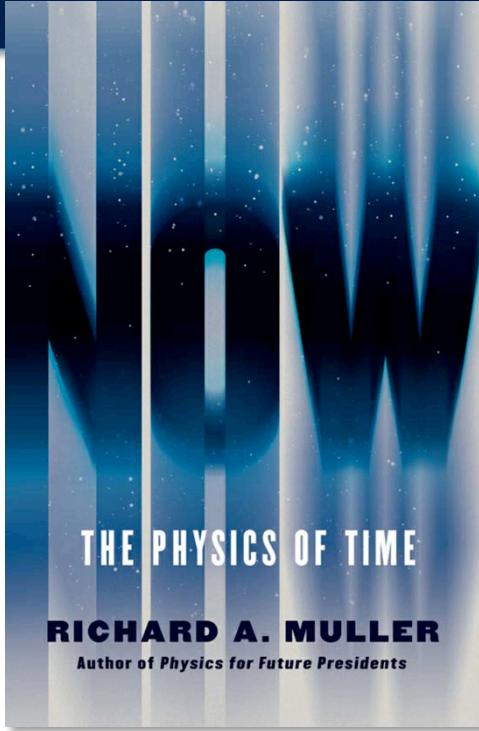
A cognitive illusion?

An anthropic fact?



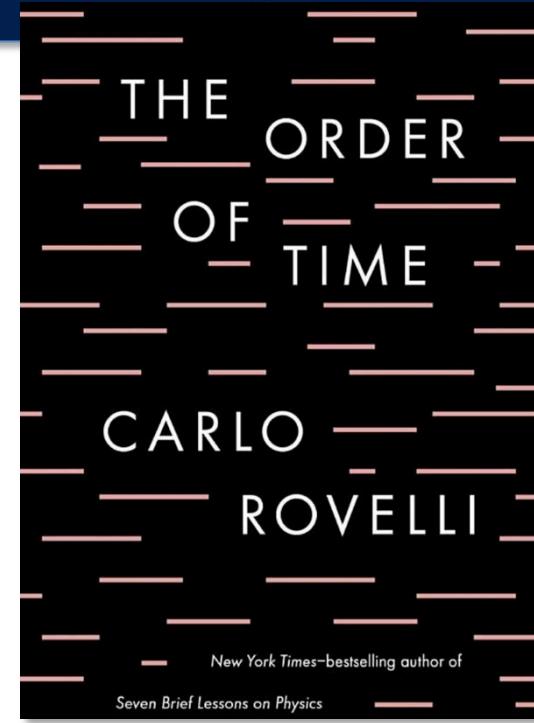


What is Time?



2016

Muller: Gives a theory of time that requires big black holes to collide somewhere near us to test it.



2018

Rovelli: “The nature of time is perhaps the greatest remaining mystery.”



How can we build systems based
on something we do not
understand

?



Deterministic Timing

Is our goal for our models to accurately reflect the timing of our implementation?

or

Is our goal for the implementation to accurately reflect the timing of the model?

If it's the latter, then deterministic timing makes perfect sense!



Desirable Properties in a Model of Time

- A “present” that separates the past and future
 - Needed for a notion of “state”
- Support for causality
 - If A causes B , then every observer should see A before B .
- A well-defined “observer”
 - Otherwise, stuck trying to solve the physics problem.
- A notion of “simultaneity”
 - If A can precede B and B can precede A , then A can be simultaneous with B



Desirable Properties in a Model of Time

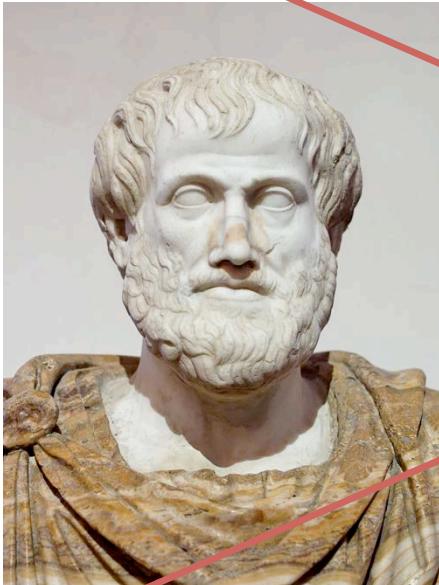
- A “present” that separates the past and future
- Support for causality
- A well-defined “observer”
- A notion of “simultaneity”

All are problematic in physics but useful in models.

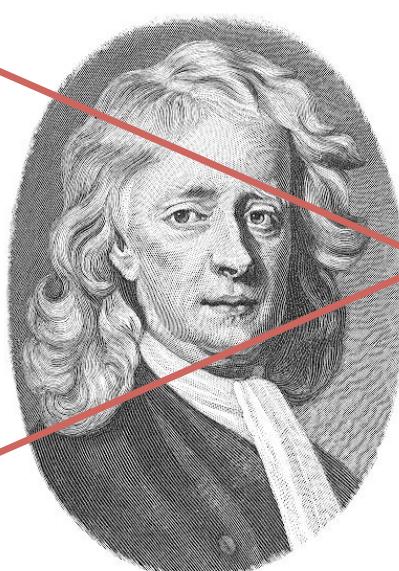


What is Time?

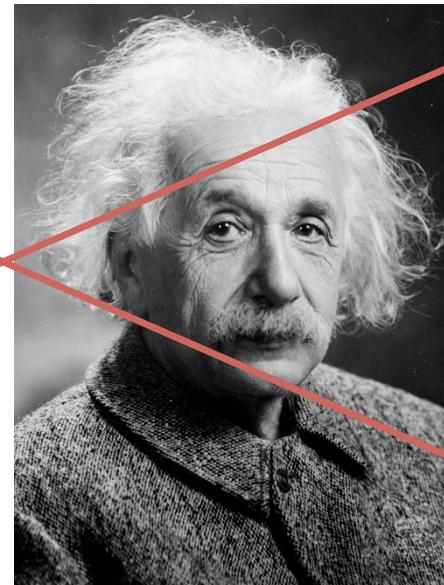
Change



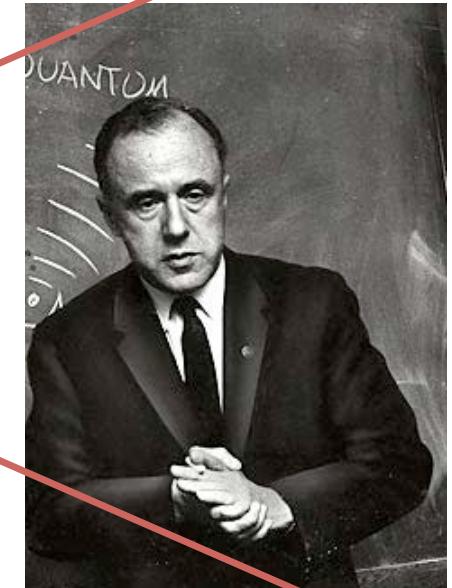
Smooth



Relative



Discrete



Aristotle

Newton

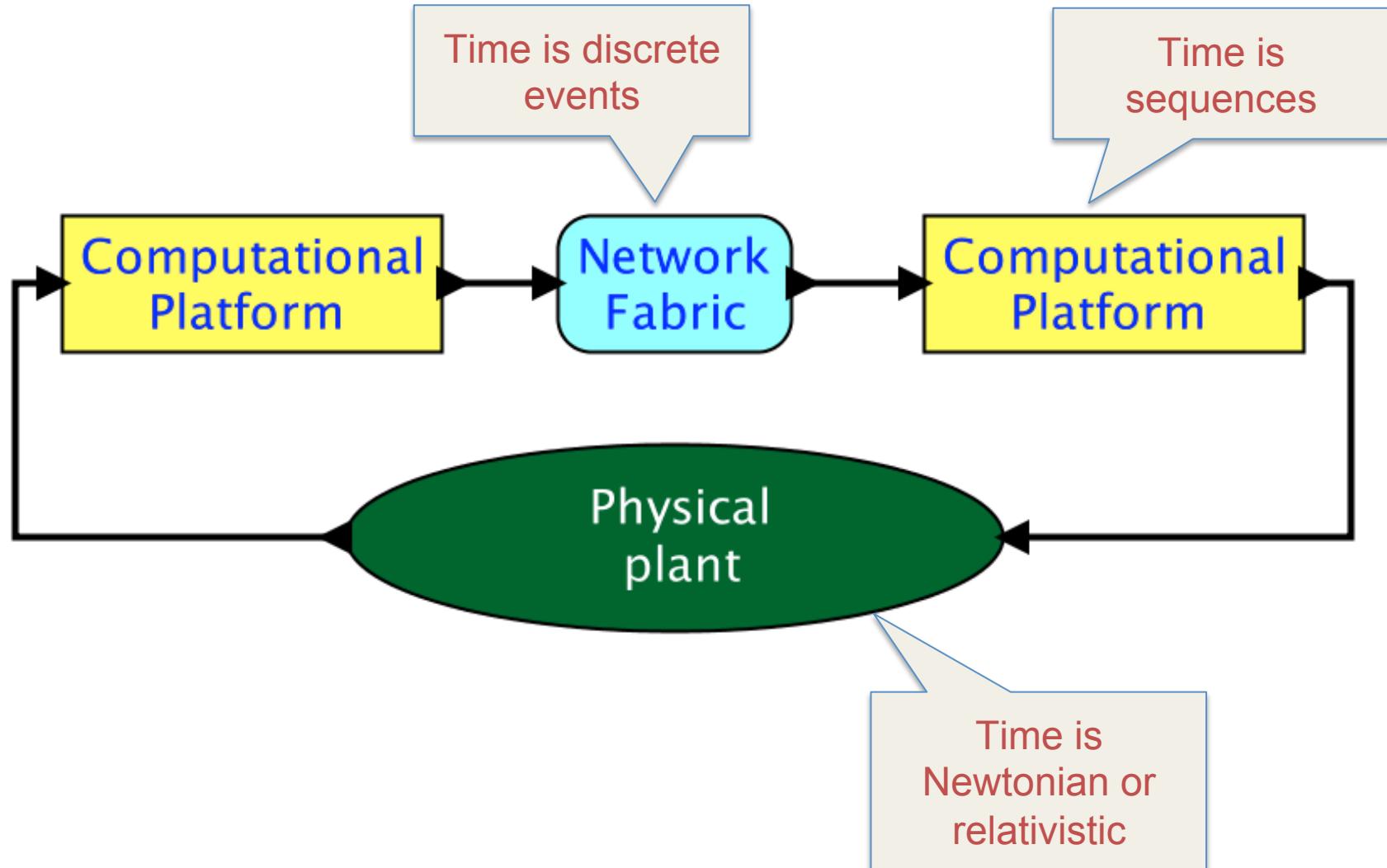
Einstein

Wheeler

All of these are about scientific models, not engineering models.



Cyber-Physical Systems Pattern





Computation given in an
untimed, imperative language.
Physical plant modeled with
ODEs or DAEs

```
1 void initTimer(void) {  
2     SysTickPeriodSet(SysCtlClockGet() / 1000);  
3     SysTickEnable();  
4     SysTickIntEnable();  
5 }  
6 volatile uint timer_count = 0;  
7 void ISR(void) {  
8     if(timer_count != 0) {  
9         timer_count--;  
10    }  
11 }  
12 int main(void) {  
13     SysTickIntRegister(&ISR);  
14     .. // other init  
15     timer_count = 2000;  
16     initTimer();  
17     while(timer_count != 0) {  
18         ... code to run for 2 seconds  
19     }  
20     ... // other code  
21 }
```

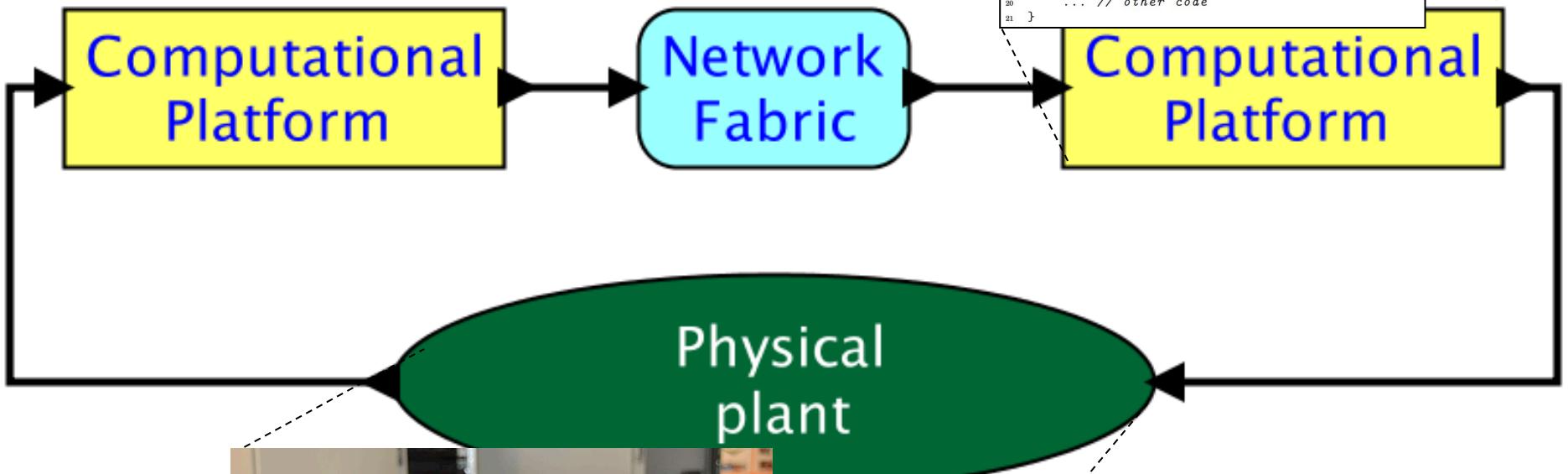


Image: Wikimedia Commons



Computational Platform

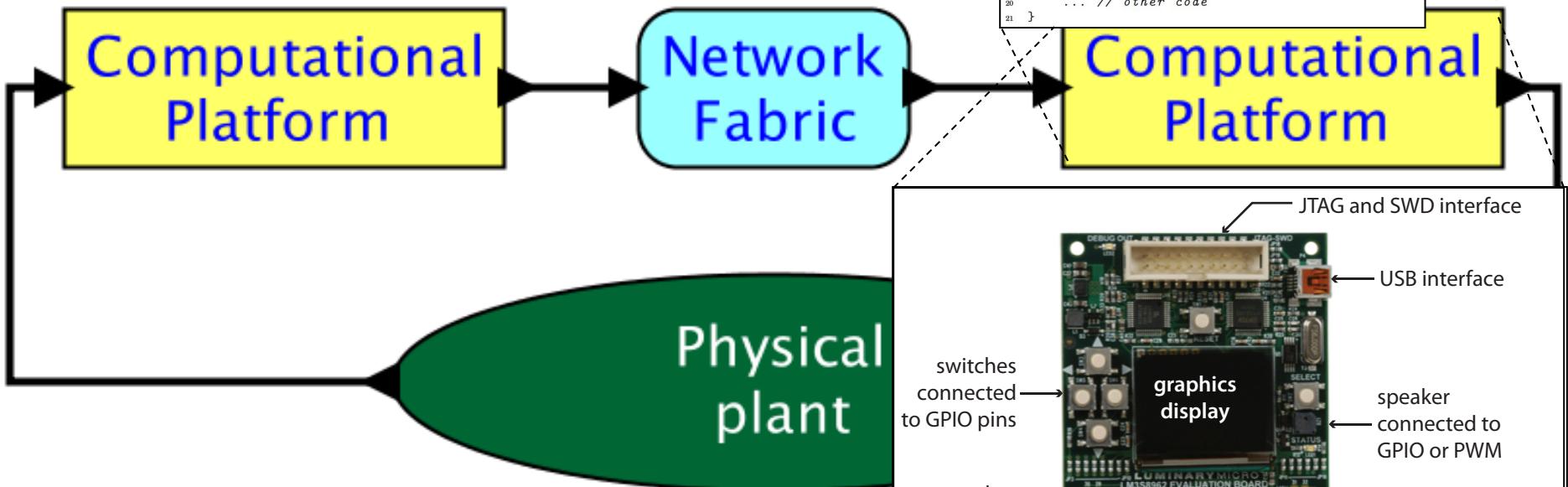
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17     while(timer_count != 0) {  
18         ... code to run for 2 seconds  
19     }  
20     ... // other code  
21 }
```

plant

This code is attempting
to control timing. But
will it really?



Emergent Timing



Timing behavior emerges from the combination of the program and the hardware platform.

```
1 void initTimer(void) {
2     SysTickPeriodSet(SysCtlClockGet() / 1000);
3     SysTickEnable();
4     SysTickIntEnable();
5 }
6 volatile uint timer_count = 0;
7 void ISR(void) {
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17     while(timer_count != 0) {
18         .. code to run for 2 seconds
19     }
20     .. // other code
21 }
```

Stellaris LM3S8962 evaluation board (Luminary Micro 2008, now Texas Instruments)



Frozen Designs



Everything about the design, down to wire lengths and microprocessor chips, must be frozen at the time of design.



CCA 2.0
Boeing Dreamscape



Contrast with correctness criteria in software

We can safely assert that line 8 does not execute, *regardless of the choice of microprocessor!*

```
1 void foo(int32_t x) {  
2     if (x > 1000) {  
3         x = 1000;  
4     }  
5     if (x > 0) {  
6         x = x + 1000;  
7         if (x < 0) {  
8             panic(); ←  
9         }  
10    }  
11 }
```

We can develop **absolute confidence** in the software, in that only a **hardware failure** is an excuse.

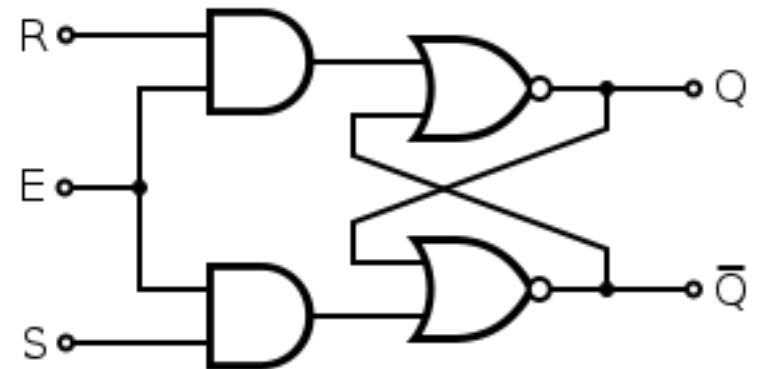
But not with regards to timing!!



Hardware is Good at Timing

Synchronous digital logic
delivers precise, repeatable
timing.

*... but the overlaying software
abstractions discard timing.*



```
// Perform the convolution.  
for (int i=0; i<10; i++) {  
    x[i] = a[i]*b[j-i];  
    // Notify listeners.  
    notify(x[i]);  
}
```



Projects at Berkeley Focused on *Engineering Models* for CPS

Deterministic models for CPS:

- PTIDES: distributed real-time software
 - <http://chess.eecs.berkeley.edu/ptides>
- PRET: time-deterministic architectures
 - <http://chess.eecs.berkeley.edu/pret>
- Lingua Franca: a programming model
 - <https://github.com/icyphy/lingua-franca>

Together, these technologies give a model for distributed and concurrent real-time systems that is deterministic, has controlled timing, and is implementable.



Model-Based Design of Cyber-Physical Systems

Changing the Question:

Is the question whether we can build models
describing the behavior of cyber-physical systems?

Or

Is the question whether we can make cyber-physical
systems that behave like our models?