

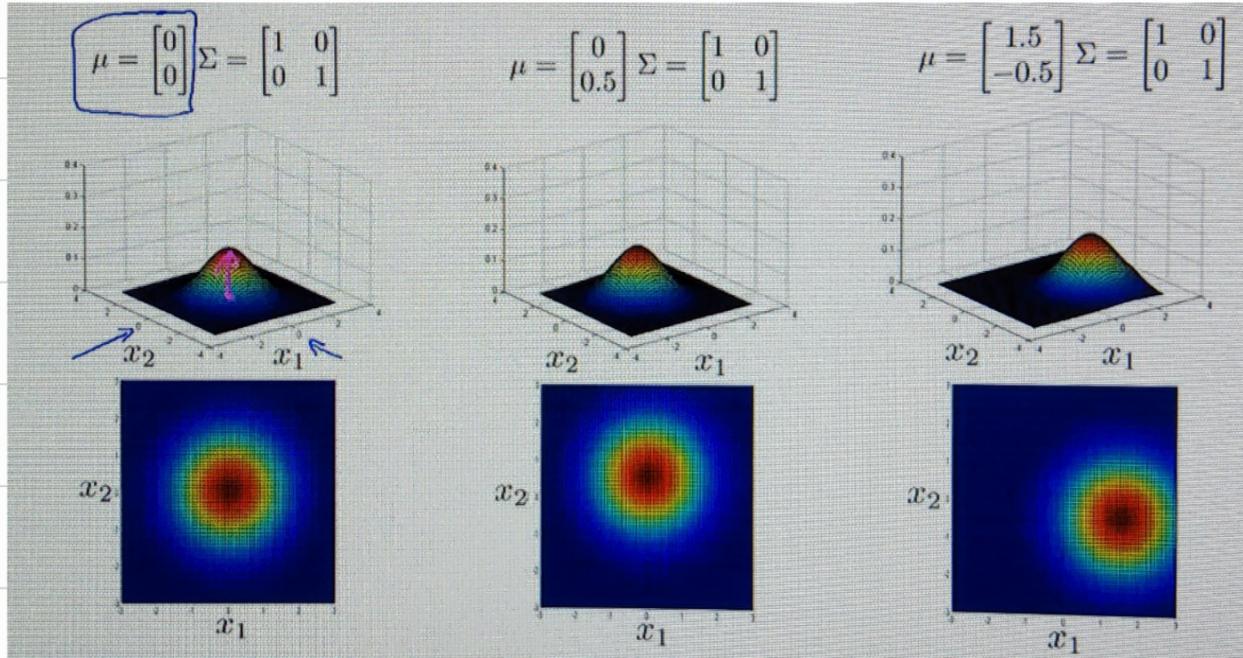
Multivariate Gaussian Distribution

$$x \in \mathbb{R}^n$$

$p(x)$ 를 $p(x_1) \cdot p(x_2) \cdot \dots$ 가 아니라

All in one go로 구하기

$$\mu \in \mathbb{R}^n, \Sigma \in \mathbb{R}^{n \times n}$$



Anomaly Detection using the Multivariate Gaussian Distribution

$$\mu = \frac{1}{m} \sum_{i=1}^m x^{(i)}$$

$$\Sigma = \frac{1}{m} \sum_{i=1}^m (x^{(i)} - \mu)(x^{(i)} - \mu)^T$$

1. Fit model $p(x)$ by setting

2. Given a new example x , compute

$$p(x) = \frac{1}{(2\pi)^{\frac{n}{2}} |\Sigma|^{\frac{1}{2}}} \exp\left(-\frac{1}{2}(x-\mu)^T \Sigma^{-1} (x-\mu)\right)$$

Flag an anomaly if $p(x) < \epsilon$

Original model vs. Multivariate Gaussian

- | | |
|---|--|
| - Manually create features to capture anomalies where x_1, x_2 take unusual comb. of values | + Automatically captures correlations b/w. features |
| + Computationally cheaper | - Computationally more expensive |
| + OK even if m is small | - Must have $m > n$, or else Σ is non-invertible |