

# The problem of overfitting

## Overfitting 과적합

ex1.  $\theta_0 + \theta_1 x$  Underfit, High Bias 편향

ex2.  $\theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$  Overfit, High Variance 분산

「 If we have too many features,  
the learned hypothesis may fit the training set very well,  
but fail to generalize to new examples. 」

과적합 피하려면,

### 1. Reduce number of features

- Manually select which features to keep

- Model selection algorithm

### 2. Regularization

- Keep all the features, but reduce

- magnitude/values of parameters  $\theta_j$

- Works well when we have a lot of features,  
each of which contributes a bit to  
predicting  $y$ .

# Regularization

↳ Small values for parameters  $\theta_0, \theta_1, \dots, \theta_n$

- "Simpler" hypothesis

- Less prone to overfitting

$$J(\theta) = \frac{1}{2m} \left[ \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^n \theta_j^2 \right]$$

regularization parameter

- Controls a trade off

btw. two different goals.

① fitting the trainset well )

② keeping the parameters small

## Regularized linear regression

Gradient Descent ( $\theta_0 \in \text{penalize } X$ )

$$\theta_j := \theta_j - \alpha \cdot \left[ \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \frac{\lambda}{m} \theta_j \right]$$

( $\frac{\partial}{\partial \theta_j} J(\theta)$ ) <regularized>

같다

$$\theta_j := \theta_j \left( 1 - \alpha \cdot \frac{\lambda}{m} \right) - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

less than 1,  $\theta_j$ 는 규제 시 더 작게 update

# Regularized logistic regression

$$J(\theta) = - \left[ \frac{1}{m} \sum_{i=1}^m y^{(i)} \log h_{\theta}(x^{(i)}) + (1-y^{(i)}) \log (1-h_{\theta}(x^{(i)})) \right] \\ + \frac{\lambda}{2m} \sum_{j=1}^n \theta_j^2$$

↳ means to explicitly exclude  
the bias term,  $\theta_0$

## Gradient descent

Repeat {

$$\rightarrow \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)}$$

$$\rightarrow \theta_j := \theta_j - \alpha \underbrace{\left[ \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)} + \frac{\lambda}{m} \theta_j \right]}_{\substack{(j=1, 2, 3, \dots, n) \\ \theta_1, \dots, \theta_n}} \quad \leftarrow$$

$$\frac{\partial J(\theta)}{\partial \theta_j}$$

$$h_{\theta}(x) = \frac{1}{1+e^{-\theta^T x}}$$