

## Week 2 Homework:

### Section 1.3: 5, 7, 10, 15, 17, 31, 58

#5

p	q	r	$q \vee r$	$p \wedge (q \vee r)$	$p \wedge q$	$p \wedge r$	$(p \wedge q) \vee (p \wedge r)$
T	T	T	T	T	T	T	T
T	T	F	T	T	T	F	T
T	F	T	T	T	F	T	T
F	T	T	T	F	F	F	F
T	F	F	F	F	F	F	F
F	T	F	T	F	F	F	F
F	F	T	T	F	F	F	F
F	F	F	F	F	F	F	F

#7

- Jan is not rich or is not happy.
- Carlos will not bicycle and will not run tomorrow.
- Mei does not walk and does not take the bus to class.
- Ibrahim is not smart or is not hard working.

#10

a.

p	q	$\neg p$	$p \vee q$	$\neg p \wedge (p \vee q)$	$(\neg p \wedge (p \vee q)) \rightarrow q$
T	T	F	T	F	T
T	F	F	T	F	T
F	T	T	T	T	T
F	F	T	F	F	T

b.

p	q	r	$p \rightarrow q$	$q \rightarrow r$	$((p \rightarrow q) \wedge (q \rightarrow r))$	$p \rightarrow r$	$((p \rightarrow q) \wedge (q \rightarrow r)) \rightarrow (p \rightarrow r)$
T	T	T	T	T	T	T	T
T	T	F	T	F	F	F	T

T	F	T	F	T	F	T	T
F	T	T	T	T	T	T	T
T	F	F	F	T	F	F	T
F	F	T	T	T	T	T	T
F	T	F	T	F	F	T	T
F	F	F	T	T	T	T	T

c.

p	q	$p \rightarrow q$	$p \wedge (p \rightarrow q)$	$(p \wedge (p \rightarrow q)) \rightarrow q$
T	T	T	T	T
T	F	F	F	T
F	T	T	F	T
F	F	T	F	T

d.

p	q	r	$p \vee q$	$p \rightarrow r$	$(p \vee q) \wedge (p \rightarrow r)$	$q \rightarrow r$	$(p \vee q) \wedge (p \rightarrow r) \wedge (q \rightarrow r)$	$((p \vee q) \wedge (p \rightarrow r) \wedge (q \rightarrow r)) \rightarrow r$
T	T	T	T	T	T	T	T	T
T	T	F	T	F	F	F	F	T
T	F	T	T	T	T	T	T	T
F	T	T	T	T	T	T	T	T
T	F	F	T	F	F	T	F	T
F	F	T	F	T	F	T	F	T
F	T	F	T	T	T	F	F	T
F	F	F	F	T	F	T	F	T

#15

It's a tautology.

p	q	$\neg q$	$p \rightarrow q$	$\neg q \wedge (p \rightarrow q)$	$\neg p$	$(\neg q \wedge (p \rightarrow q)) \rightarrow \neg p$
T	T	F	T	F	F	T
T	F	T	F	F	F	T
F	T	F	T	F	T	T
F	F	T	T	T	T	T

#17

They're logically equivalent.

$p$	$q$	$p \leftrightarrow q$	$\neg(p \leftrightarrow q)$	$\neg q$	$p \leftrightarrow \neg q$
T	T	T	<b>F</b>	F	<b>F</b>
T	F	F	<b>T</b>	T	<b>T</b>
F	T	F	<b>T</b>	F	<b>T</b>
F	F	T	<b>F</b>	T	<b>F</b>

#31

They're not logically equivalent.

$p$	$q$	$r$	$p \rightarrow q$	$(p \rightarrow q) \rightarrow r$	$q \rightarrow r$	$p \rightarrow (q \rightarrow r)$
T	T	T	T	<b>T</b>	T	<b>T</b>
T	T	F	T	<b>F</b>	F	<b>F</b>
T	F	T	F	<b>T</b>	T	<b>T</b>
F	T	T	T	<b>T</b>	T	<b>T</b>
T	F	F	F	<b>T</b>	T	<b>T</b>
F	F	T	T	<b>T</b>	T	<b>T</b>
F	T	F	T	<b>F</b>	F	<b>T</b>
F	F	F	T	<b>F</b>	T	<b>T</b>

#58

All five.

**Section 2.1:** 3, 5, 7, 9, 10, 14, 21, 35, 37

#3

- a. The second is a subset of the first.
- b. Neither is a subset of the other.
- c. The first is a subset of the second.

#5

- a. They are equal.
- b. They are not equal.
- c. They are not equal.

#7

- a. Yes
- b. No
- c. Yes
- d. No
- e. No

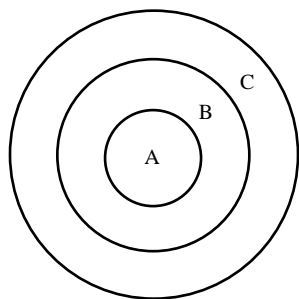
#9

- a. False
- b. False
- c. False
- d. True
- e. False
- f. False
- g. True

#10

- a. True
- b. True
- c. False
- d. True
- e. True
- f. False
- g. False

#14



#21

- a.  $\mathcal{P}(\{a\}) = \{\emptyset, \{a\}\}$
- b.  $\mathcal{P}(\{a, b\}) = \{\emptyset, \{a\}, \{b\}, \{a, b\}\}$
- c.  $\mathcal{P}(\{\emptyset, \{\emptyset\}\}) = \{\emptyset, \{\emptyset\}, \{\emptyset, \{\emptyset\}\}\}$

#35

$mn$

#37

$m^n$