# The potential of using sets of specimens to handle species concepts: initial thoughts

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## 1 Problem

Recent increases in the rate of specimen digitisation in natural history museums (e.g. [1]), combined with persistent identifiers for these specimens [2] allows for robust species concepts defined by a collection (set) of specimens.

This paper experiments with using mathematical set notation to define operations on groups of specimens that may be considered equivalent to taxonomic and nomenclatural acts.

At the present time insufficient numbers of specimens have been assigned unique identifiers for this solution to be generally practical. It is presented here as an example potential use of unique identifiers, and to encourage discussion as to whether this approach has any merit (it may not).

The mathematics of relational databases is understood in terms of manipulations (relations) of sets. The expression of taxonomic and nomenclatural acts as functions on sets may aid the design of systems that record and track species concepts, which will by necessity need to be stored in databases. This approach is the reverse of [3] who developed an object-orientated model, and later showed it could be made into a relational database.

## 1.1 Reduction of problem

Species concepts are generally considered to comprise all organisms that are defined by that concept, that is to say that all wild living organisms that match the description and primary types are included. Placing the entirety of a population into a set is impractical, so here concepts are confined to specimens. Specimens are increasingly citable 'objects' and are here considered to include physical specimens, nucleotide sequences, etc. These concept sets may be considered to be a representative subset of the population if philosophically desirable.

This work deals solely with the species concept. Similarly methods (nested sets) could be applied to genus- and family- group concepts if so desired, with modification for the differing method of type-designation at these levels.

This paper does not deal with publications for the purpose of clarity. The association of publications of new species with their type specimens is straightforward, if time consuming for the historical literature. It is hoped that any real world system would have this functionality.

#### 1.2 Nomenclature

The assignment of scientific names to species concepts is a great aid in communicating about organisms. This approach does not change anything relating to the naming of concepts. If anything it may help with algorithmically determining the name of a species concept based on specimens.

## 2 Introduction

We consider x to be a collection (set) of specimens  $(s_1, s_2, s_3, ...)$  including a number of primary type specimens  $(t_1, t_2, t_3, ...)$ .

$$x = \{s_1, s_2, s_3, ..., t_1, t_2, t_3, ...\}$$

A competent taxonomist takes this set of specimens, and sorts them into groups they consider to represent species. If the group has been recently well studied then the piles may each contain a single primary type.

$$x_1 = \{s_1, ..., t_1\}$$

$$x_2 = \{s_2, ..., t_2\}$$

$$x_3 = \{s_3, ..., t_3\}$$

where  $x_n \subset x$ ;  $x = x_1 \cup x_2 \cup x_3 \cup ...$ 

Each  $x_n$  is a species concept, typified by the specimen  $t_n$  when there is a single primary type. No specimen appears in more than one subset.

## 2.1 Synonymy

If the taxonomist selected set contains multiple primary types this is an indication of synonymy.

$$x_n = \{s_a, s_b, s_c, ..., t_x, t_y\}$$

**Define** type cardinality as the number of valid types in a set.

$$typec(x) = |\{t|t \in x\}|$$

Assuming that  $t_n$  are valid types then typification can be resolved by the appropriate nomenclatural code.

- 1. When typec(x) = 1 then the concept can be named by the primary type.
- 2. When typec(x) > 1 then a selection of primary type is needed following the appropriate rules of nomenclature, following the concept of priority.
- 3. When typec(x) = 0 then the concept does not contain a type. The set should be expanded to include an appropriate primary type, or if no appropriate type is available then a specimen from the set should be described as the primary type.

#### 2.1.1 Precedence

Of the valid types the oldest is the one used to formalise the species concept. If information on when the types were scientifically described is available we can select the type with the lowest date value.

Define

$$type(x) = min(\{t_{[date]} | t \in x\})$$

## 3 Comparison of species concepts

## 3.1 Identity of species concepts

The identity of species concepts in this scheme occurs when the concepts are sets containing the same specimens. Identity between concepts is potentially not the most useful way of determining if two or more sets are compatible (see Consistency). The mathematical identity of two sets is equivalent to each set being a subset of the other.

$$x = y \iff x \in y \land y \in x$$

## 3.2 Consistency of species concepts

Test to see if two, non-identical, species concepts are compatible.

Author A: 
$$x_A = \{x_1, x_2, x_3\}$$
  
Author B:  $x_B = \{x_1, x_2, x_3, x_4\}$ 

The species concepts  $x_A$  and  $x_B$  can be considered to be consistent. An example would be where Author A creates their concept before Author B. Author B later expands Author A's concept with the addition of a new specimen. As Author A has not placed  $x_4$  in any other species concept these two concepts can be considered to be compatible: it is only the fact that Author A was not aware of  $x_4$  that they did not include it in  $x_A$ .

**Define** species concepts are *consistent* when the only specimens not in the intersection of the two concepts are not placed in another concept by either author.

 $consitent(x_a, x_B) = \forall x_n \notin x_A \cap x_B \text{ and } x_A, x_B \text{ not in other concepts by the same authors}$ 

## 4 Expanding scope of a species concept

## 4.1 Identification of expanded scope

We can test that  $x_B$  is an expansion of the scope of  $x_A$  by checking that  $x_A$  is a subset of  $x_B$  and that  $x_b$  has a larger cardinality than  $x_A$ .

$$x_A \subset x_B \land |x_A| < |x_B|$$

## 4.2 Expansion of scope

It should be noted that both of the following operations will result in the creation of a new species concept.

### 4.2.1 Addition of a specimen to a species concept

Adding a specimen to an existing species concept can be achieved through the union of that concept with the new specimen.

$$x_B = x_A \cup x_4$$

#### 4.2.2 Synonymy of two previous species concepts

If two concepts, both previously considered to be valid, are found to be synonyms of each other then a new concept can be created that is the union of these two.

$$x_{new} = x_A \cup x_B$$

## 5 Reducing scope of a species concept

## 5.1 Identification of reduced scope

## 5.2 Reduction in scope

It should be noted that both of the following operations will result in the creation of a new species concept.

## 5.2.1 Removal of specimens from a species concept

The creation of a species concept  $de\ novo$  based on those specimens the author wishes to retain is perhaps the easiest way forward, however there may be merit in some instances of explicitly recording the removal of specimens in relation to an existing concept. The specimens to exclude are defined by  $x_B$ .

$$x_{new} = \{x_A | x_A \not\subset x_B\}$$

### 5.2.2 Splitting of a species concept

The same operation as above can be used, with  $x_B$  as set representing a species concept rather than any set of specimens.

## 6 Remarks

The ability to store and manipulate species concepts, whether they be *de novo* concepts (such as from the description of new species) or relative to existing concepts (e.g. the creation or removal of synonymy) can be achieved simply through the use of sets of specimens, assuming that specimens have stable, persistent identifiers. The creation of new concepts becomes resource cheap and objective (at least in the definition of the concept).

It is not currently feasible, and may never be, for the creator of a concept to identify all relevant digitised specimens that may form part of that concept. The creation of an objective list of specimens that were used to form that concept however is certainly feasible. Given the low cost of creating a new concept, it would be easy for other individuals and institutions to create a new concept that expands the original to include additional specimens (e.g. a taxonomist finds the species from a new area; a museum digitises its collection of *Aus bus* and adds those specimens to the existing concept).

Given that digitising efforts may focus on the primary types held by an institution, and that this metadata of specimens is almost certain to be recorded the creation of initial 'specimen species concepts' based solely on these type series could be achieved automatically, providing a starting concept dataset.

To create a usable system of species concepts based on specimens a robust citation system for concepts needs to be created, with persistent identifiers. Persistent identifiers would allow the easy expansion and changing of concepts as new specimens are collected or digitised. Life Sciences Identifiers (LSIDs) or Digital Object Identifiers (DOIs) could be used for this purpose.

## References

- [1] Vladimir Blagoderov et al. "No specimen left behind: industrial scale digitization of natural history collections". In: *ZooKeys* 209 (2012), p. 133.
- [2] Robert P. Guralnick et al. "Community Next Steps for Making Globally Unique Identifiers Work for Biocollections Data". In: *ZooKeys* 494 (2015), pp. 133–154. DOI: 10.3897/zookeys.494.9352.
- [3] Nozomi Ytow, David R Morse, and David Mcl Roberts. "Nomencurator: a nomenclatural history model to handle multiple taxonomic views". In: *Biological journal of the Linnean Society* 73.1 (2001), pp. 81–98.