

**Assignment 3 Theoretical Part**

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**Out:** 4/03/2018**Due:** 4/10/2018 (deadline: midnight)**Late submissions:** Late submissions result in 10% deduction for each day. The assignment will no longer be accepted 3 days after the deadline.

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**Office hours:**

		Monday	Wed	Thu	Fri
Guido Gerig	office 10.094	2 - 4pm			
Yida Zhou	<a href="mailto:yz4499@nyu.edu">yz4499@nyu.edu</a>			1-3pm	
Zebin Xu	<a href="mailto:zebinxu@nyu.edu">zebinxu@nyu.edu</a>		2 - 4pm		
Andrew Dempsey	<a href="mailto:ad4338@nyu.edu">ad4338@nyu.edu</a>				10 - noon
Monil D. Shah	<a href="mailto:mds747@nyu.edu">mds747@nyu.edu</a>	4 - 6pm			

Location: Cubicle spaces in front of my office named 10.098 A,B,D,E,H.

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**A) Theoretical questions:****A1) Hough Transform: Parametrization**

The standard parametrization of a line,  $y = m_0 x + b_0$ , with  $m_0$  and  $b_0$  slope and intercept, has not become the standard parametrization for the Hough transform for finding lines.

- Explain why this option did not become a popular choice.
- Would you still use it, what can you say about the discrete grid of the Hough space with axes  $m_0$  and  $b_0$  in regard to Hough space cell spacing and its representation of lines.

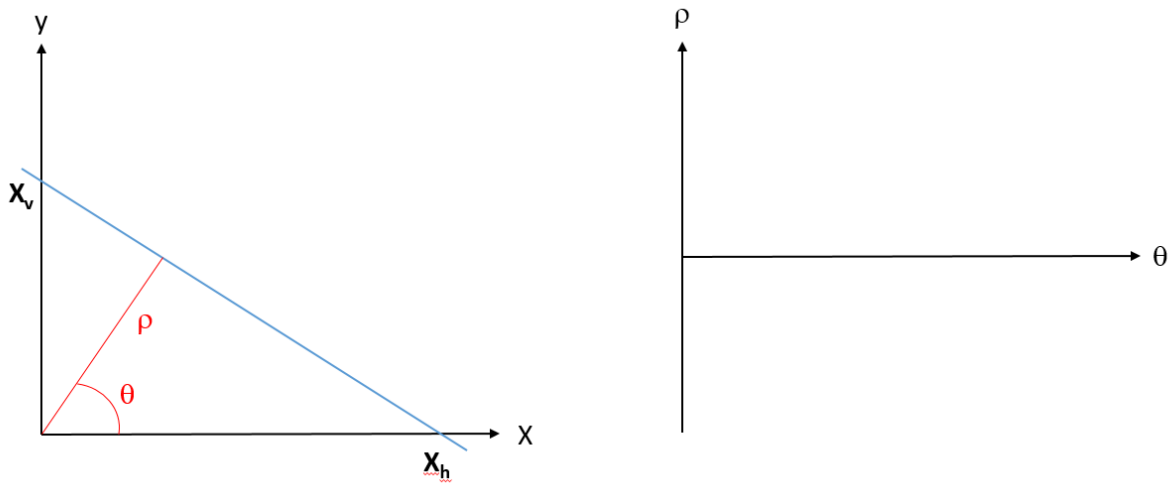
**A2) Hough Transform: Polar representation I**

Show that the polar representation of a line,  $x \cos \theta + y \sin \theta = \rho$ , represents a Cosine function in parameter space with axes  $\theta$  and  $\rho$ . (Remember that a general Cosine function is given as  $y = a \cos(\alpha - \delta)$ , with  $a$ =amplitude and  $\delta$ = phase shift).

### A3): Hough Transform: Polar representation II

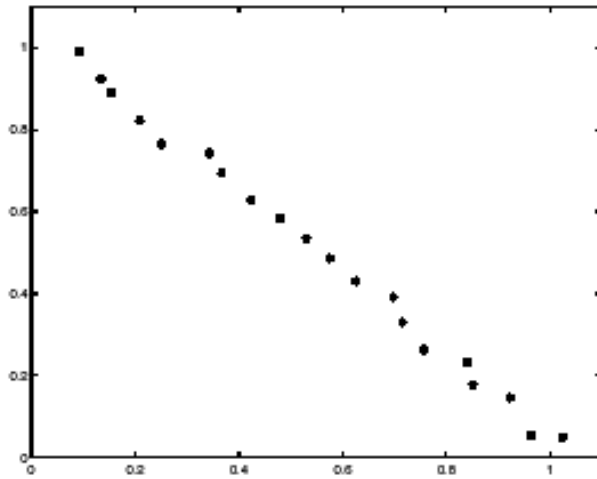
Given a scenario with a line in  $(x,y)$ -space intersecting with the horizontal axis at  $\bar{x}_h$  and with the vertical axis at  $\bar{x}_v$ , calculate and plot the corresponding Cosine curves in the  $(\theta, \rho)$  parameter space.

Calculate the intersection of the two parameter curves and discuss how its coordinates  $(\theta, \rho)$  represent the line  $l$  in image space.



### A4) Noisy line structures

Given points forming a line but its locations corrupted by noise (see below), how would noise affect the clustering of curves in Hough space? What could you do to still find a peak with associated parameters that would represent the noisy line?



#### A5) Hough Transform for Ellipses

We have learned that the Hough transform for circles requires three parameters, two for the center and one for the radius, thus spanning a 3-D parameter space. Now let us find ellipses in its standard form (no orientation) with varying size?

Would the Generalized Hough Transform (GHT), as discussed in the course using R-tables for creating a template, eventually offer a solution? Sketch it with a drawing and some short explanation. What about finding ellipses in different orientations given the GHT?