

## Physics 421 - Lecture 16

### Numerical Integration

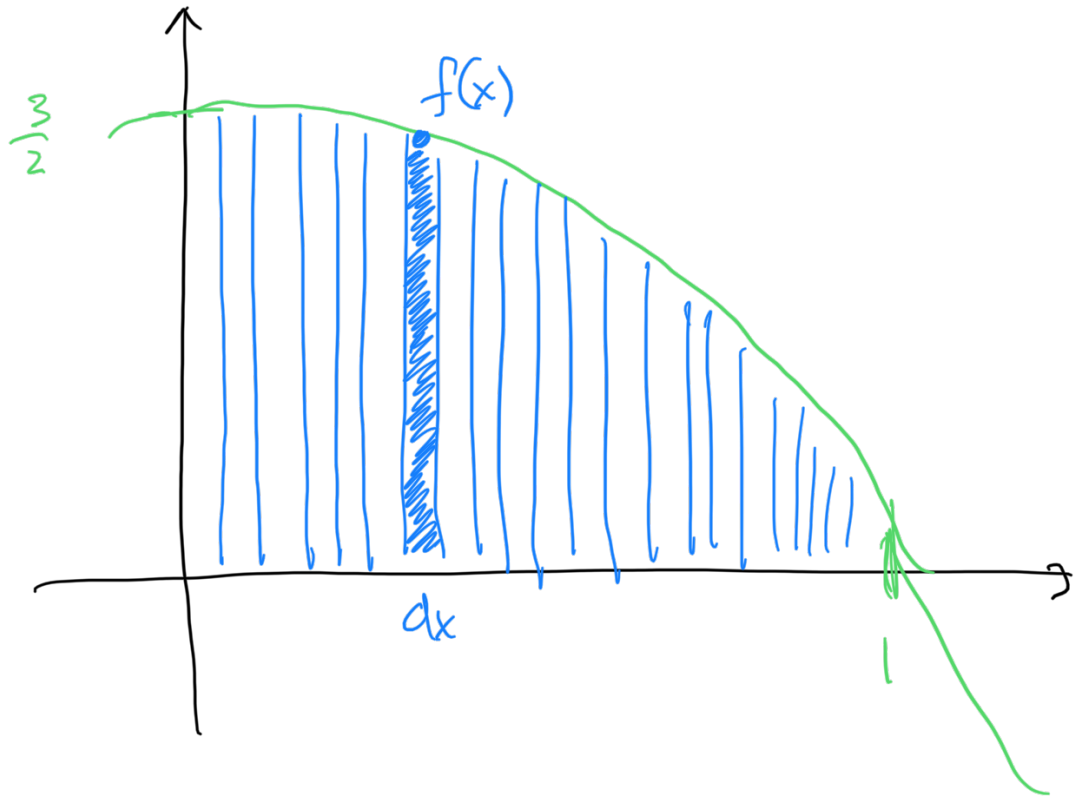
(actually, one of the first  
"killer apps" for  
computers !!)

Example:  $\int_0^1 \frac{3}{2} (1 - x^2) dx = 1$

$$\left( \begin{aligned} &= \left. \frac{3}{2}x - \frac{1}{2}x^3 \right|_0^1 \\ &= \frac{3}{2} - \frac{1}{2} = 1 \end{aligned} \right)$$

Nice test case, because we  
can compare our answer to 1

Can compare ...



$$dA = f(x) dx$$

$$A = \sum_{i=1}^N dA$$

$$\left( \approx \int f(x) dx \right)$$

→ Midpoint Method

Analysis of Data From P341

# Midterm.

97 students

Bell Curve

35

↳ what do I expect?

1950 →

$$\mu = 60\%$$
$$\sigma = 15\%$$

$$\mu + \sigma \rightarrow 75\%$$

1980 →

$$\mu = 65\%$$
$$\sigma = 15\%$$

(😊)  $\mu + \sigma \rightarrow \underline{\underline{80\%}}$

Canadian Grading Scale.



80

87

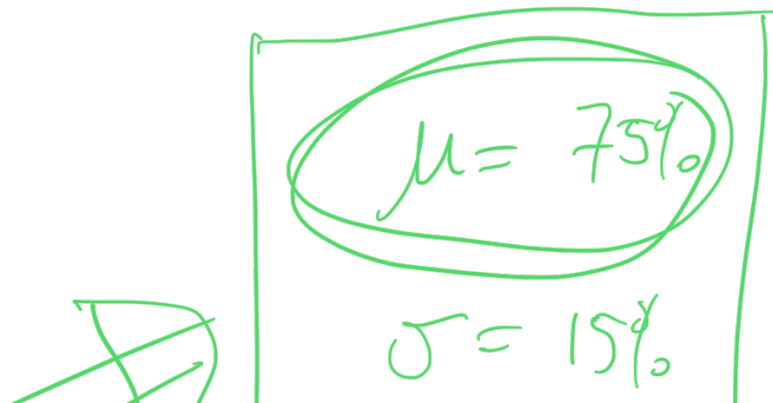
A-

A

400 Engineers  $\rightarrow$  7

780%

2020





😊  $\mu + \sigma \rightarrow 90\%$

$$\bar{x} = 76.6$$

$$s = 12.5$$

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"If you do the homework,  
and understand it, you'll  
do fine/better on  
the tests."

?

$$MY = \beta_0 + \beta_1 HW$$


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Non-linear binning of data.

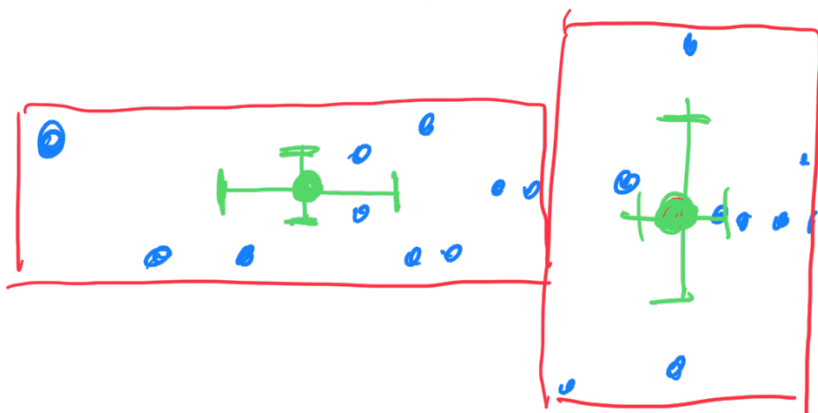
plt.hist( )



|

$$\sigma_{\mu} = \frac{S}{\sqrt{n}}$$

10 data pts



Sum val, Sum x val

1st Loop

$$\bar{x} = \frac{1}{N} \sum_{i=1}^N x_i$$

Sum x  
Sum v

2nd Loop

$$S = \sqrt{\frac{1}{N-1} \sum_{i=1}^N (x_i - \bar{x})^2}$$

R M S !!

97 → prime number :-)

9, 9, 9, 99, 9, 9, 9, 9, 7  
↑

2nd Year