Lecture 1 - Introduction in declarative programming. Recursion

Official web site: www.cs.ubbcluj.ro/~hfpop/pfl

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Czibula, G., Pop, H.F., Elemente avansate de programare în Lisp și Prolog. Aplicații în Inteligența Artificială., Ed. Albastră, Cluj-Napoca, 2012

Programming and programming languages

> LANGUAGES

- Procedural (imperative) high level languages
 - o Fortran, Cobol, Algol, Pascal, C, ...
 - o program sequence of instructions
 - o the assignment statement, control structures for the control of sequential execution, branching and cycling
 - o the role of the programmer "what" and "how"
 - 1. to describe what is to be calculated
 - 2. to organize the calculation

HOW

- 3. to organize memory management
- !!! it is argued that the assignment instruction is dangerous in high-level languages, just as the GO TO instruction was considered dangerous for structured programming in the '68s.
- Declarative (descriptive, applied) very high level languages
 - based on expressions
 - o expressive, easy to understand (have a simple basis), extensible

- o programs can be seen as descriptions that state information about values, rather than instructions to determine values or effects.
- o they give up instructions
 - 1. thus they protect users from making too many mistakes
 - 2. they are generated from mathematical principles analysis, design, specification, implementation, abstraction and reasoning (deductions of consequences and properties) become more and more formal activities.
- o the role of the programmer "what" (not "how")
- o two classes of declarative languages
 - 1. **functional languages** (eg Lisp, ML, Scheme, Haskell, Erlang)
 - Focus on values of data described by expressions (built through applications of functions and definitions of functions), with automatic evaluation of expressions
 - 2. **logical languages** (e.g. Prolog, Datalog, Parlog),
 - ➤ focus on logical assertions that describe the relationships between data values and automatic derivations of answers to questions, starting from these assertions.
- o applications in Artificial Intelligence automated proofs, natural language processing and speech understanding, expert systems, machine learning, intelligent agents, etc.
- Multiparadigm languages: F#, Python, Scala (imperative, functional, object oriented)
- ➤ Interactions between declarative and imperative languages declarative languages that provide interfaces with imperative languages (eg C, Java): SWI Prolog, GNU Prolog, etc.
- ➤ Logtalk integrates logic and object-oriented programming
- ➤ Logic programming in **Python**:
 - o Karen
 - o **SymPy** library for simbolic computations

Recursion

- general mechanism to elaborate programs
- recursion arose from practical necessities (direct transcription of recursive mathematical formulas; see Ackermann's function)
- recursion is the mechanism by which a subprogram (function, procedure) calls itself
 - o two types of recursion: **direct** or **indirect**
- !!! Result
 - o any calculable function can therefore be expressed and programmed) in terms of recursive functions
- two things to consider in describing a recursive algorithm: **the recursive rule** and **the termination condition**
- advantage of recursion: source text that is extremely short and very clear.

- **disadvantage** of recursion: filling the stack segment if the number of recursive calls, respectively of the formal and local parameters of the recursive subprograms is high enough.
 - declarative languages have specific mechanisms to optimize the recursion (see the mechanism of tail recursion in Prolog).

Examples of recursion

Remarks

- a list is a sequence of items $(l_1 l_2 ... l_n)$
- the empty list (with 0 elements) is denoted by \bigcirc
- adding an item to a list is denoted by ⊕
- 1. Create list (1,2,3, ... n)
 - a) directly recursive

$$creareLista(n) = \begin{cases} \emptyset & daca \ n = 0 \\ creareLista(n-1) \oplus n & altfel \end{cases}$$

b) using a recursive auxiliary function to create the sublist (i, i + 1, ..., n)

// create the list consisting of the elements i, i + 1,..., n

Recursive mathematical model

$$creare(i,n) = \begin{cases} \phi & daca \ i > n \\ i \oplus creare(i+1,n) & altfel \end{cases}$$

// create the list consisting of elements 1, 2, ..., n

$$creareLista(n) = creare(1, n)$$

Pseudocode

Data representation: singly linked list with dynamic allocation of nodes.

NodeLSI

e: TElement // useful information of node

urm: ^NodeLSI // address the following node is stored

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LSI
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prim: ^NodeLSI // address of the first node in the list
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Function createNodeLSI(e)

{pre: e: TElement}

{post: return a ^NodeLSI having e as useful information }

{allocates a storing space for a NodeLSI }

{p: ^NodLSI}

allocate(p)

[p].e ← e

[p].urm ← NIL

{result returned by the function }

createNodeLSI ← p

EndFunction

Function create(i, n)

{post: return a ^NodLSI pointer towards the head of the linked list for the list for the li
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{post: return a ^NodLSI, pointer towards the head of the linked list formed by }

{ elements i, i+1,..., n }

If i > n then

create ← NIL

else

{ allocate a storage space for a NodeLSI with usefun information e }

q ← createNodeLSI(i)

{ create the link between node q and the head of the linked list formed }

{ by elements i+1,..., n }

[q].urm ← create(i+1, n)

create ← q

EndIf
```

EndFunction

Function createList(n)

{post: return a ^NodeLSI, pointer towards the head of the linked list formed by } { elements 1, 2,..., n }

$$createList \leftarrow create(1, n)$$

EndFunction

- 2. Given a natural number n, calculate the sum 1+2+3+...+n.
 - a) directly recursive

$$suma(n) = \begin{cases} 0 & daca \ n = 0 \\ n + suma(n-1) & alt fel \end{cases}$$

b) using a recursive auxiliary function for calculating the sum i + (i + 1) + ... + n

$$suma_aux(n,i) = \begin{cases} 0 & daca \ i > n \\ i + suma(n,i+1) & alt fel \end{cases}$$

$$suma(n) = suma_aux(n, 0)$$

3. Add an item at the end of a list.

// build the list (l1, l2,..., ln, e)
$$adaug(e, l_1 l_2 \dots l_n) = \begin{cases} (e) & daca \quad l \ e \ vida \\ l_1 \oplus adaug(e, l_2 \dots l_n) & alt fel \end{cases}$$

4. Search for an element in a list.

$$apare(E, l_1 l_2 \dots l_n) = \begin{cases} fals & daca \ l \ e \ vida \\ adevarat & daca \ \ l_1 = E \\ apare(E, l_2 \dots l_n) & alt fel \end{cases}$$

5. Count the number of occurrences of an item in the list.

$$nrap(E, l_1 l_2 \dots l_n) = \begin{cases} 0 & daca \ l \ e \ vida \\ 1 + nrap(E, l_2 \dots l_n) & daca \ \ l_1 = E \\ nrap(E, l_2 \dots l_n) & alt fel \end{cases}$$

6. Check if a numeric list is set.

$$eMultime(l_1l_2...l_n) = \begin{cases} adevarat & daca \ l \ e \ vida \\ fals & daca \ \ l_1 \in (l_2...l_n) \\ eMultime(l_2...l_n) & altfel \end{cases}$$

7. Transform a numeric list into a set.

$$\mathit{multime}(l_1l_2\ldots l_n) = \begin{cases} \phi & \textit{daca } l \; e \; \textit{vida} \\ \mathit{multime}(l_2\ldots l_n) & \textit{daca } \quad l_1 \in (l_2\ldots l_n) \\ l_1 \oplus \mathit{multime}(l_2\ldots l_n) & \textit{altfel} \end{cases}$$

8. Return the inverse of a list.

$$\mathit{invers}(l_1 l_2 \dots l_n) = \begin{cases} \phi & \mathit{daca} \ l \ e \ \mathit{vida} \\ \\ \mathit{invers}(l_2 \dots l_n) \oplus l_1 & \mathit{altfel} \end{cases}$$

9. Remove all occurrences of an item from a list.

$$sterger(E, l_1 l_2 ... l_n) = \begin{cases} \phi & daca \ l \ e \ vida \\ l_1 \oplus sterger(E, l_2 ... l_n) & daca \ \ l_1 \neq E \\ sterger(E, l_2 ... l_n) & alt fel \end{cases}$$

10. Return the k-th element of a list (k > 1).

$$element(l_1l_2...l_n,k) = \begin{cases} \phi & daca \ l \ e \ vida \\ l_1 & daca \ k = 1 \\ element(l_2,...l_n,k-1) & alt fel \end{cases}$$

11. Return the difference between two sets represented as lists.

$$\textit{diferenta}(l_1l_2\dots l_n,p_1p_2\dots p_m) = \begin{cases} \phi & \textit{daca } l \ e \ vida \\ \textit{diferenta}(l_2...l_n,p_1p_2...p_m) & \textit{daca } \ l_1 \in (p_1p_2...p_m) \\ l_1 \oplus \textit{diferenta}(l_2...l_n,p_1p_2...p_m) & \textit{altfel} \end{cases}$$

Homework

- 1. Verify whether a natural number is prime.
- 2. Calculate the sum of the first k elements in a numeric list ($l_1 l_2 \dots l_n$)
- 3. Remove the first k even numbers from a numeric list.