



DMC ONLINE

#YoMeQuedoEnCasa

Deep Learning & Web Scraping and Text Mining

PhD. Edwyn Javier Aldana Bobadilla





DMC ONLINE

DMC
Perú

Reglas Básicas



Puntualidad



Mantener silenciado el micrófono durante la sesión



Las preguntas se realizarán por el chat/ en caso sea necesario se habilita el micrófono



Realizar las actividades encomendadas

#YoMeCapacitoEnCasa

www.dmc.pe



DMC ONLINE



Dinámica de las sesiones

7:00 PM – 8:30 PM

Parte 1

8:30 PM – 8:40 PM

Receso

8:40 PM – 10:00 PM

Parte 2

Los recursos (scripts, datasets, presentaciones) serán compartidos en la nube, en un URL habilitado por el profesor.

#YoMeCapacitoEnCasa



DMC ONLINE



Calificaciones

Asistencia (Curso)

mínimo 80% sesiones para recibir la certificación

Exámen Final

(40%)

+

Trabajo final

(60%)

#YoMeCapacitoEnCasa



DMC ONLINE

#YoMeCapacitoEnCasa

Preliminares

Aprendizaje Automático

Técnicas para crear **modelos computacionales** con capacidad de decisión basada en la **experiencia**.

Ejemplos:

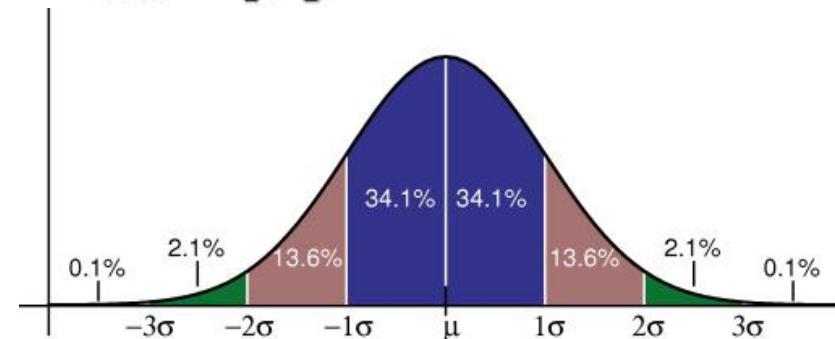
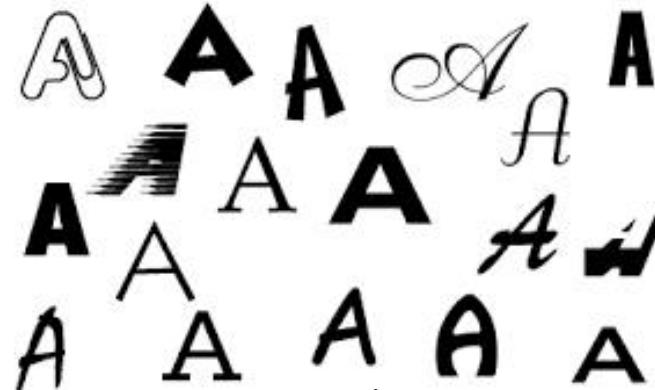
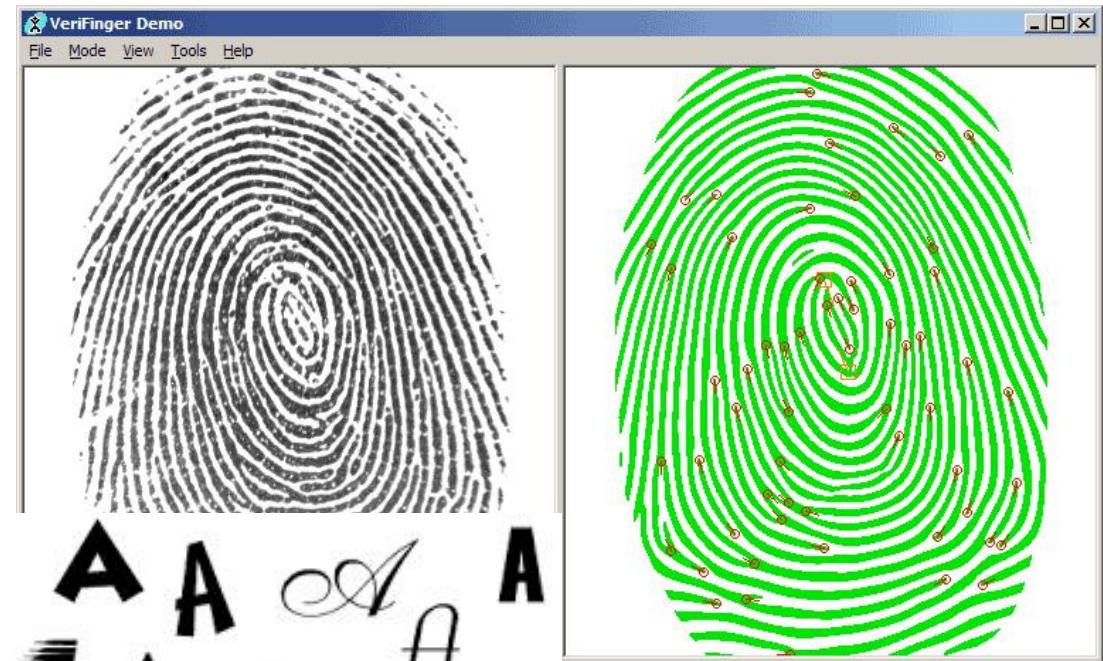
- Detección de transacciones fraudulentas en tarjetas de crédito.
- Correo no deseado
- Vehículos autónomos



Aprendizaje Automático

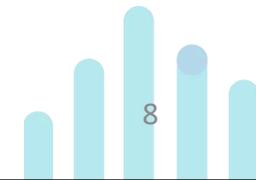
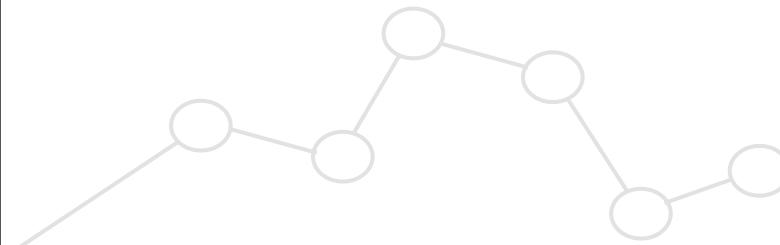
Areas relacionadas:

- Reconocimiento de patrones.
- Teoría del aprendizaje
- Estadística
- Probabilidad



1) Problema o tarea a resolver (T)

- I. Jugar ajedrez.
- II. Reconocer caracteres escritos a mano.
- III. Conducir un automóvil a través de una autopista.
- IV. Realizar el estudio de un crédito bancario a un cliente.
- V. Reconocer discurso ofensivo o que incite a la violencia



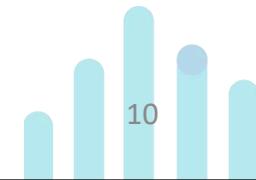
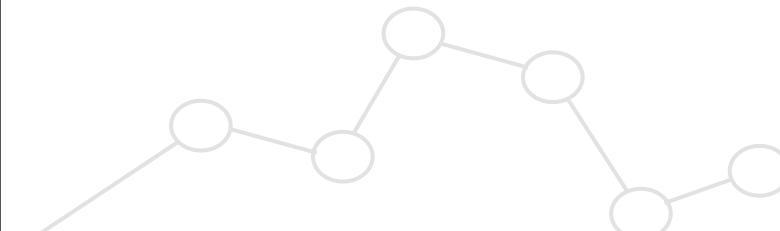
2) Conocimiento previo o experiencia (E)

- I. Conjunto de todos los posibles estados del tablero de ajedrez.
- II. Muestra de **imágenes** con caracteres escritos a mano.
- III. Secuencia de **imágenes** del entorno asociadas a acciones ejecutadas por un conductor humano (complejo).
- IV. Información de ingreso, egresos y comportamiento financiero de un conjunto de clientes.
- V. Corpus conteniendo **sentencias** del discurso, o un conjunto de **audios** conteniendo dichas sentencias.



3) Medida de desempeño (P)

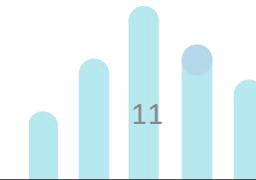
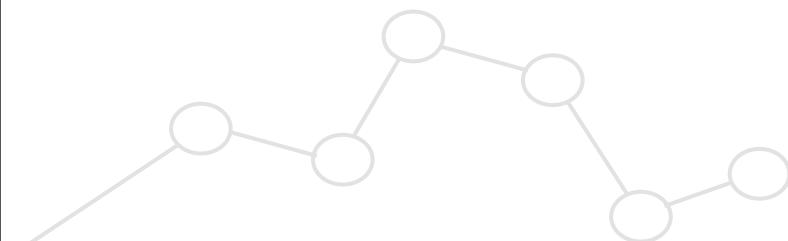
- I. Número de juegos ganados por contrincantes humanos.
- II. Porcentaje de caracteres “bien clasificados”.
- III. Tiempo o distancia recorrida antes que un error ocurra (observado y corregido por intervención humana).
- IV. Porcentaje de cartera morosa.
- V. Efectividad en la predicción de conductas violentas.



Representación de la experiencia (E)

- Las computadoras trabajan en un **espacio numérico finito**
- Es importante que la información relacionada con la experiencia E sea mapeada a dicho espacio numérico.
- E incluirá aquellos atributos o propiedades importantes del problema a ser resuelto (**Extracción de Características**).
- Generalmente E se representa como un conjunto de vectores de la forma:

$$\vec{x} = [x_1, x_2, \dots, x_n] \in \Re^n$$



Representación de la experiencia (E)

Ejemplo:

- Problema (T): Reconocer las frutas en la imagen:



Representación de la experiencia (E)

Ejemplo:

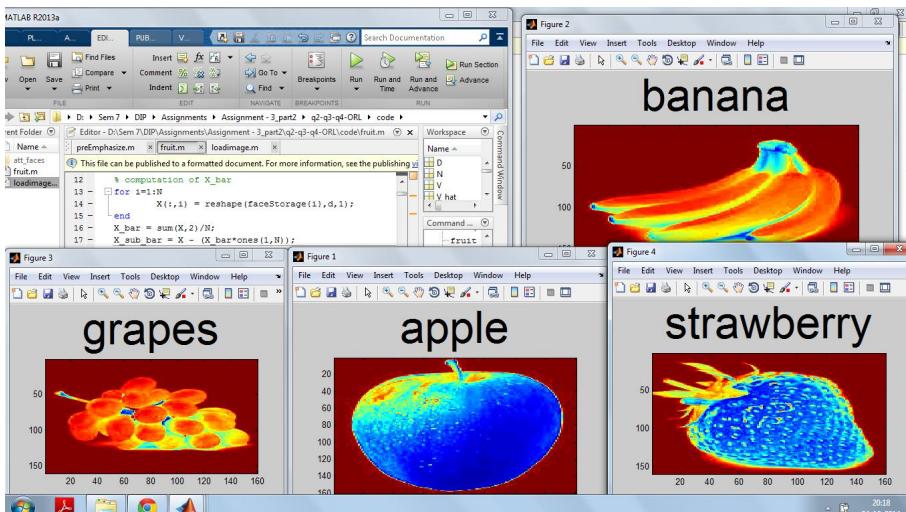
- Problema (T): Reconocer las frutas en la imagen
- Experiencia (E): ?



Representación de la experiencia (E)

Ejemplo 1:

- Problema (T): Reconocer las frutas en la imagen
- Experiencia (E): ?



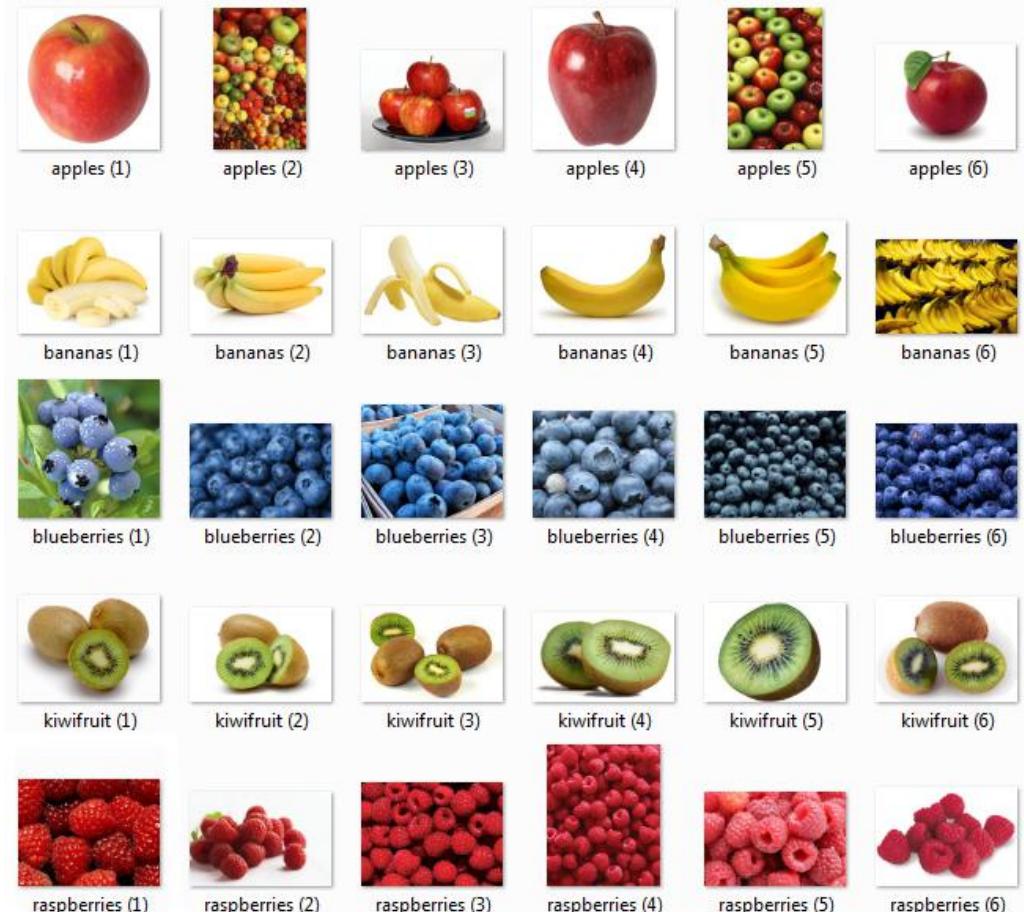
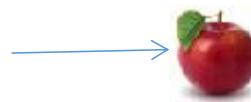
Representación de la experiencia (E)

Ejemplo 1 :

- Problema (T): Reconocer las frutas en la imagen
- Experiencia (E):

Extracción de características a partir de los píxeles de la imagen.

255	0	137	137	137	137	0
0	128	255	128	137	255	137
128	0	0	64	128	64	64
128	128	0	255	137	255	0
0	255	128	137	137	137	0
128	137	137	137	0	255	64
255	128	128	128	128	64	64



Representación de la experiencia (E)

Ejemplo 2:

- Problema (T): Realizar estudio de crédito



Representación de la experiencia (E)

Ejemplo 2:

- Problema (T): Realizar estudio de crédito.
- Experiencia (E):

$$\vec{x} = [x_1, x_2, \dots, x_n] \in \Re^n$$

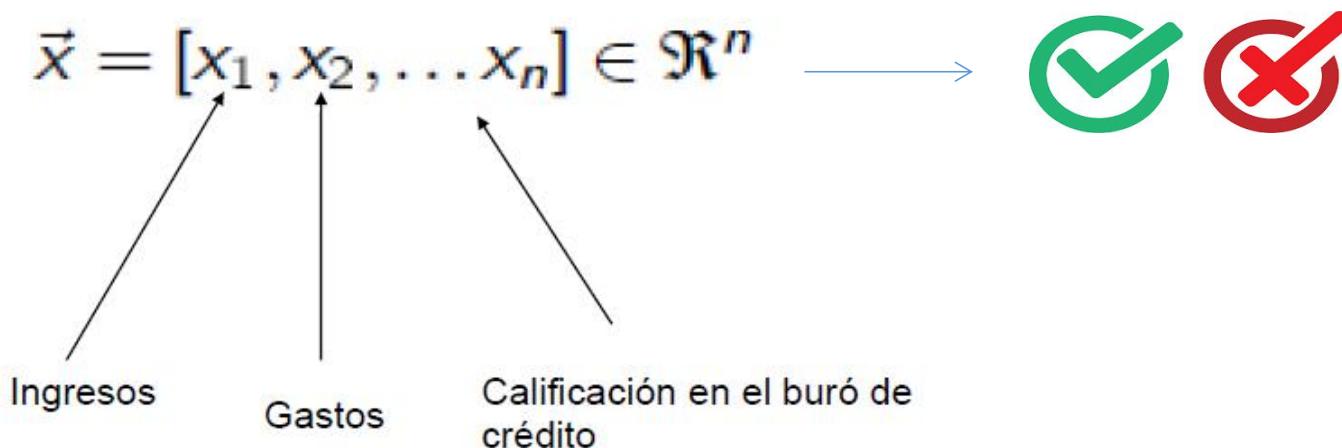
Ingresos Gastos Calificación en el buró de crédito



Representación de la experiencia (E)

Ejemplo 2:

- Problema (T): Realizar estudio de crédito.
- Experiencia (E):

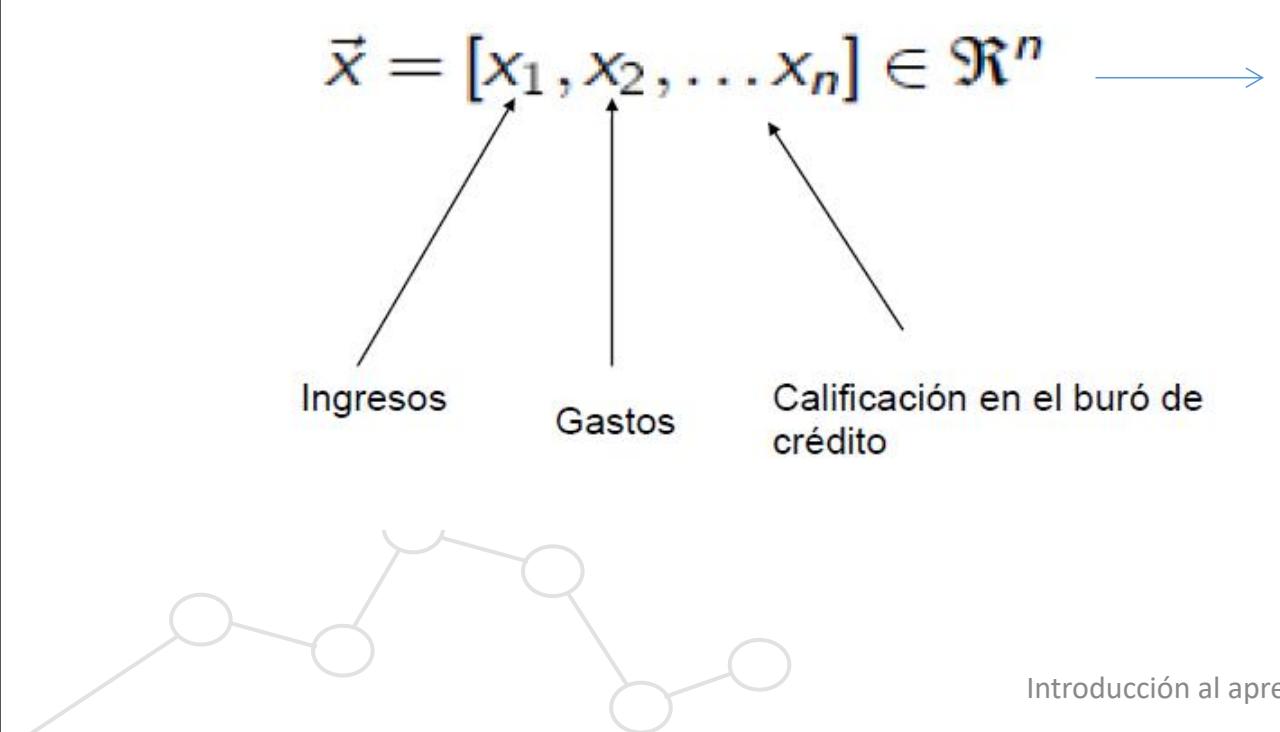


Representación de la experiencia (E)

Ejemplo 2:

- Problema (T): Realizar estudio de crédito.
 - Experiencia (E):

Es este tipo de problemas usualmente se tienen las características, no se requiere el proceso de **extracción**, solo **selección**.



\vec{x}	y
4.9	3.0
4.7	3.2
4.6	3.1
5.0	3.6
5.4	3.9
4.6	3.4
5.0	3.4
4.4	2.9

Representación de la experiencia (E)

Ejemplo 3:

- Problema (T): Determinar si un correo electrónico es no deseado SPAM
- Experiencia (E): Miles de correos electrónicos categorizados como **spam y no spam**.



Representación de la experiencia (E)

Ejemplo 3:

- Problema (T): Determinar si un correo electrónico es no deseado SPAM
- Experiencia (E): Conjunto de palabras de correos SPAM y NO-SPAM

En este caso la **extracción de características** no es un problema trivial.



Primera aproximación al aprendizaje

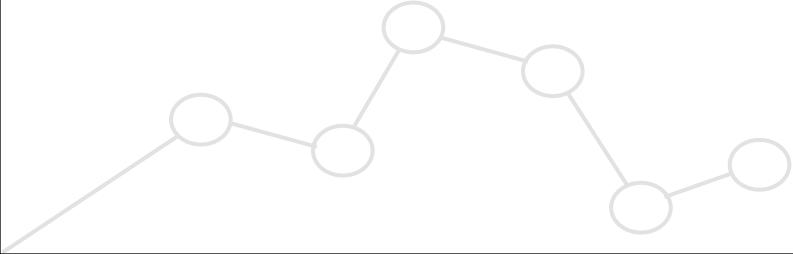
- Problema (T): Realizar estudio de crédito
- Experiencia (E): Atributos de clientes en el espacio numérico.

\vec{x}	y		
4.9	3.0	1.4	1
4.7	3.2	1.3	0
4.6	3.1	1.5	0
5.0	3.6	1.4	1
5.4	3.9	1.7	1
4.6	3.4	1.4	1
5.0	3.4	1.5	0
4.4	2.9	1.4	1

- Debemos encontrar un modelo M de la forma:

$$Y = F(X)$$

Tipos de aprendizaje



Introducción al aprendizaje automático



Aprendizaje

- Encontrar un modelo del problema basado en la **experiencia**.
- Como se mencionó la experiencia se debe presentar a la computadora codificada en un espacio numérico.
- La estructura más común es a través de un vector denominado **vector de características** o **patrón** de la forma:

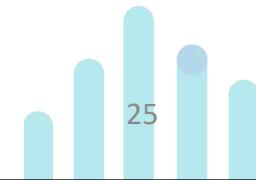
$$\vec{x} = [x_1, x_2, \dots, x_n]$$

- En tal caso la experiencia es un conjunto de instancias de x denominadas en común como **dataset**.

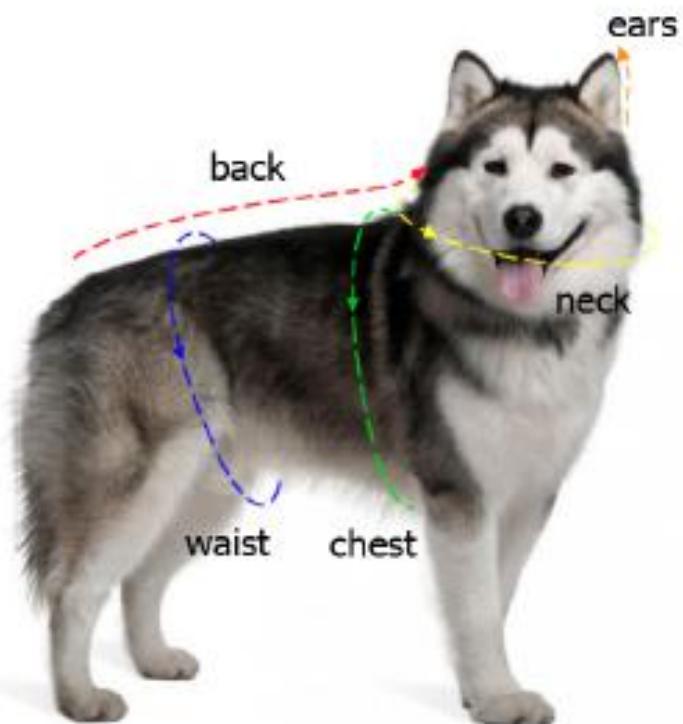
Aprendizaje

En general las tareas de aprendizaje se clasifican en :

- Aquellas donde se busca un modelo basado en información a priori de la variable de decisión.
- Aquellas donde el modelo debe inferir el valor de la variable de decisión sin un conocimiento previo.
- En el primer caso hablamos de **aprendizaje supervisado**.
- En el segundo caso hablamos de **aprendizaje no supervisado**



Aprendizaje



$$\vec{x} = \begin{matrix} 120 & 80 & 50 & 60 & 10 \end{matrix}$$

Aprendizaje

$$\vec{x} = \begin{array}{cccccc} \textcolor{red}{120} & \textcolor{green}{80} & \textcolor{yellow}{50} & \textcolor{teal}{60} & \textcolor{orange}{10} & \text{Malamute} \end{array}$$



$$\vec{x} = \begin{array}{cccccc} \textcolor{red}{30} & \textcolor{green}{20} & \textcolor{yellow}{10} & \textcolor{teal}{5} & \textcolor{orange}{5} & \text{Chihuahua} \end{array}$$



$$\vec{x} = \begin{array}{cccccc} \textcolor{red}{100} & \textcolor{green}{60} & \textcolor{yellow}{40} & \textcolor{teal}{50} & \textcolor{orange}{10} & \text{Pitbull} \end{array}$$



$$\vec{x} = \begin{array}{cccccc} \textcolor{red}{80} & \textcolor{green}{50} & \textcolor{yellow}{40} & \textcolor{teal}{45} & \textcolor{orange}{15} & \text{Bull dog} \end{array}$$

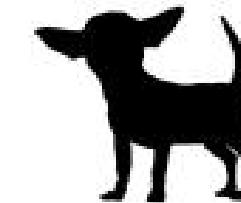


Aprendizaje

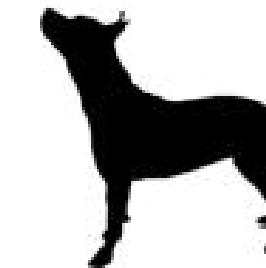
$$\vec{x} = \begin{array}{cccccc} \text{red} & \text{green} & \text{yellow} & \text{blue} & \text{orange} & \text{?} \\ 120 & 80 & 50 & 60 & 10 & \end{array}$$



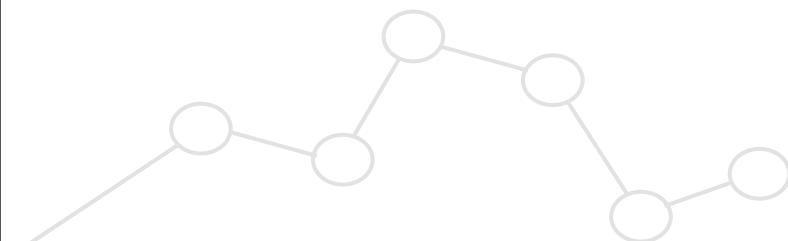
$$\vec{x} = \begin{array}{cccccc} \text{red} & \text{green} & \text{yellow} & \text{blue} & \text{orange} & \text{?} \\ 30 & 20 & 10 & 5 & 5 & \end{array}$$



$$\vec{x} = \begin{array}{cccccc} \text{red} & \text{green} & \text{yellow} & \text{blue} & \text{orange} & \text{?} \\ 100 & 60 & 40 & 50 & 10 & \end{array}$$



$$\vec{x} = \begin{array}{cccccc} \text{red} & \text{green} & \text{yellow} & \text{blue} & \text{orange} & \text{?} \\ 80 & 50 & 40 & 45 & 15 & \end{array}$$



Aprendizaje

Supervised Learning



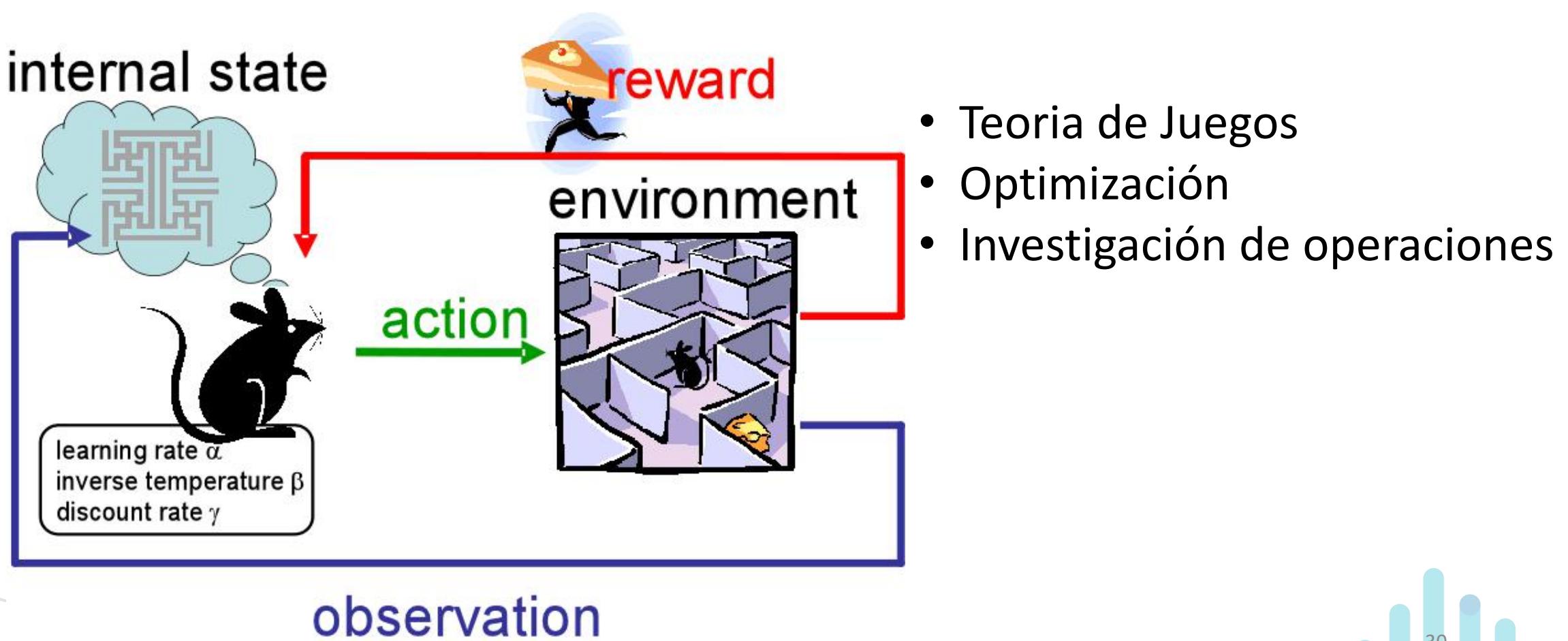
Unsupervised Learning

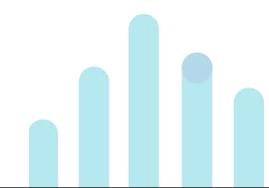
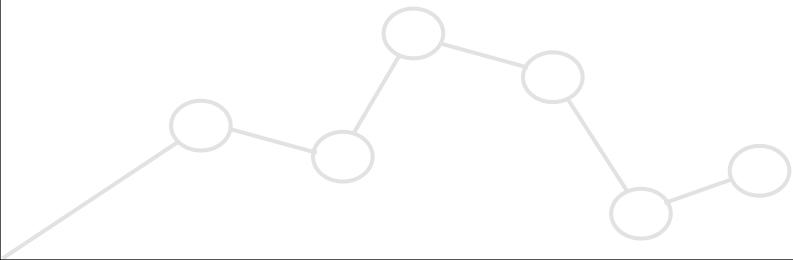
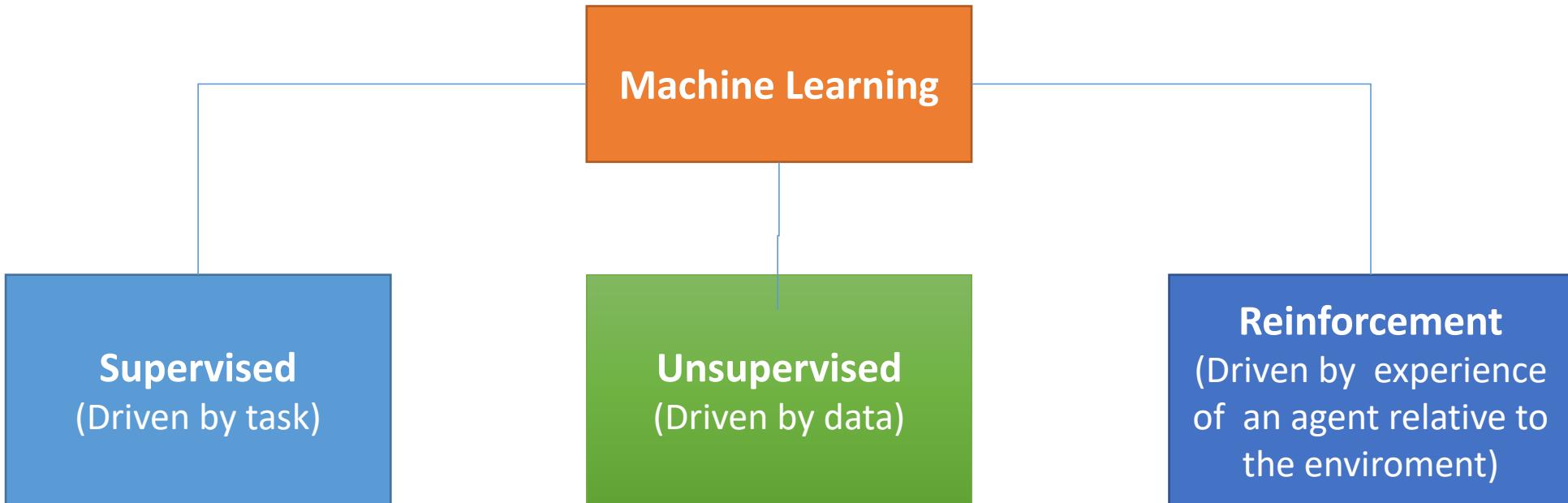


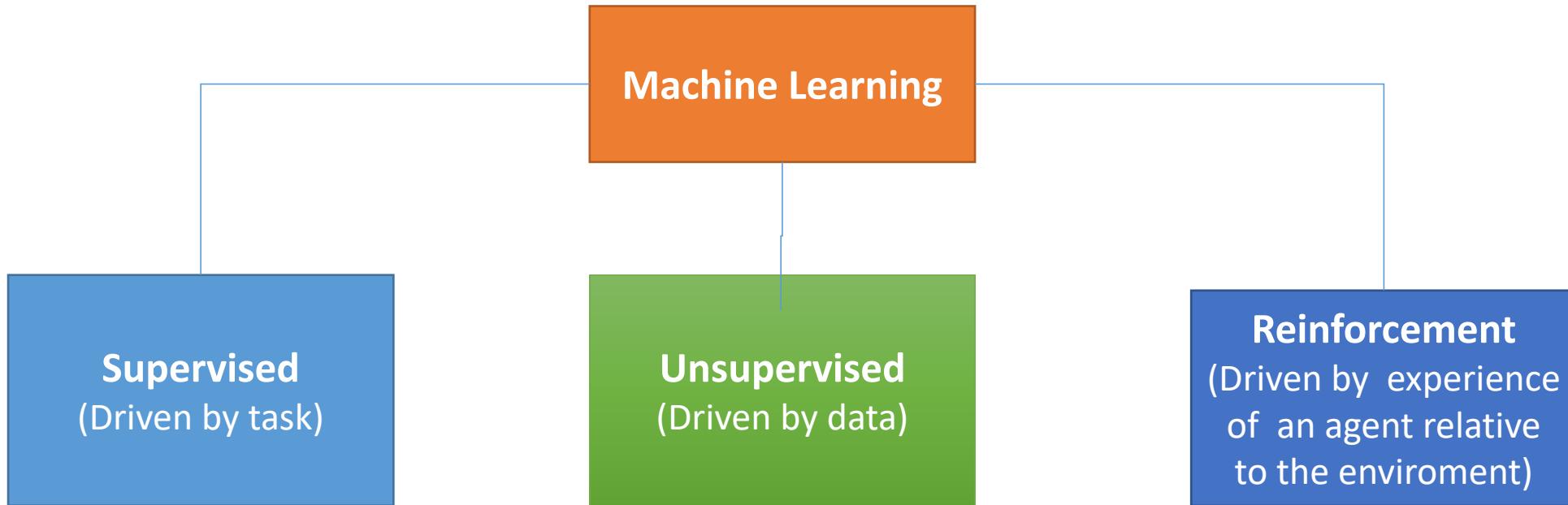
Introducción al aprendizaje automático



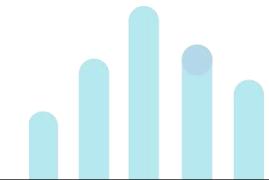
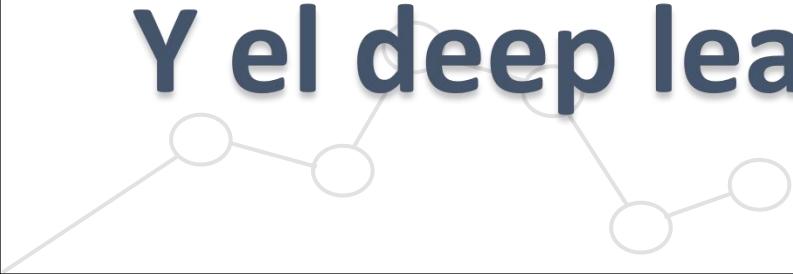
Otros tipos de aprendizaje



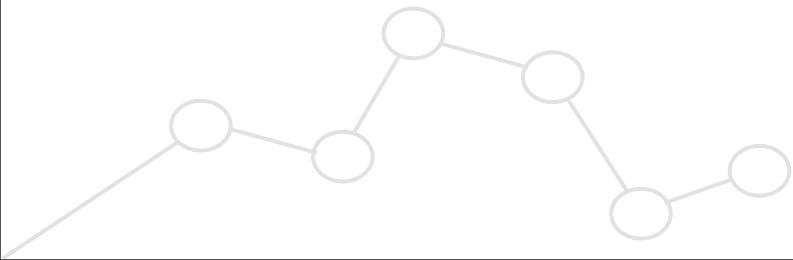
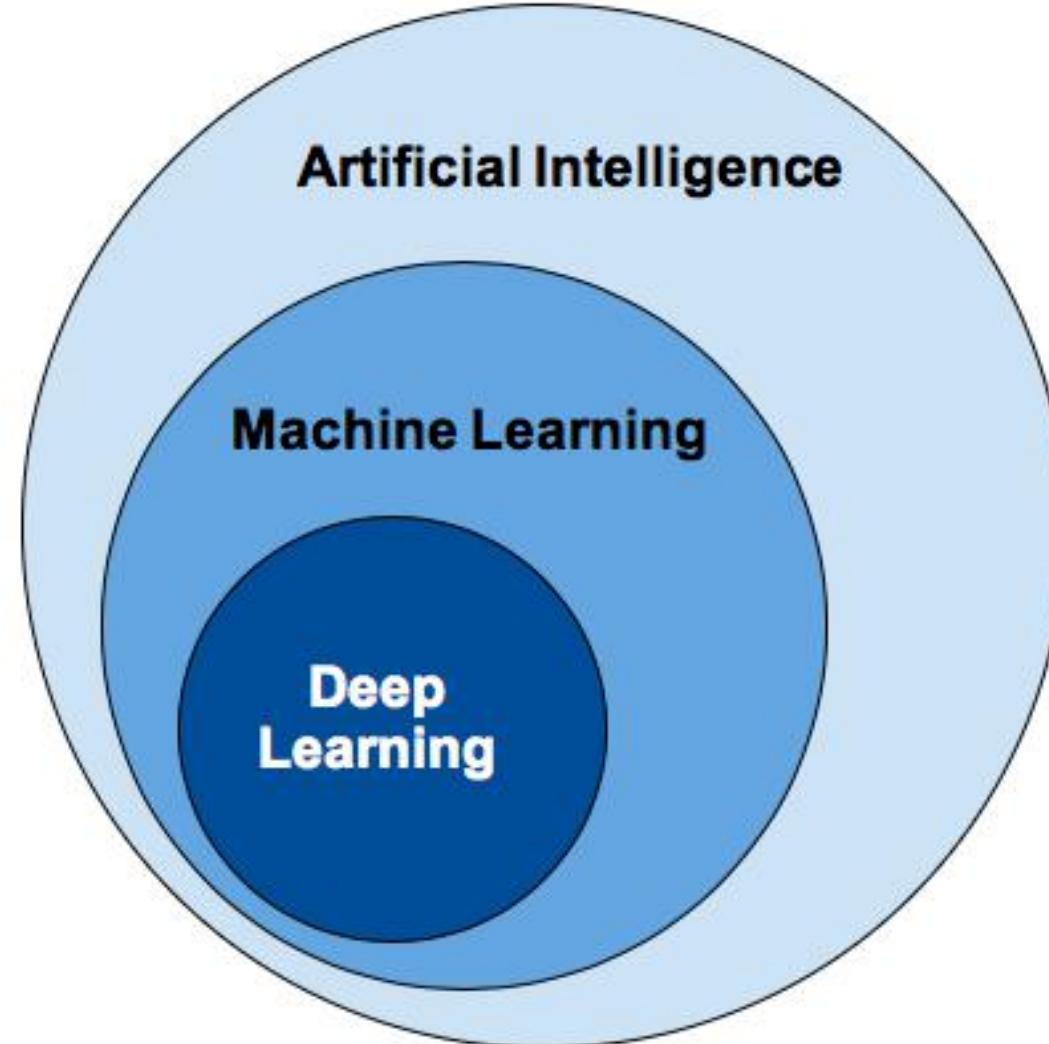




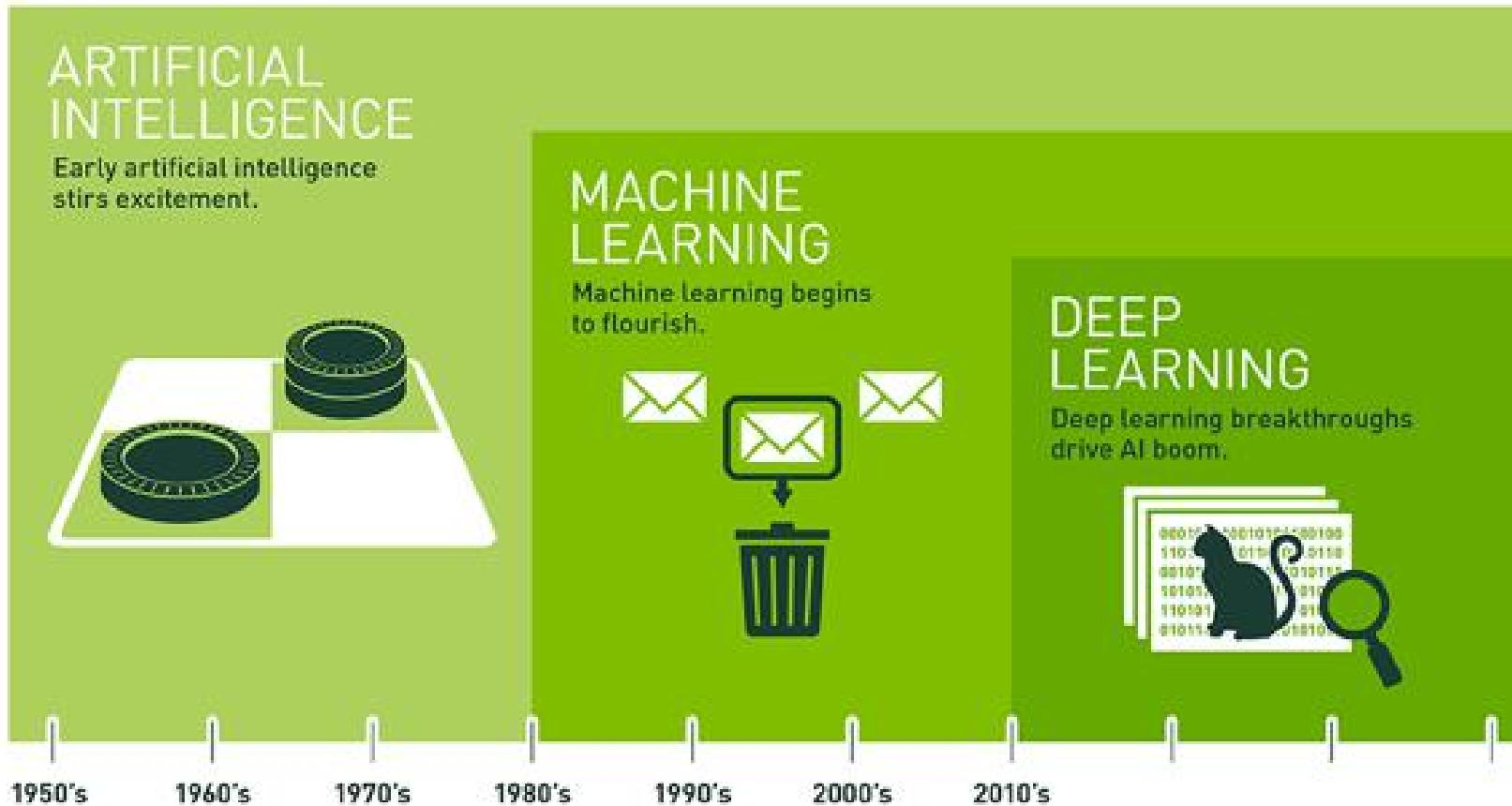
Y el deep learning?



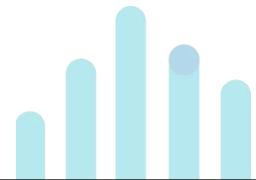
Artificial Intelligence, Machine Learning and Deep Learning



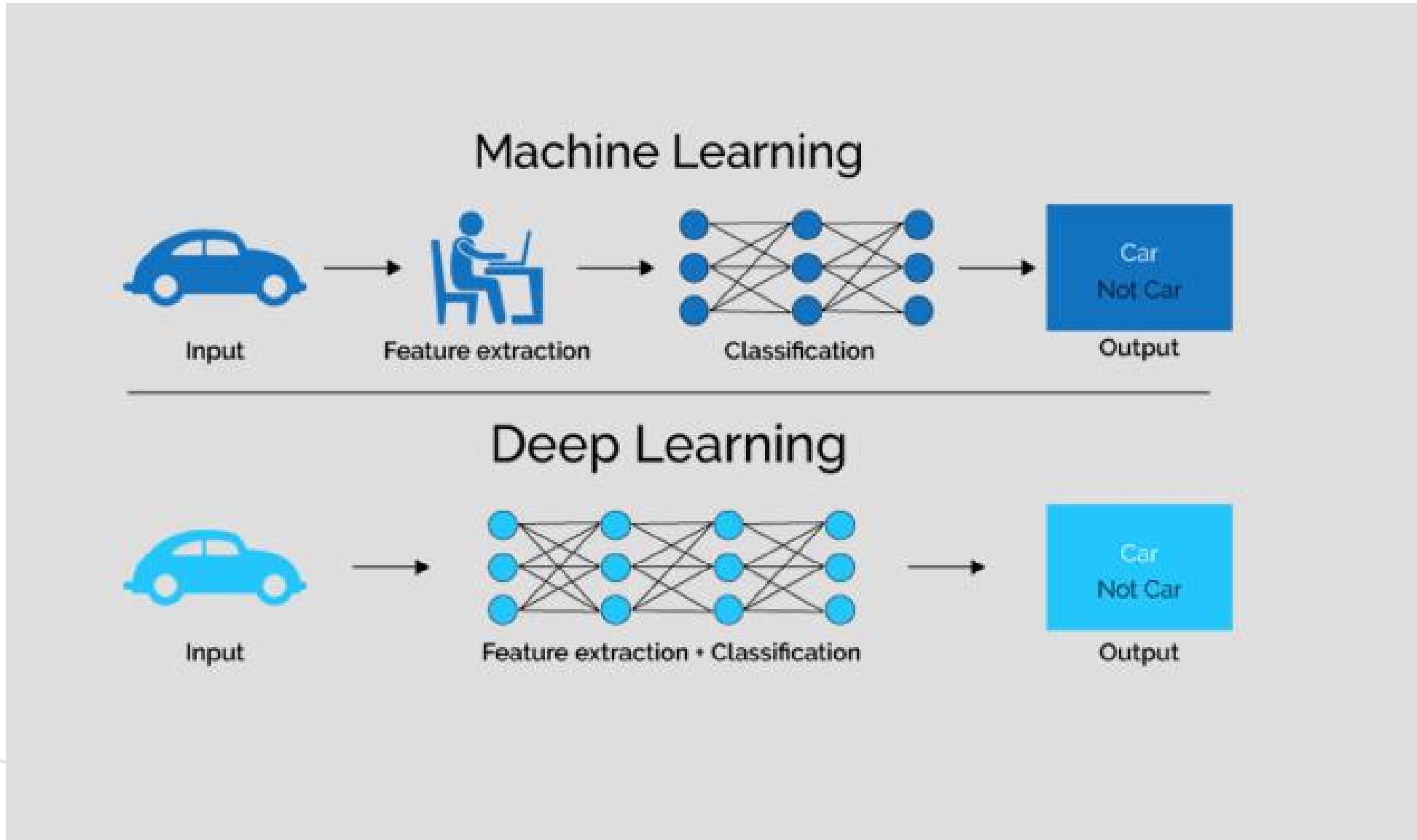
Evolution



Since an early flush of optimism in the 1950s, smaller subsets of artificial intelligence – first machine learning, then deep learning, a subset of machine learning – have created ever larger disruptions.

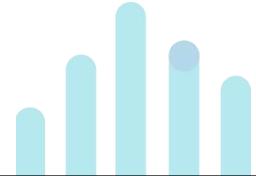
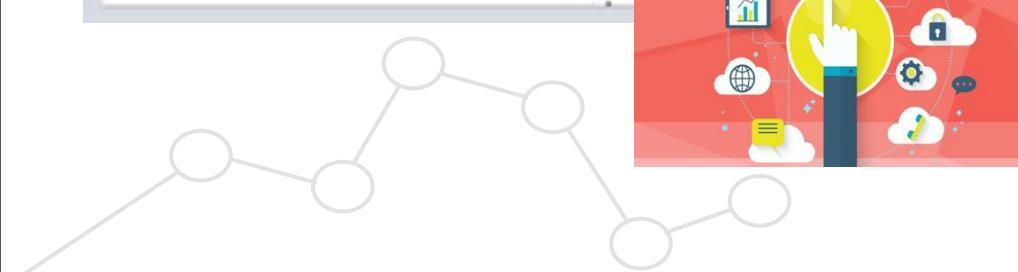


Machine Learning vs. Deep Learning

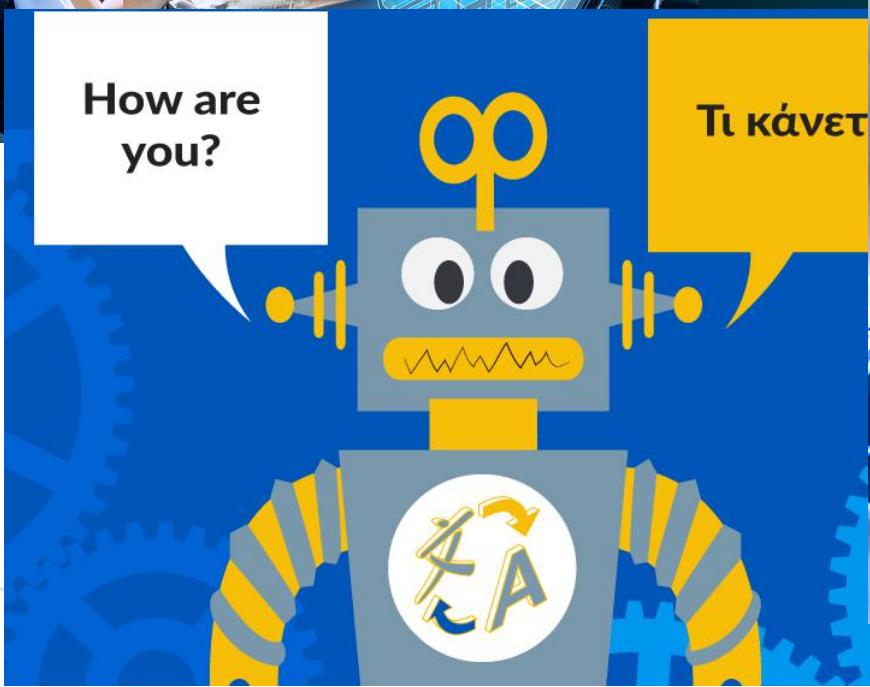


Common Machine Learning Applications

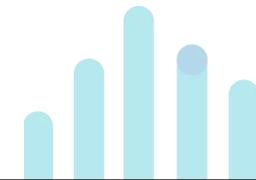
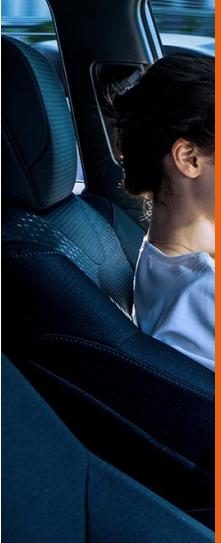
Retail	Marketing	Healthcare	Telco	Finance
<ul style="list-style-type: none">• Demand forecasting• Supply chain optimization• Pricing optimization• Market segmentation and targeting• Recommendations	<ul style="list-style-type: none">• Recommendation engines & targeting• Customer 360• Click-stream analysis• Social media analysis• Ad optimization	<ul style="list-style-type: none">• Predicting Patient Disease Risk• Diagnostics and Alerts• Fraud	<ul style="list-style-type: none">• Customer churn• System log analysis• Anomaly detection• Preventative maintenance• Smart meter analysis	<ul style="list-style-type: none">• Risk Analytics• Customer 360• Fraud• Credit scoring



Deep Learning Applications



Deep Learning Applications



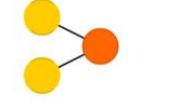
Neural Networks: The foundations of Deep Learning

- Input Cell
- Backfed Input Cell
- △ Noisy Input Cell
- Hidden Cell
- Probabilistic Hidden Cell
- △ Spiking Hidden Cell
- Capsule Cell
- Output Cell
- Match Input Output Cell
- Recurrent Cell
- Memory Cell
- △ Gated Memory Cell
- Kernel
- Convolution or Pool

A mostly complete chart of Neural Networks

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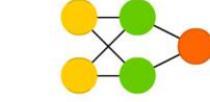
Perceptron (P)



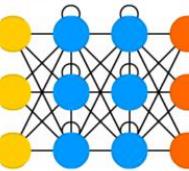
Feed Forward (FF)



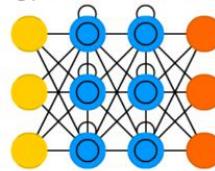
Radial Basis Network (RBF)



Recurrent Neural Network (RNN)



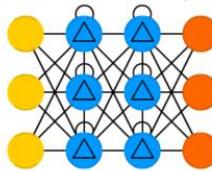
Long / Short Term Memory (LSTM)



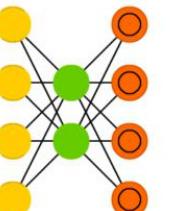
Deep Feed Forward (DFF)



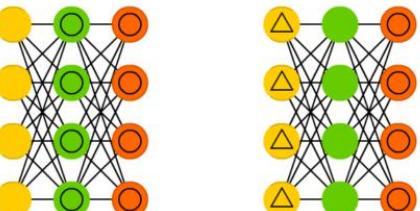
Gated Recurrent Unit (GRU)



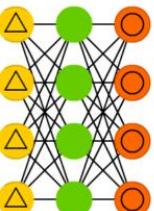
Auto Encoder (AE)



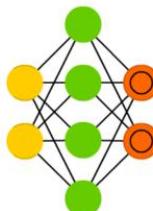
Variational AE (VAE)



Denoising AE (DAE)



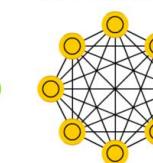
Sparse AE (SAE)



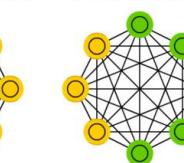
Markov Chain (MC)



Hopfield Network (HN)



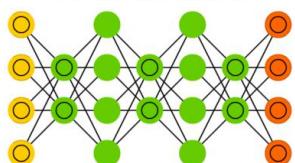
Boltzmann Machine (BM)



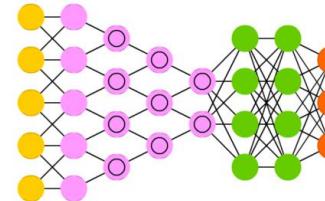
Restricted BM (RBM)



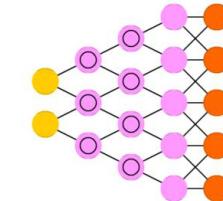
Deep Belief Network (DBN)



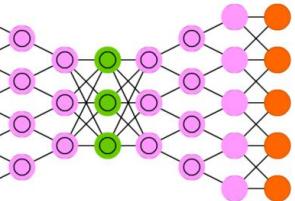
Deep Convolutional Network (DCN)



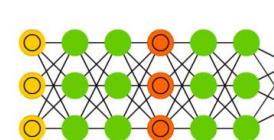
Deconvolutional Network (DN)



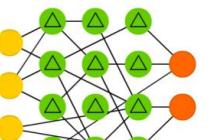
Deep Convolutional Inverse Graphics Network (DCIGN)



Generative Adversarial Network (GAN)



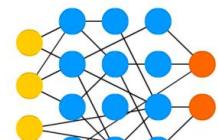
Liquid State Machine (LSM)



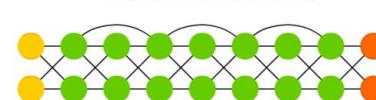
Extreme Learning Machine (ELM)



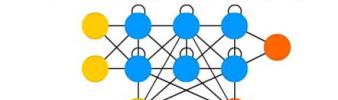
Echo State Network (ESN)



Deep Residual Network (DRN)



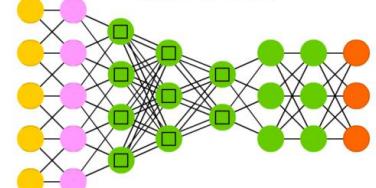
Differentiable Neural Computer (DNC)



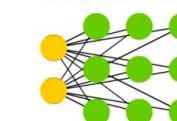
Neural Turing Machine (NTM)



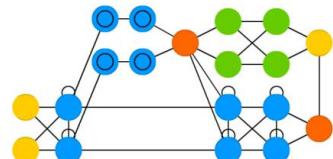
Capsule Network (CN)



Kohonen Network (KN)



Attention Network (AN)





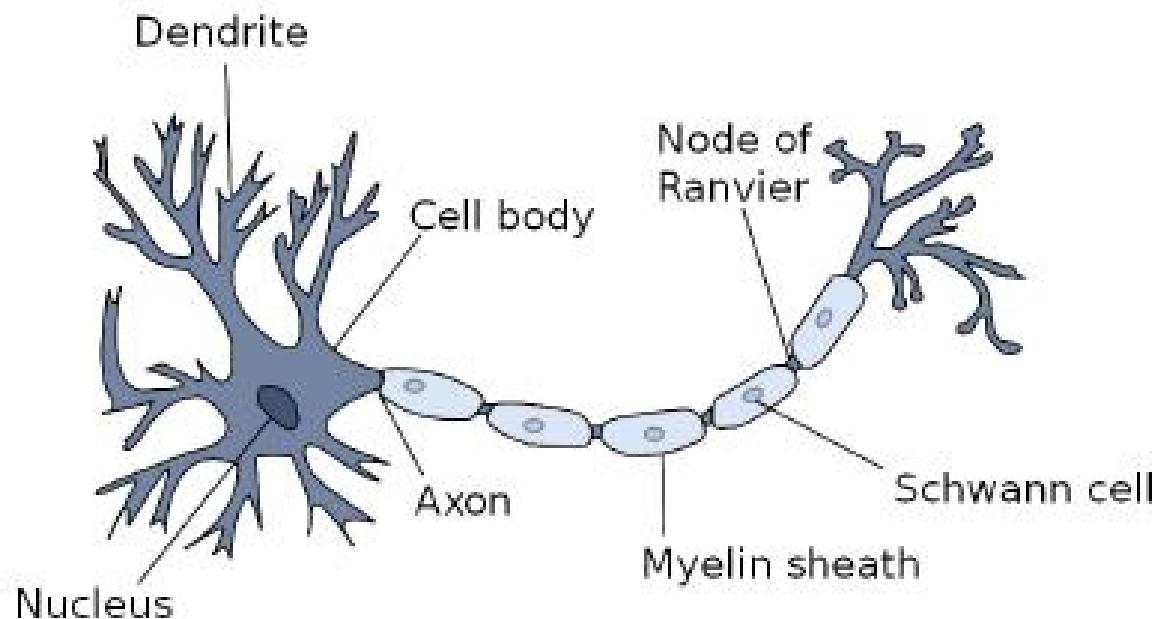
DMC ONLINE

#YoMeCapacitoEnCasa

Neural Networks and Deep Learning

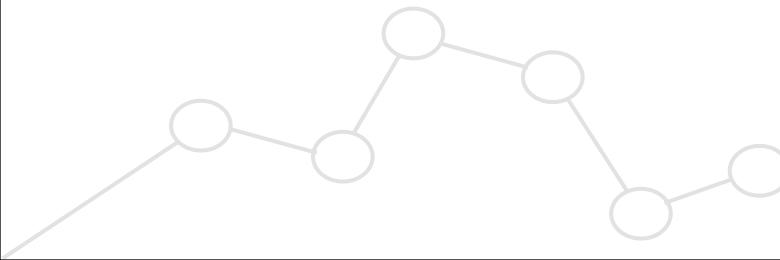
What is a neuron?

- Typically a neuron is defined as an information processing unit.



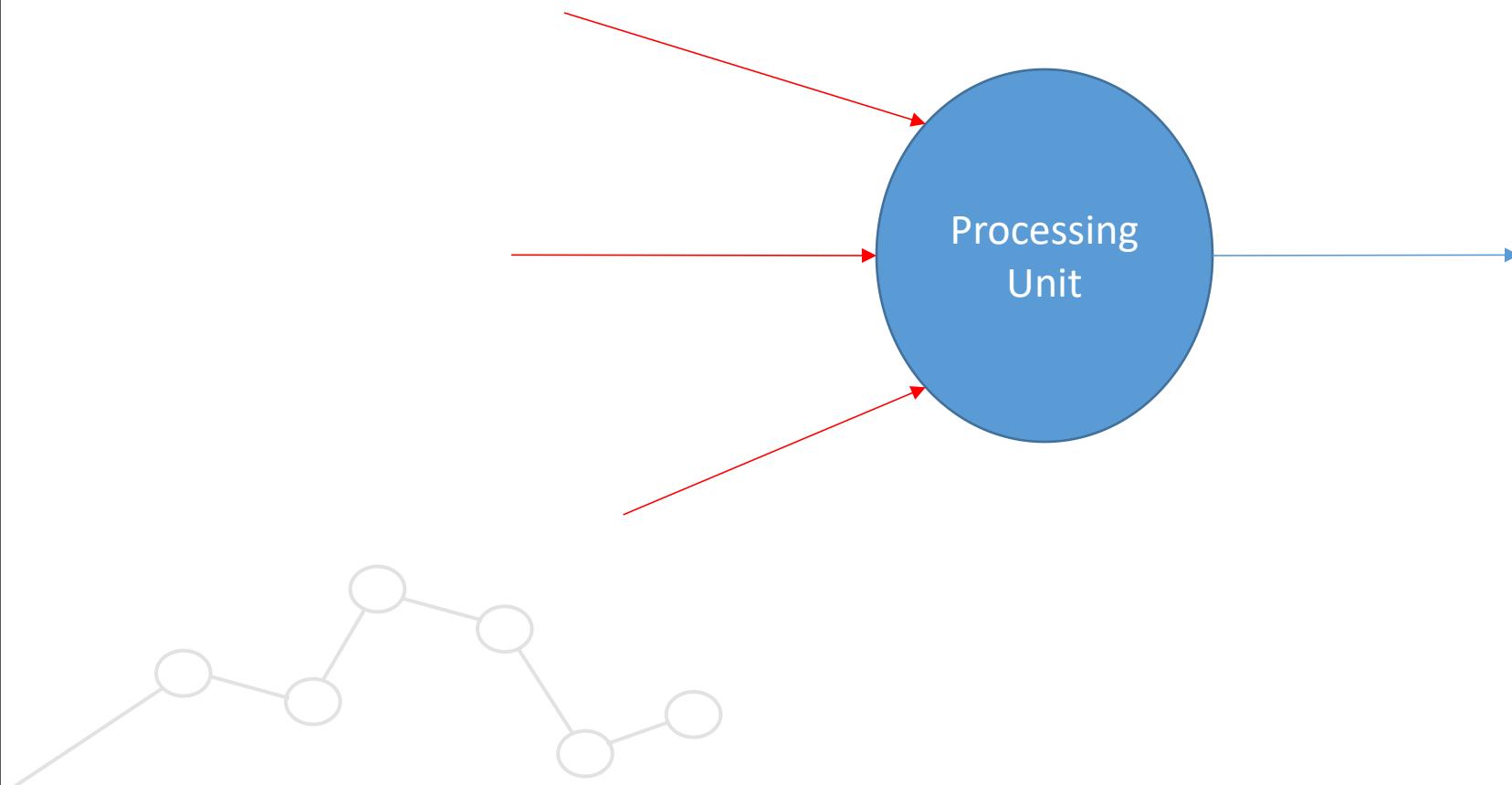
What is a neuron?

- From biology, a neuron processes electrochemical **input signals** which come from other neurons.
- The result of such processing is another electrochemical signal which is called **output**.
- This signal is transmitted to other neuron through the **axon**.



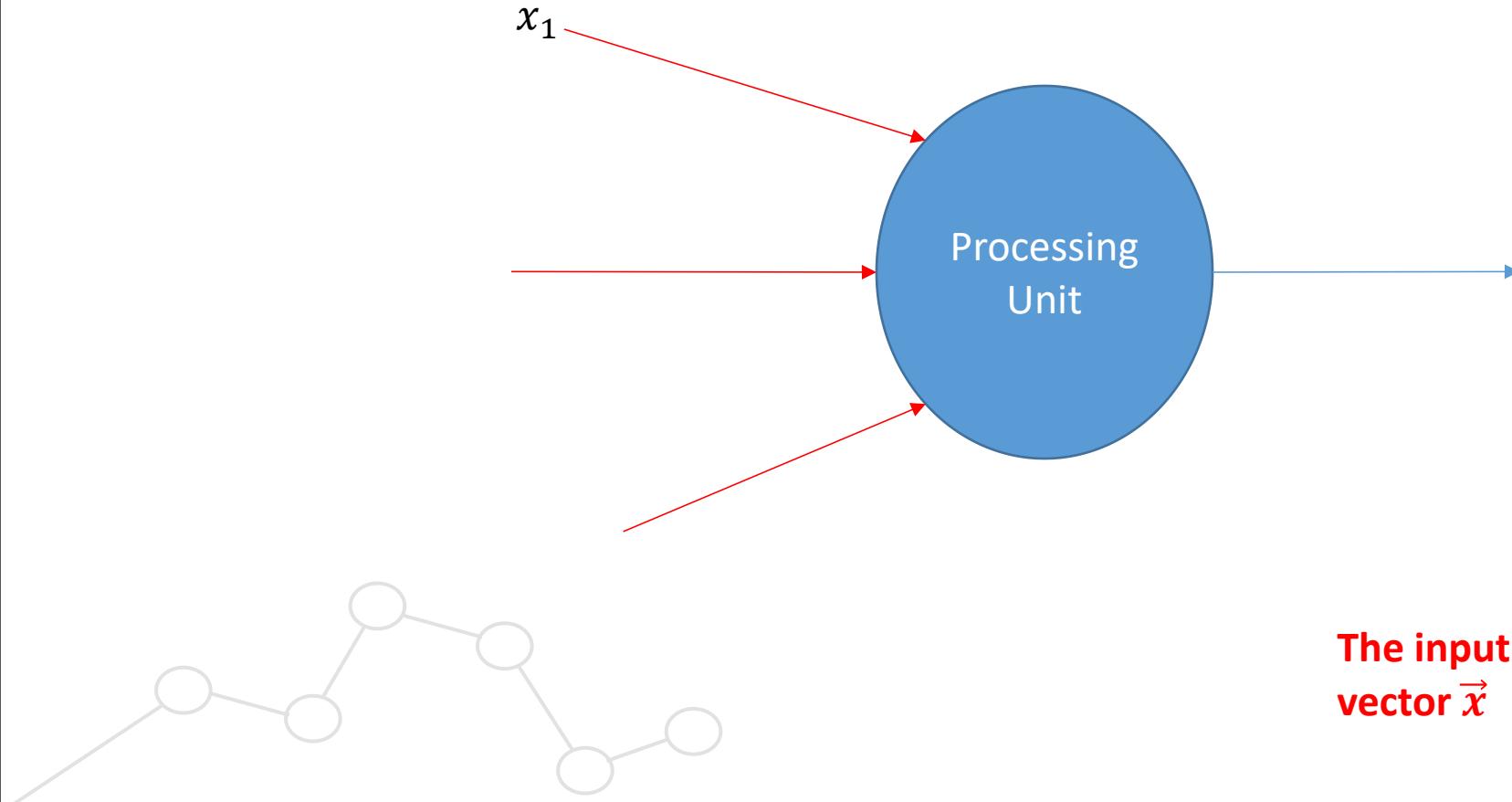
Artificial Neuron

- Inspired by biological neurons

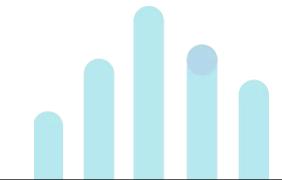


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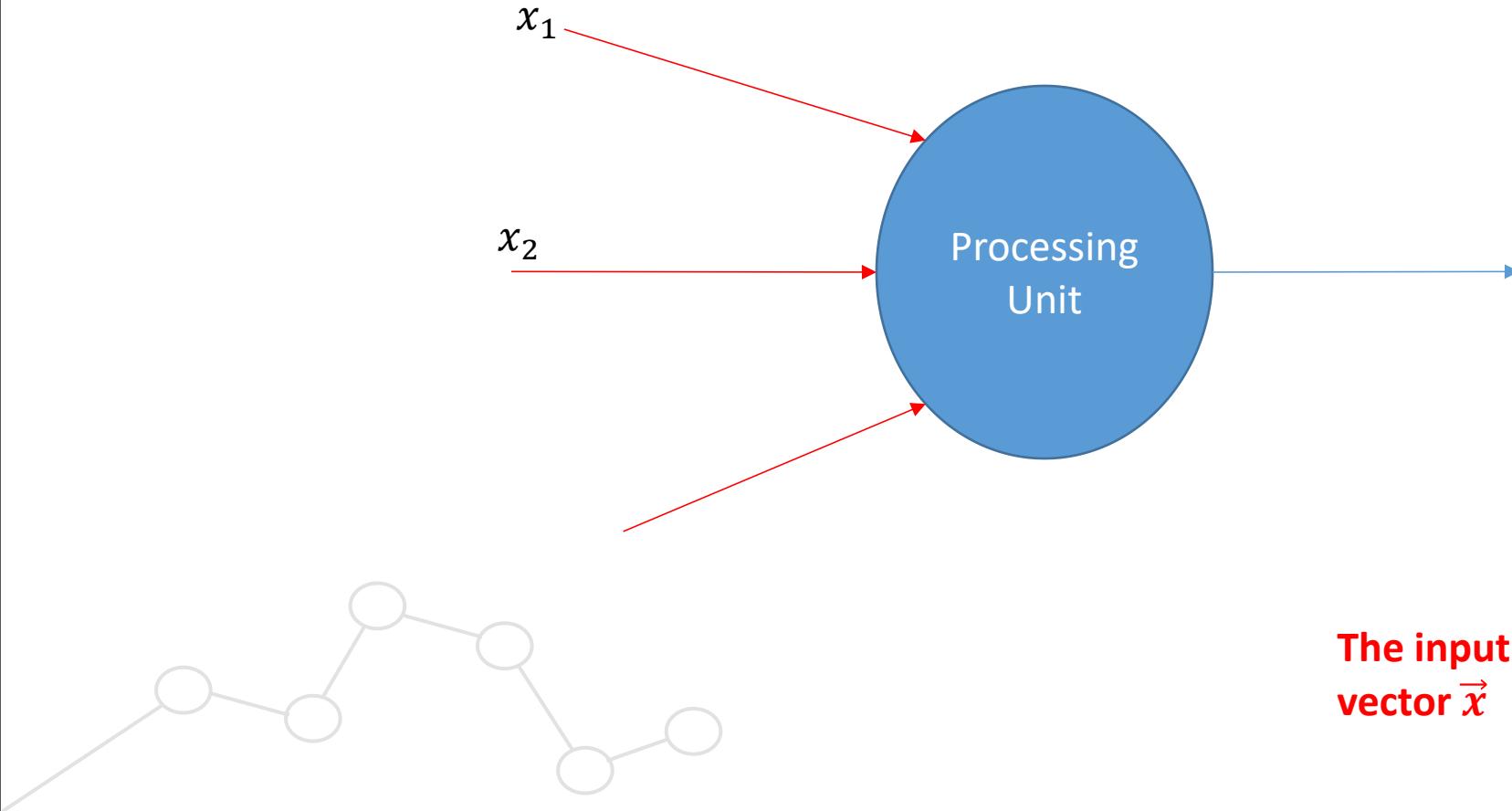


The input of a neuron is a
vector \vec{x}

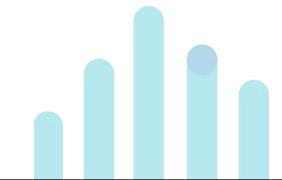


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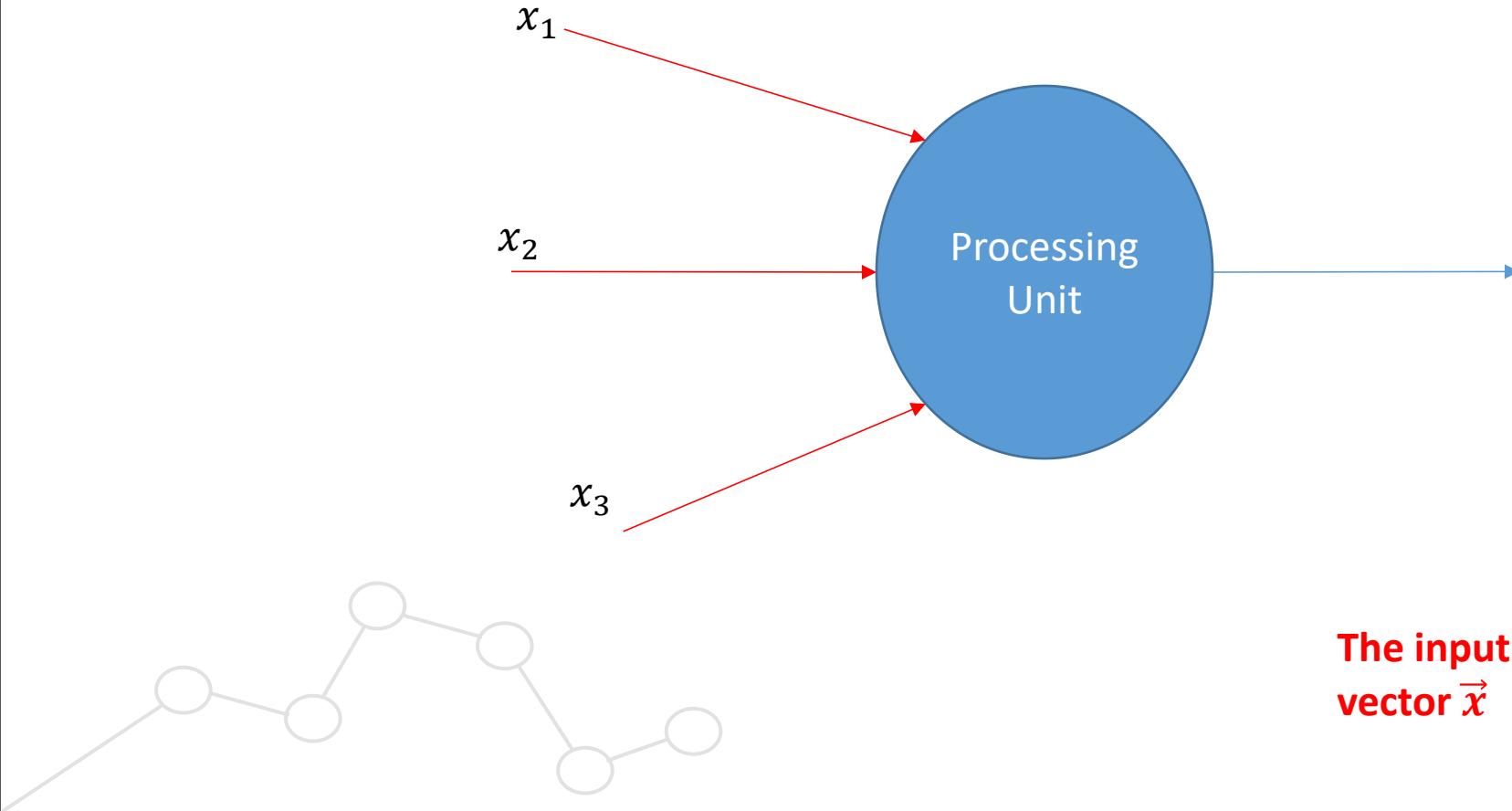


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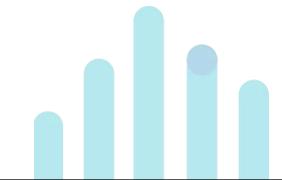


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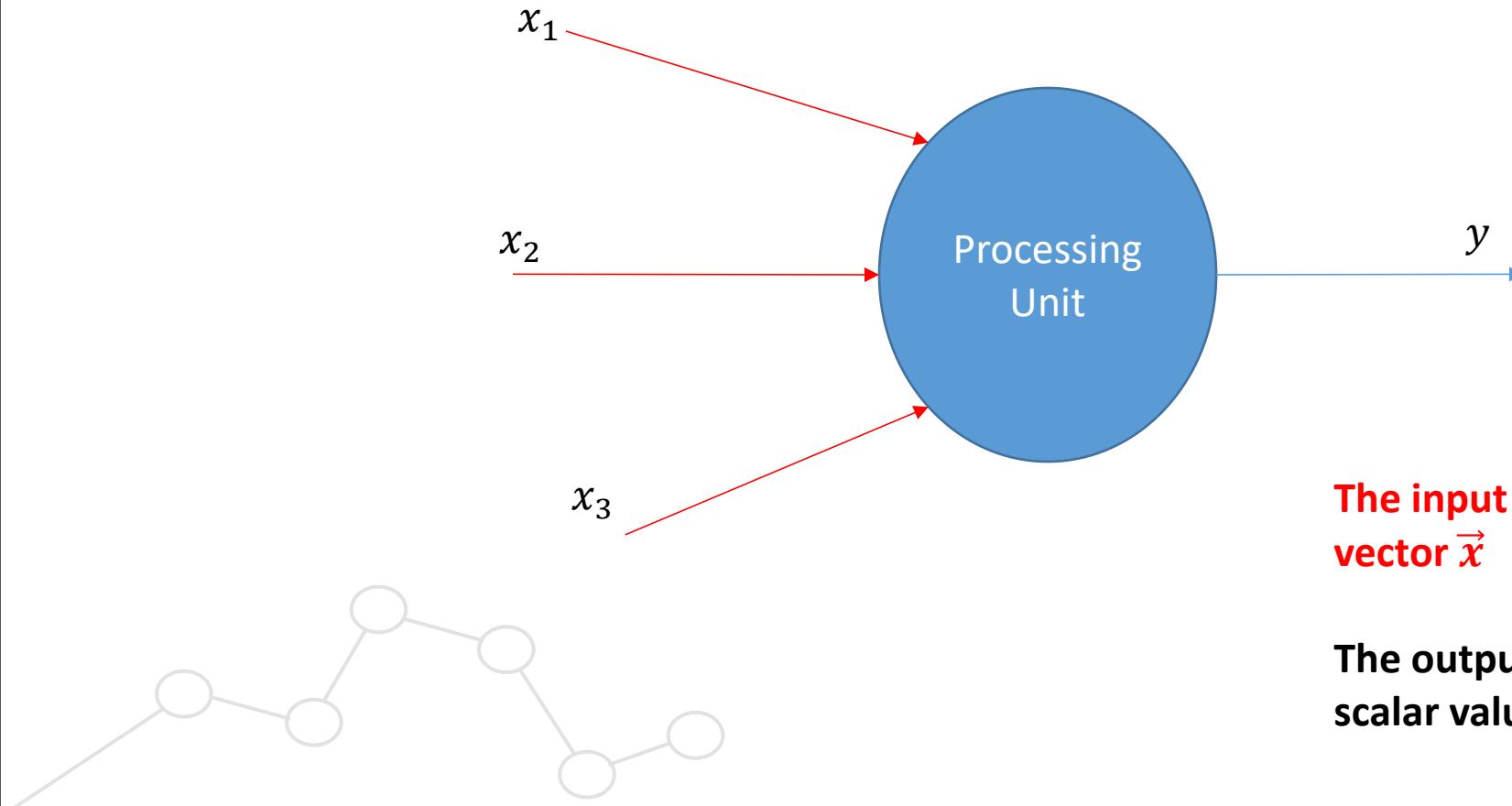


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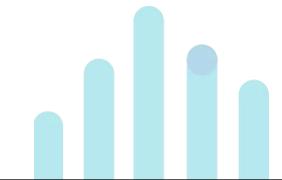
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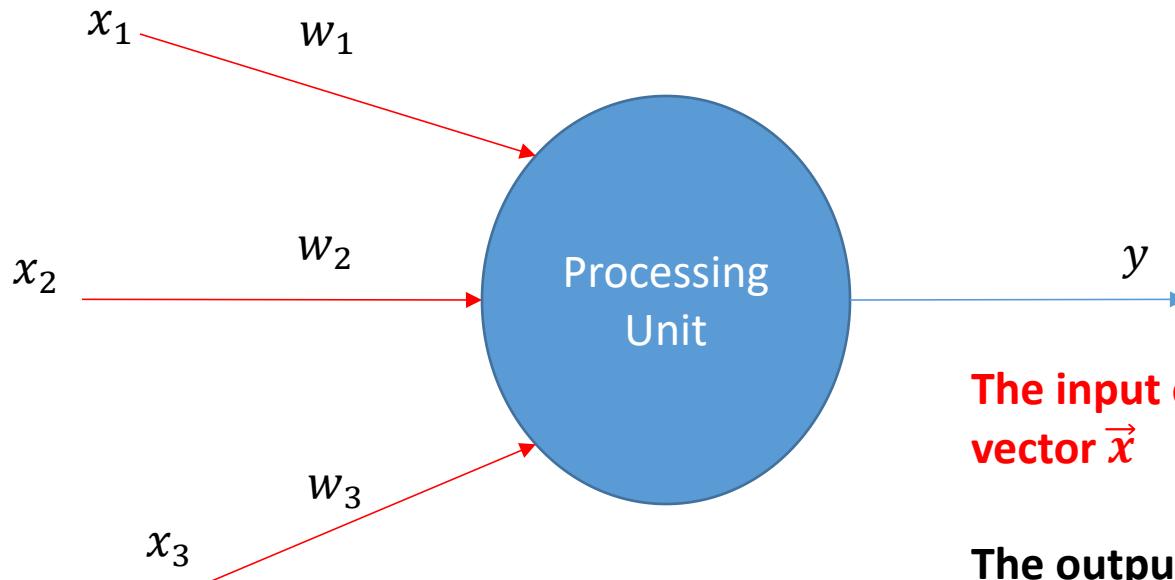
The input of a neuron is a vector \vec{x}

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Artificial Neuron

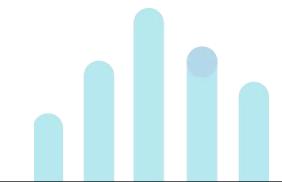
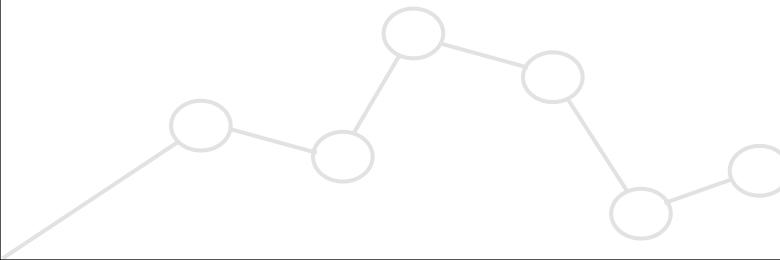
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The importance of a component of \vec{x} is weighted with a value w_i



Artificial Neuron

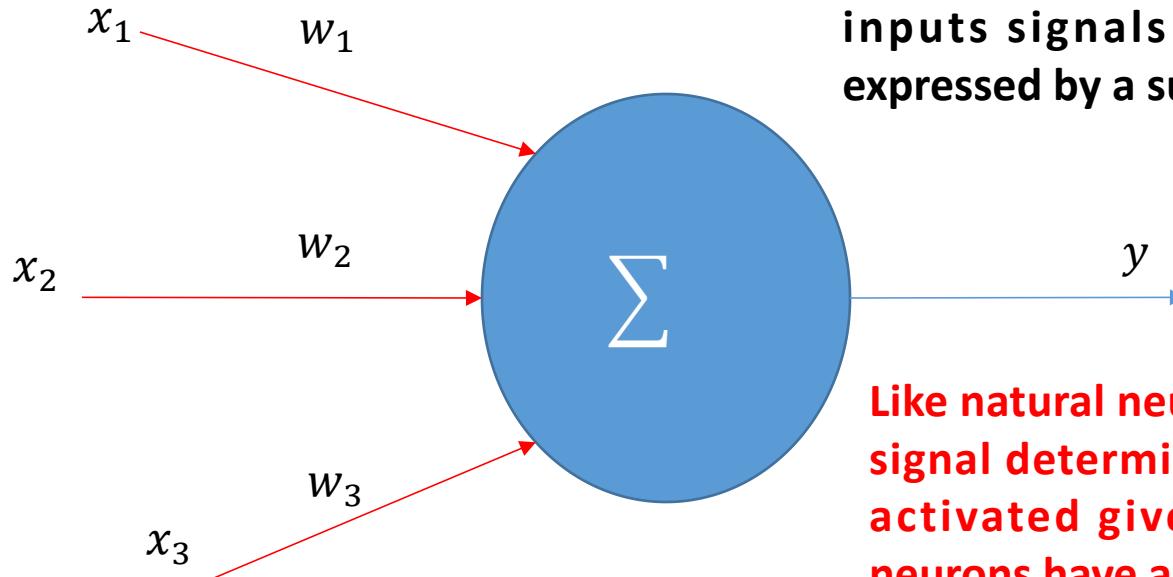
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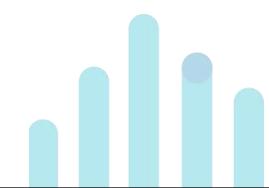
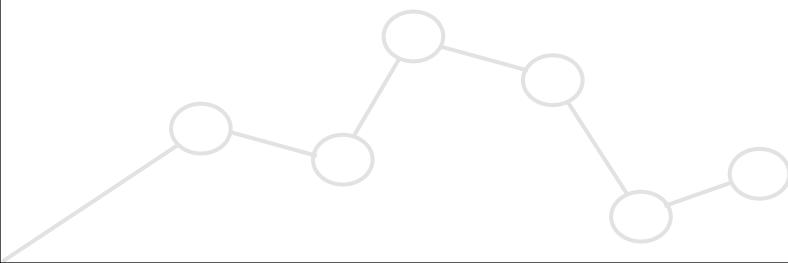
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The processing unit summarized the inputs signals (mathematically it is expressed by a sum).



Like natural neurons, the value of output signal determine if the neuron must be activated given its inputs. Thus, the neurons have an activation threshold.



Artificial Neuron

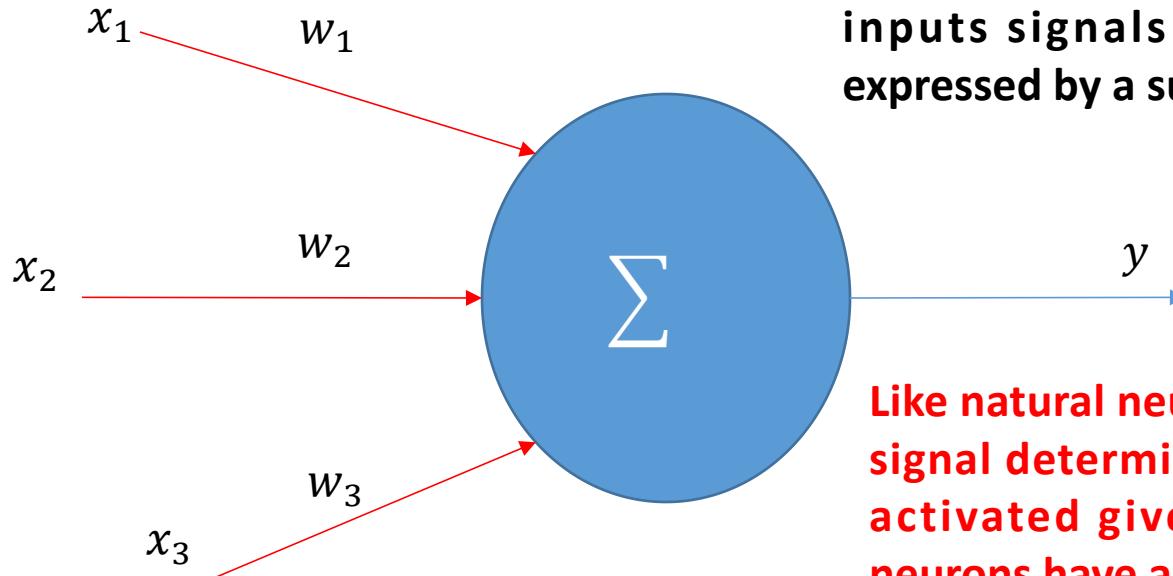
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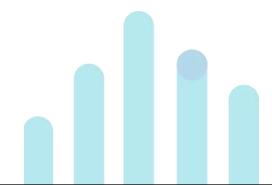
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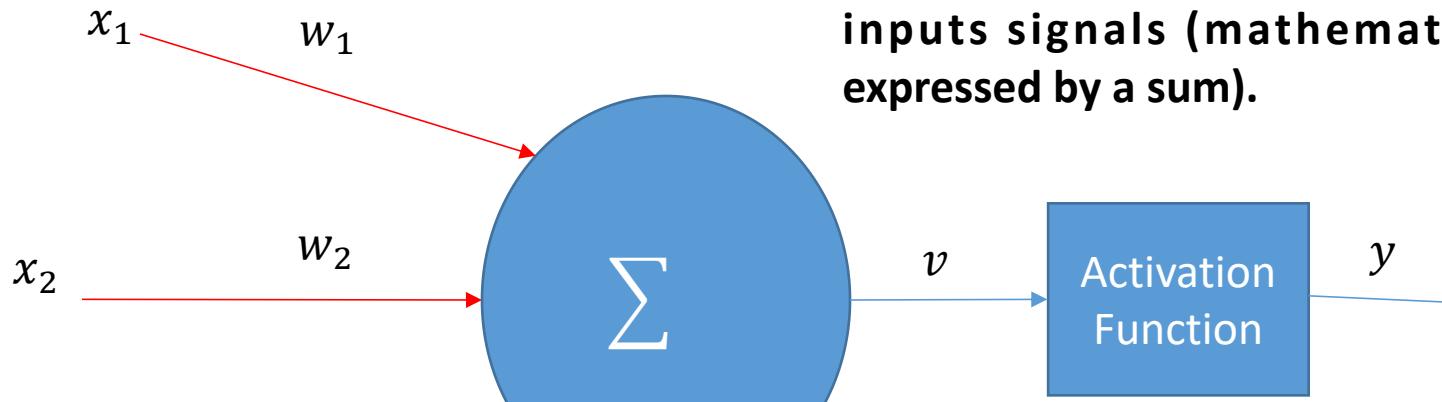
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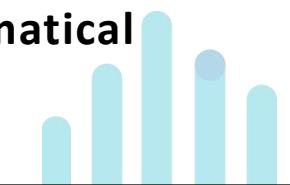
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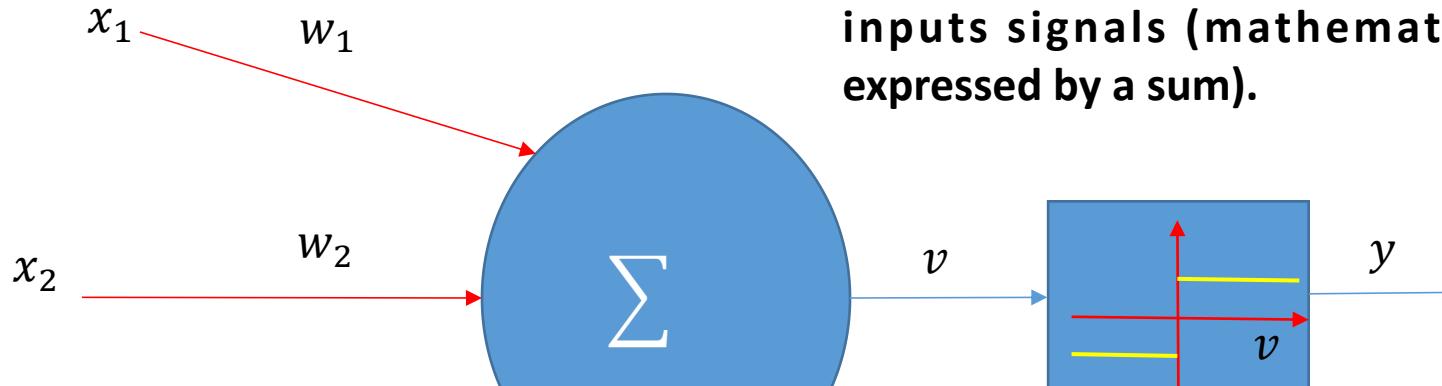
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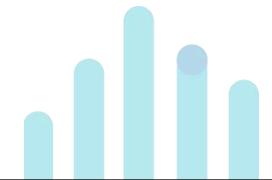
The output of the neuron is a scalar value

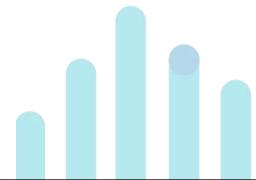
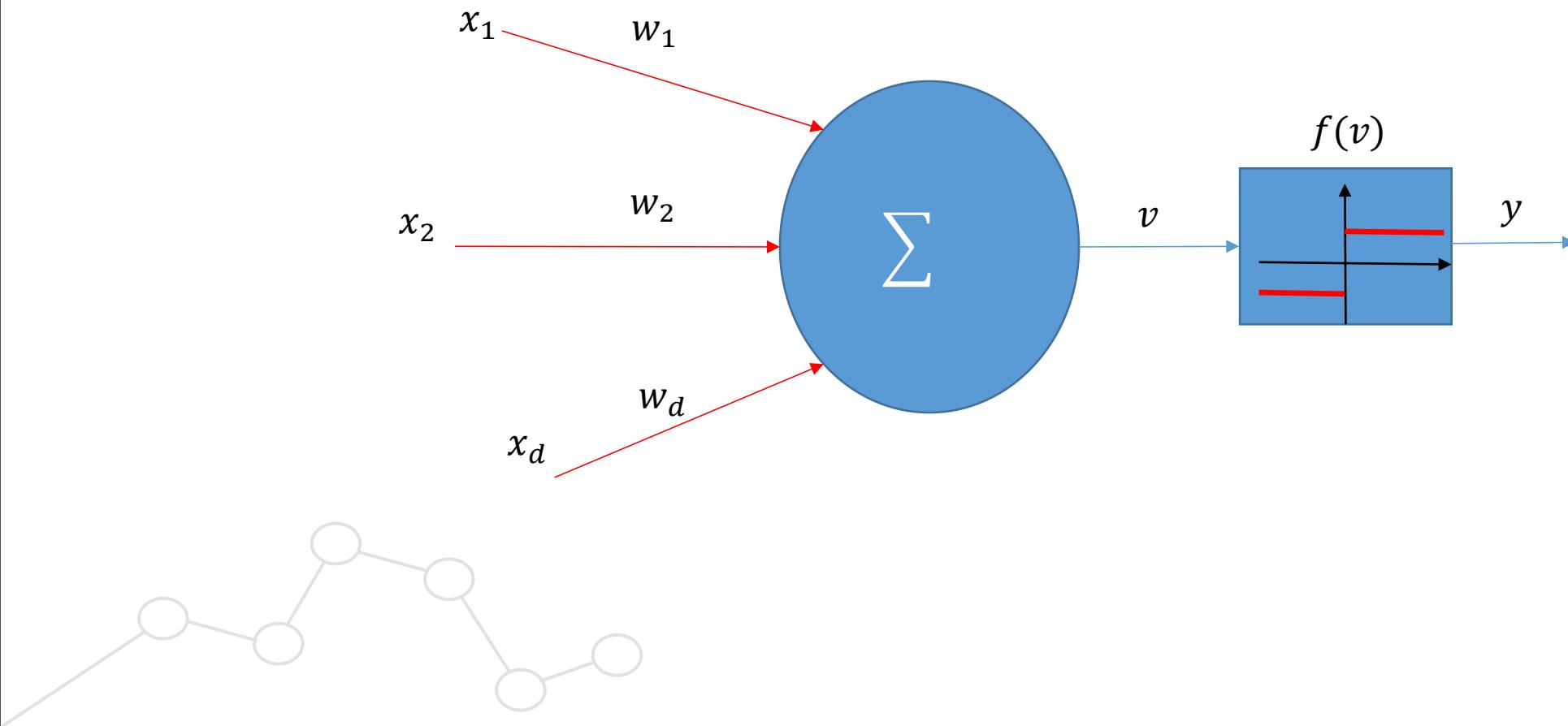
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What constraint(s) must be satisfied by the activation function?





Artificial Neuron

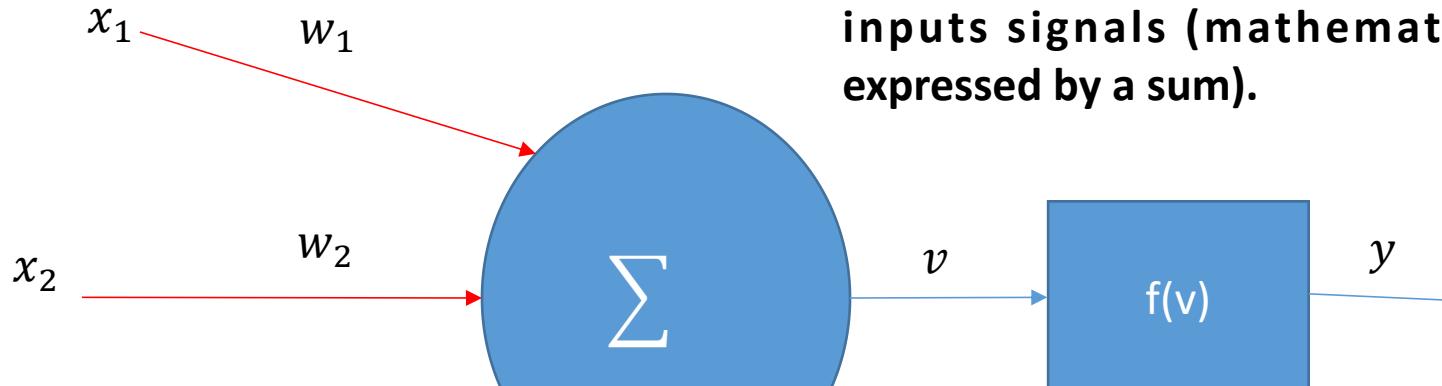
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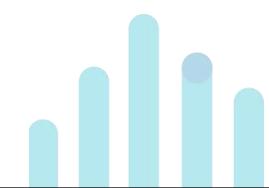
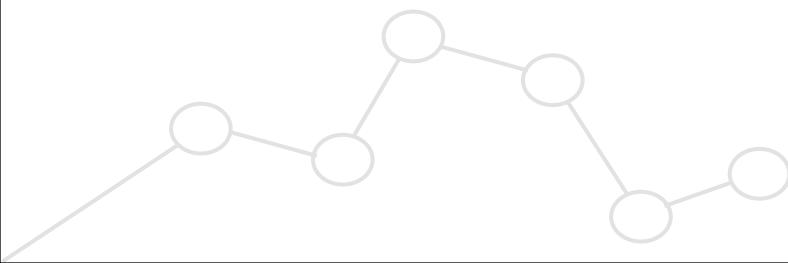
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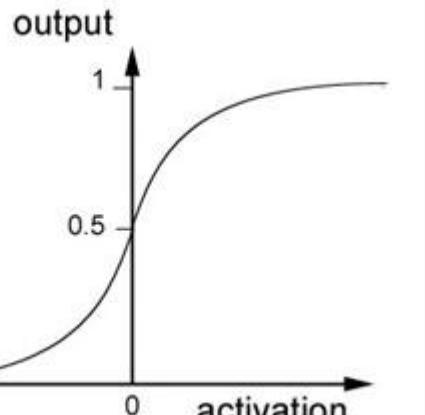
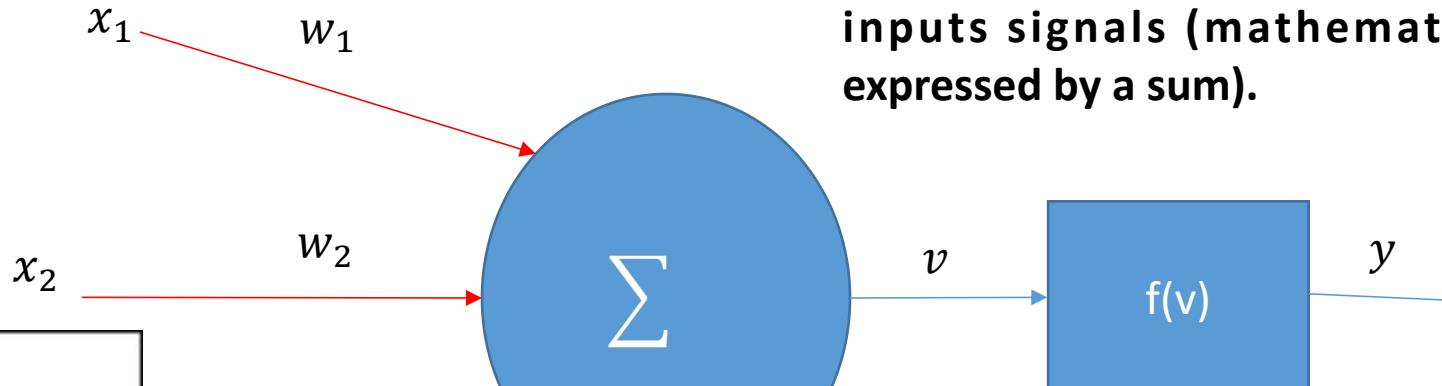
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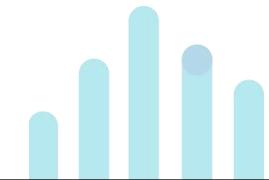
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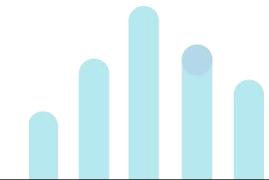
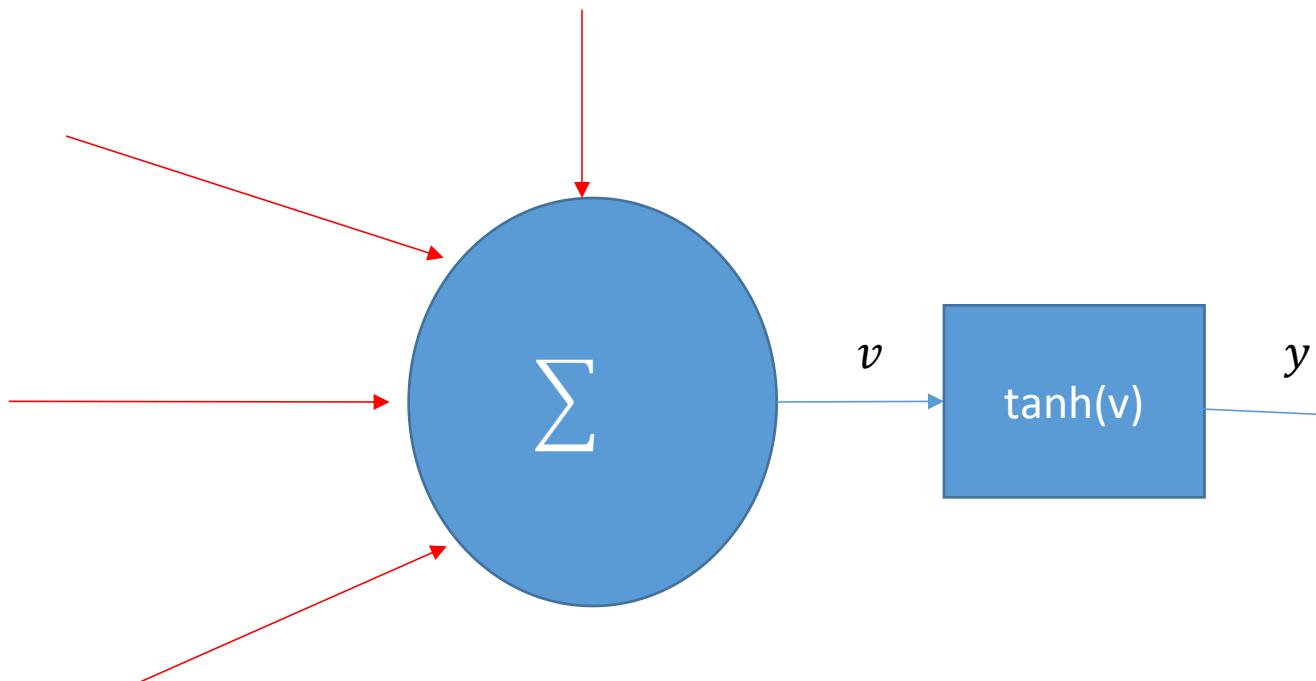
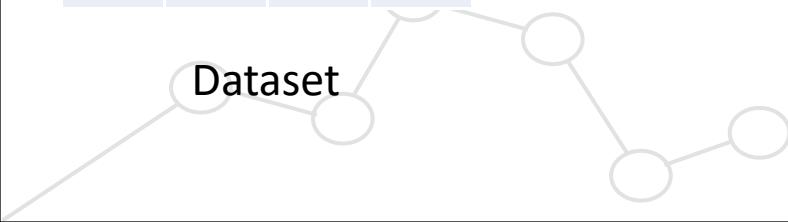
Why an artificial network is able to classify?



Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

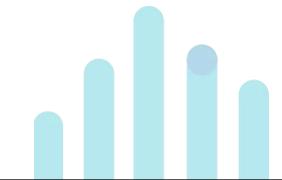
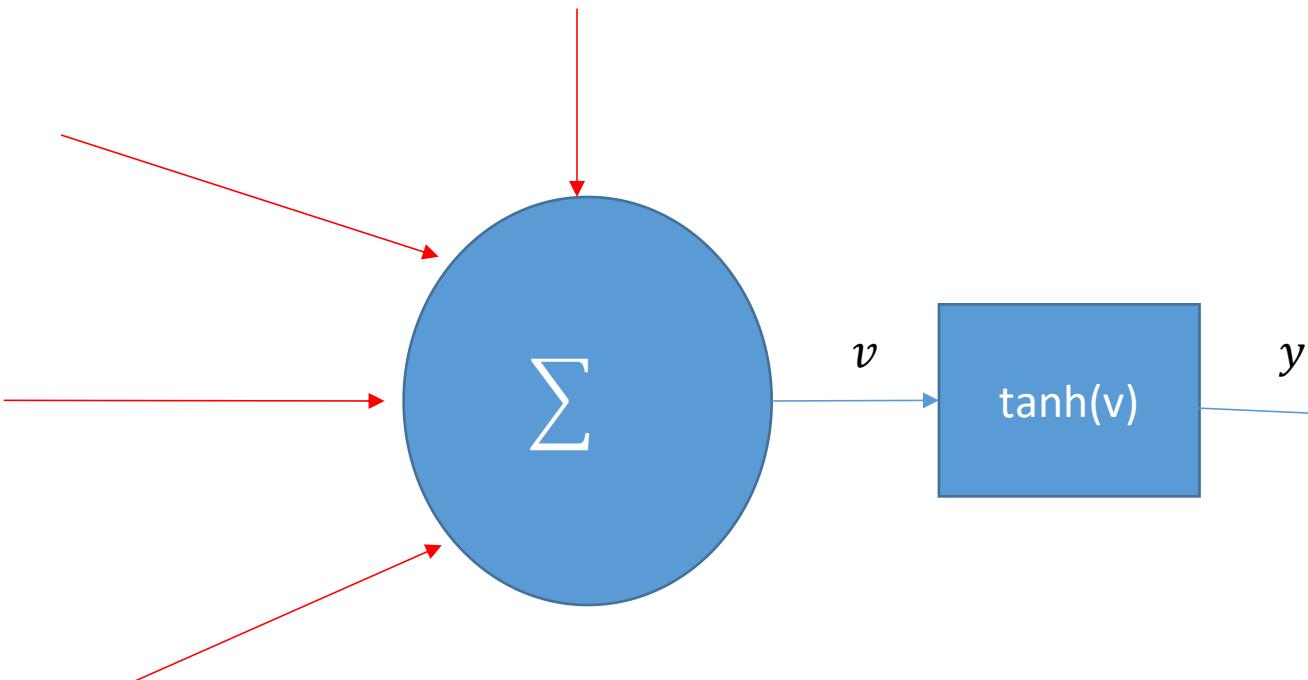
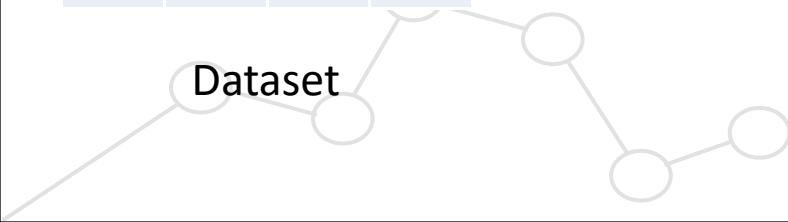


Artificial Neuron

- Training a neuron (perceptron).

Step 1: A random vector W is generated

X1	X2	X3	c
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8	0	8	1



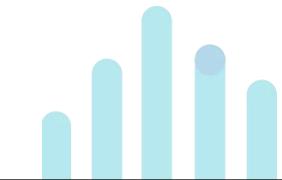
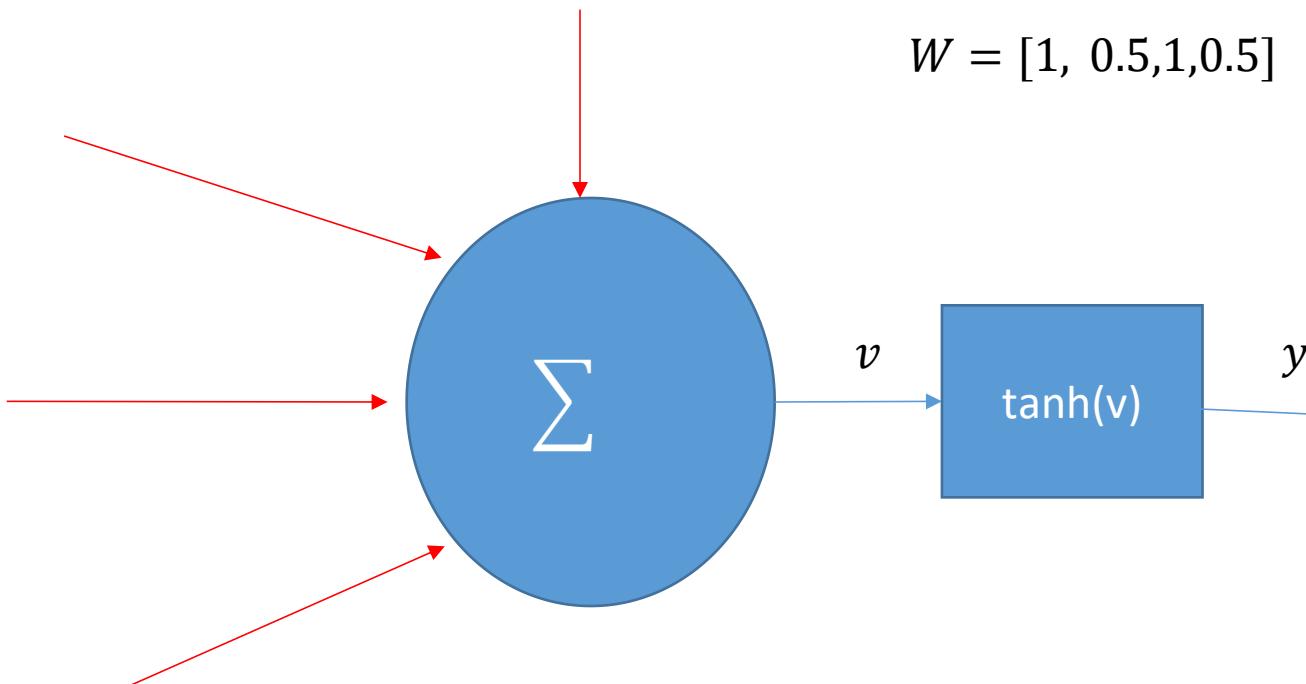
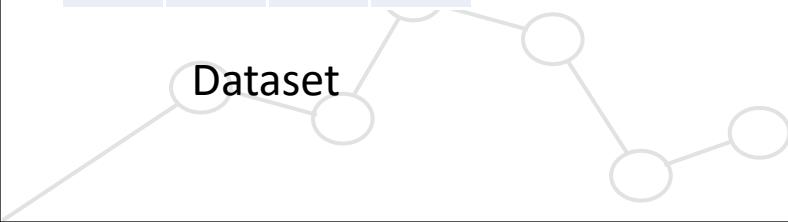
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$$W = [1, 0.5, 1, 0.5]$$

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

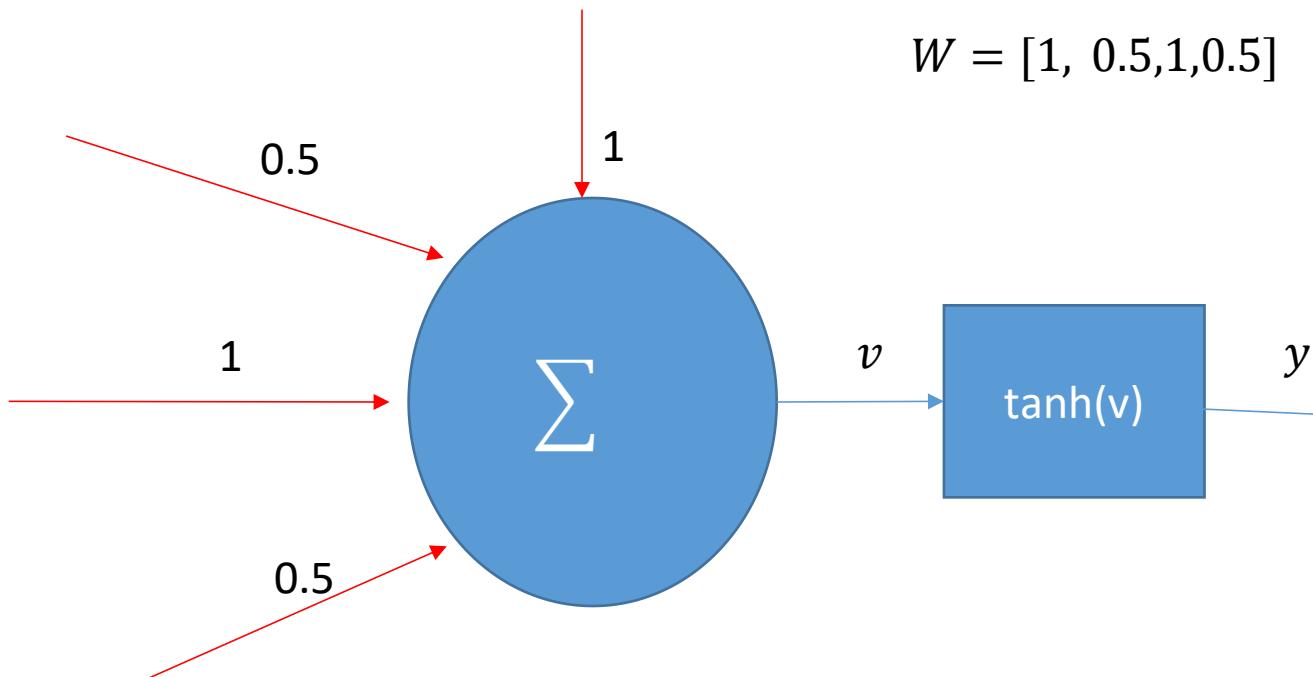


Artificial Neuron

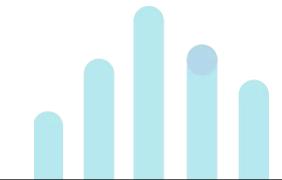
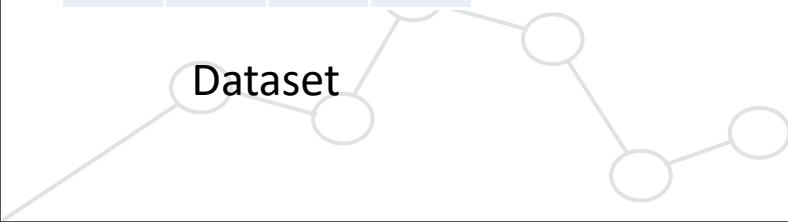
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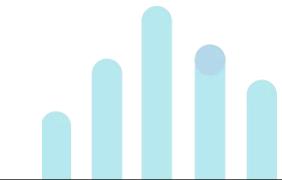
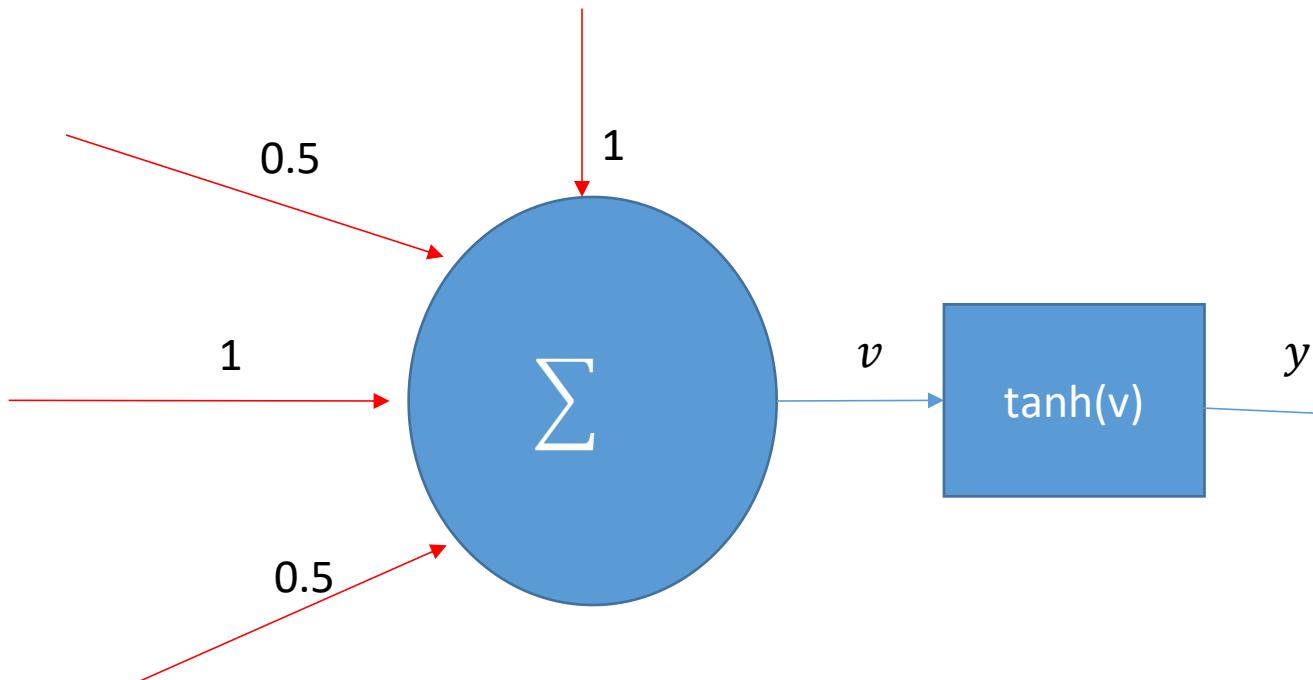
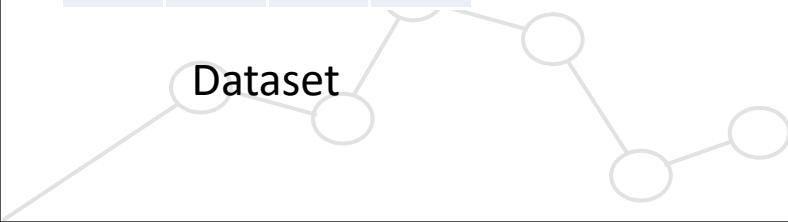


Artificial Neuron

- Training a neuron (perceptron).

Step 2: The first pattern is presented to the perceptron

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

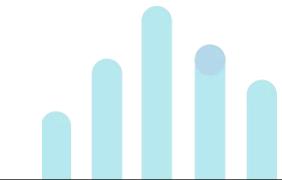
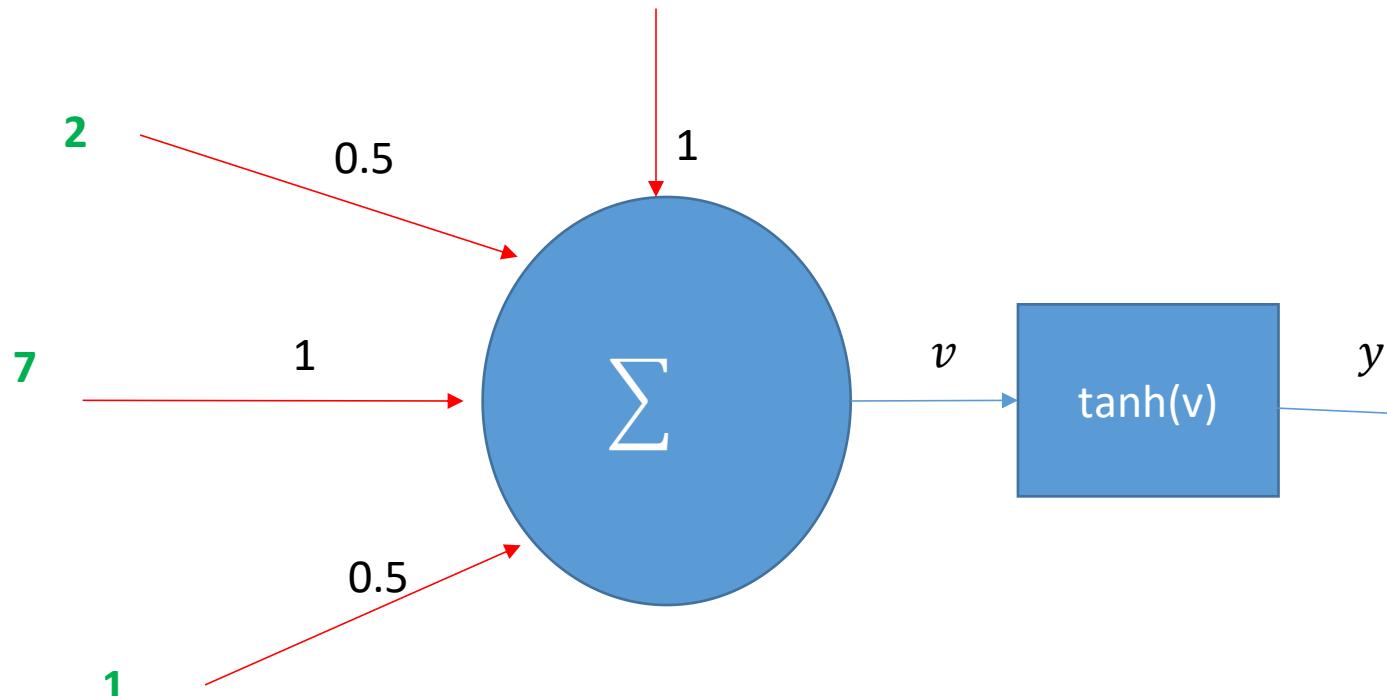
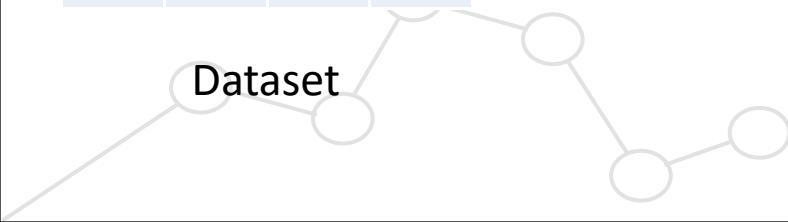


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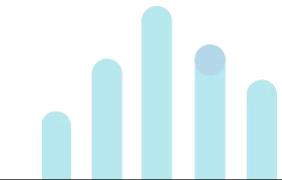
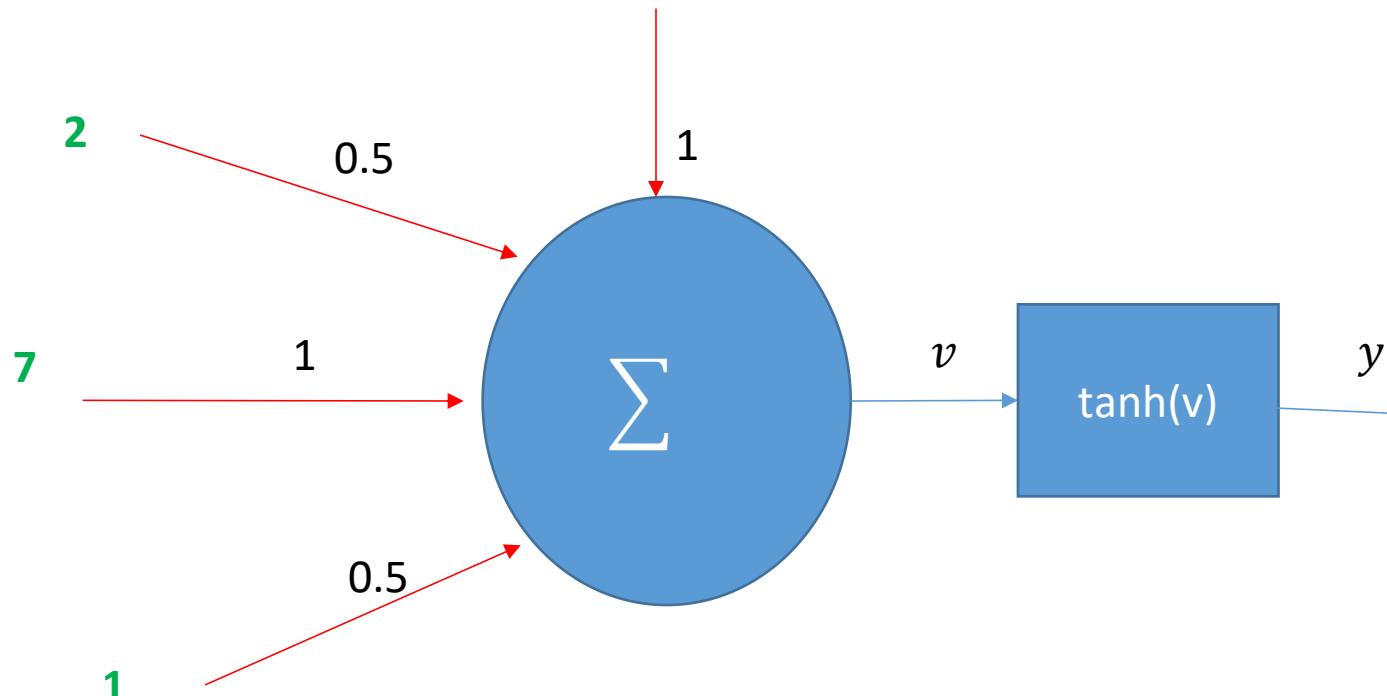
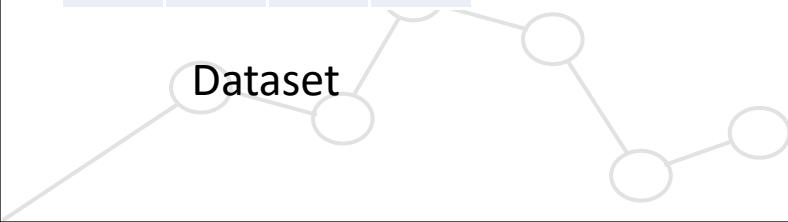


Artificial Neuron

- Training a neuron (perceptron).

Step 3: The output of the perceptron is determined.

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

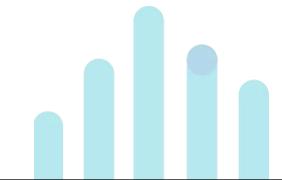
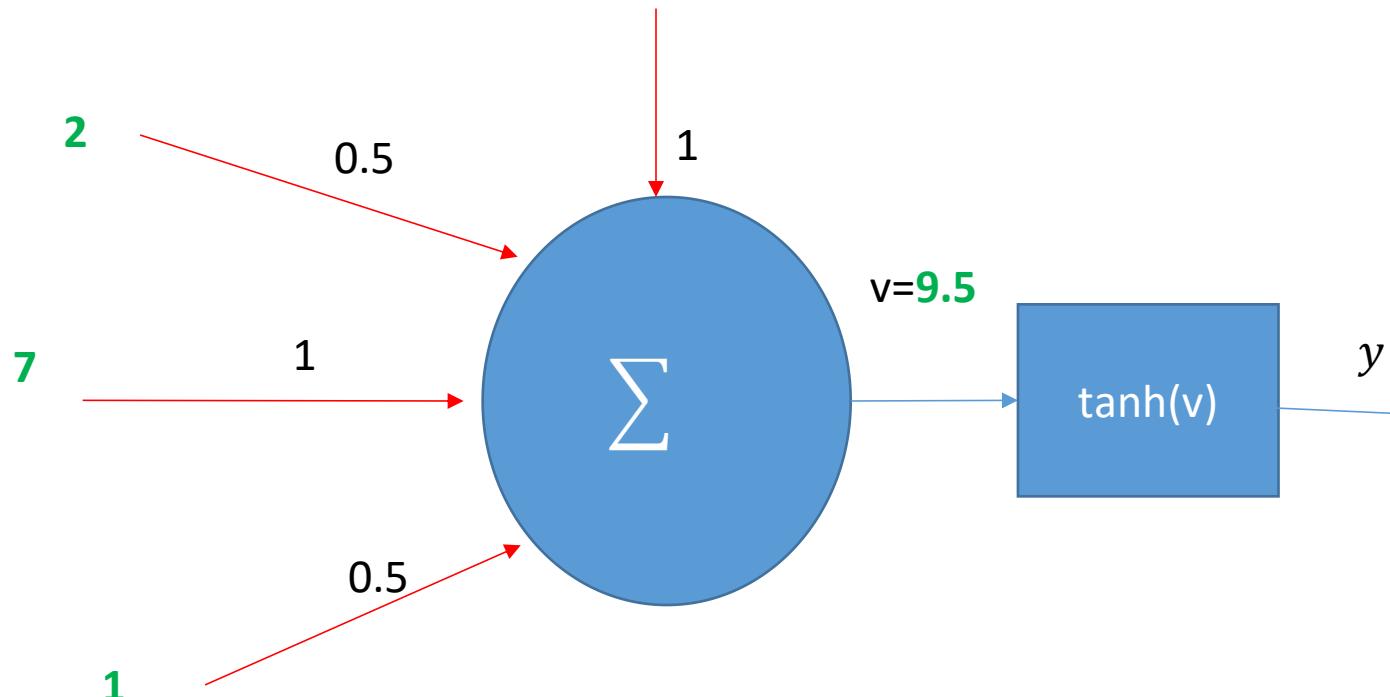
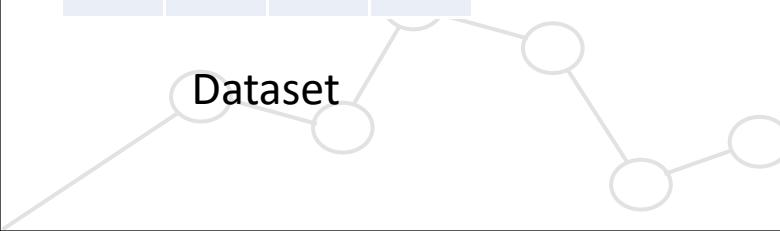


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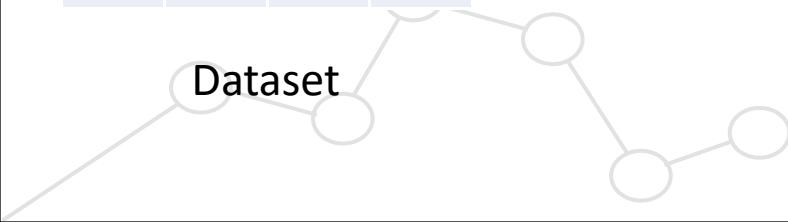
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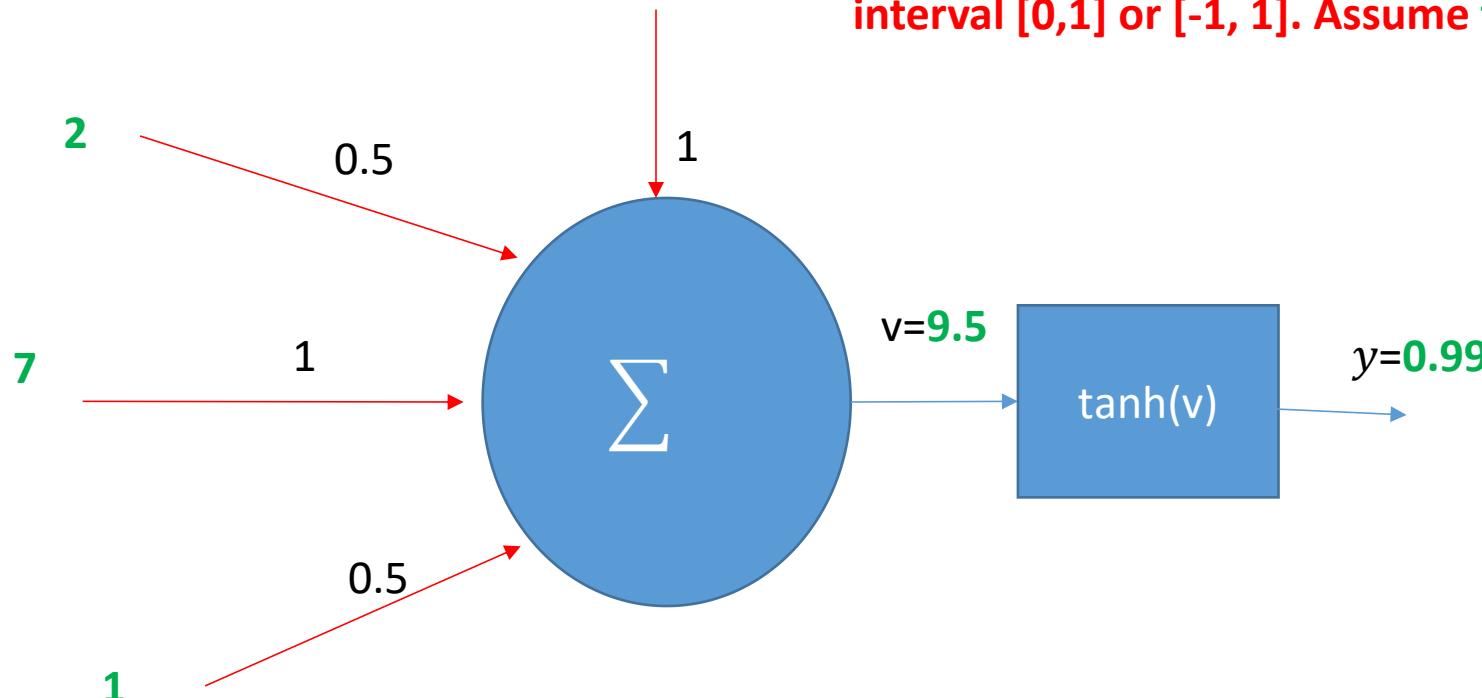
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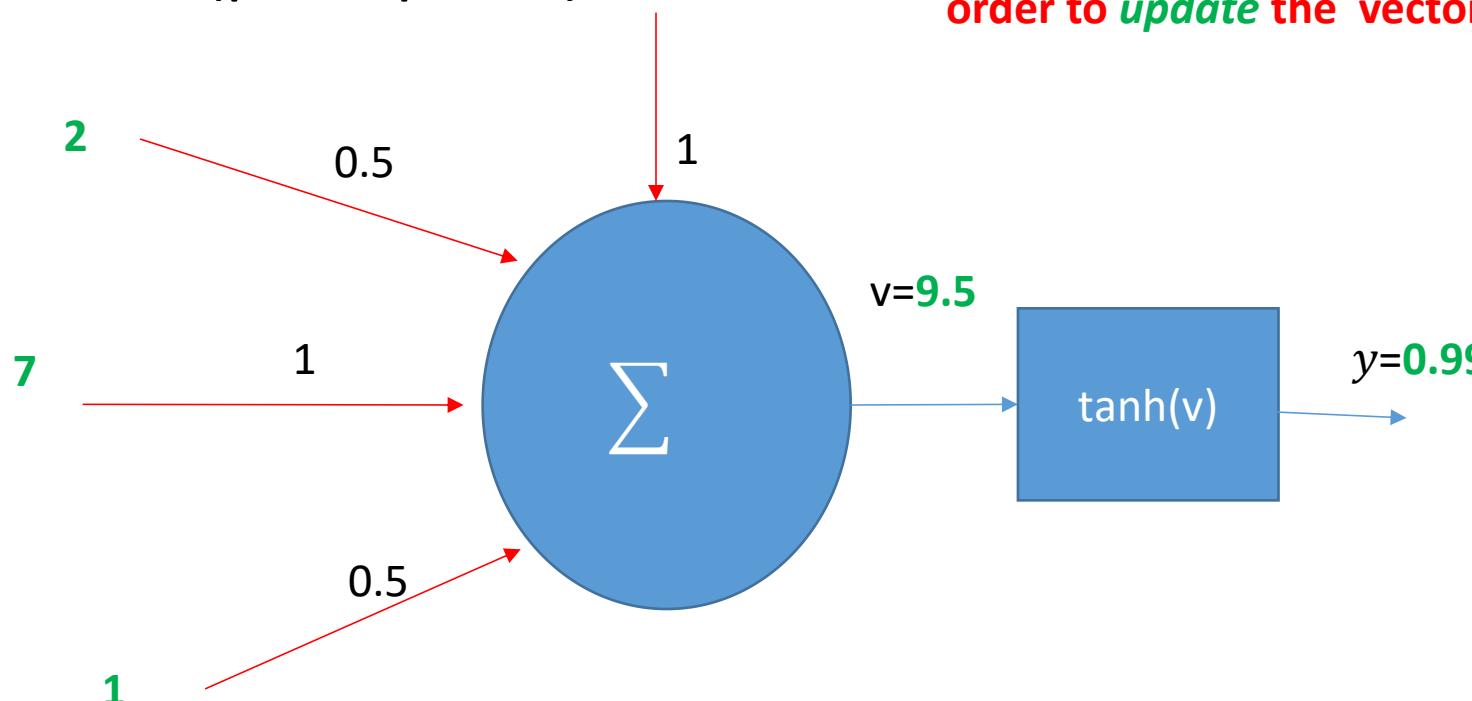
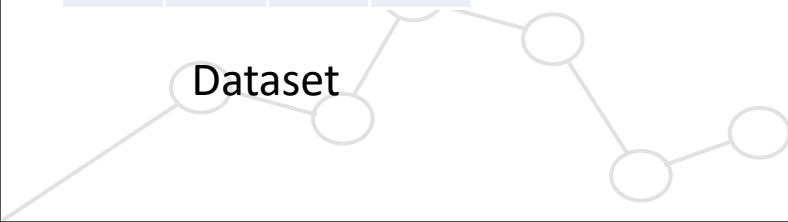
Step 4: The value of y is calculated based on activation function. Recall that such function allows to normalize the output as an closed interval $[0,1]$ or $[-1, 1]$. Assume the last interval.



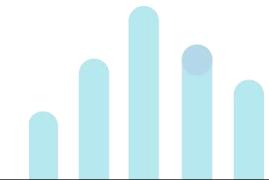
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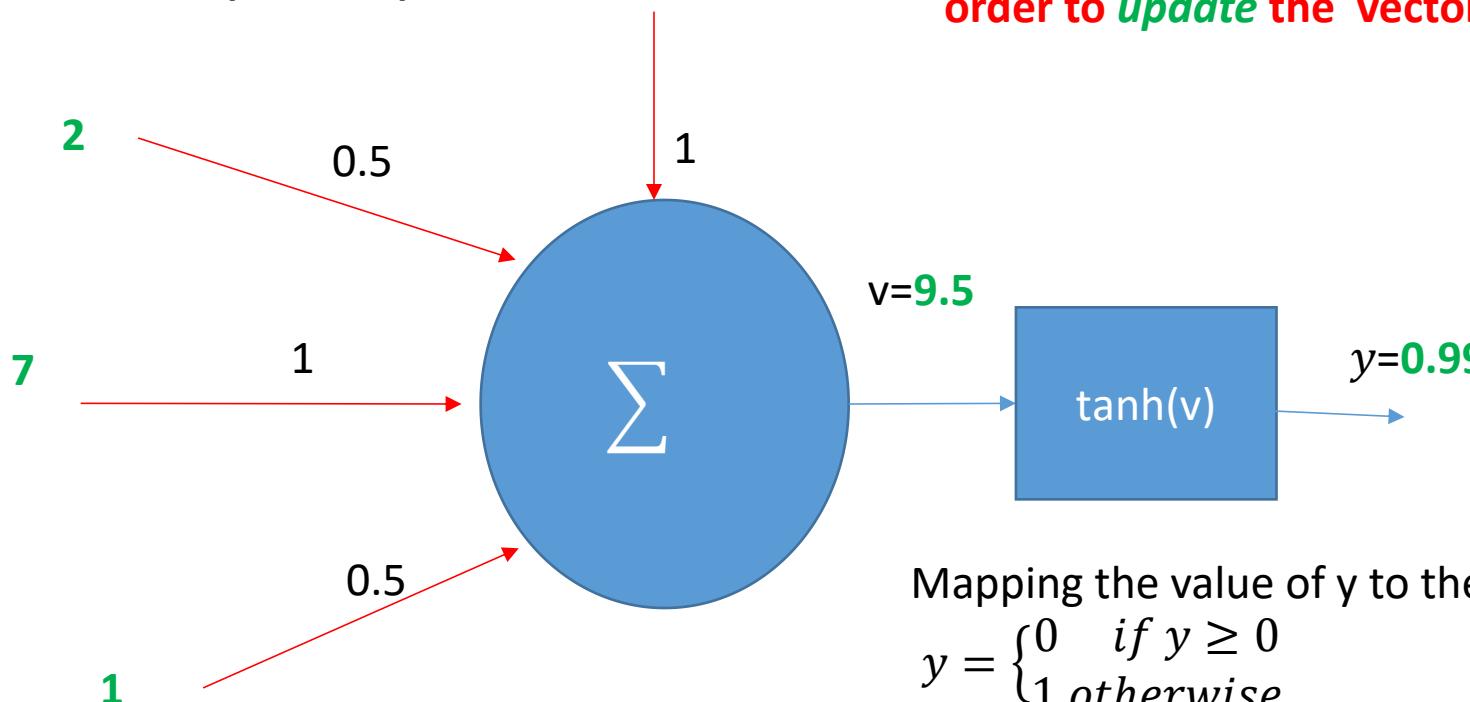
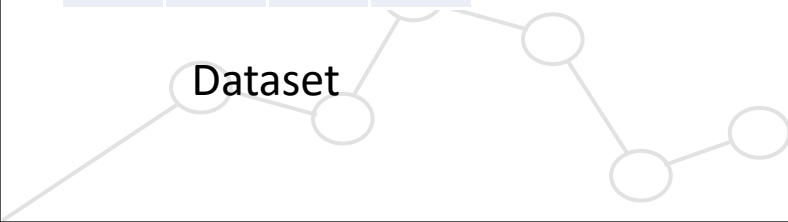
Step 5: The value of y is evaluated in order to *update* the vector W .



Artificial Neuron

- Training a neuron (perceptron).

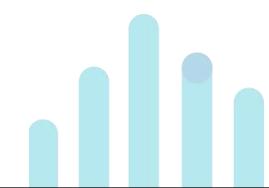
X1	X2	X3	c
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3	6	5	1
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6	8	5	0
7	9	7	1
8	0	8	1



Step 5: The value of y is evaluated in order to *update* the vector W .

Mapping the value of y to the class label.

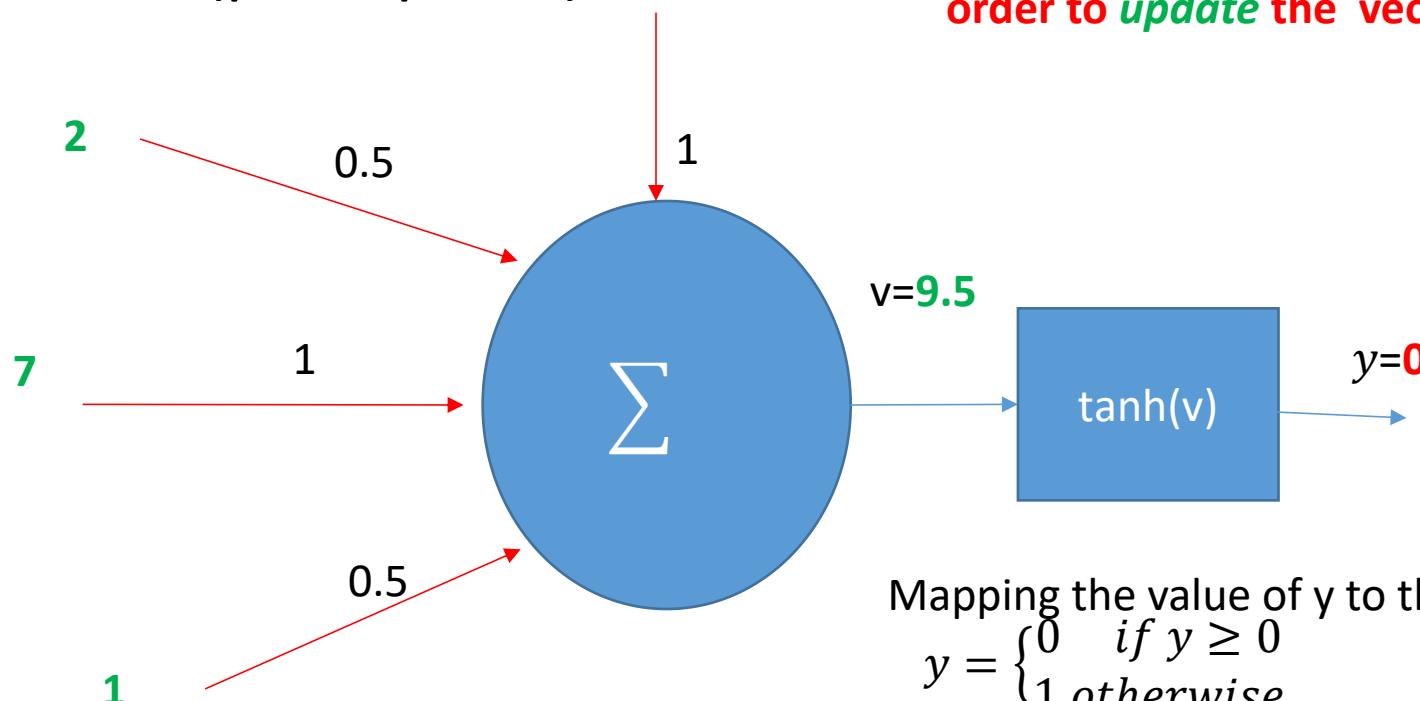
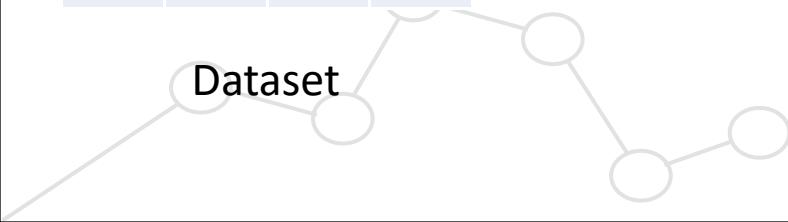
$$y = \begin{cases} 0 & \text{if } y \geq 0 \\ 1 & \text{otherwise} \end{cases}$$



Artificial Neuron

- Training a neuron (perceptron).

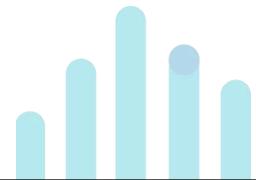
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



Step 5: The value of y is evaluated in order to *update* the vector W .

Mapping the value of y to the class label.

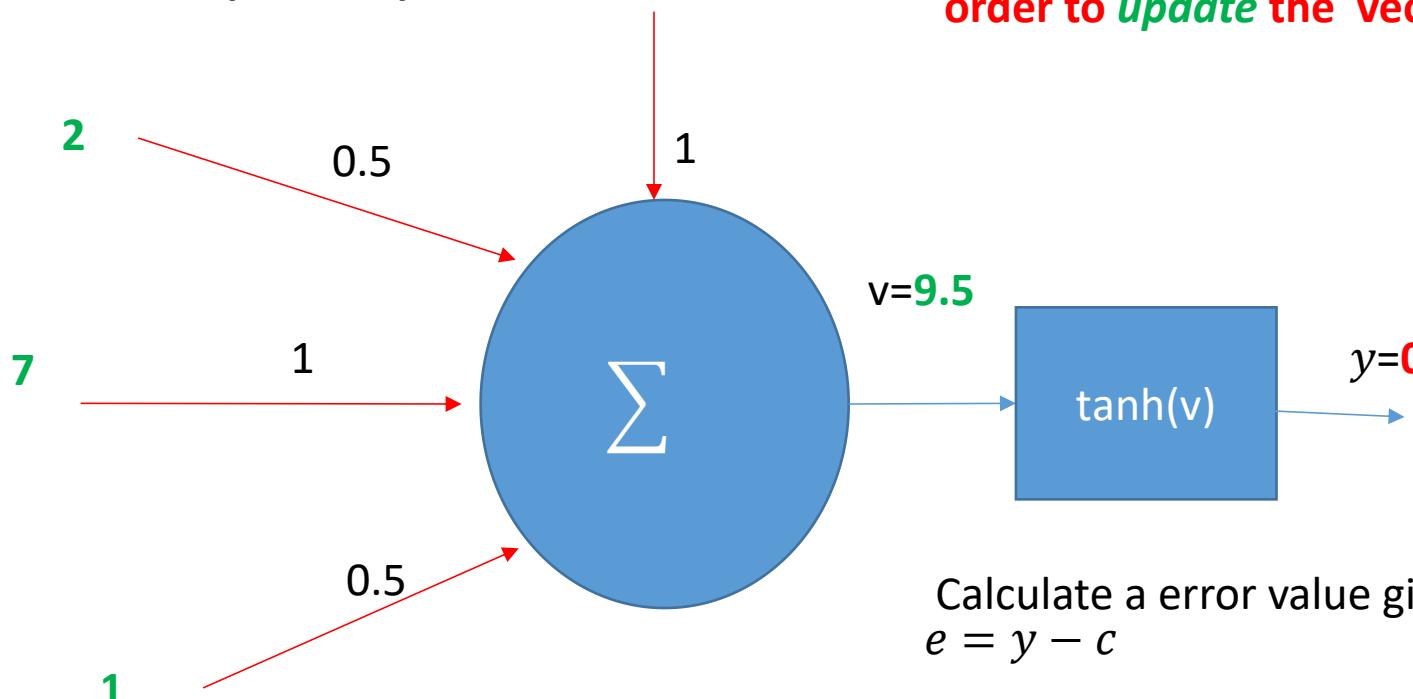
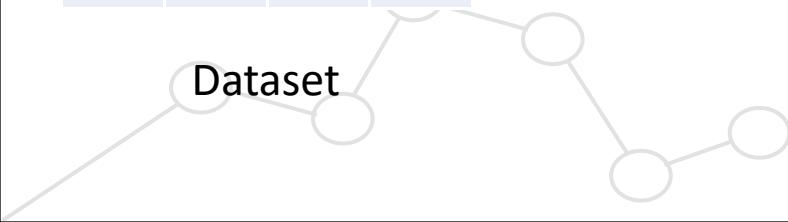
$$y = \begin{cases} 0 & \text{if } y \geq 0 \\ 1 & \text{otherwise} \end{cases}$$



Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



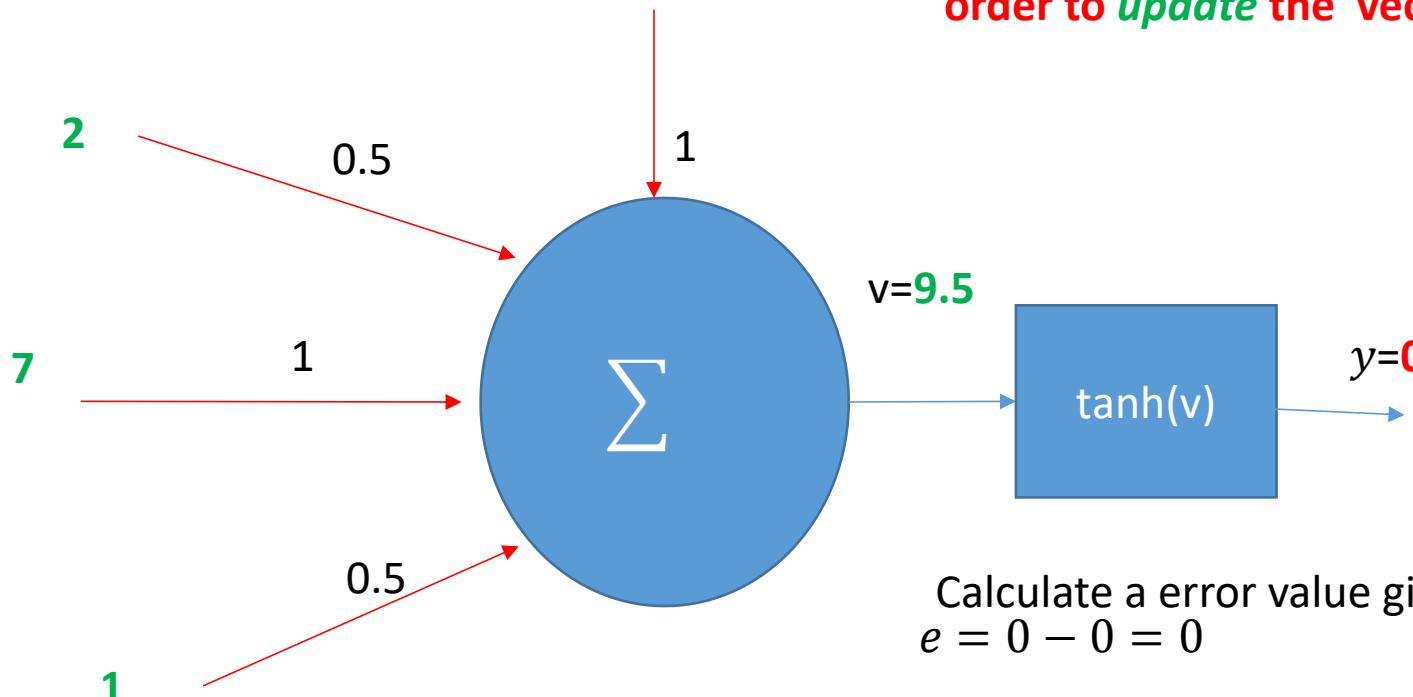
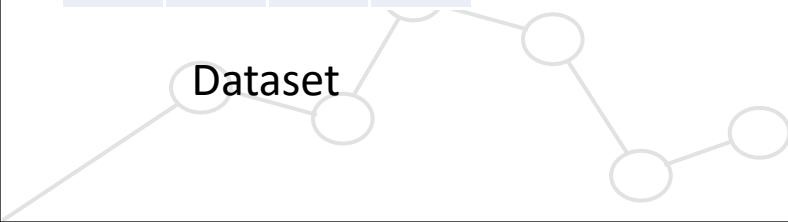
Calculate a error value given the expected class c
 $e = y - c$



Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



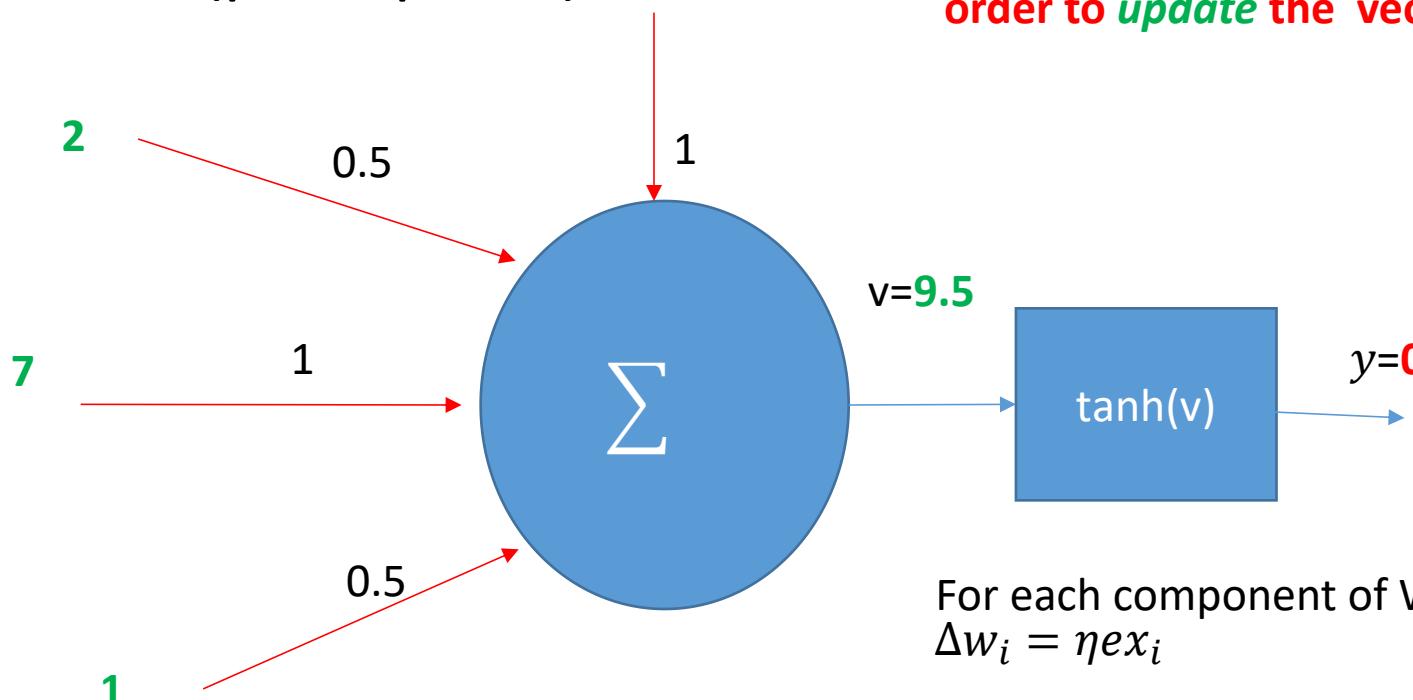
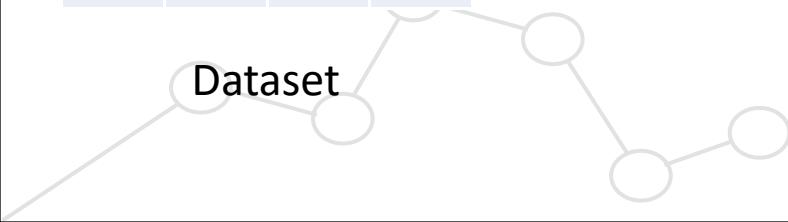
Calculate a error value given the expected class c
 $e = 0 - 0 = 0$



Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

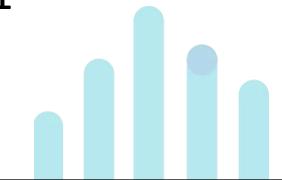


Step 5: The value of y is evaluated in order to *update* the vector W .

For each component of W , calculate a variation Δw_i
 $\Delta w_i = \eta e x_i$

Where η is a perturbation value, usually it is a small positive value. Assume $\eta=0.01$

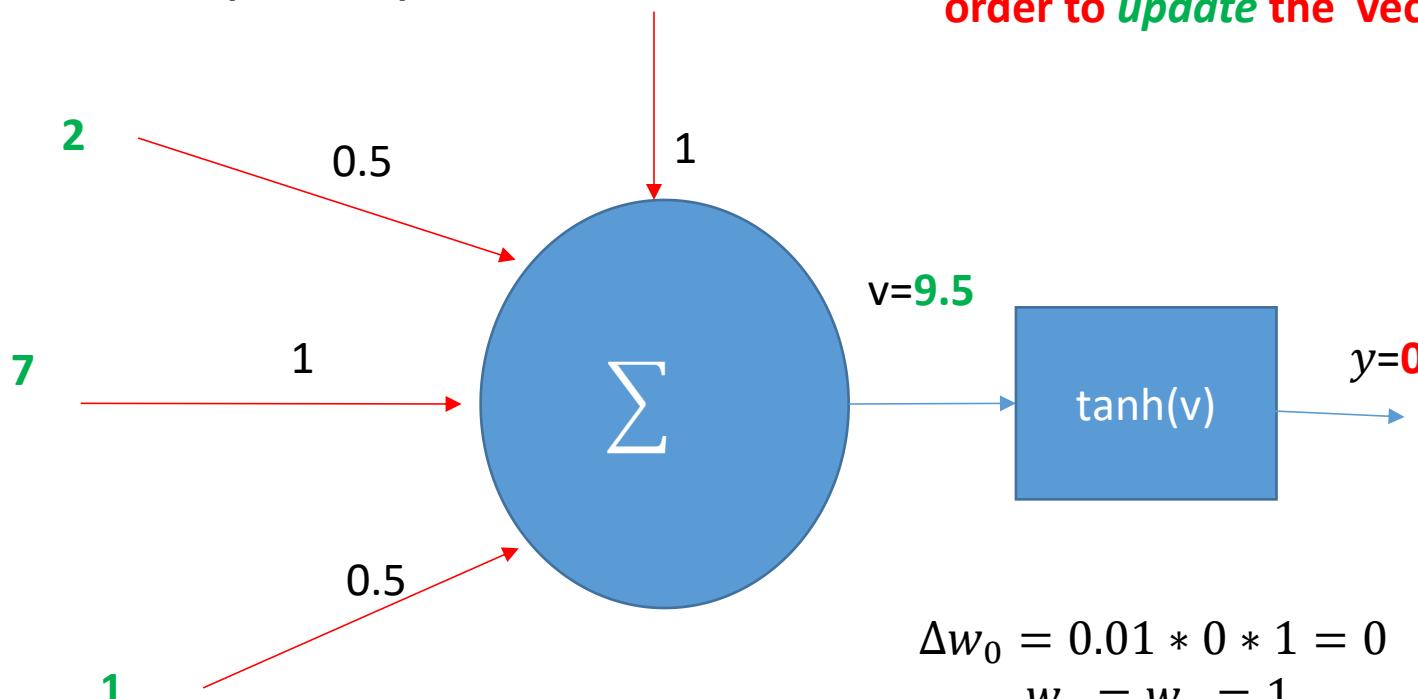
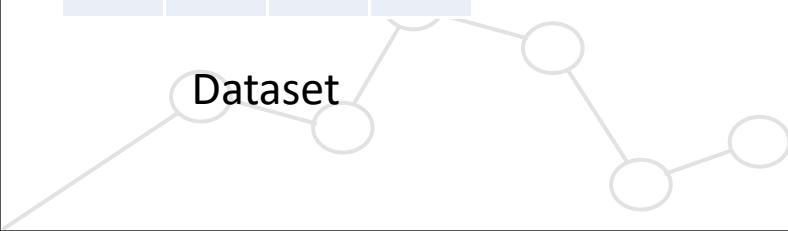
Update $w_i = w_i + \Delta w_i$



Artificial Neuron

- Training a neuron (perceptron).

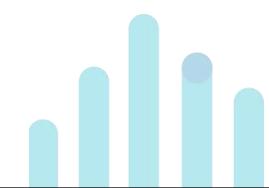
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$\Delta w_0 = 0.01 * 0 * 1 = 0$$

$$w_0 = w_0 = 1$$

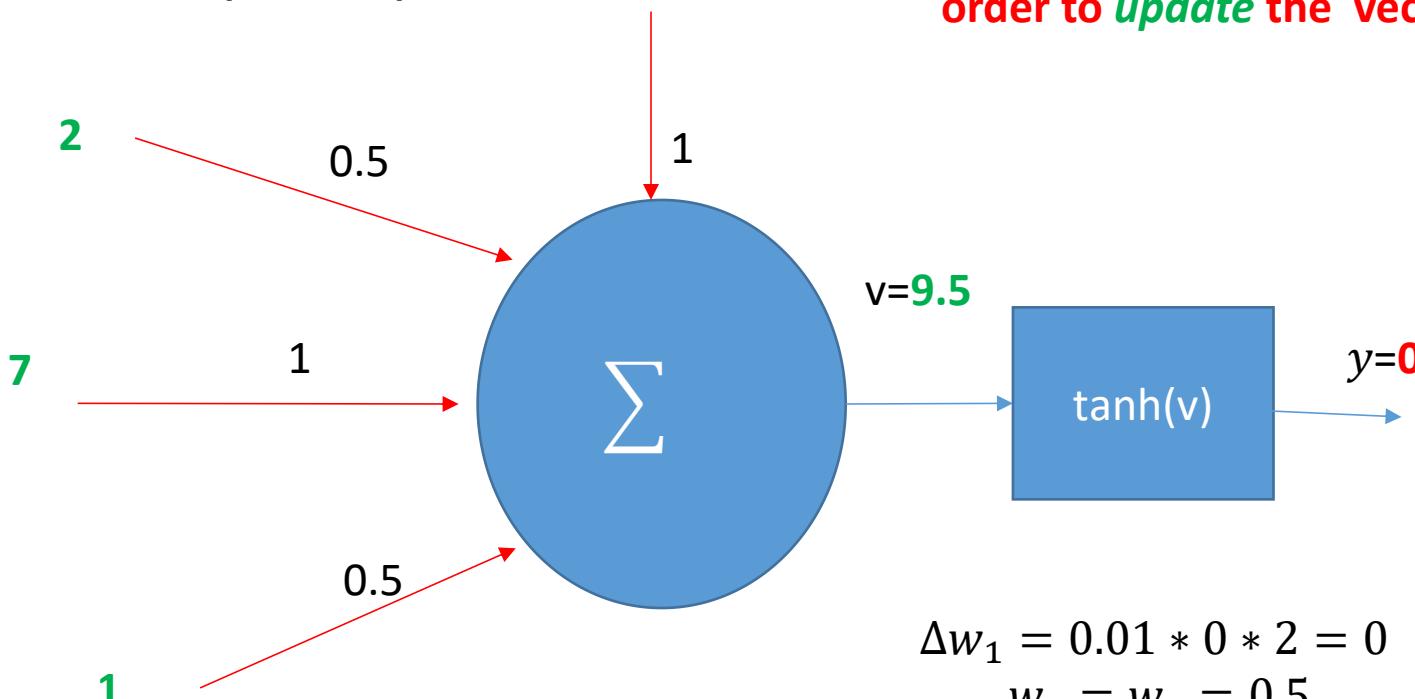
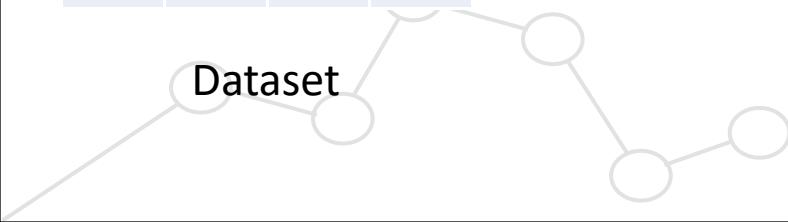
$$W = [1]$$



Artificial Neuron

- Training a neuron (perceptron).

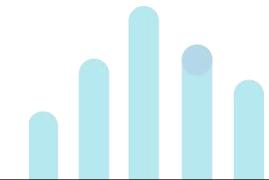
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$\Delta w_1 = 0.01 * 0 * 2 = 0$$

$$w_1 = w_1 = 0.5$$

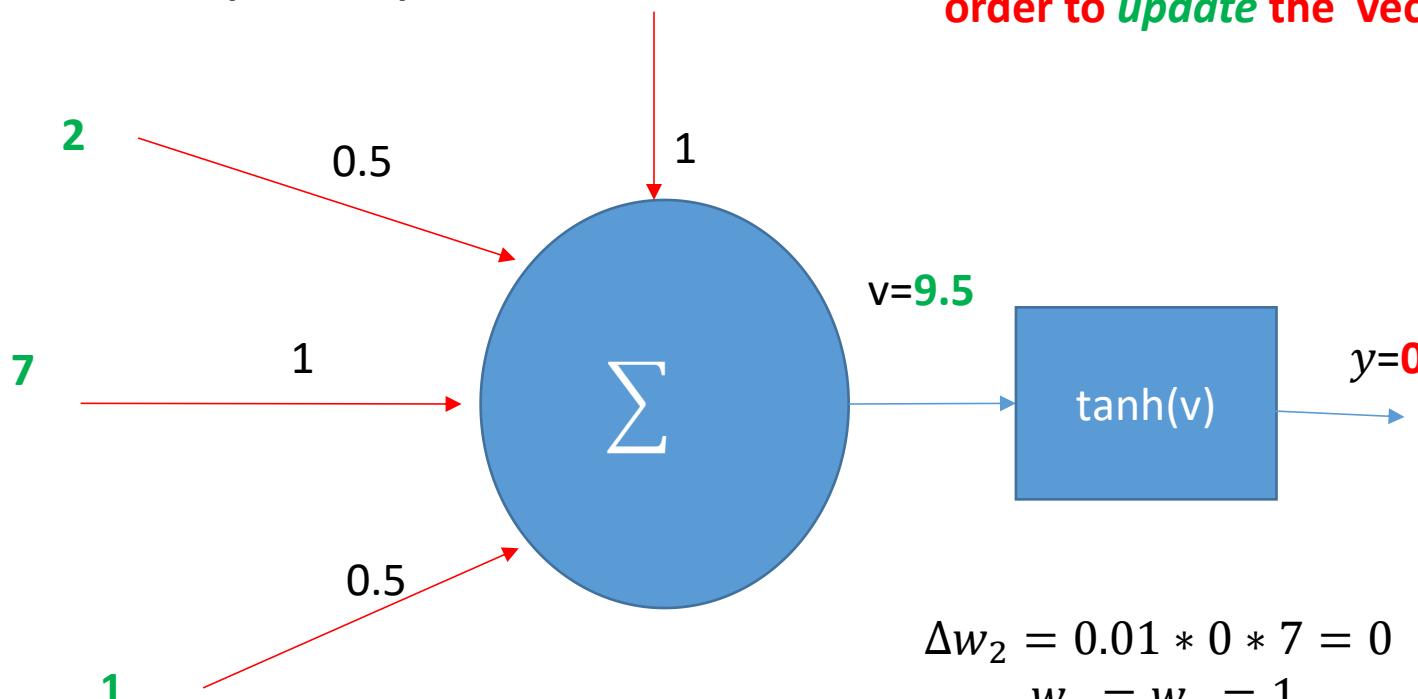
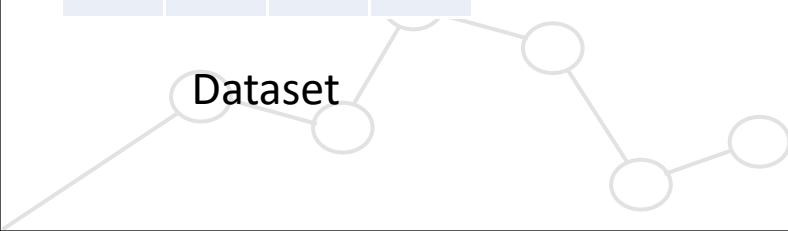
$$W = [1, 0.5]$$



Artificial Neuron

- Training a neuron (perceptron).

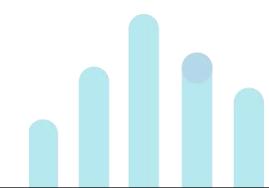
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$\Delta w_2 = 0.01 * 0 * 7 = 0$$

$$w_2 = w_2 = 1$$

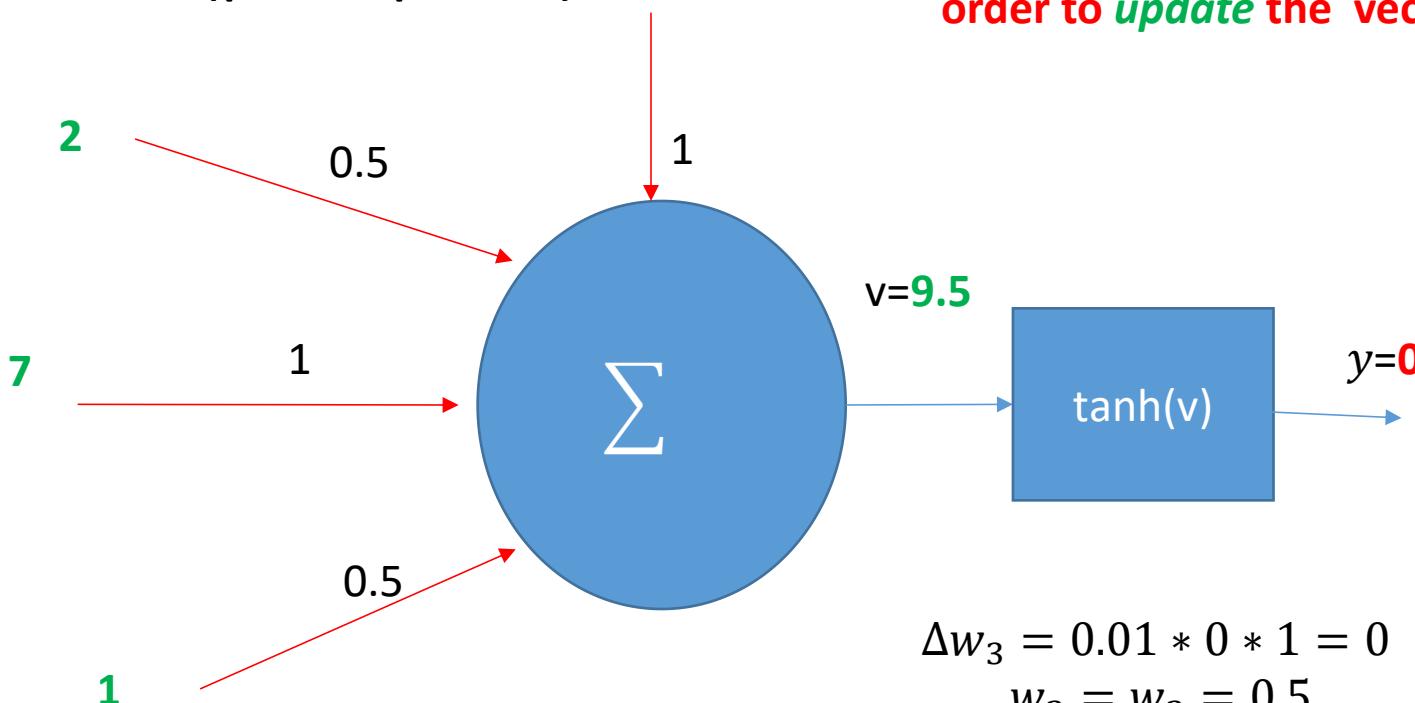
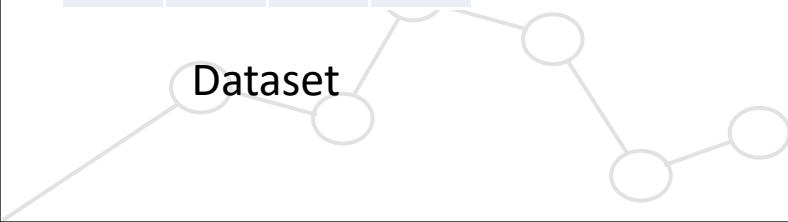
$$W = [1, 0.5, 1,$$



Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$W = [1, 0.5, 1, 0.5]$$

In this case W does not change,
Repeat steps 2-5 again with **other**
pattern

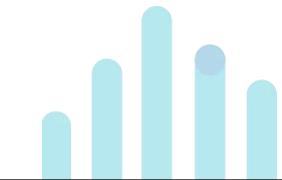
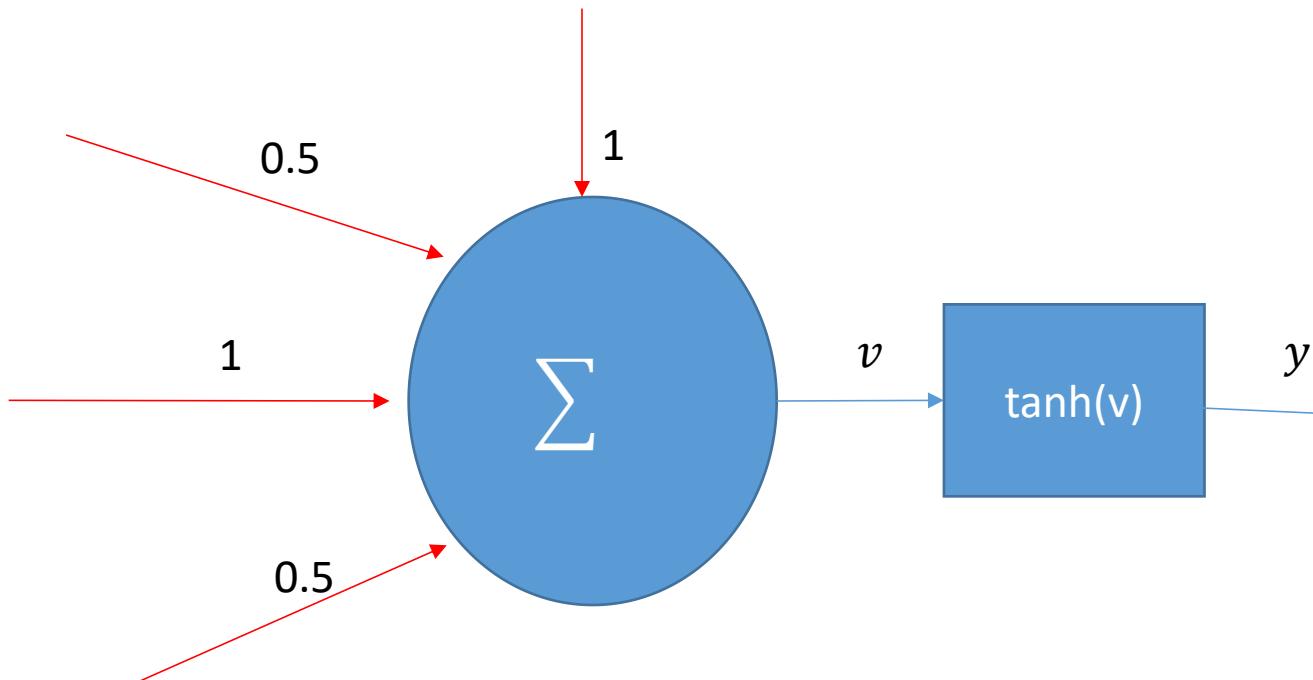
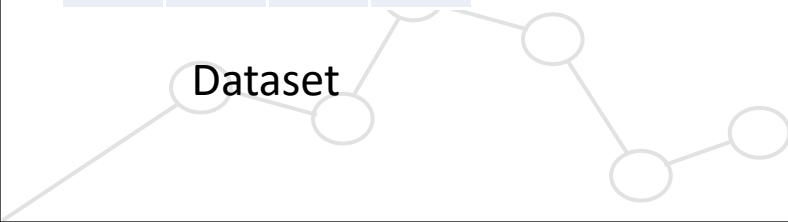


Artificial Neuron

- Training a neuron (perceptron).

Step 2: The first pattern is presented to the perceptron

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

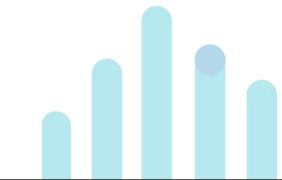
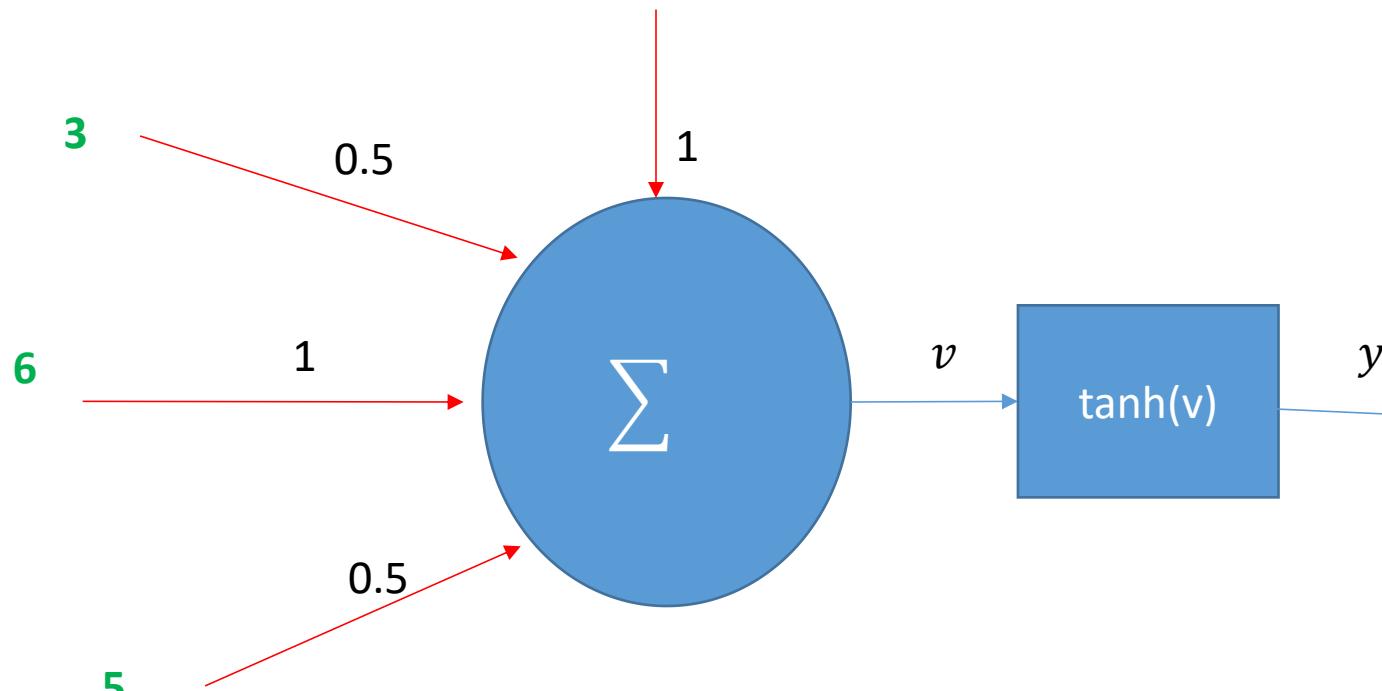
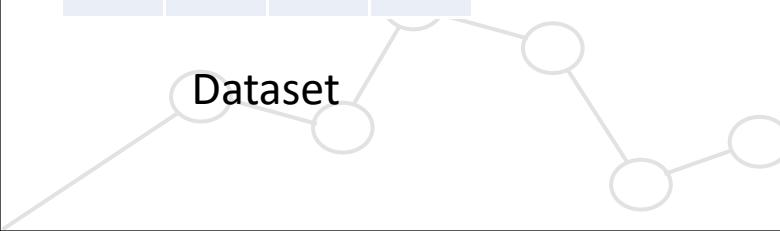


Artificial Neuron

- Training a neuron (perceptron).

Step 2: The first pattern is presented to the perceptron

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

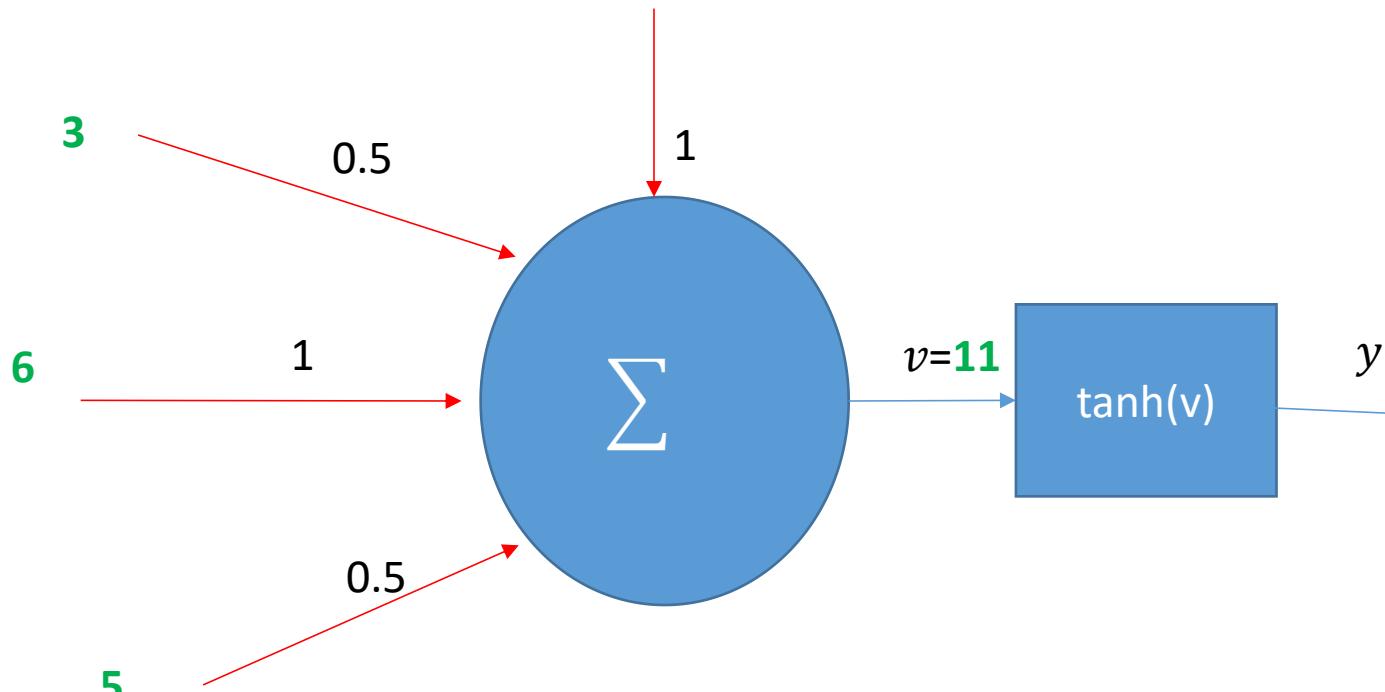
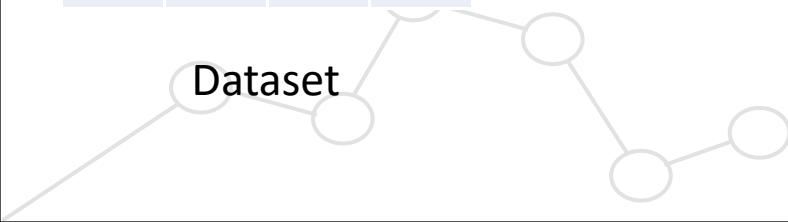


Artificial Neuron

- Training a neuron (perceptron).

Step 3: The output of the perceptron is determined.

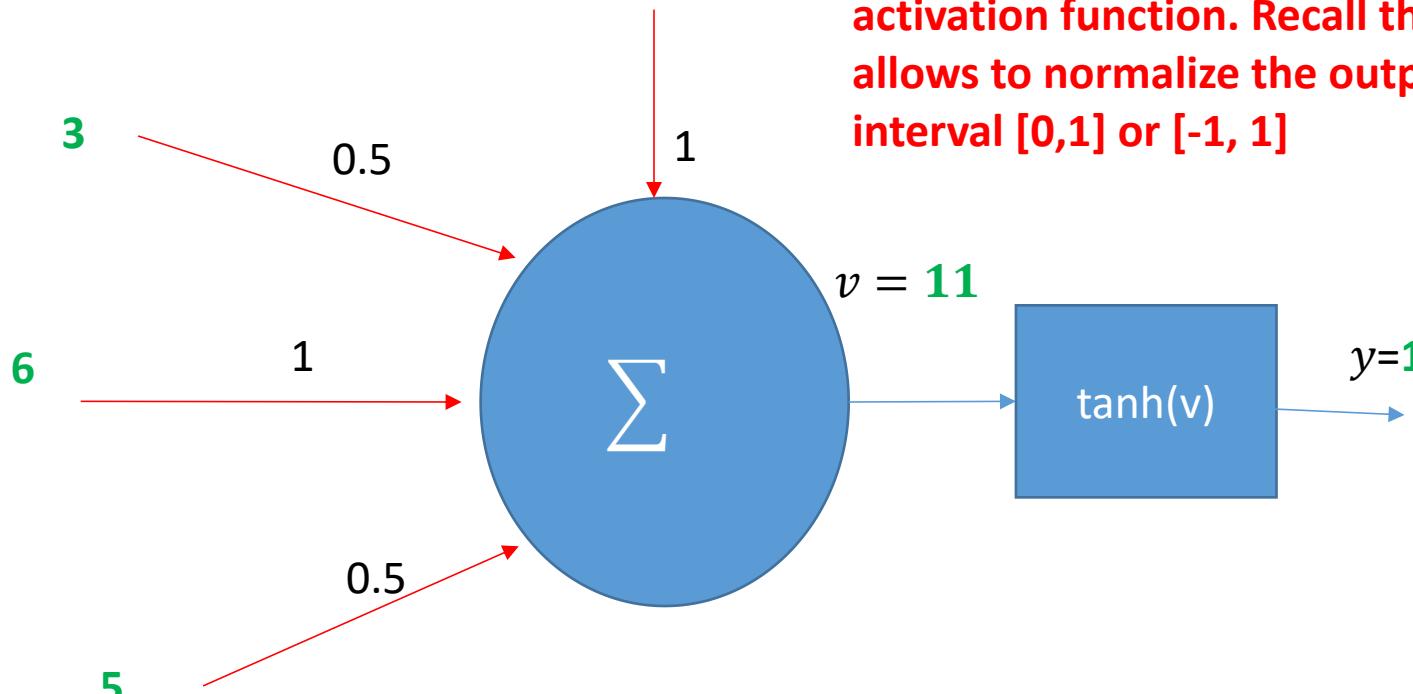
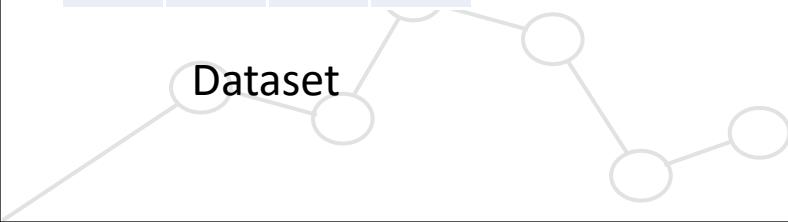
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



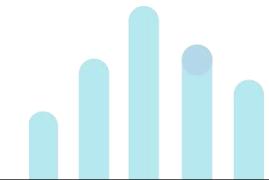
Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



Step 4: The value of y is calculated based on activation function. Recall that such function allows to normalize the output as an closed interval $[0,1]$ or $[-1, 1]$

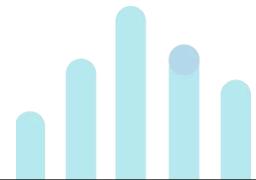
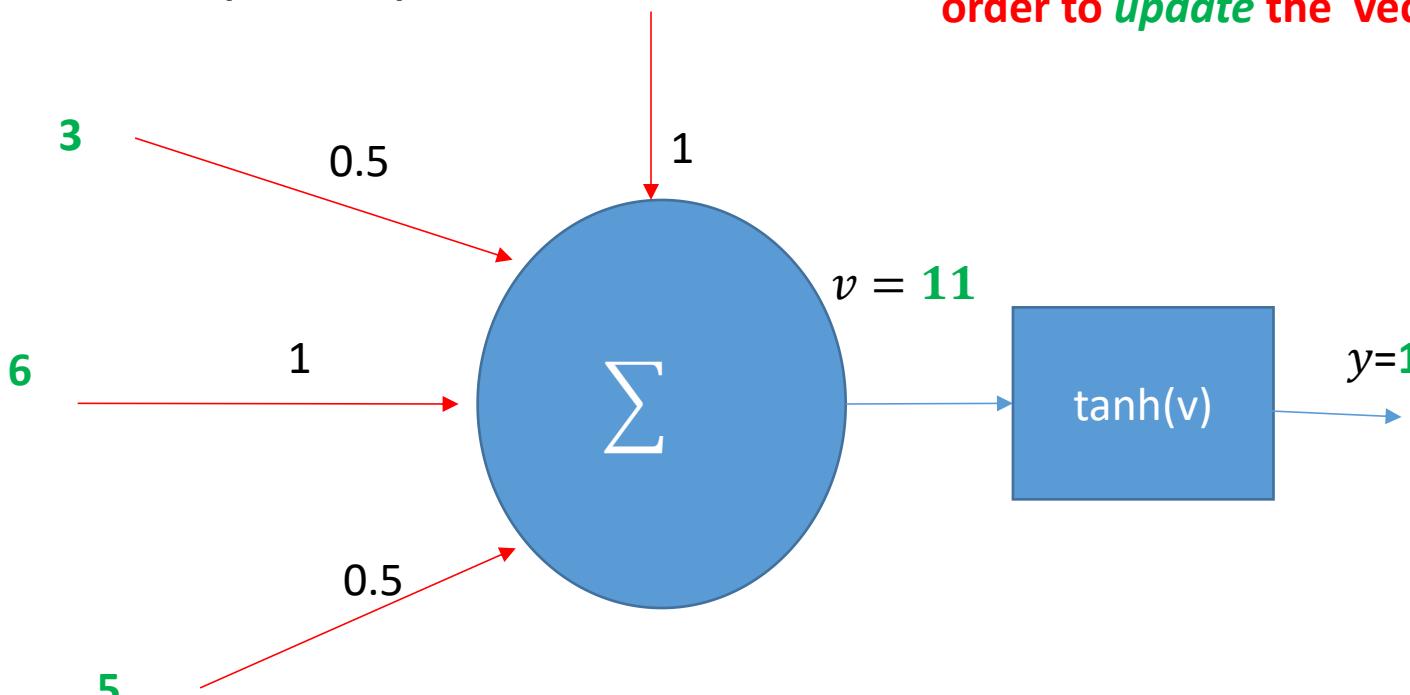
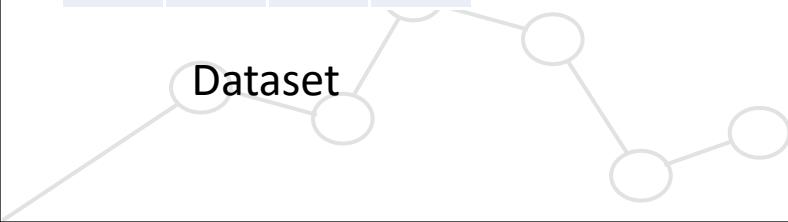


Artificial Neuron

- Training a neuron (perceptron).

Step 5: The value of y is evaluated in order to *update* the vector W .

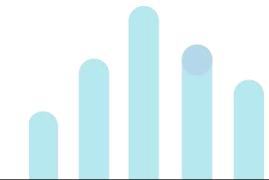
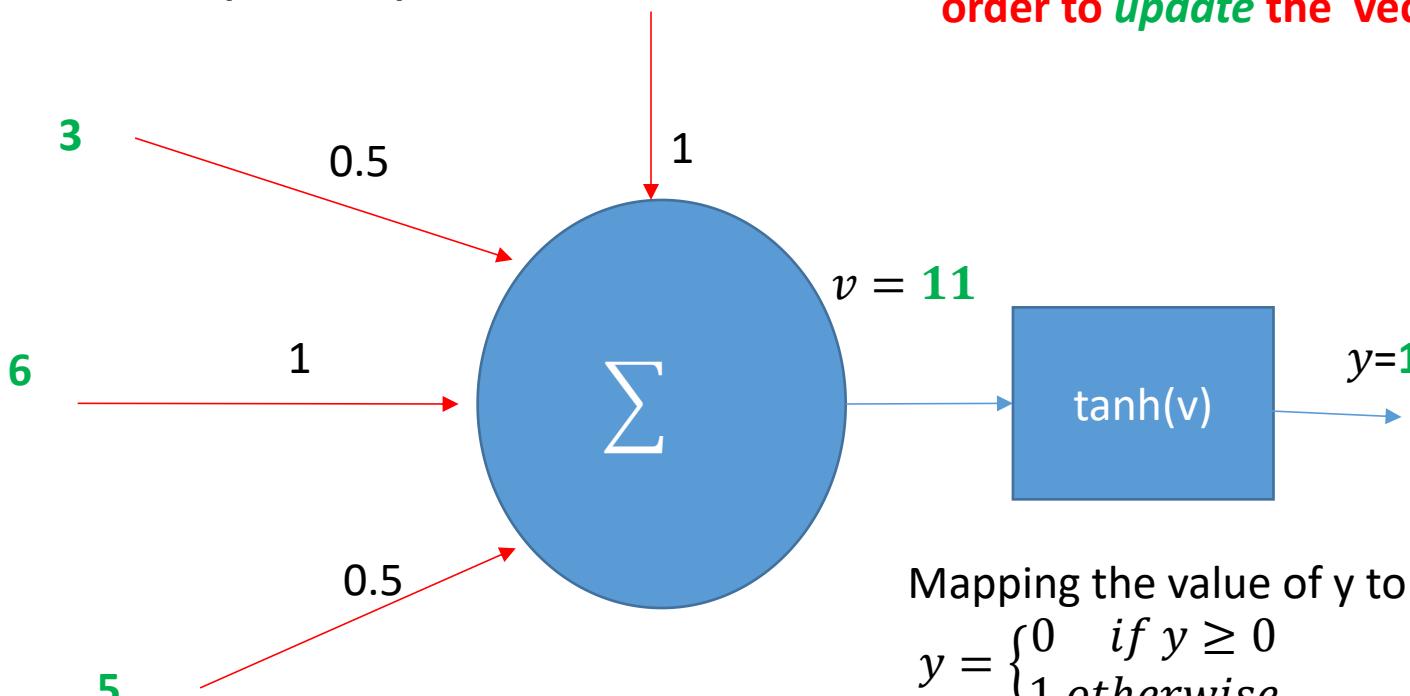
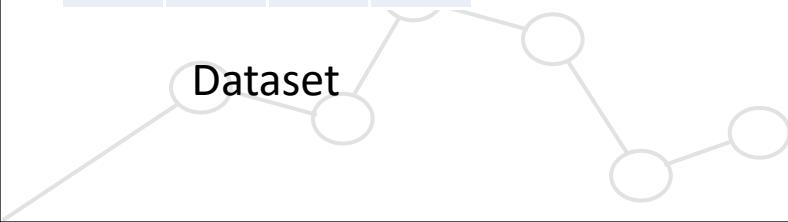
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



Artificial Neuron

- Training a neuron (perceptron).

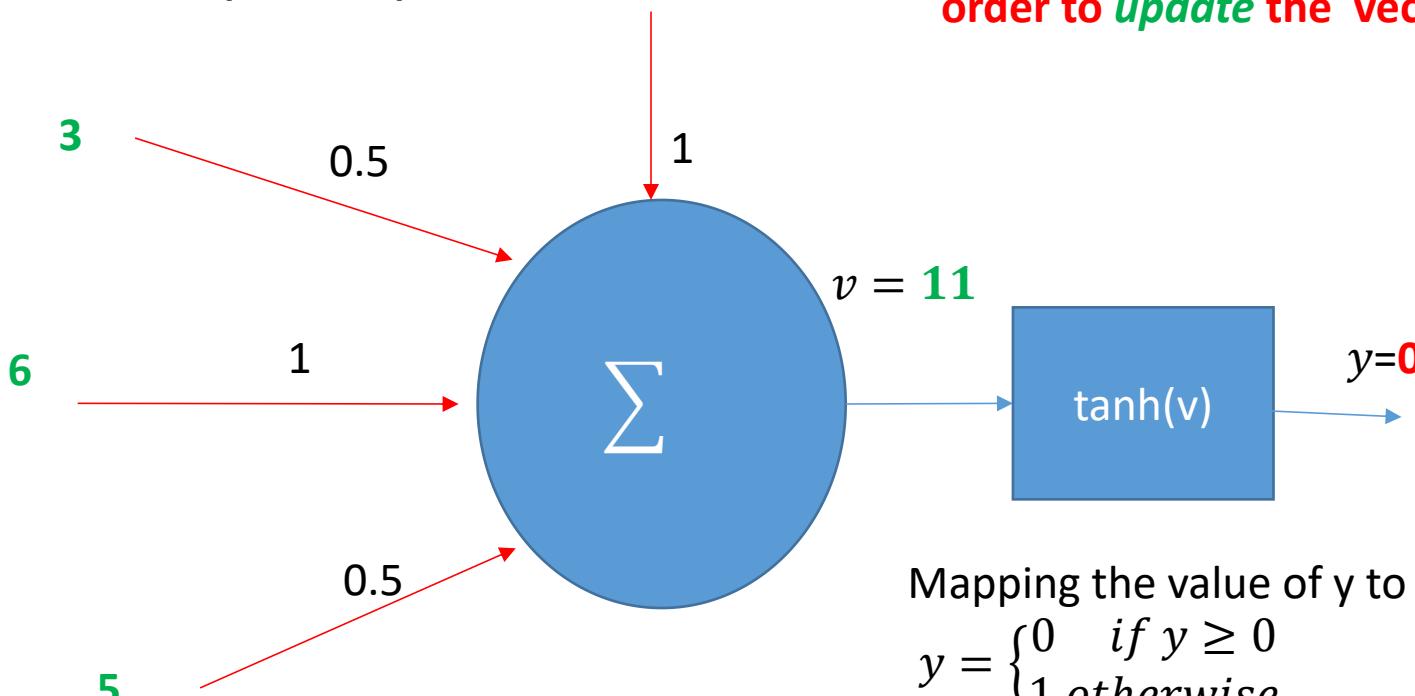
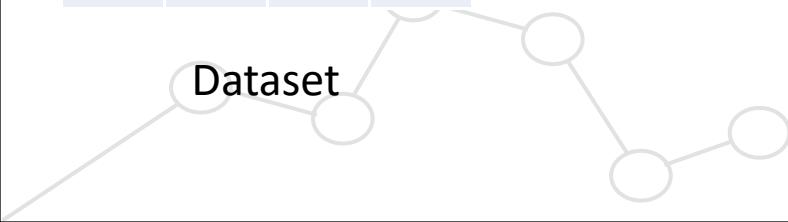
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



Artificial Neuron

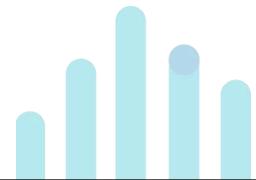
- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



Step 5: The value of y is evaluated in order to *update* the vector W .

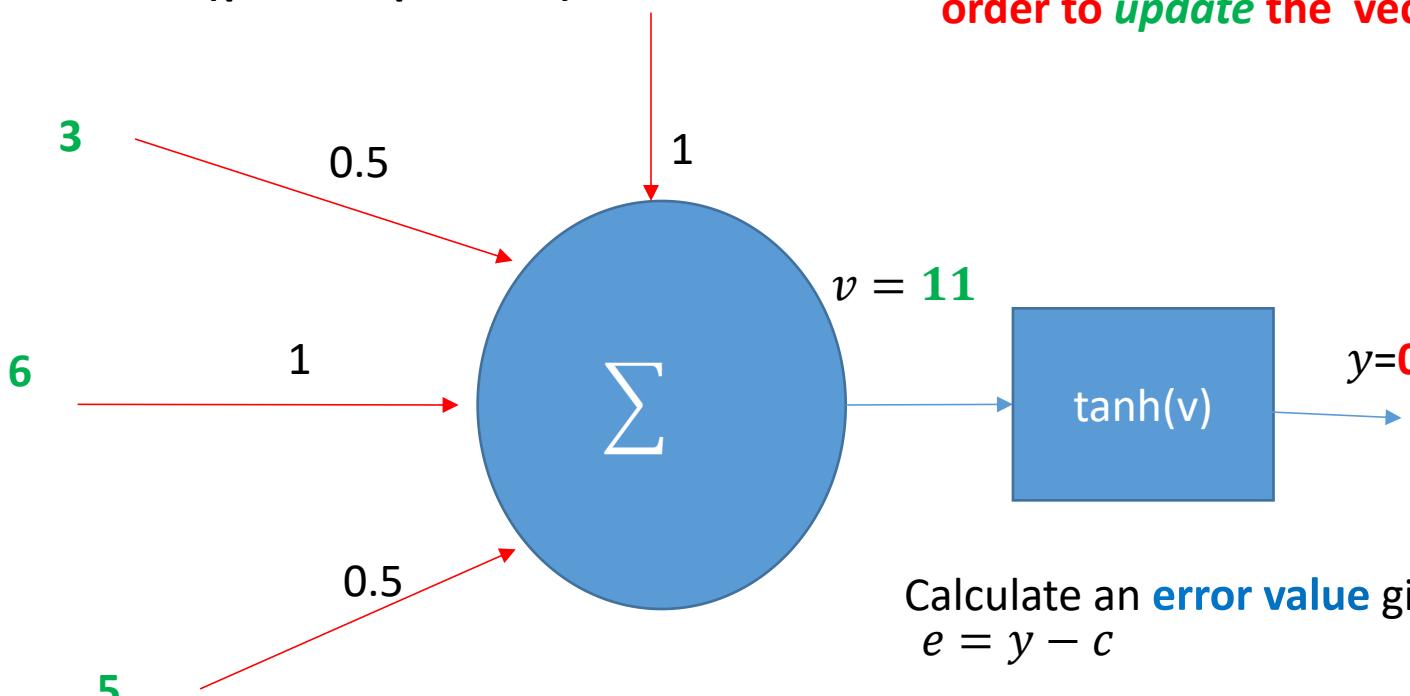
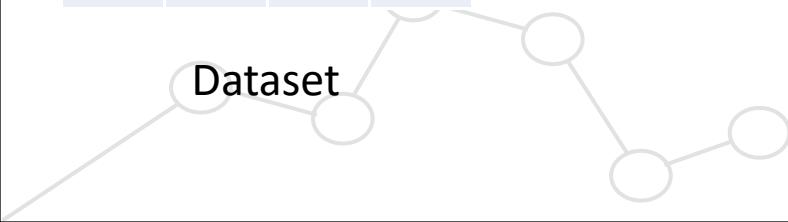
Mapping the value of y to the class label.
 $y = \begin{cases} 0 & \text{if } y \geq 0 \\ 1 & \text{otherwise} \end{cases}$



Artificial Neuron

- Training a neuron (perceptron).

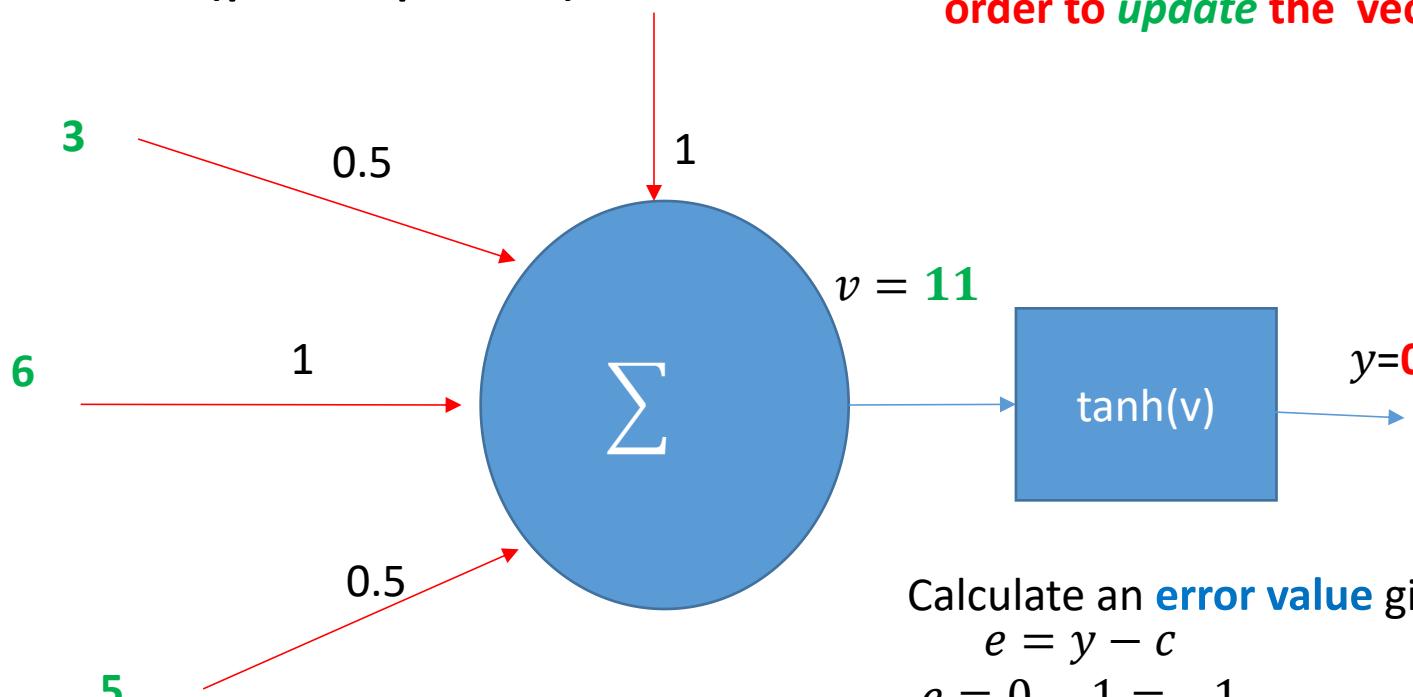
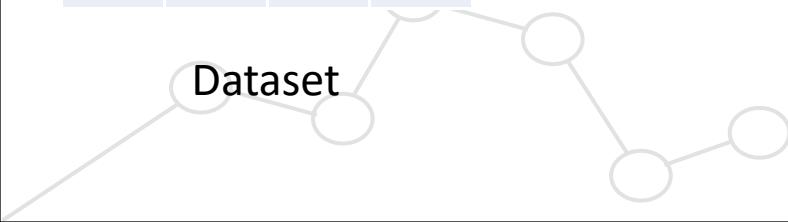
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



Step 5: The value of y is evaluated in order to *update* the vector W .

Calculate an **error value** given the expected class c

$$e = y - c$$

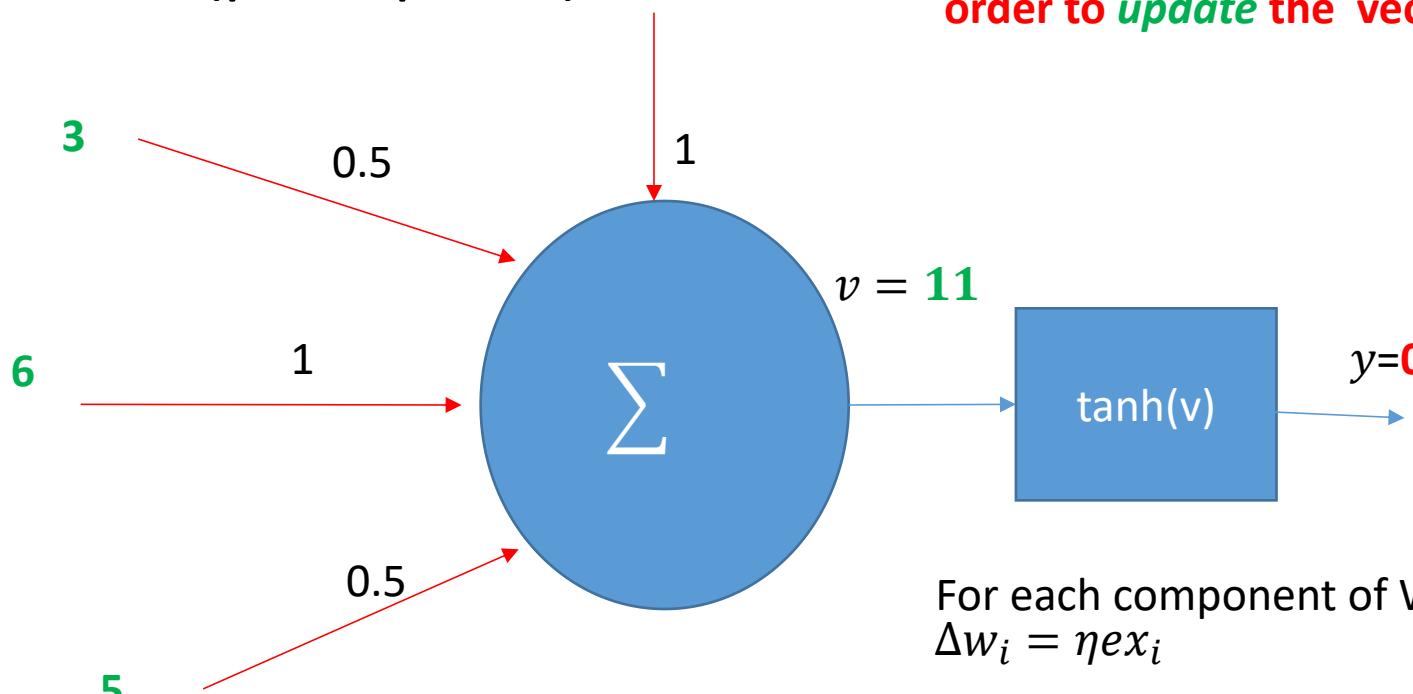
$$e = 0 - 1 = -1$$



Artificial Neuron

- Training a neuron (perceptron).

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1

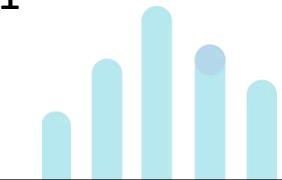


Step 5: The value of y is evaluated in order to *update* the vector W .

For each component of W , calculate a variation Δw_i
 $\Delta w_i = \eta e x_i$

Where η is a perturbation value, usually it is a small positive value. Assume $\eta=0.01$

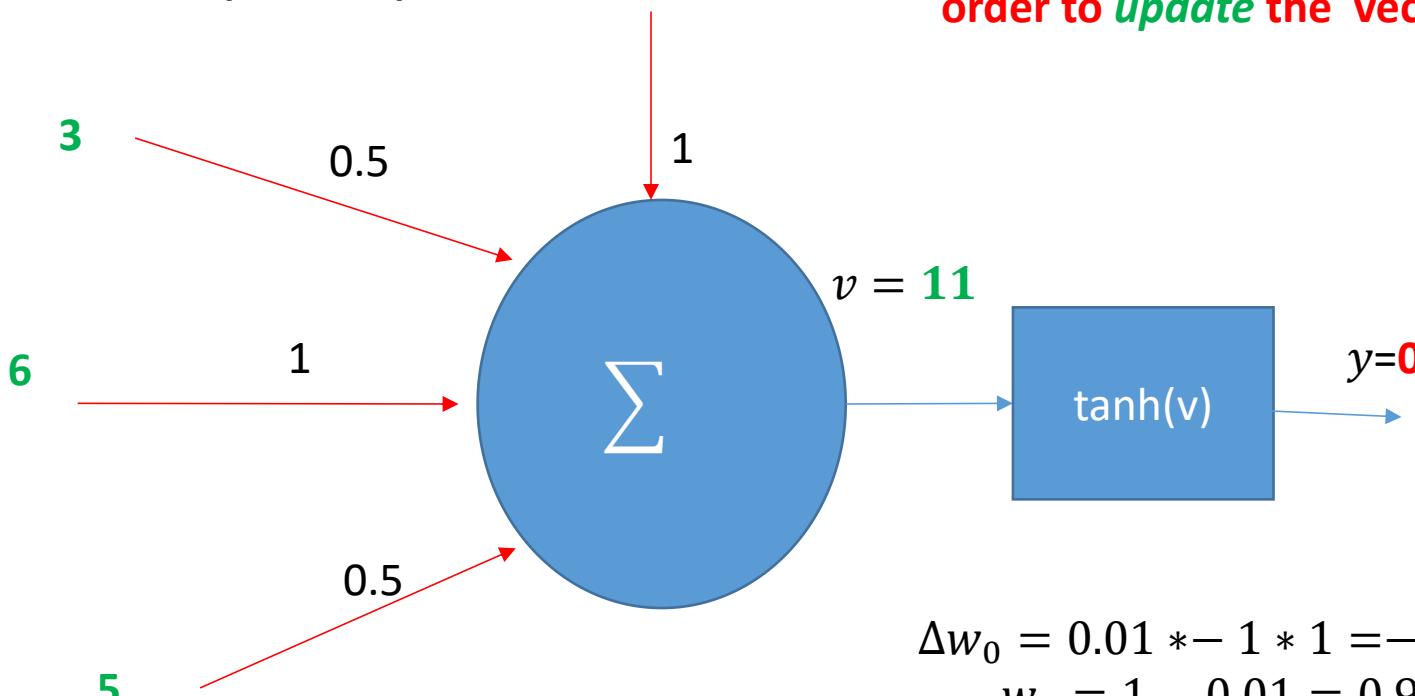
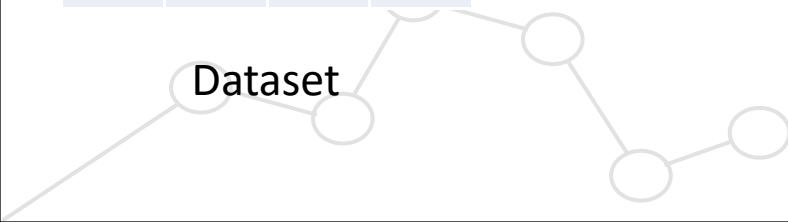
Update $w_i = w_i + \Delta w_i$



Artificial Neuron

- Training a neuron (perceptron).

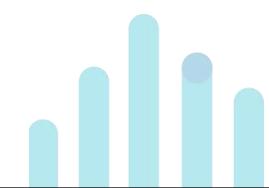
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$\Delta w_0 = 0.01 * -1 * 1 = -0,01$$

$$w_0 = 1 - 0,01 = 0,99$$

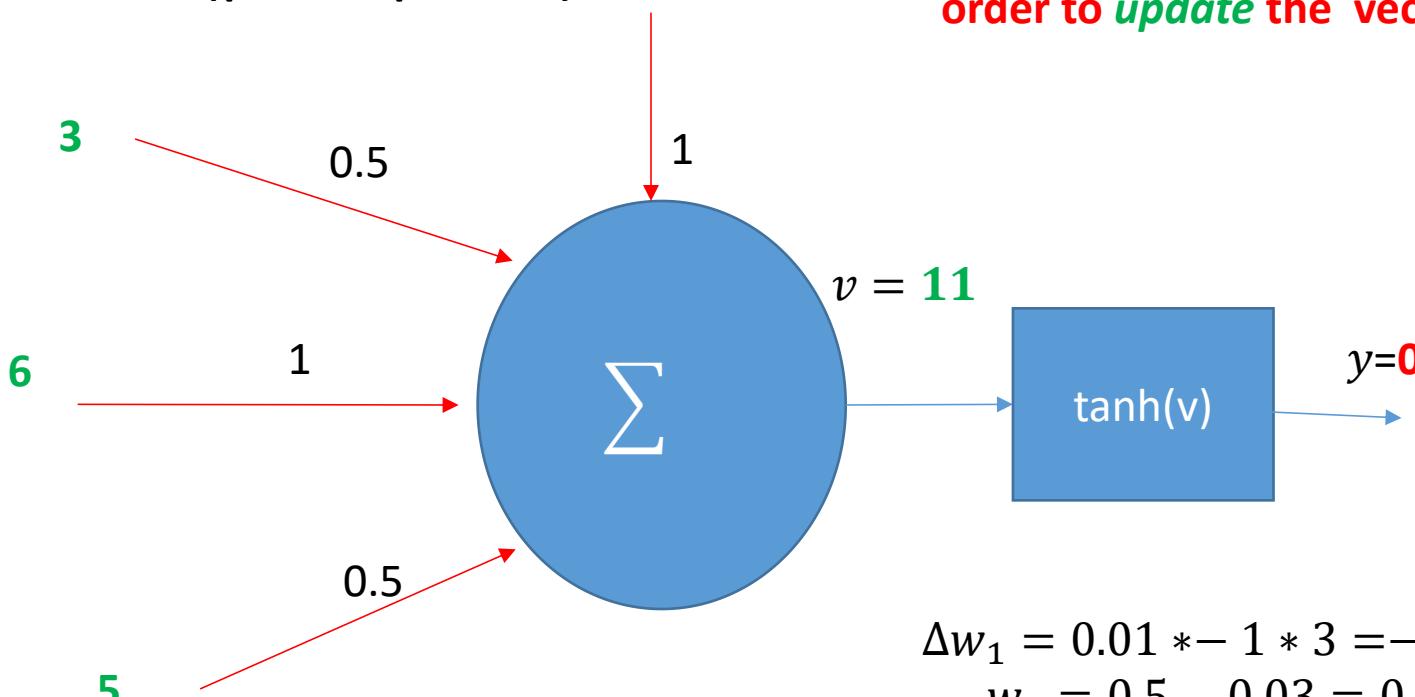
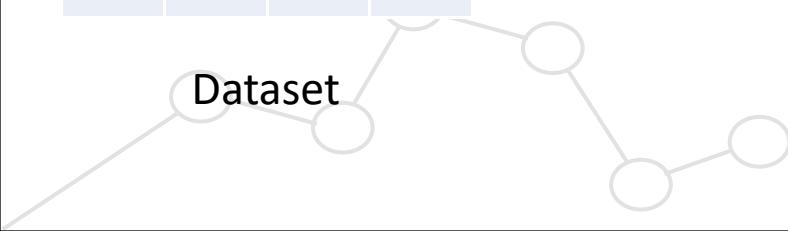
$$W = [0.99]$$



Artificial Neuron

- Training a neuron (perceptron).

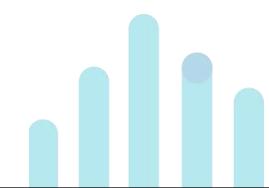
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$\Delta w_1 = 0.01 * -1 * 3 = -0.03$$

$$w_1 = 0.5 - 0.03 = 0.47$$

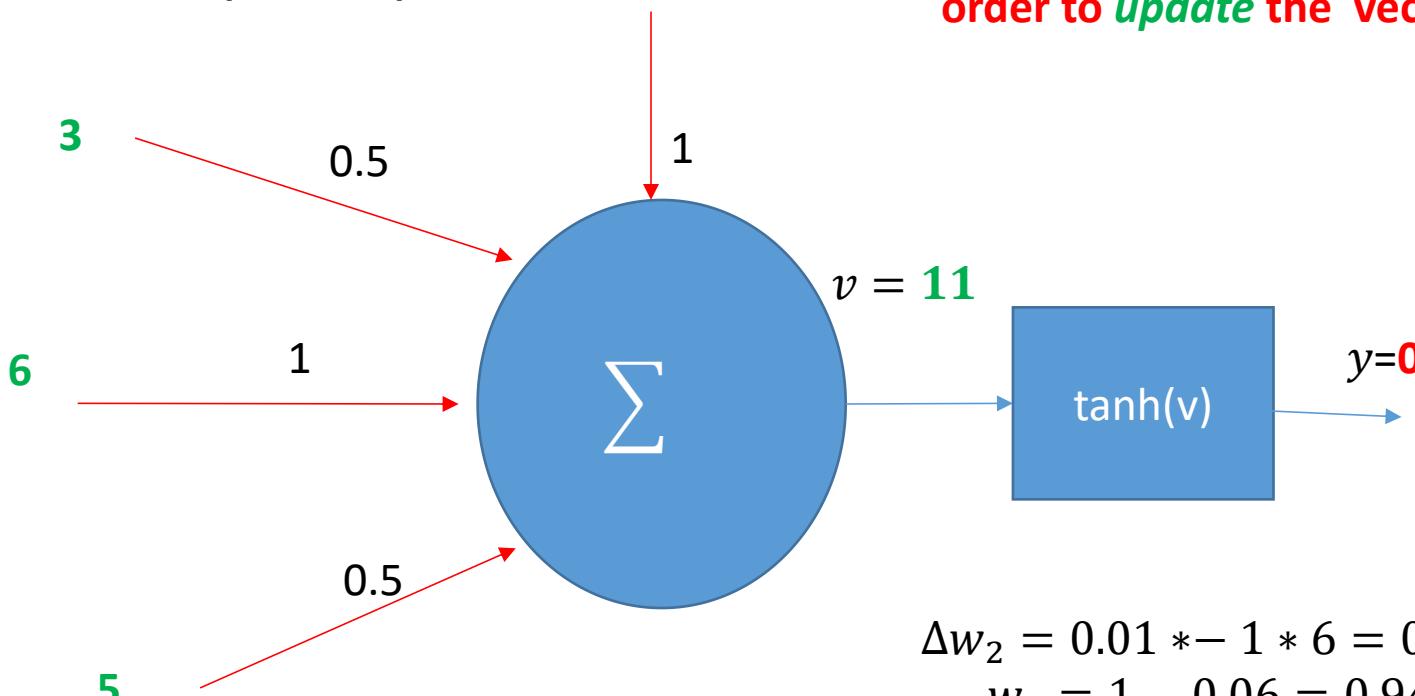
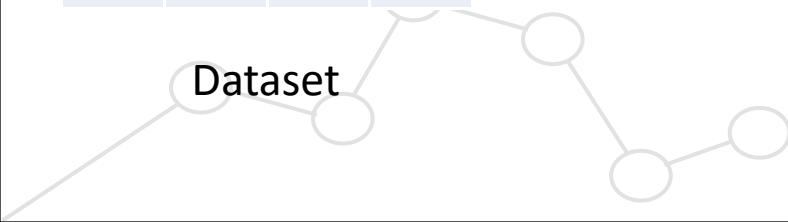
$$W = [0.97, 0.47,$$



Artificial Neuron

- Training a neuron (perceptron).

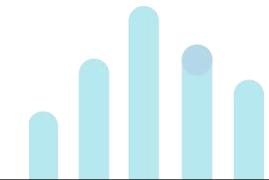
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$\Delta w_2 = 0.01 * -1 * 6 = 0.06$$

$$w_2 = 1 - 0.06 = 0.94$$

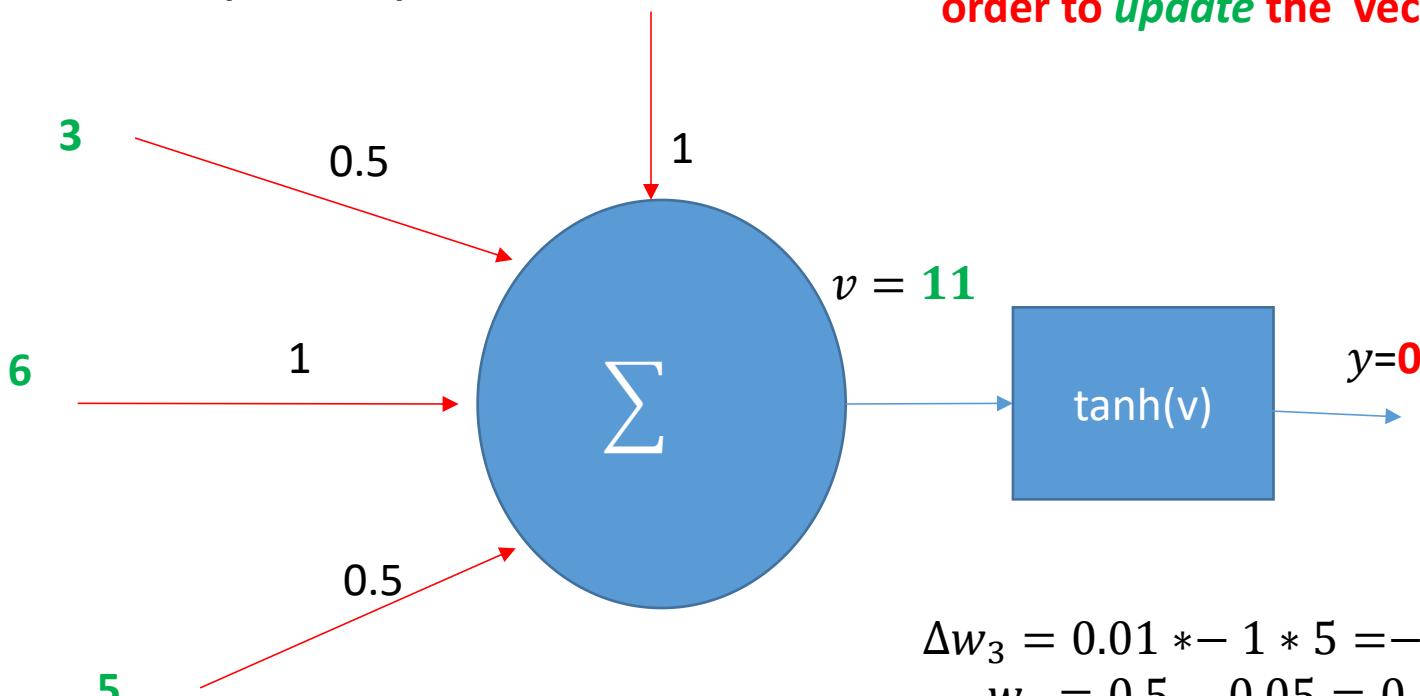
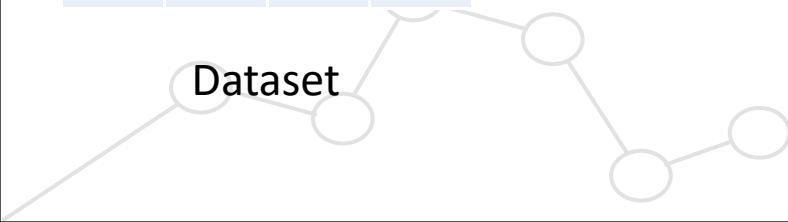
$$W = [0.97, 0.44, 0.94]$$



Artificial Neuron

- Training a neuron (perceptron).

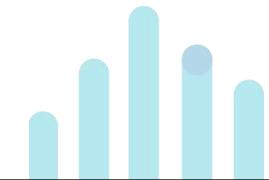
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	0
6	8	5	0
7	9	7	1
8	0	8	1



$$\Delta w_3 = 0.01 * -1 * 5 = -0.05$$

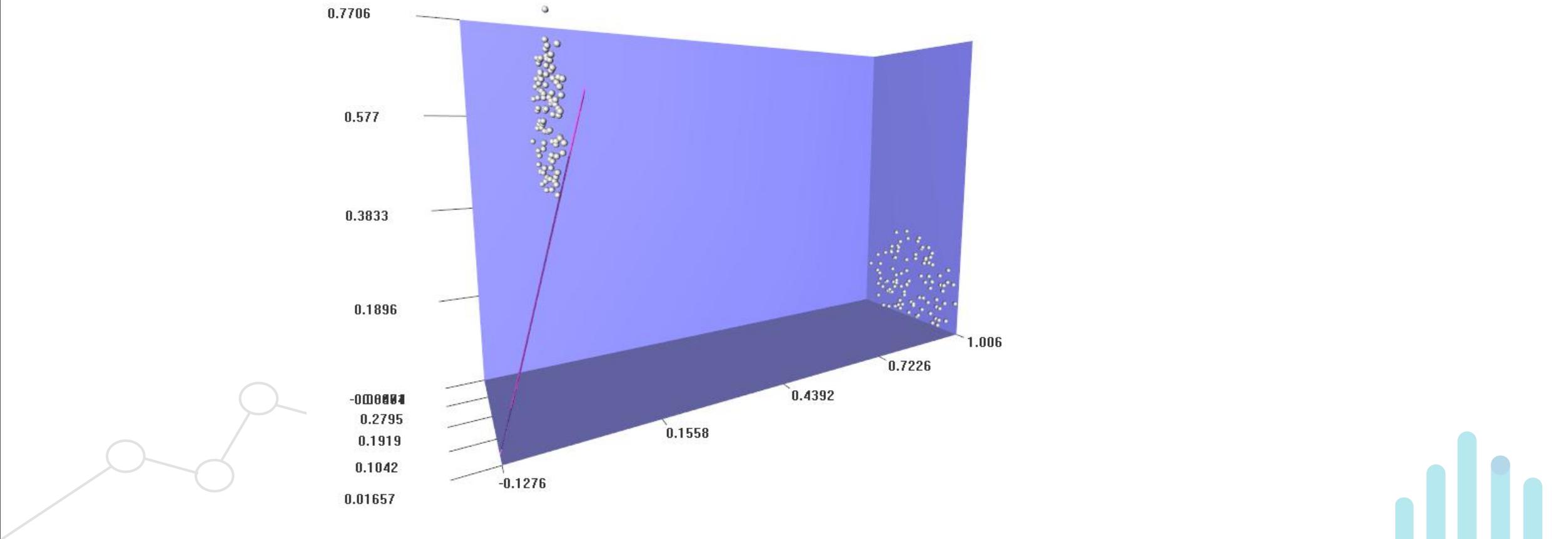
$$w_3 = 0.5 - 0.05 = 0.45$$

$$W = [0.97, 0.44, 0.94, 0.45]$$



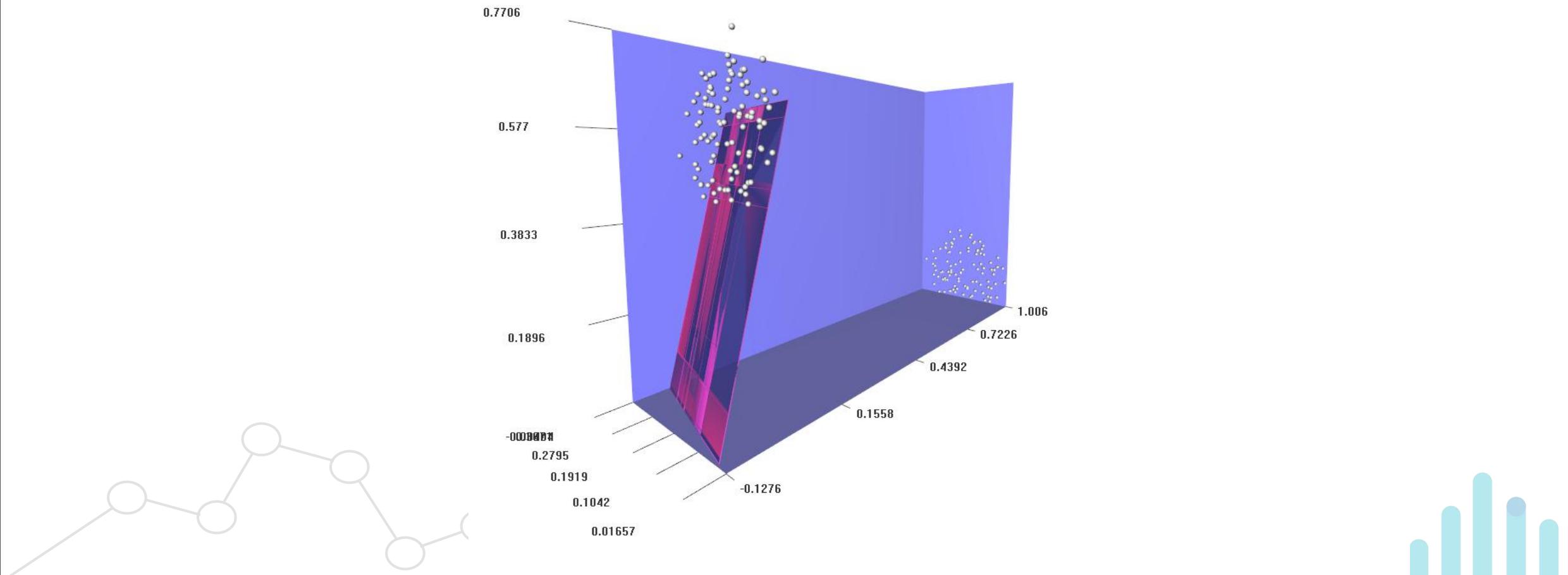
Artificial Neuron

- Example of classification based on perceptron.



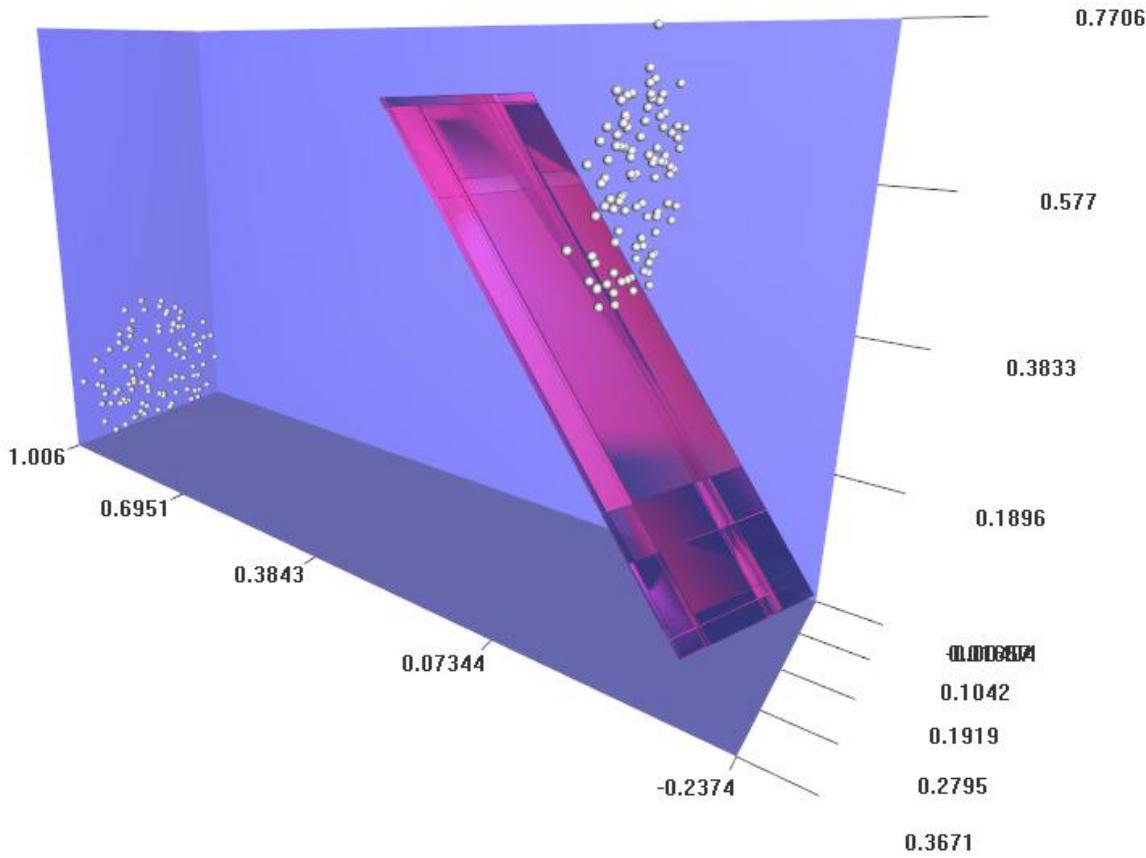
Artificial Neuron

- Example of classification based on perceptron.



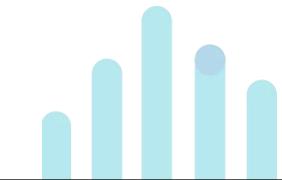
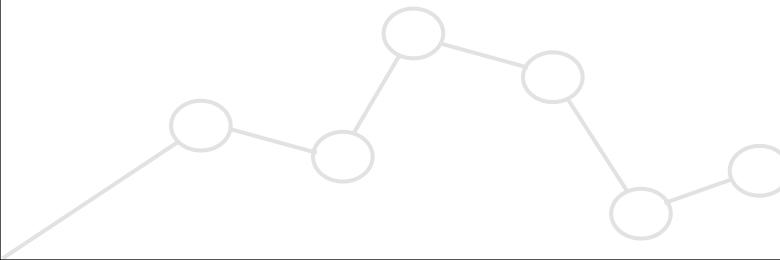
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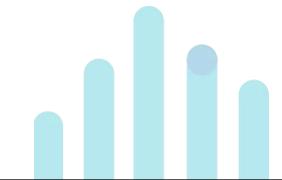
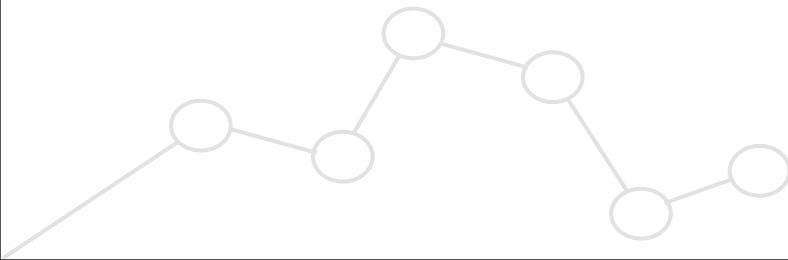
Artificial Neuron

- Although the perceptron rule finds a successful weight vector when the training n examples are linearly separable, it can fail to converge if the examples are not linearly separable.
- A second training rule, called the ***delta rule***, is designed to overcome this difficulty.
- If the **training examples are not linearly separable**, the delta rule converges toward a **best-fit approximation** to the target concept.



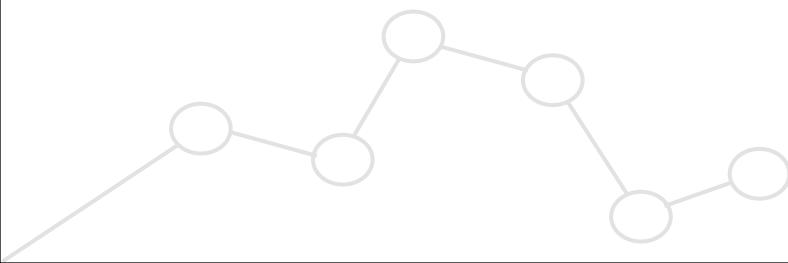
Artificial Neuron (The Delta Rule)

- The key idea behind the delta rule is to use ***gradient descent*** to search the hypothesis space of possible weight vectors to find the weights that best fit the training examples.
- This rule is important because gradient descent provides the basis for the **BACKPROPAGATION** algorithm, which can learn networks with many interconnected neurons.

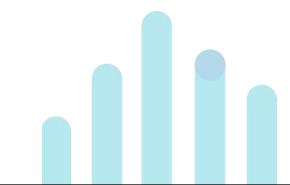


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- This rule is important because gradient descent provides the basis for the **BACKPROPAGATION** algorithm, which can learn networks with many interconnected neurons.
- The delta training rule is best understood by considering the task of training an perceptron; that is, **a linear unit** for which the output o is given by:



$$o(\vec{x}) = \vec{w} \cdot \vec{x}$$

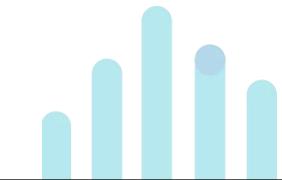
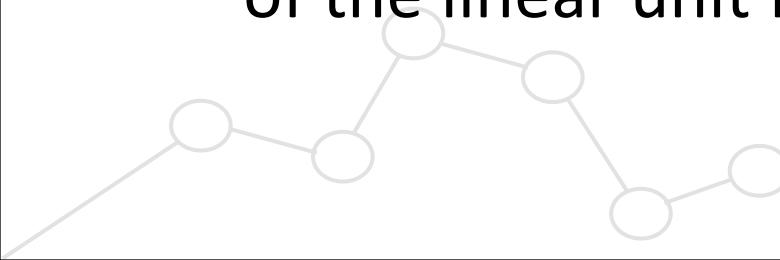


Artificial Neuron (The Delta Rule)

- The key idea behind the delta rule is to use ***gradient descent*** to search the hypothesis space of possible weight vectors to find the weights that best fit the training examples.
- We can derive a weight learning rule for linear units, specifying a measure for the ***training error*** of the weight vector, relative to the training examples.

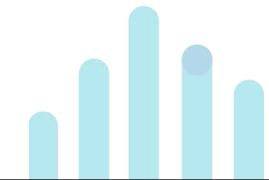
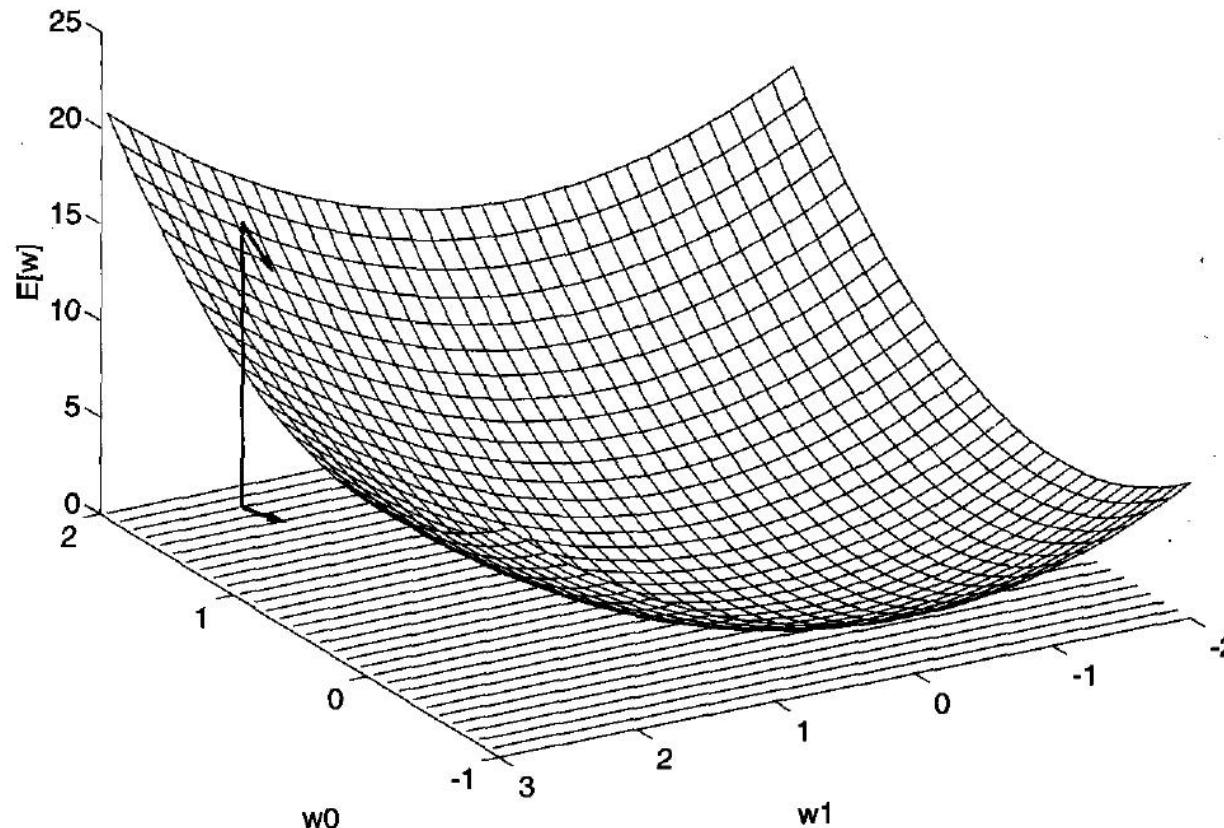
$$E(\vec{w}) \equiv \frac{1}{2} \sum_{d \in D} (t_d - o_d)^2$$

- Where t_d and o_d are the target output for training example the output of the linear unit for training example d in a dataset D.



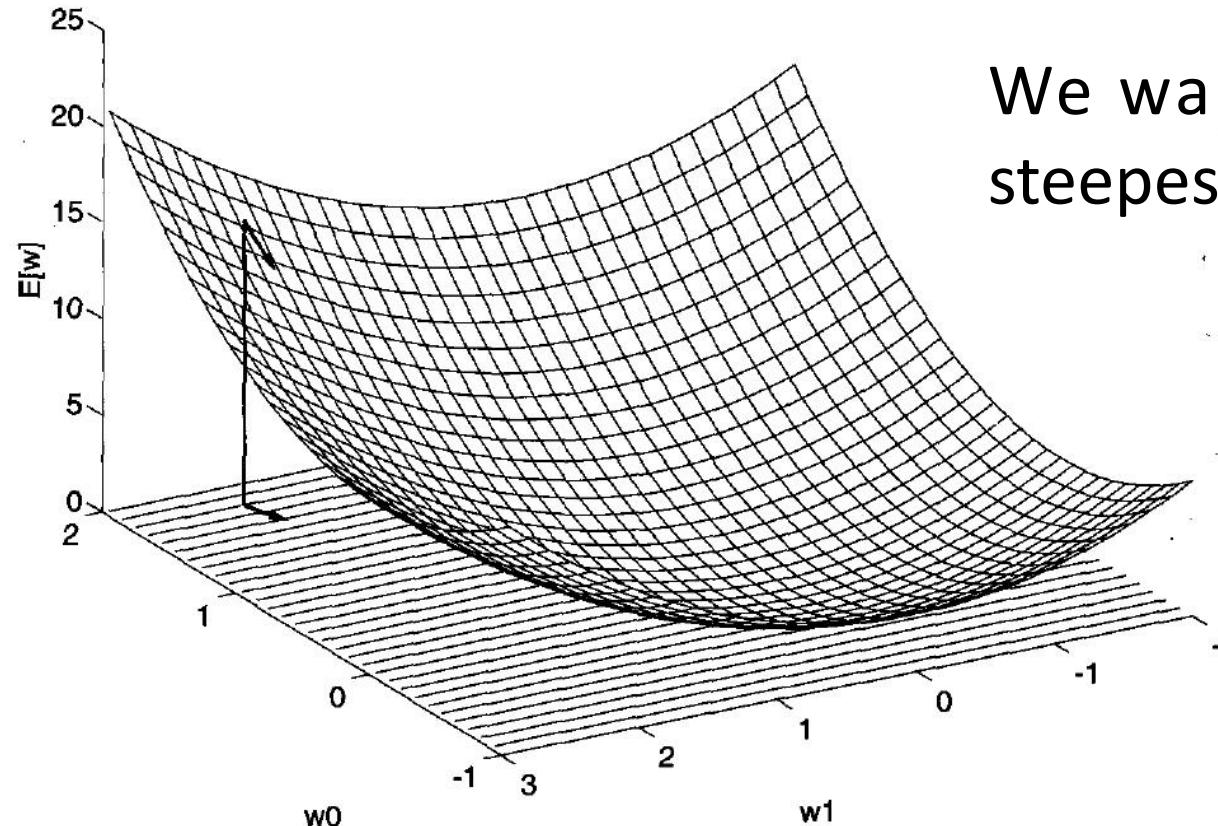
Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method

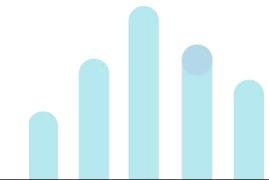
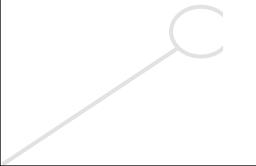


Artificial Neuron (The Delta Rule)

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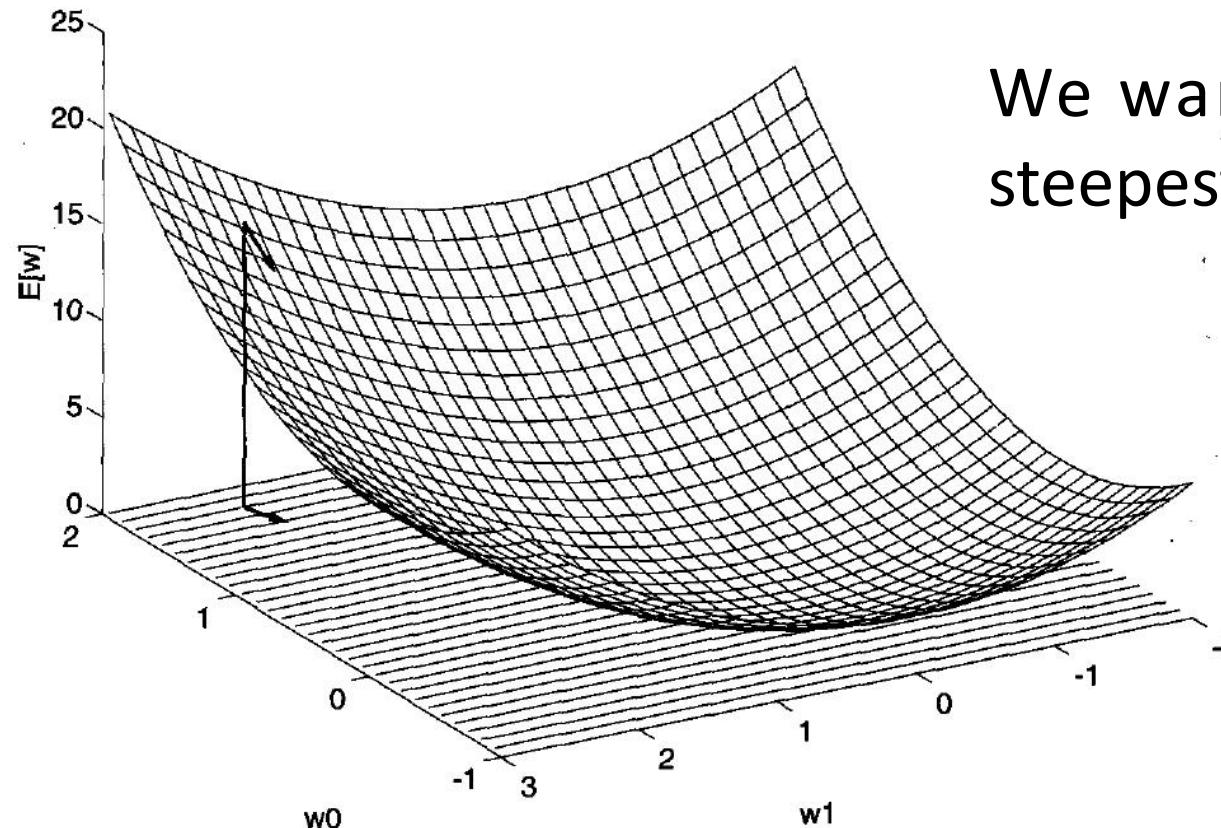


We want to calculate the direction of steepest descent along the error surface.



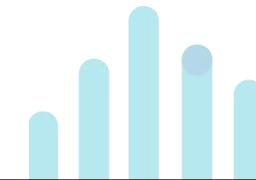
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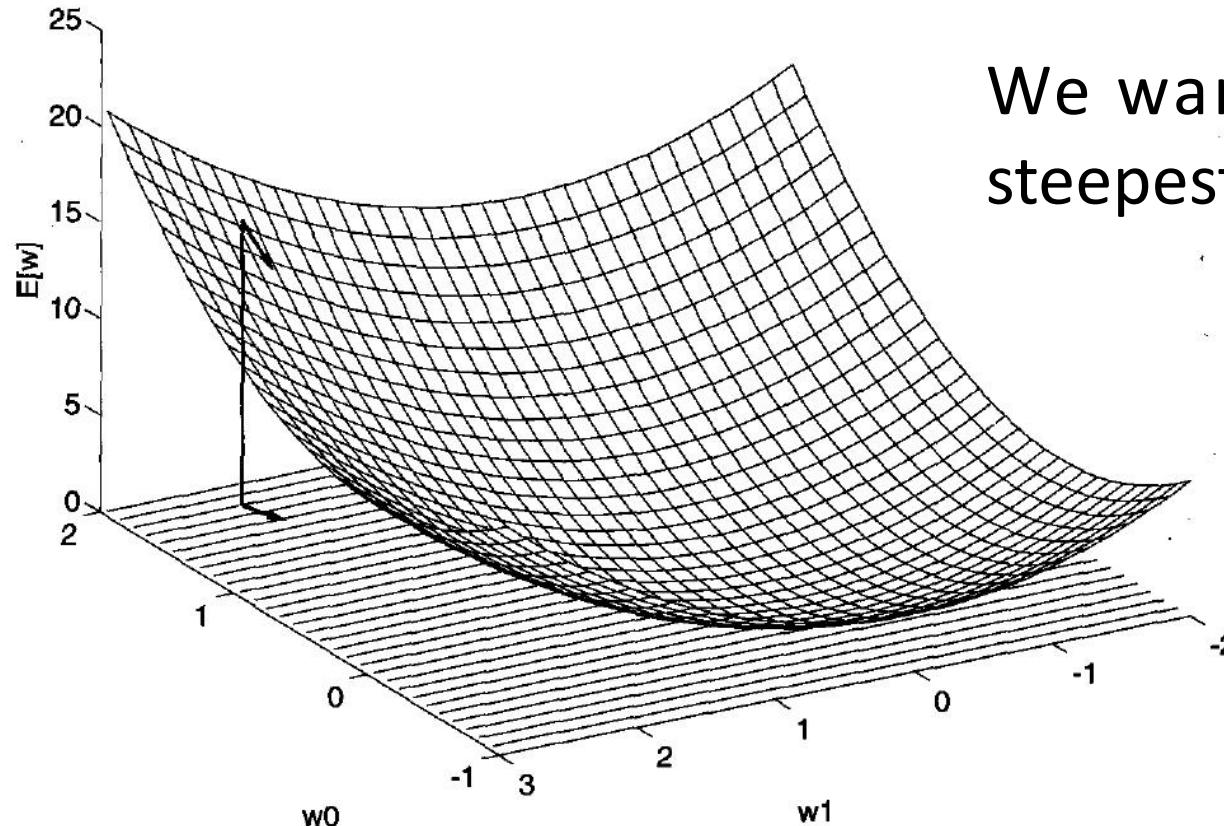
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$$\nabla E(\vec{w})$$



Artificial Neuron (The Delta Rule)

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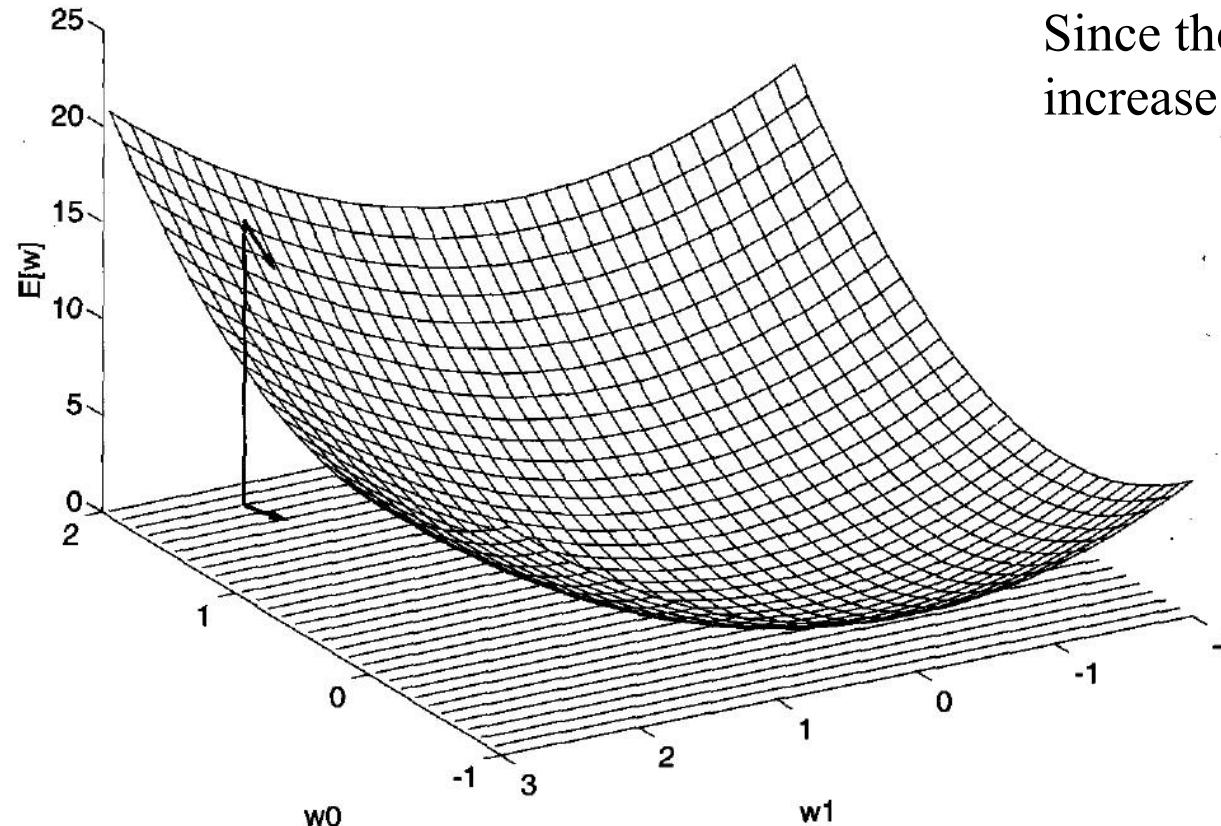
We want to calculate the direction of steepest descent along the error surface.

$$\nabla E(\vec{w}) \equiv \left[\frac{\partial E}{\partial w_0}, \frac{\partial E}{\partial w_1}, \dots, \frac{\partial E}{\partial w_n} \right]$$



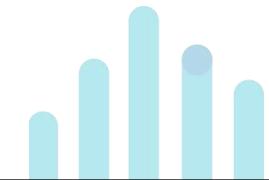
Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method



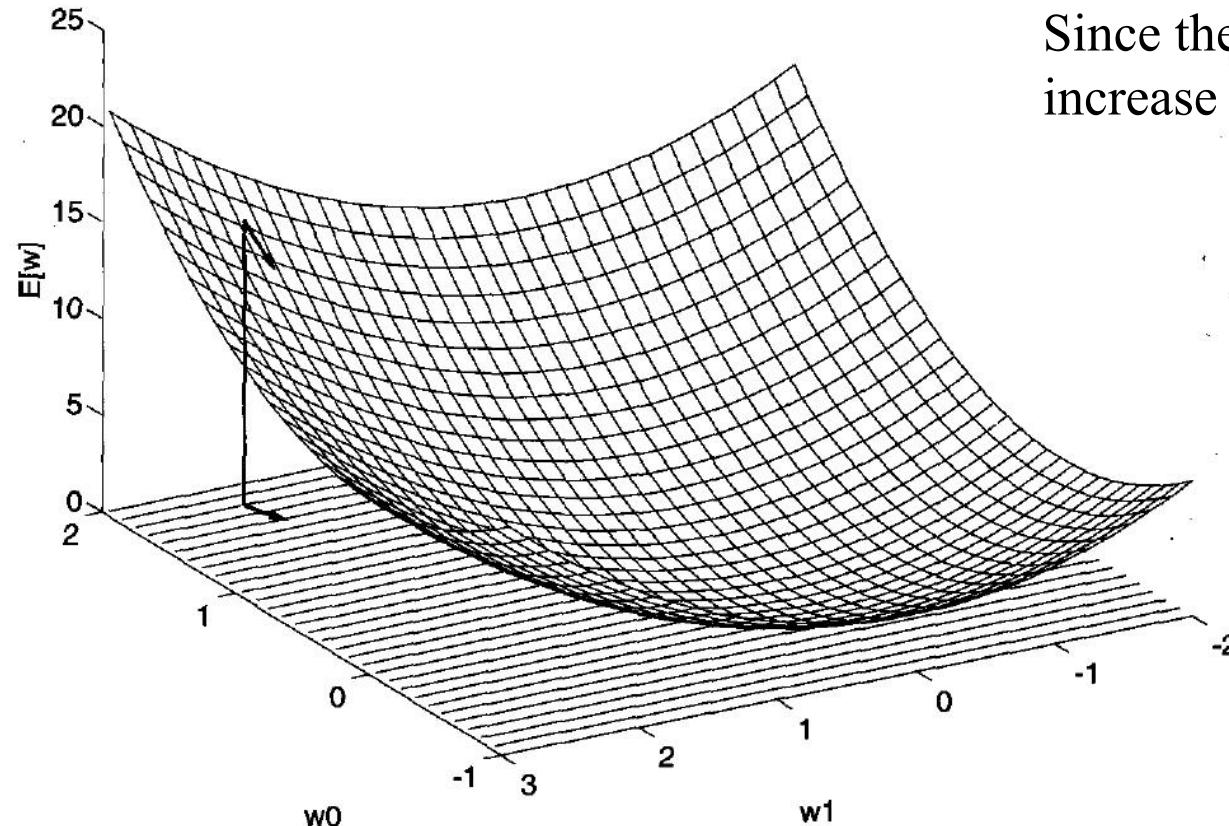
Since the gradient specifies the direction of steepest increase of E , the training rule for gradient descent is:

$$\vec{w} \leftarrow \vec{w} + \Delta \vec{w}$$



Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method

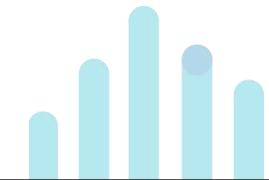


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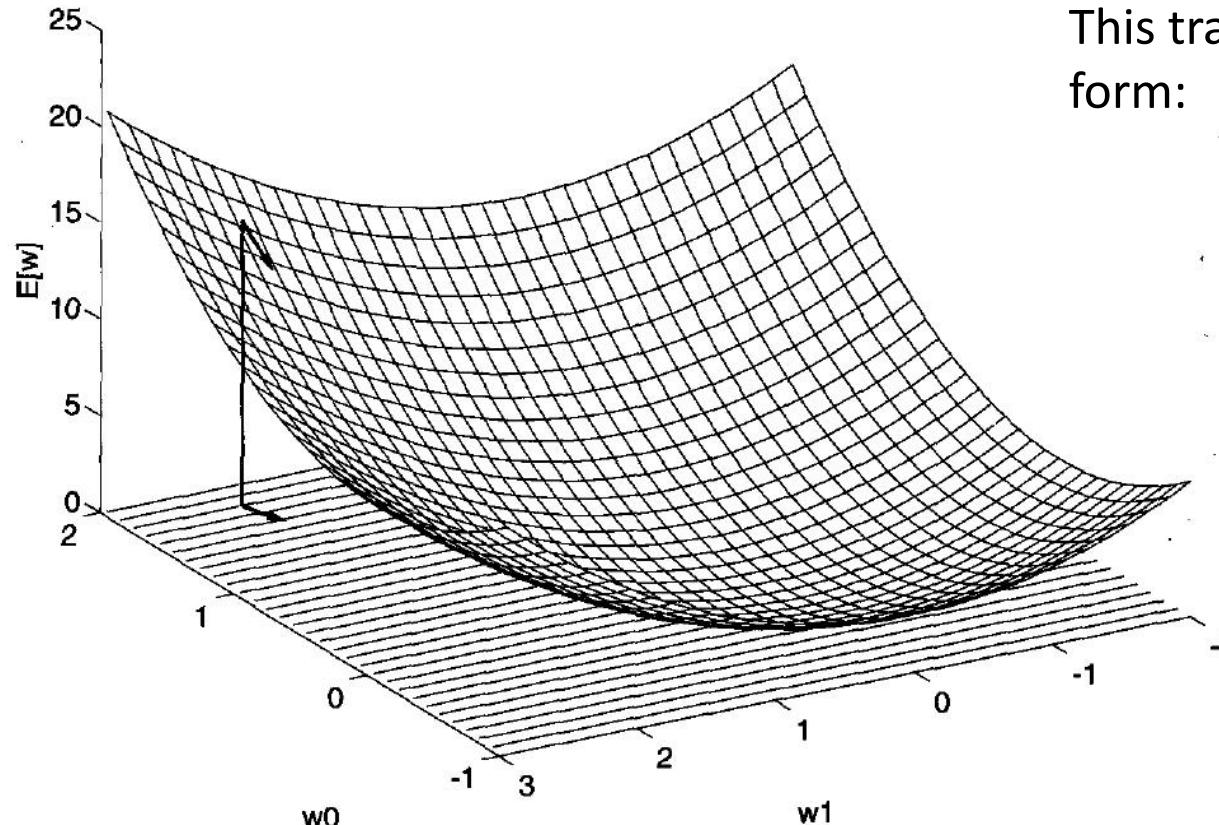
where

$$\Delta \vec{w} = -\eta \nabla E(\vec{w})$$



Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method



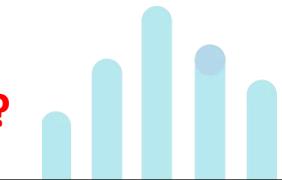
This training rule can also be written in its component form:

$$\vec{w} \leftarrow \vec{w} + \Delta \vec{w}$$

where

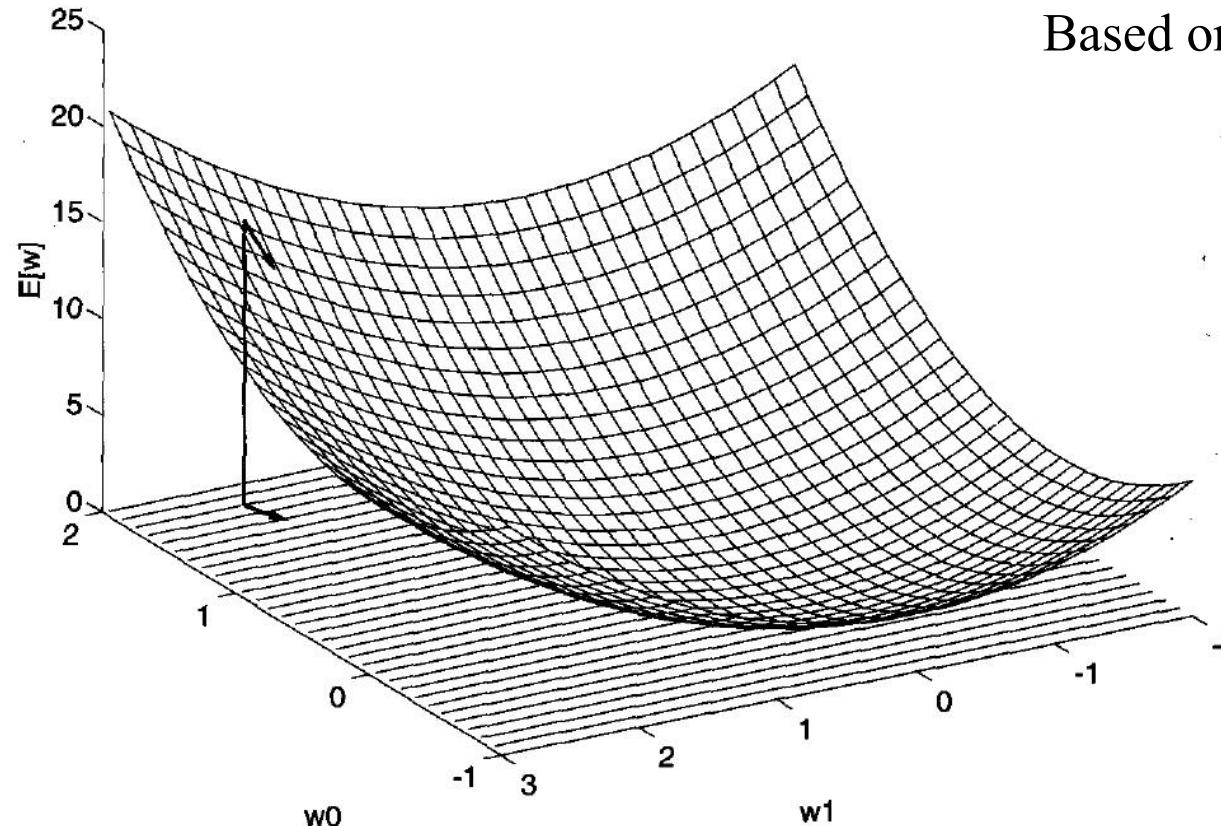
$$\Delta \vec{w} = -\eta \nabla E(\vec{w})$$

What it means the negative sign?



Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method



Based on the above the component representation is:

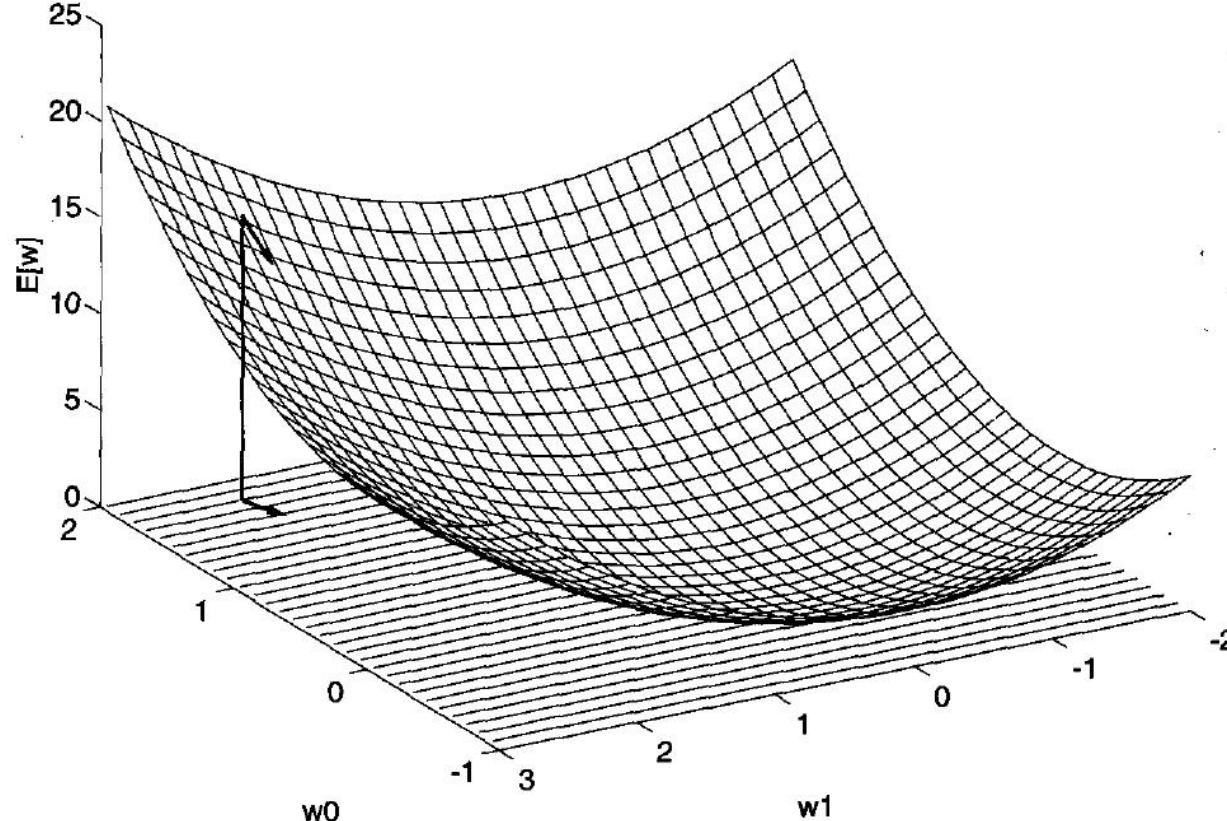
$$w_i \leftarrow w_i + \Delta w_i$$

where

$$\Delta w_i = -\eta \frac{\partial E}{\partial w_i}$$

Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method

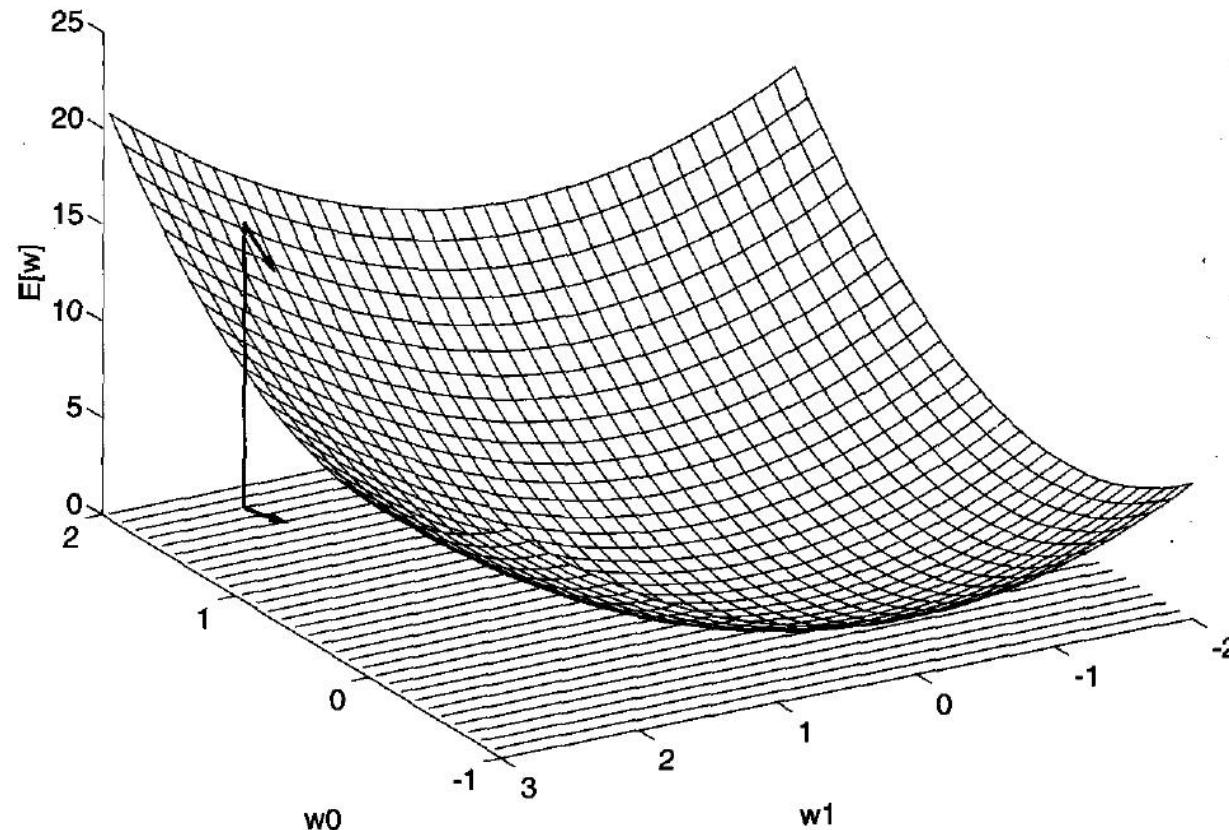


$$\Delta w_i = -\eta \frac{\partial E}{\partial w_i}$$

$$\frac{\partial E}{\partial w_i} = \frac{\partial}{\partial w_i} \frac{1}{2} \sum_{d \in D} (t_d - o_d)^2$$

Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method



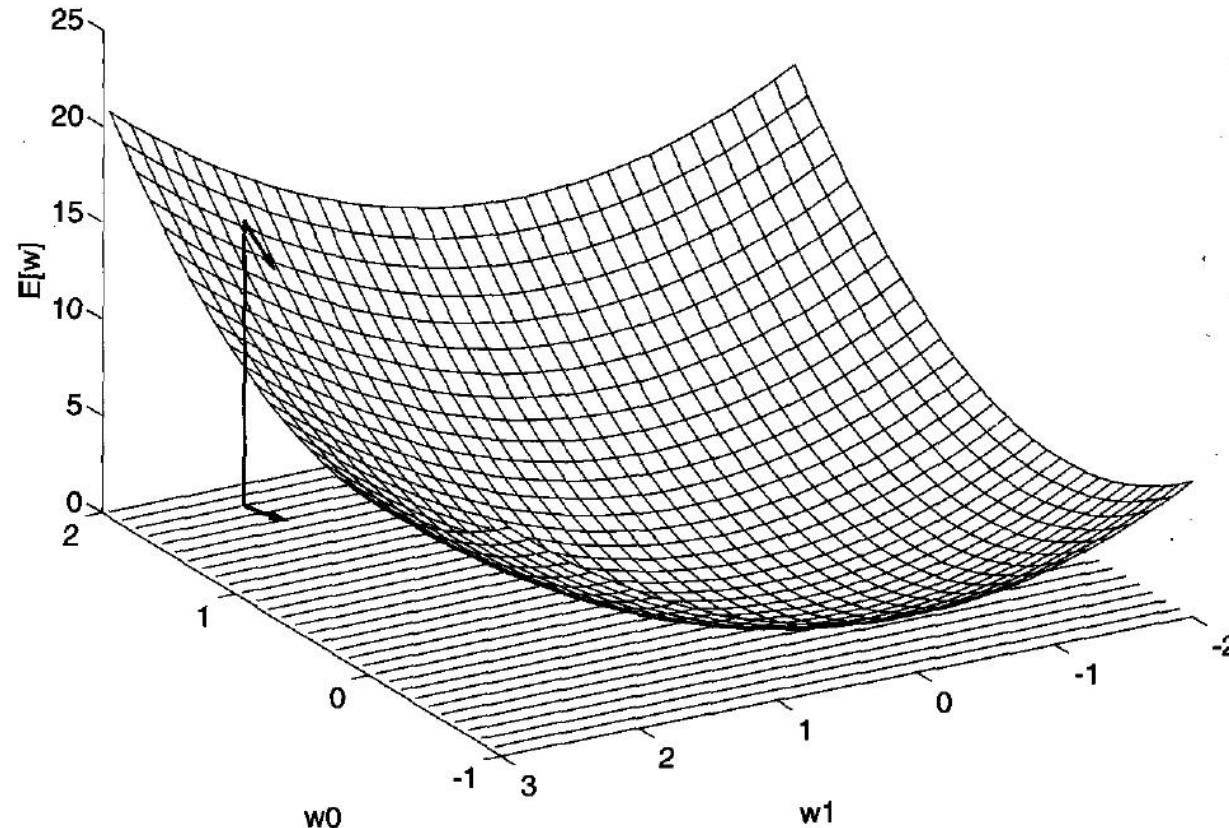
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Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method



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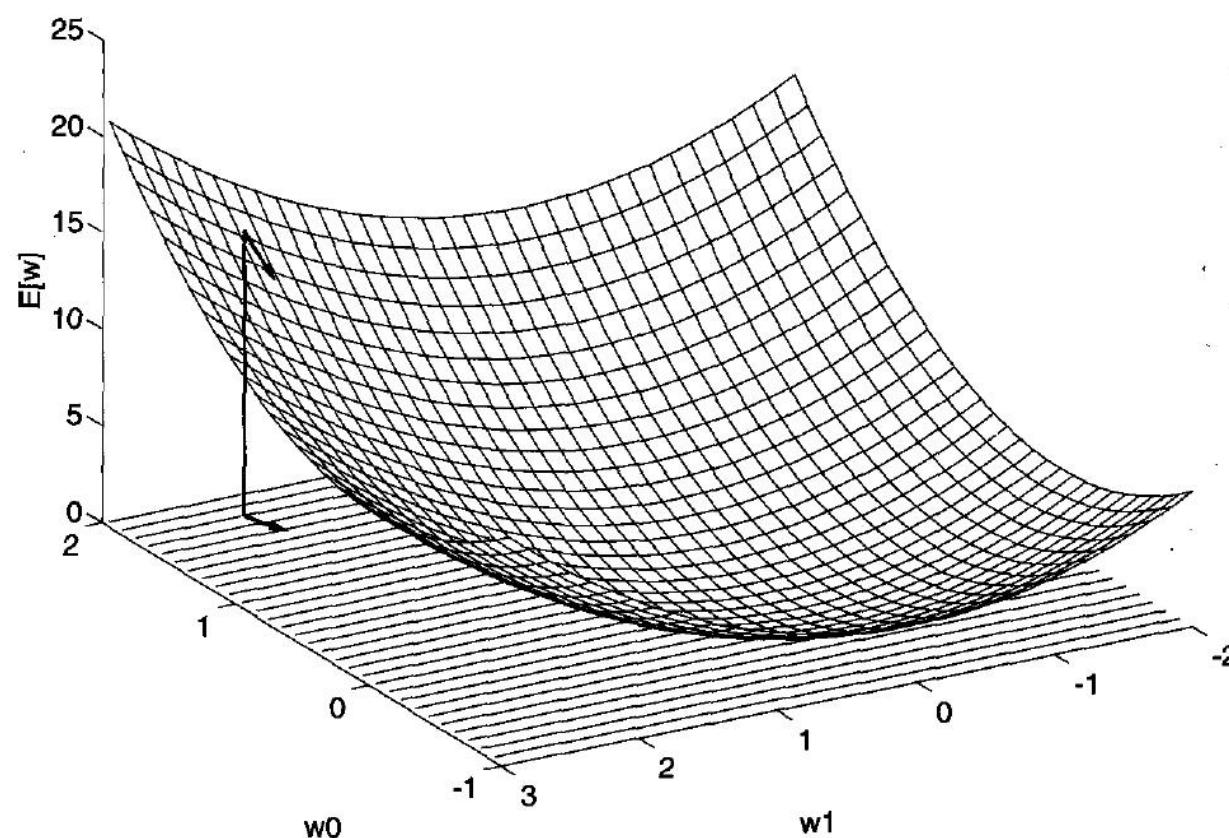
$$\frac{\partial E}{\partial w_i} = \frac{\partial}{\partial w_i} \frac{1}{2} \sum_{d \in D} (t_d - o_d)^2$$

$$= \frac{1}{2} \sum_{d \in D} \frac{\partial}{\partial w_i} (t_d - o_d)^2$$

$$= \frac{1}{2} \sum_{d \in D} 2(t_d - o_d) \frac{\partial}{\partial w_i} (t_d - o_d)$$

Artificial Neuron (The Delta Rule)

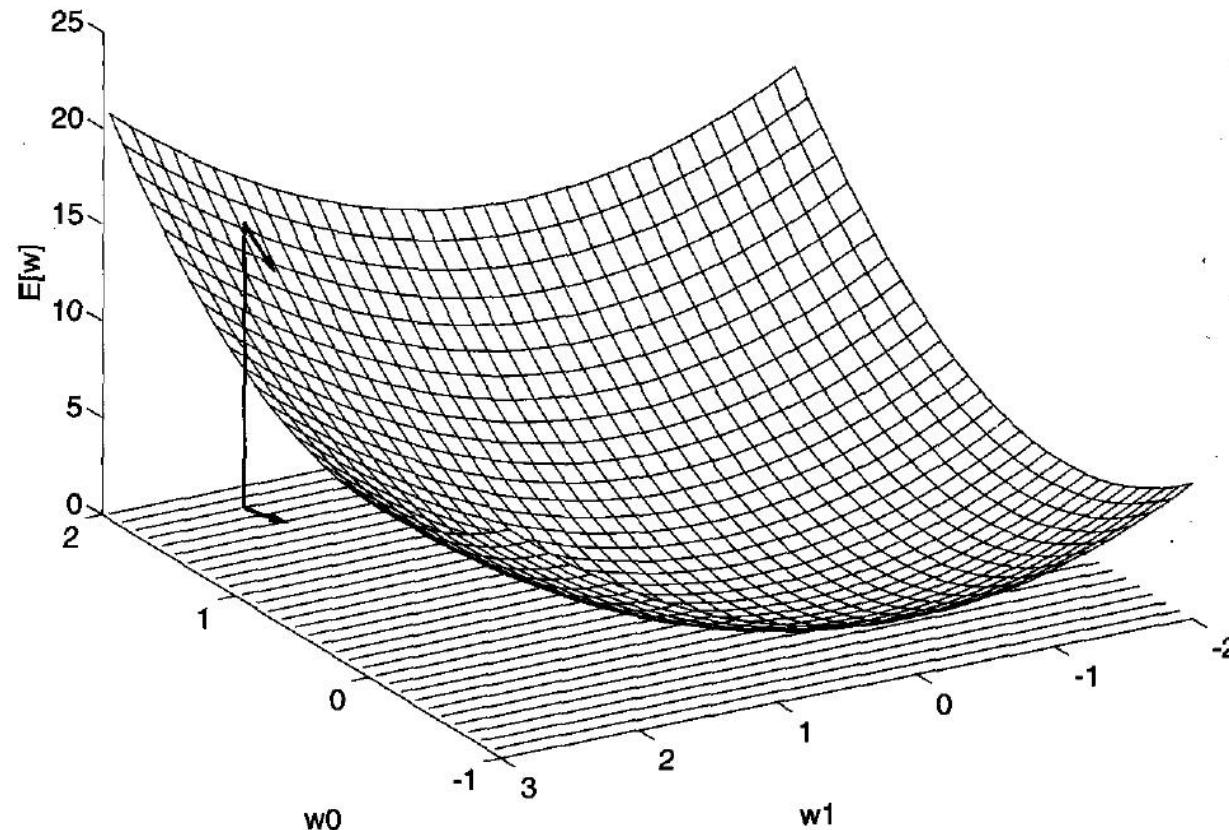
- Visualizing the gradient descendent method



$$\begin{aligned}
 E[w] &= \frac{1}{2} \sum_{d \in D} \frac{\partial}{\partial w_i} (t_d - o_d)^2 \\
 &= \frac{1}{2} \sum_{d \in D} 2(t_d - o_d) \frac{\partial}{\partial w_i} (t_d - o_d) \\
 &= \sum_{d \in D} (t_d - o_d) \frac{\partial}{\partial w_i} (t_d - \vec{w} \cdot \vec{x}_d)
 \end{aligned}$$

Artificial Neuron (The Delta Rule)

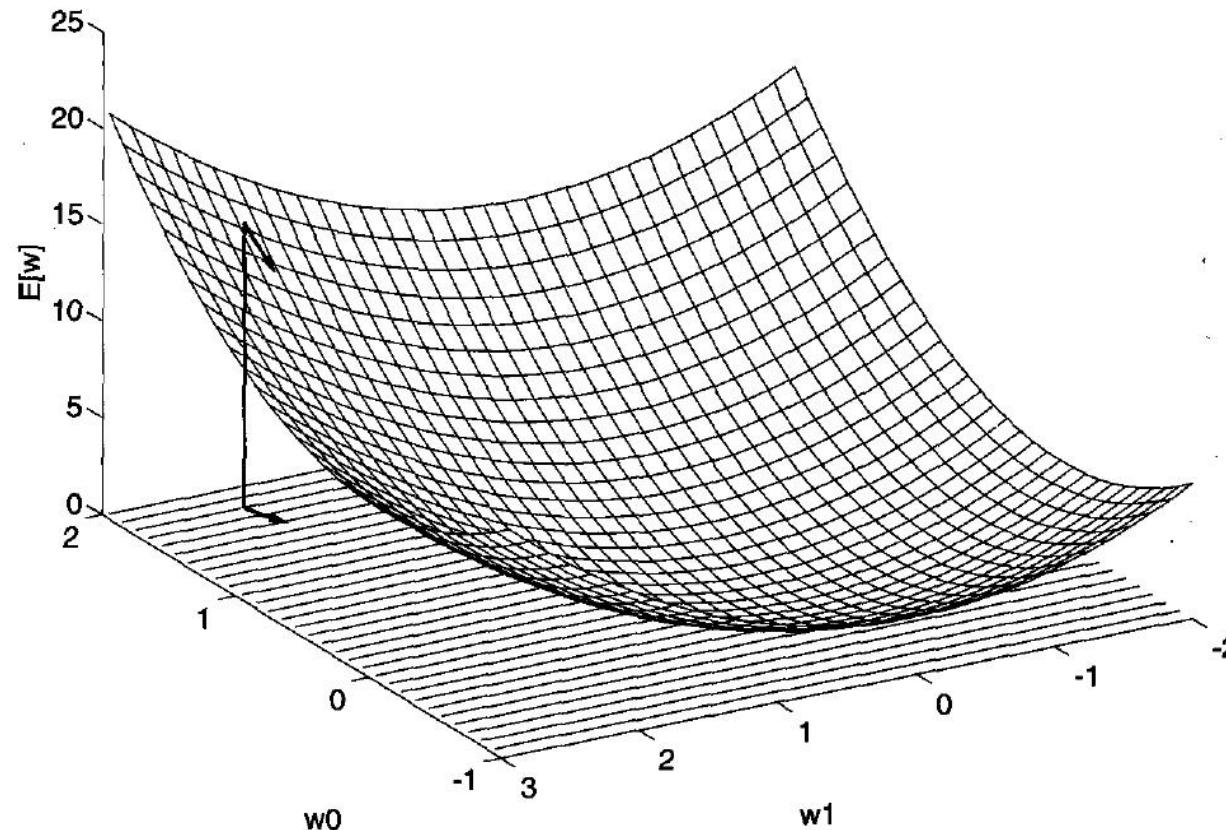
- Visualizing the gradient descendent method



$$\begin{aligned}
 E(w) &= \frac{1}{2} \sum_{d \in D} \frac{\partial}{\partial w_i} (t_d - o_d)^2 \\
 &= \frac{1}{2} \sum_{d \in D} 2(t_d - o_d) \frac{\partial}{\partial w_i} (t_d - o_d) \\
 &= \sum_{d \in D} (t_d - o_d) \frac{\partial}{\partial w_i} (t_d - \vec{w} \cdot \vec{x}_d) \\
 \frac{\partial E}{\partial w_i} &= \sum_{d \in D} (t_d - o_d)(-x_{id})
 \end{aligned}$$

Artificial Neuron (The Delta Rule)

- Visualizing the gradient descendent method



Thus:

$$\Delta w_i = -\eta \frac{\partial E}{\partial w_i}$$

$$\Delta w_i = \eta \sum_{d \in D} (t_d - o_d) x_{id}$$

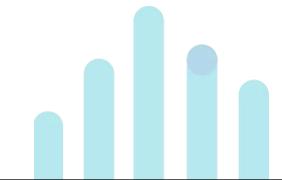
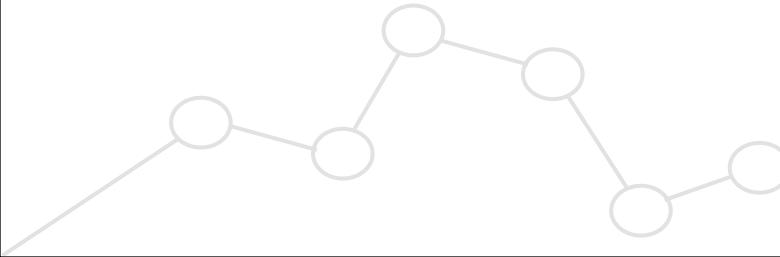
Exercises

Exercise 1

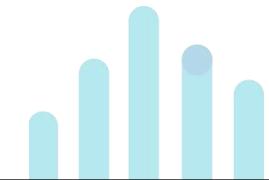
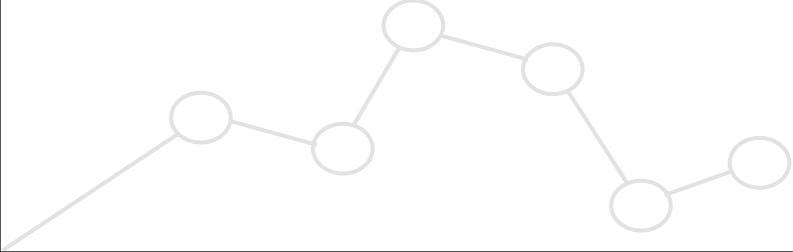
- Review the script in which a perceptron implementation is shown.

Exercise 2

- Review the script using a perceptron implementation based on **sklearn** API



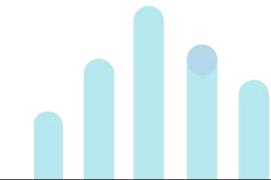
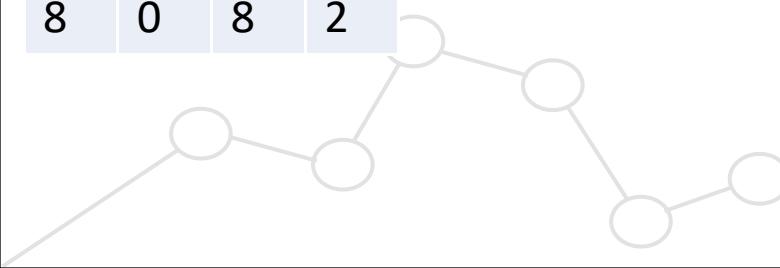
Multilayer Neural Networks



Multilayer networks

- Assume a problem that requires to learn about a set of patterns classified into **three classes**. How to solve this learning problem through artificial neurons?

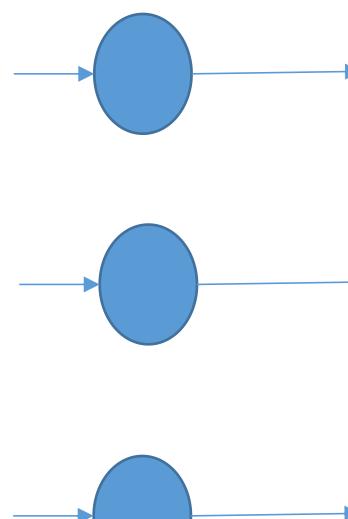
X1	X2	X3	c
2	7	1	0
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5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



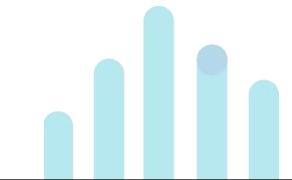
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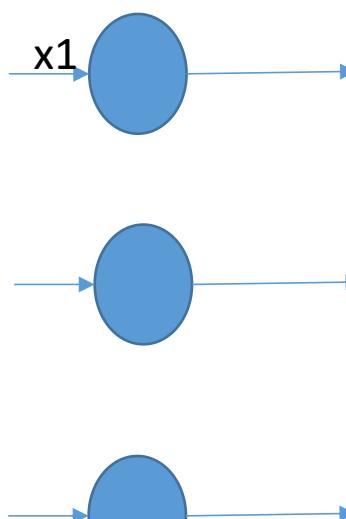
For each feature, a neuron is defined.



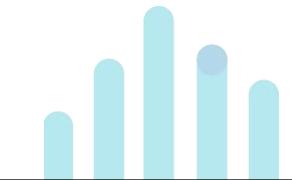
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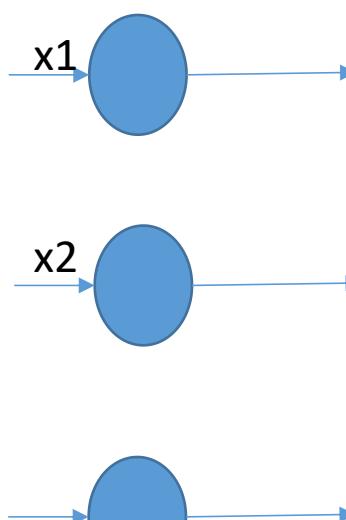
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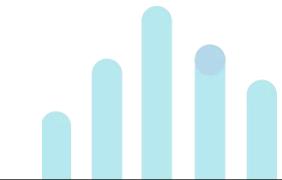
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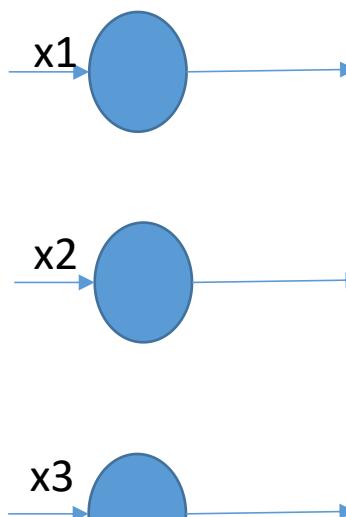
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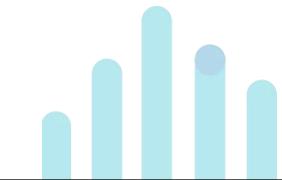
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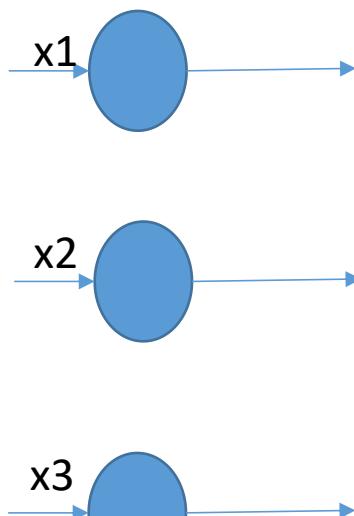
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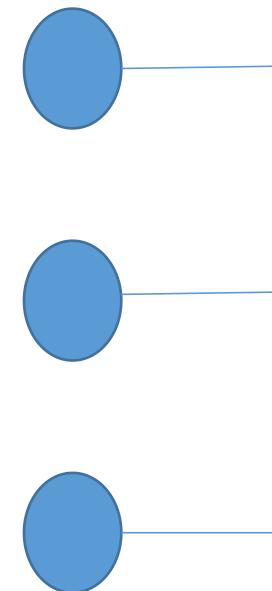
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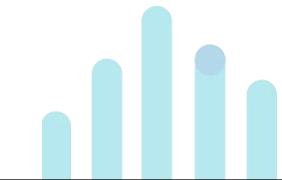
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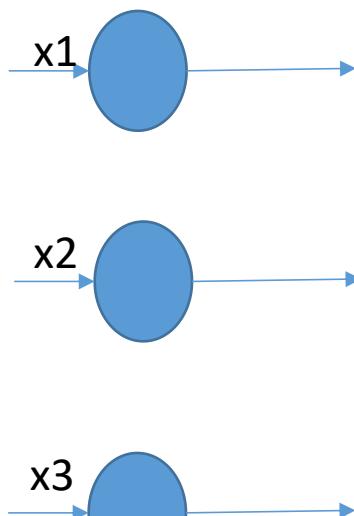
A set of neurons that encodes the class label of the input pattern is created.



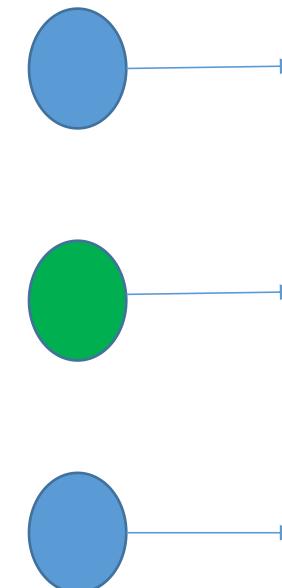
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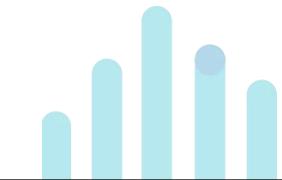


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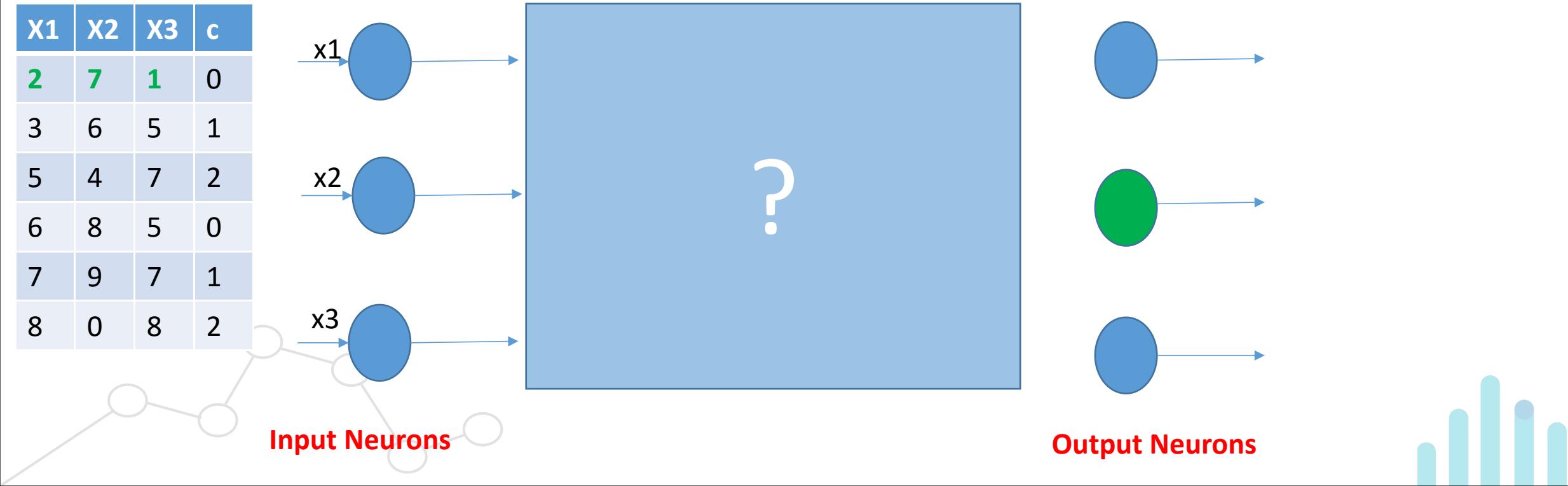
A set of neurons that represent the class label of the input pattern is created.

Note that only one neuron will be activated



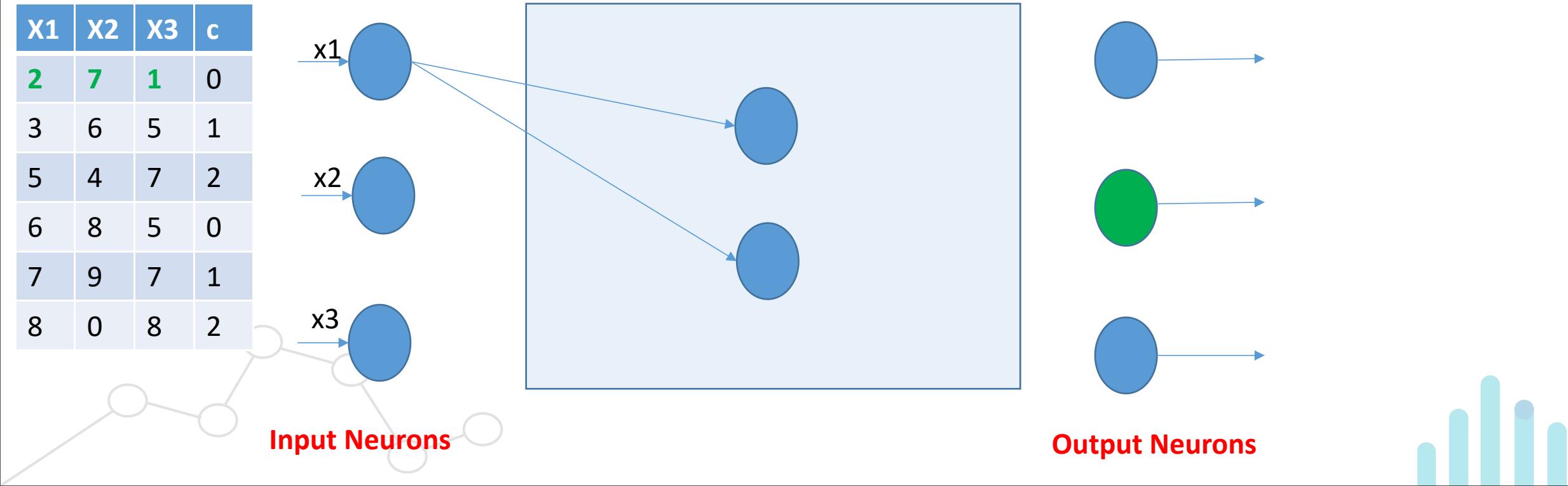
Multilayer networks

- The mystery box represent a set of neurons and interconnections that propagate the signals from input neurons to output neurons.



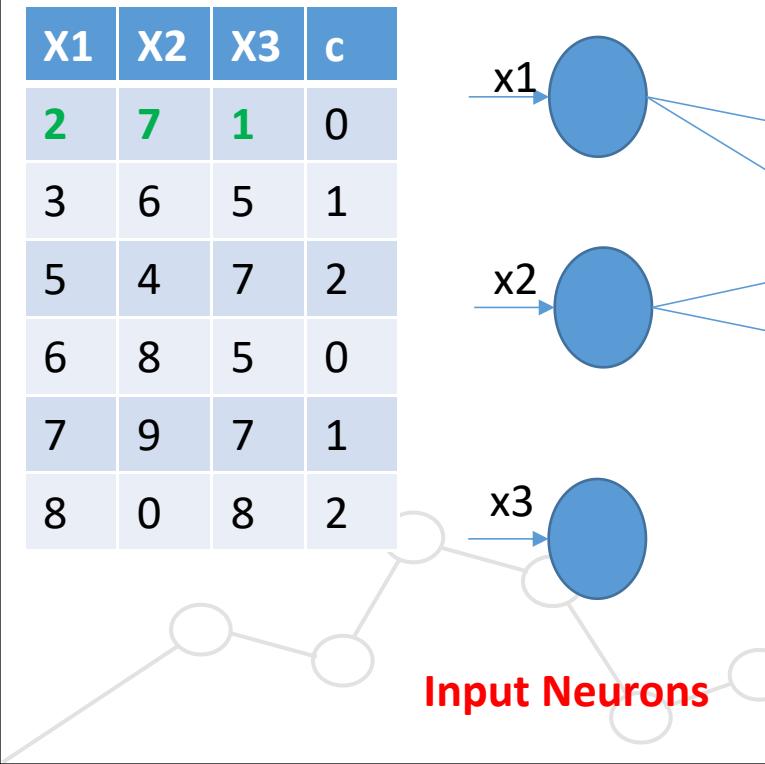
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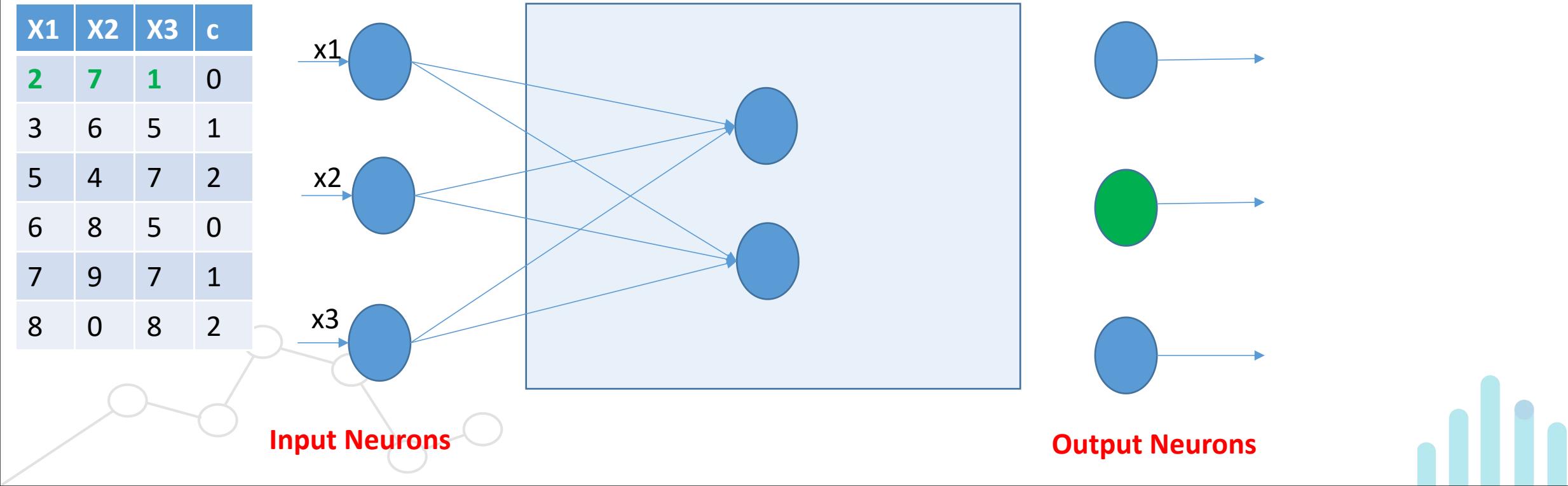
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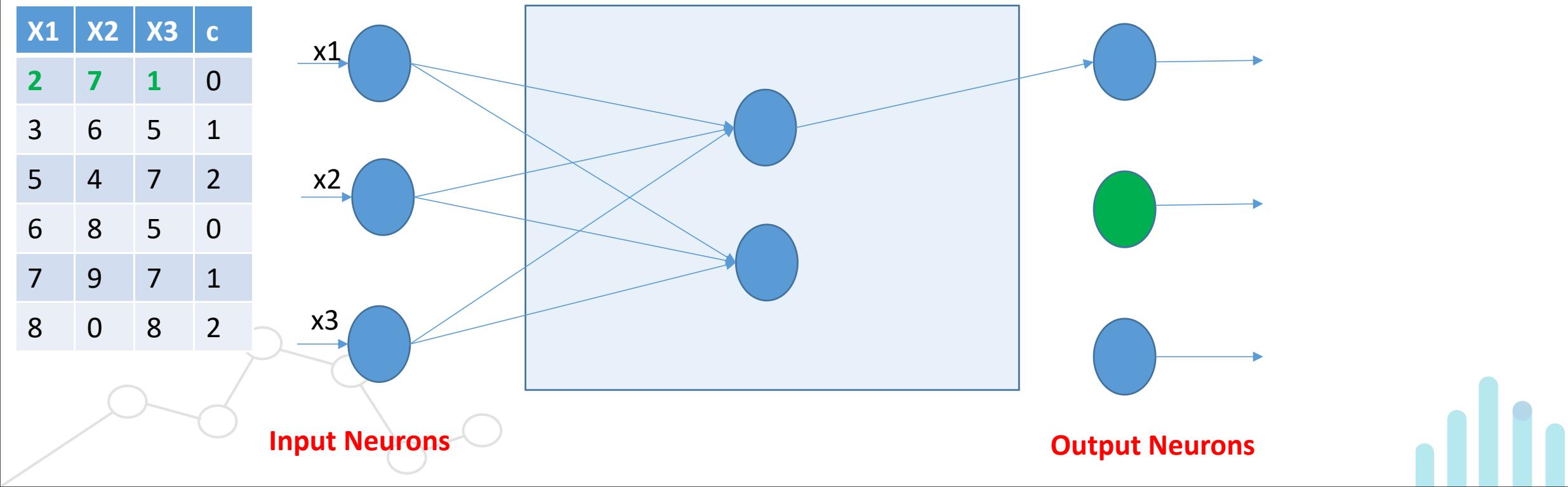
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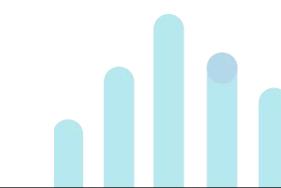
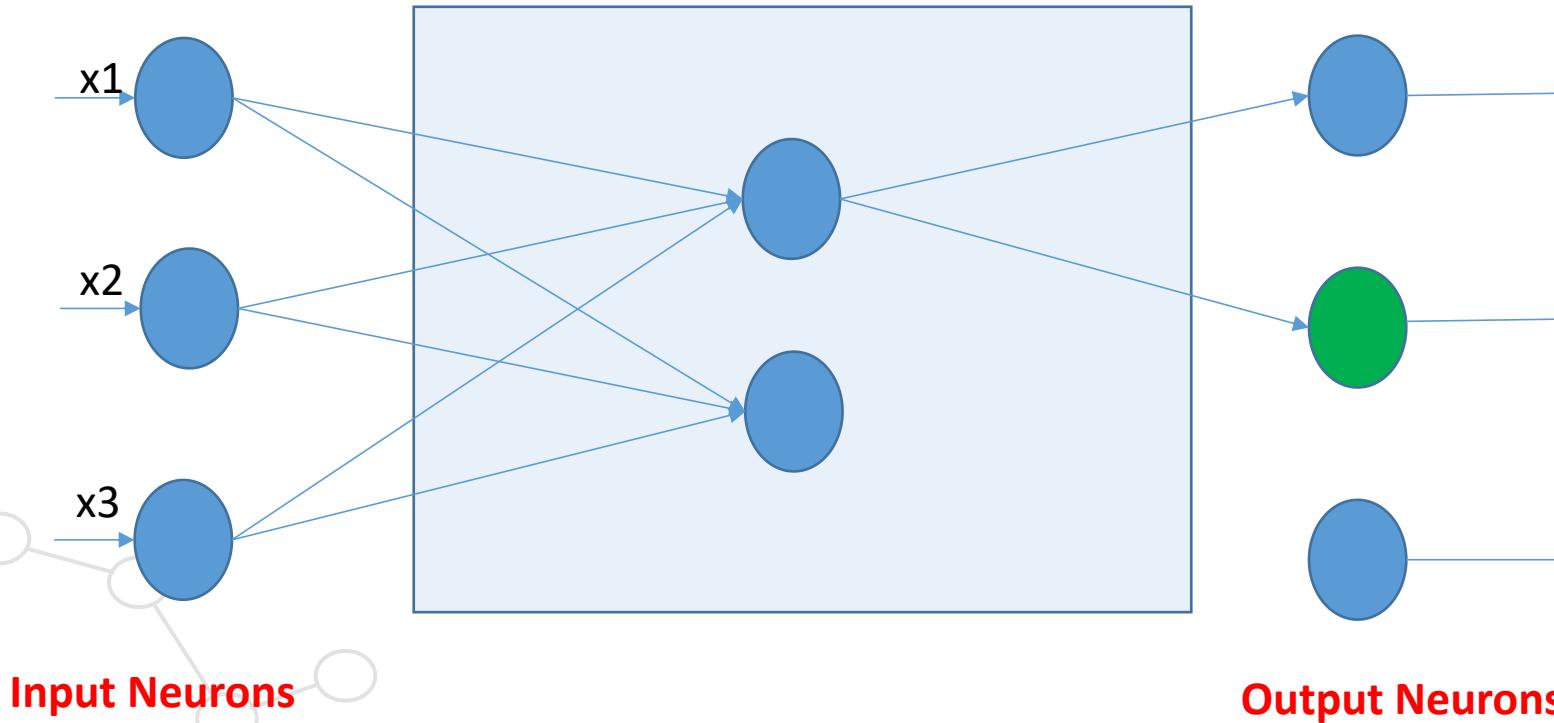
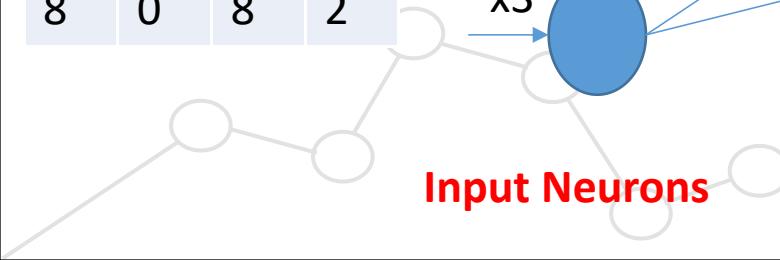
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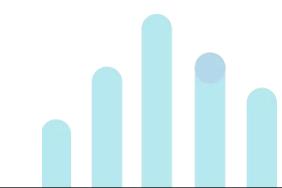
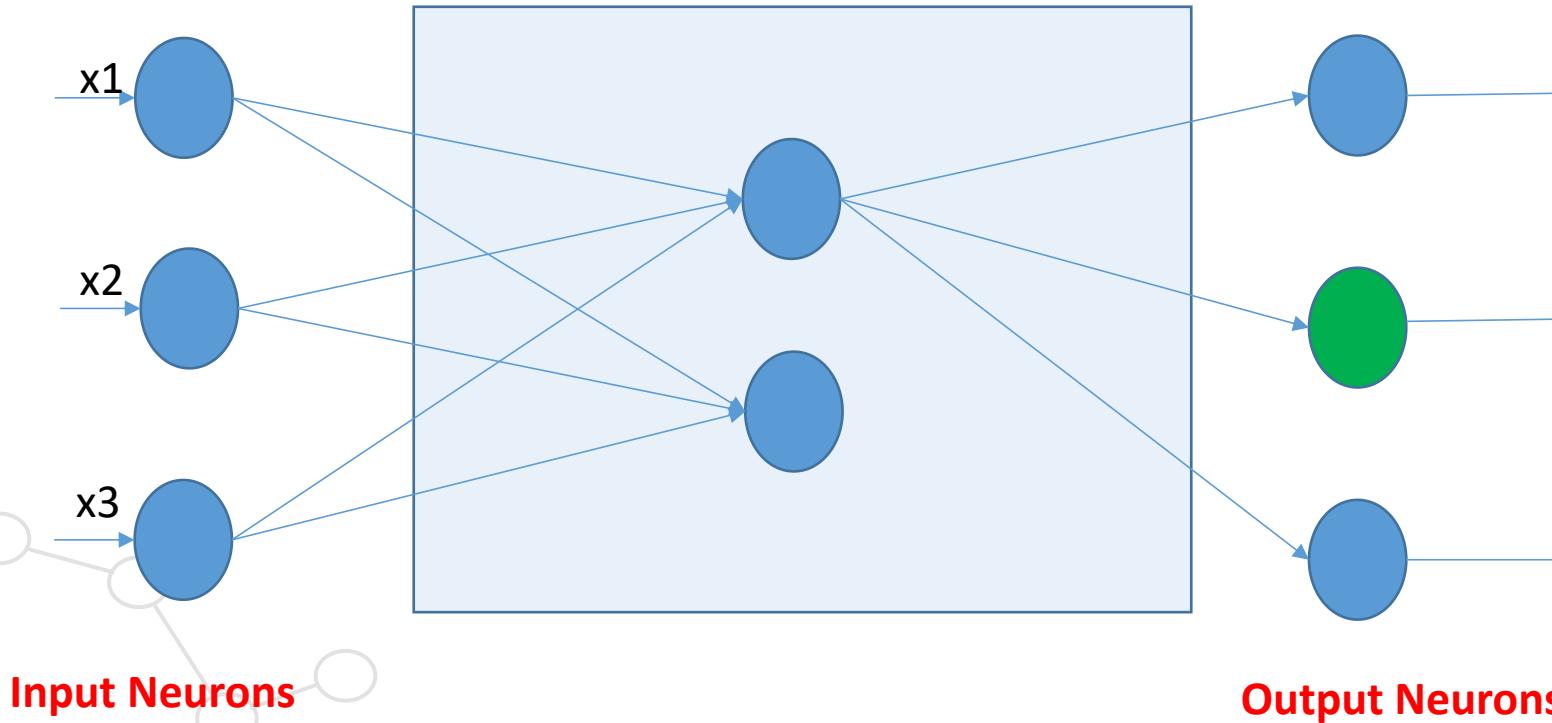
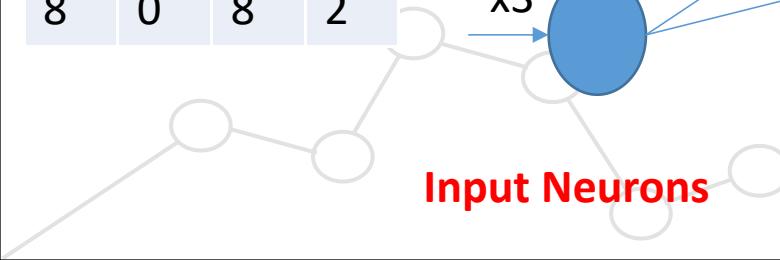
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2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks

- The mystery box represent a set of neurons and interconnections that propagate the signals from input neurons to output neurons.

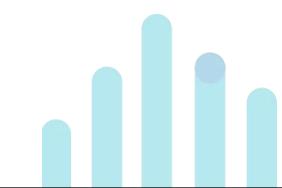
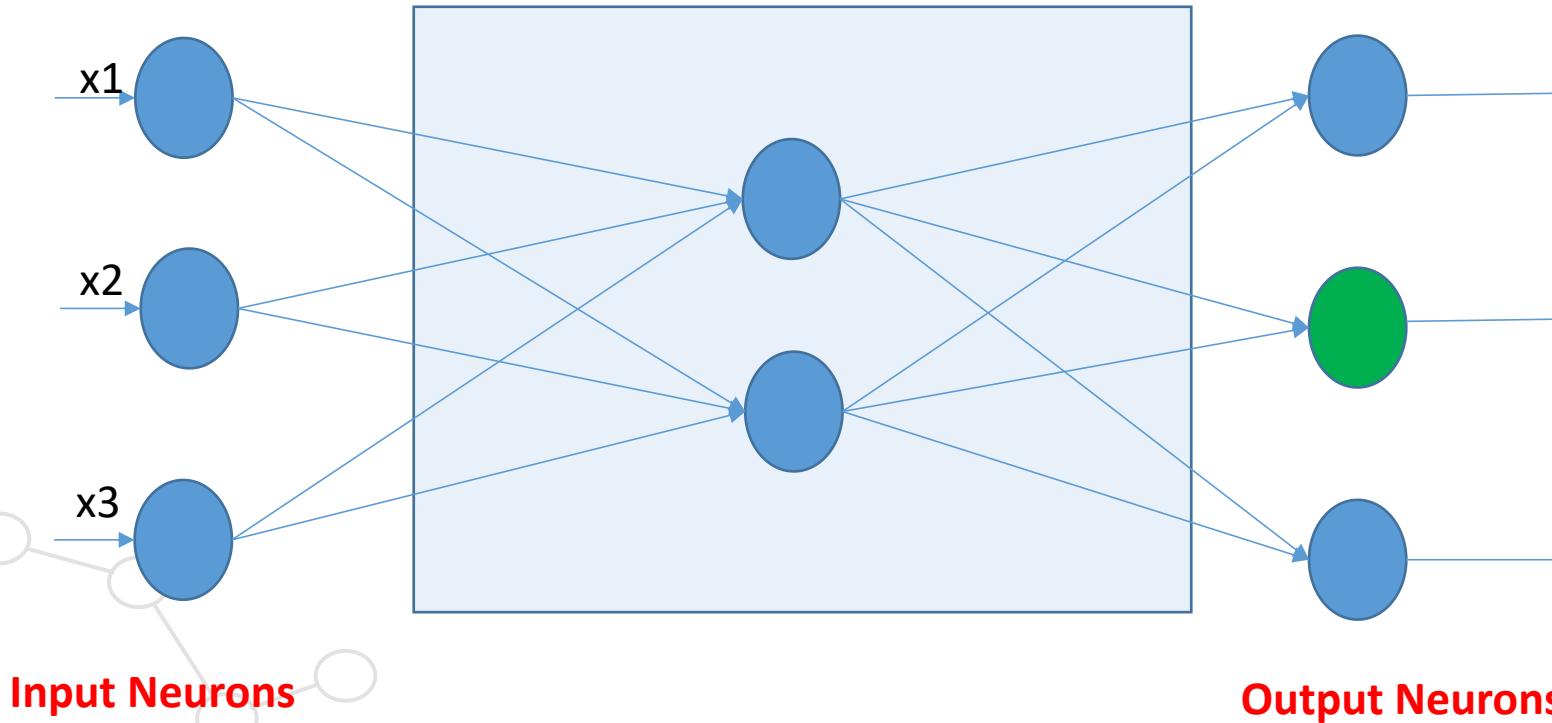
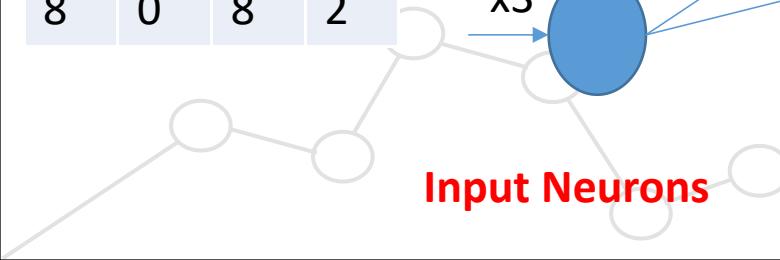
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks

- The mystery box represent a set of neurons and interconnections that propagate the signals from input neurons to output neurons.

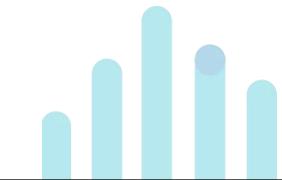
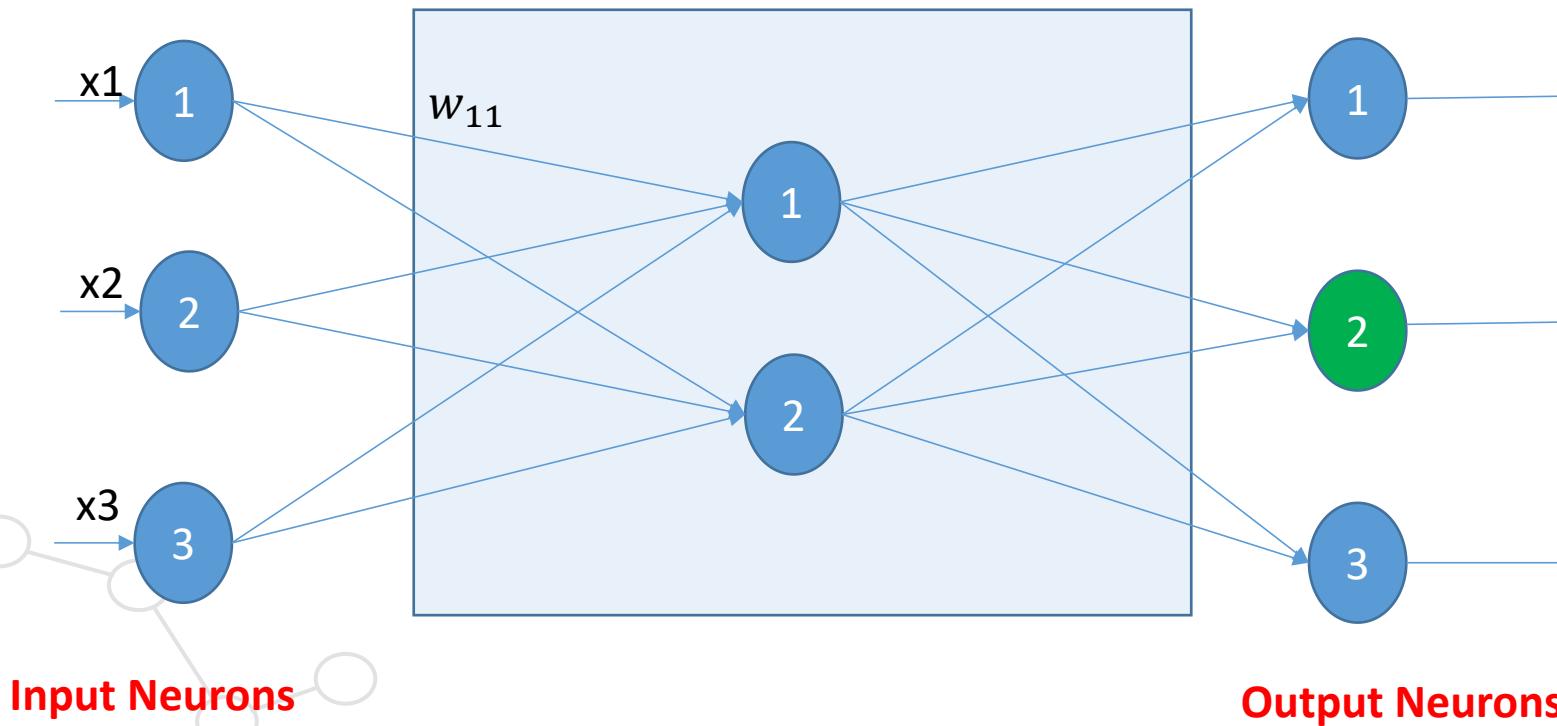
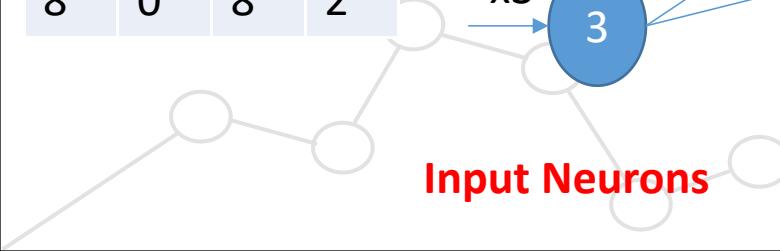
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks

- A set of weights must be defined.

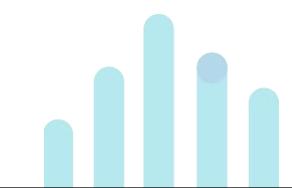
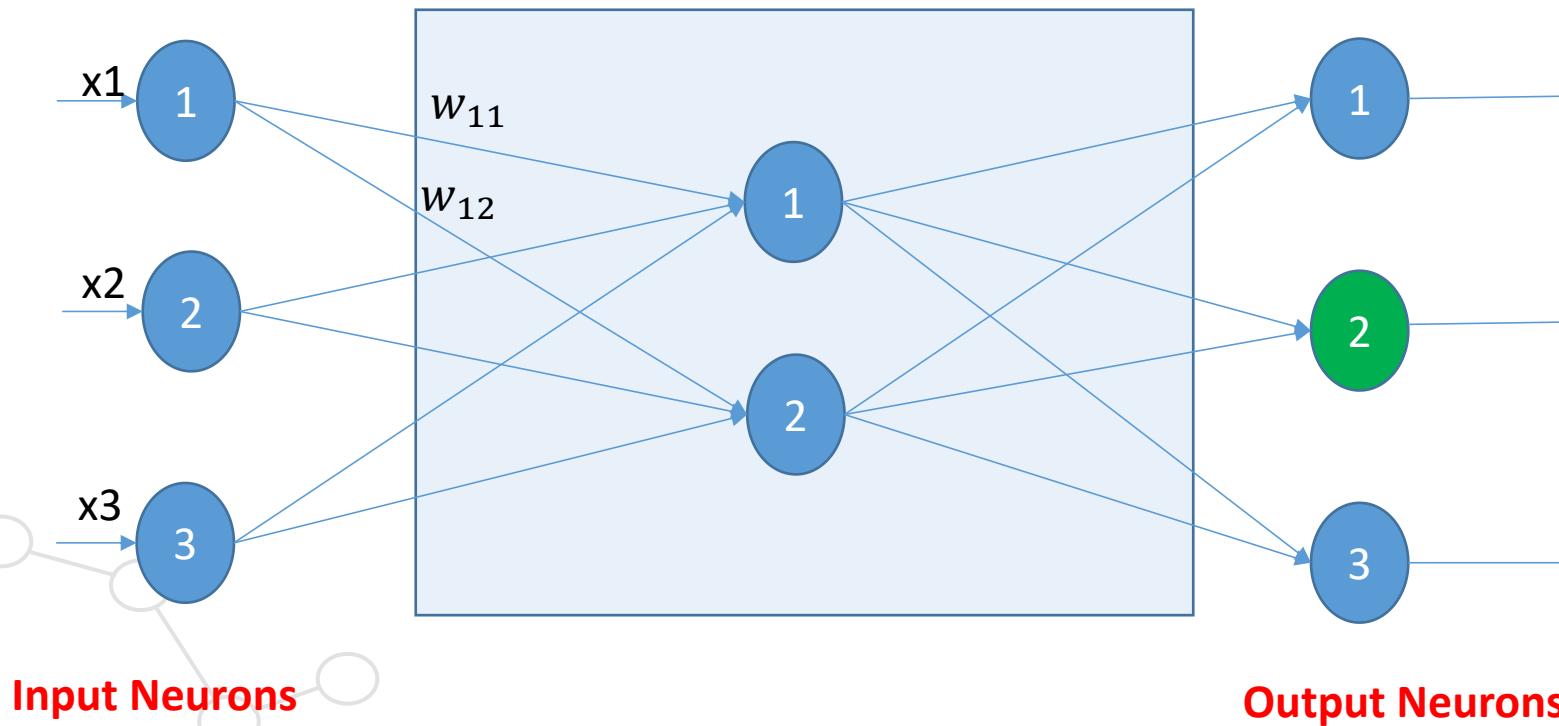
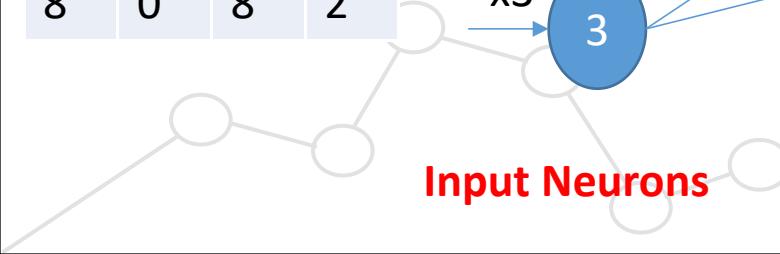
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks

- A set of weights must be defined.

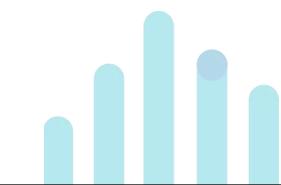
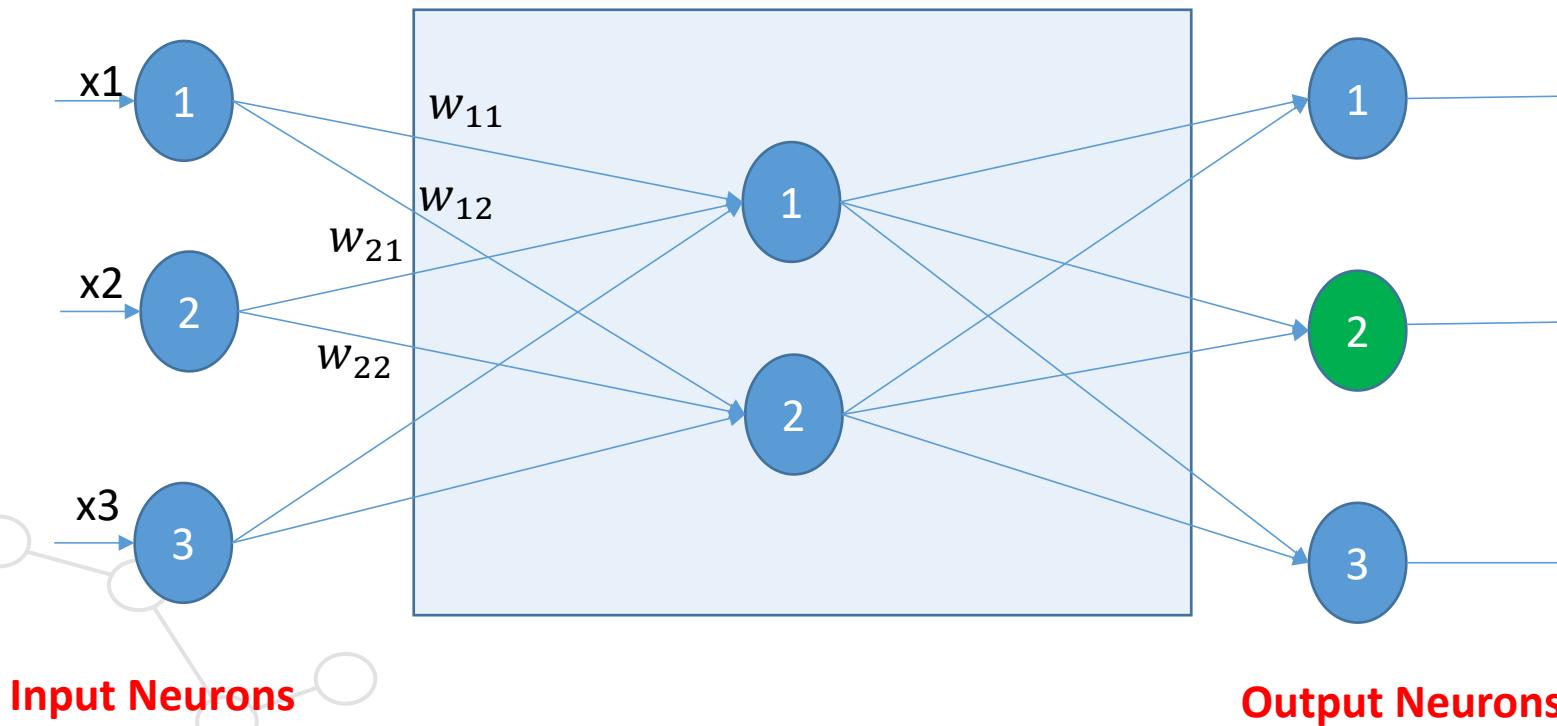
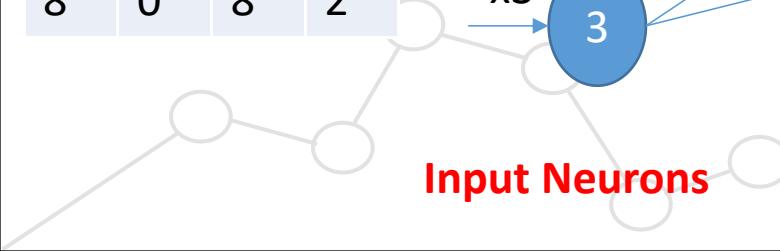
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks

- A set of weights must be defined.

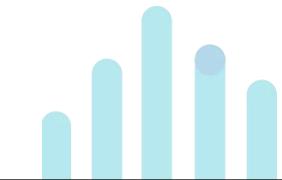
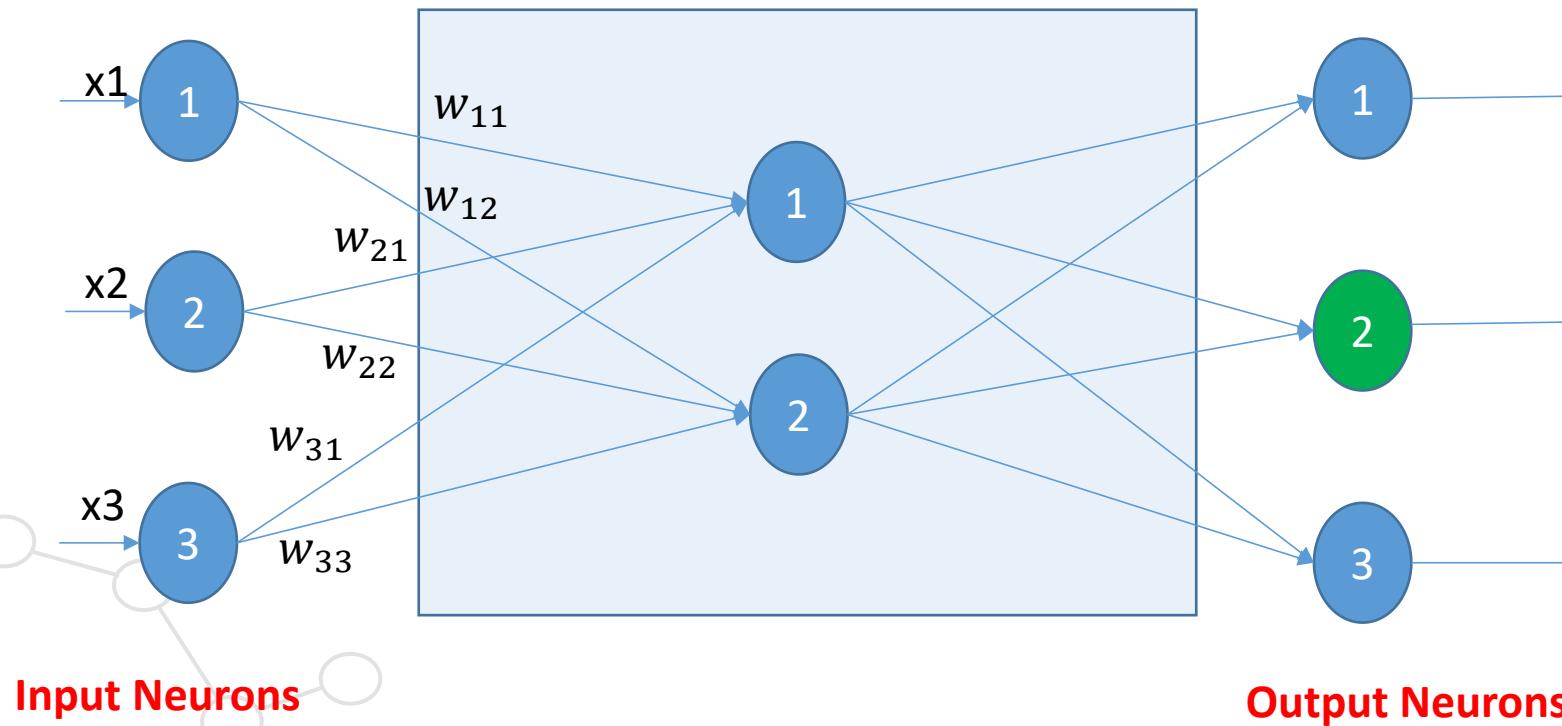
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks

- A set of weights must be defined.

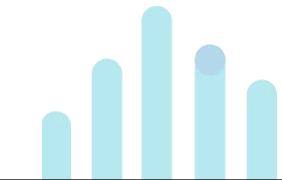
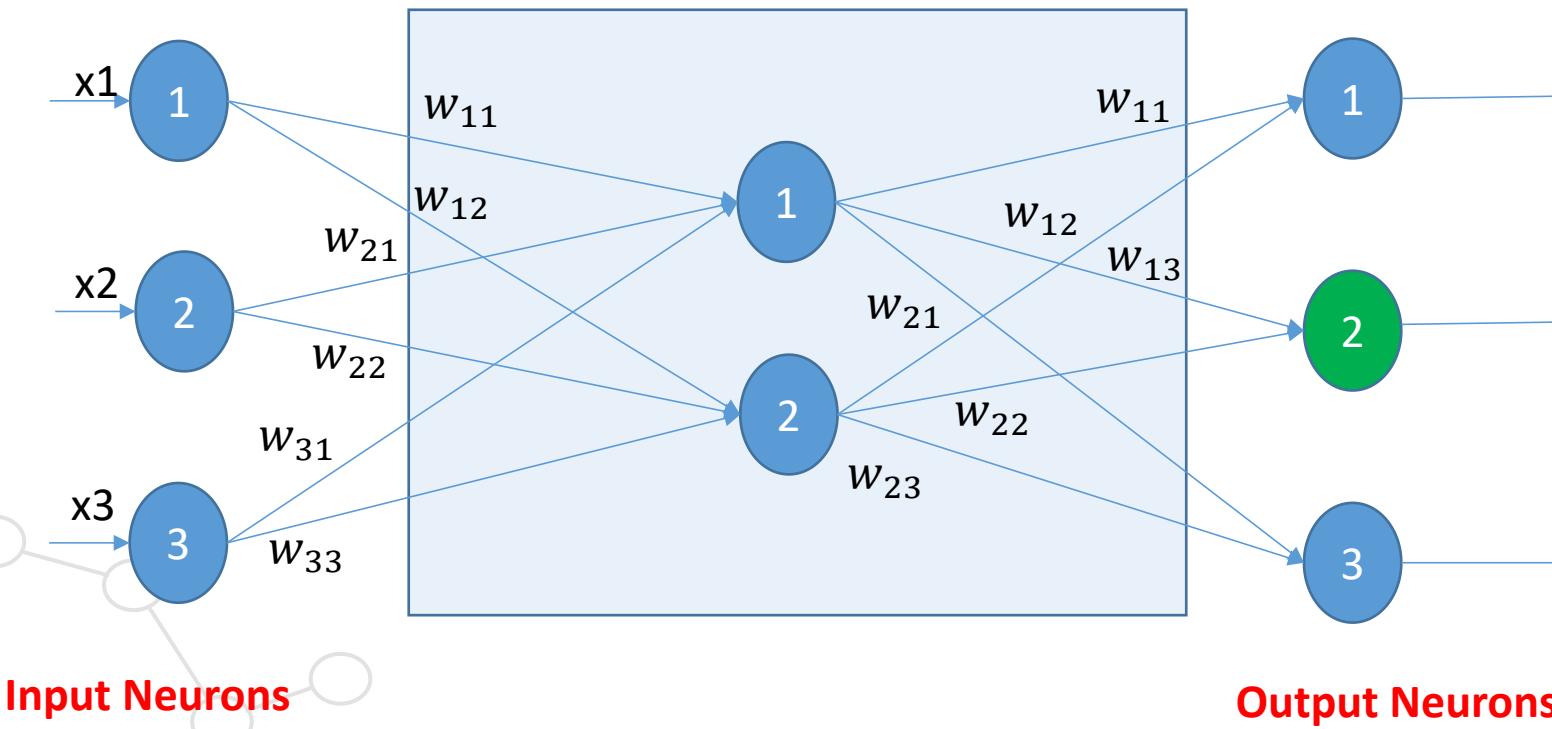
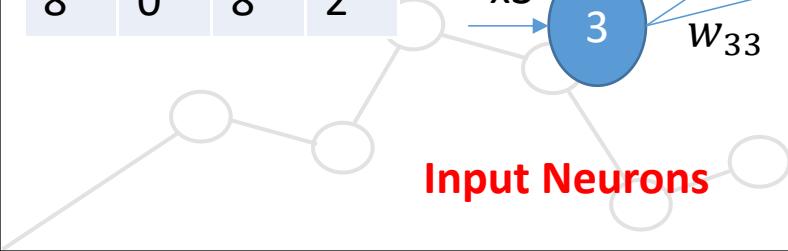
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks

- A set of weights must be defined.

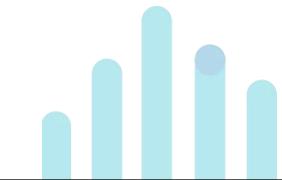
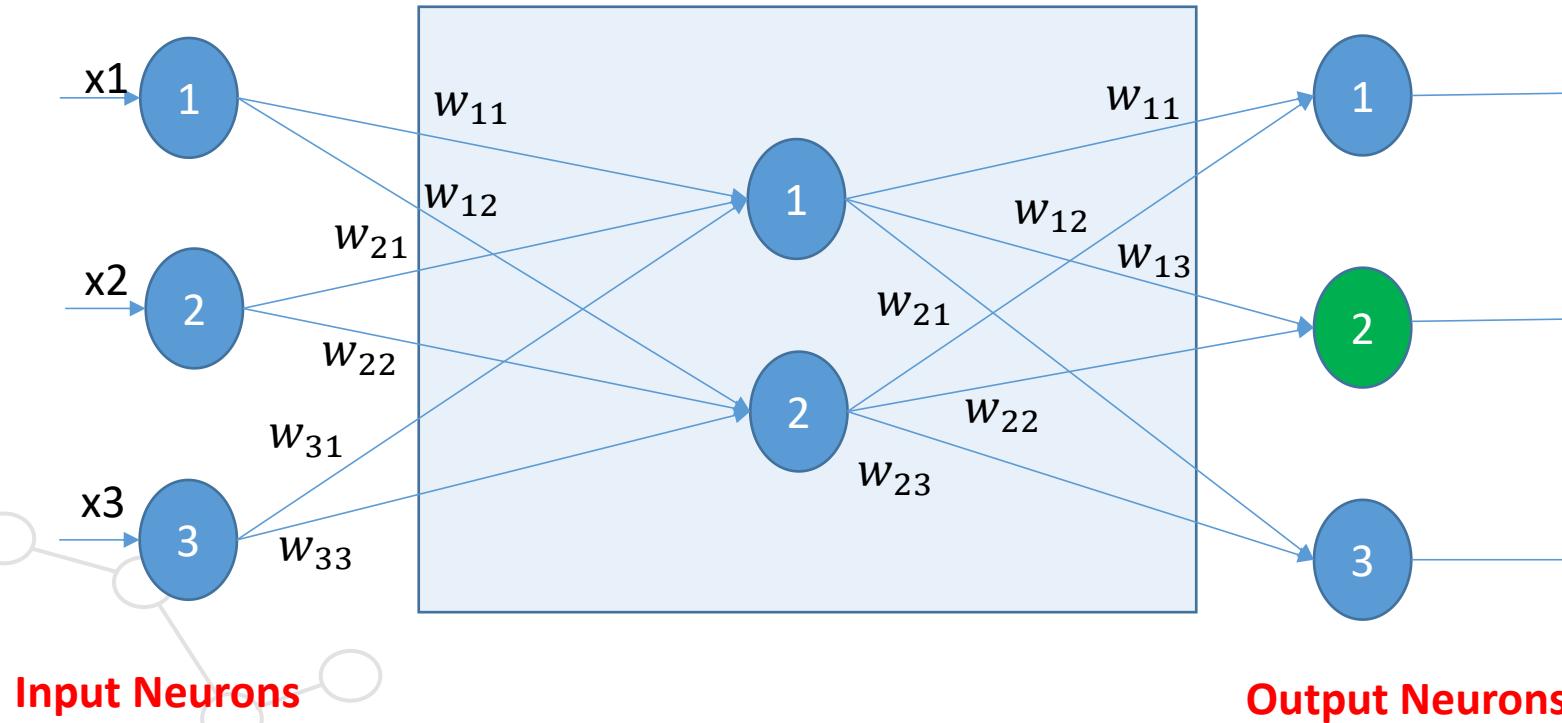
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



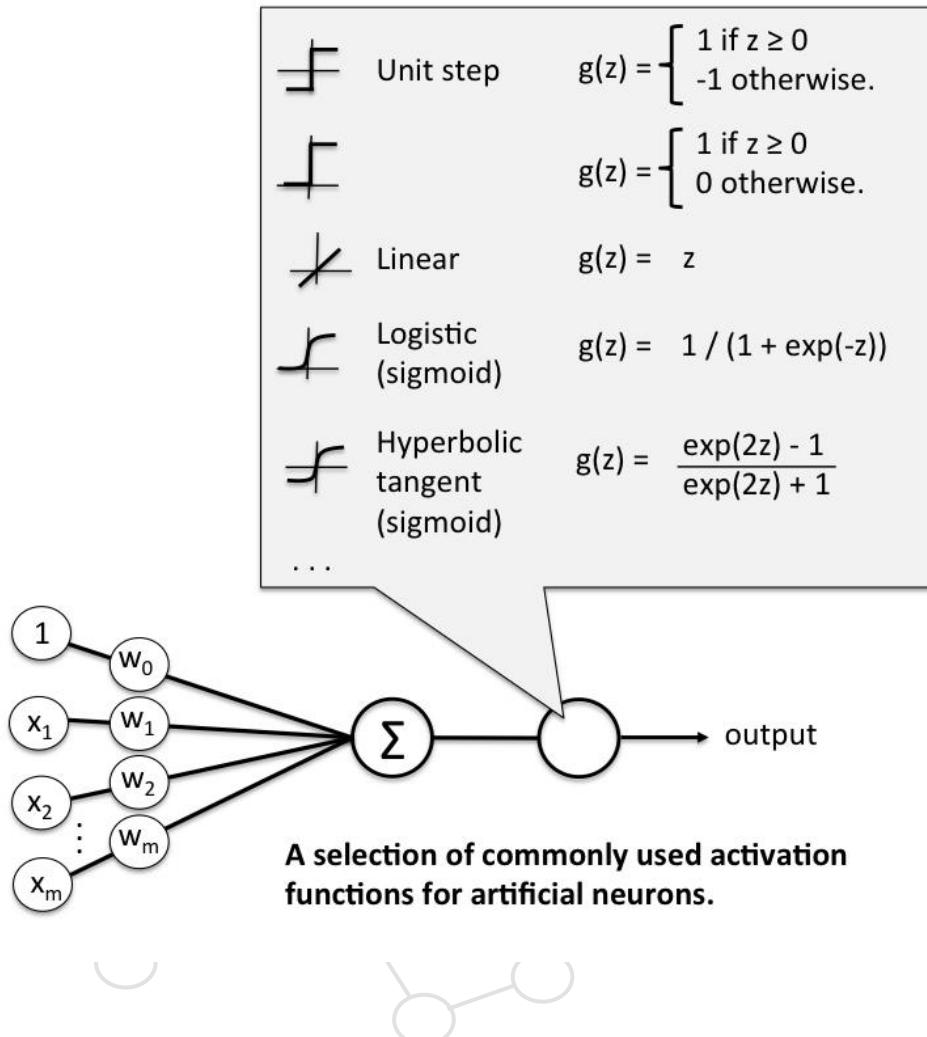
Multilayer networks

- A set of weights must be defined.
- Like perceptron, for the output of each neuron, an **activation function** is applied.

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



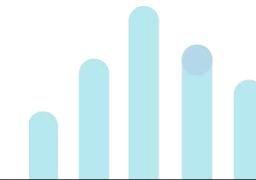
Activation Function



Typically these functions are within **Hidden layers of a Neural Network Model**.

For output layers we should use a **Softmax function** for a Classification problem to compute the probabilities for the classes.

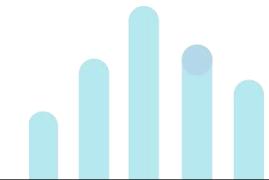
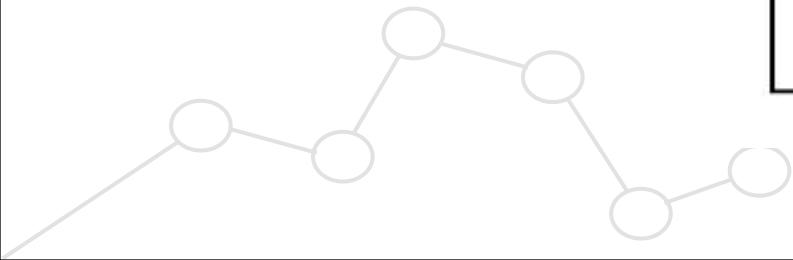
For a regression problem it should simply use a **linear function**.



Softmax Function

The softmax function converts its inputs, known as logit or logit scores, to be between 0 and 1, and also normalizes the outputs so that they all sum up to 1. In other words, the softmax function turns your logits into probabilities. Mathematically, the softmax function is defined as follows:

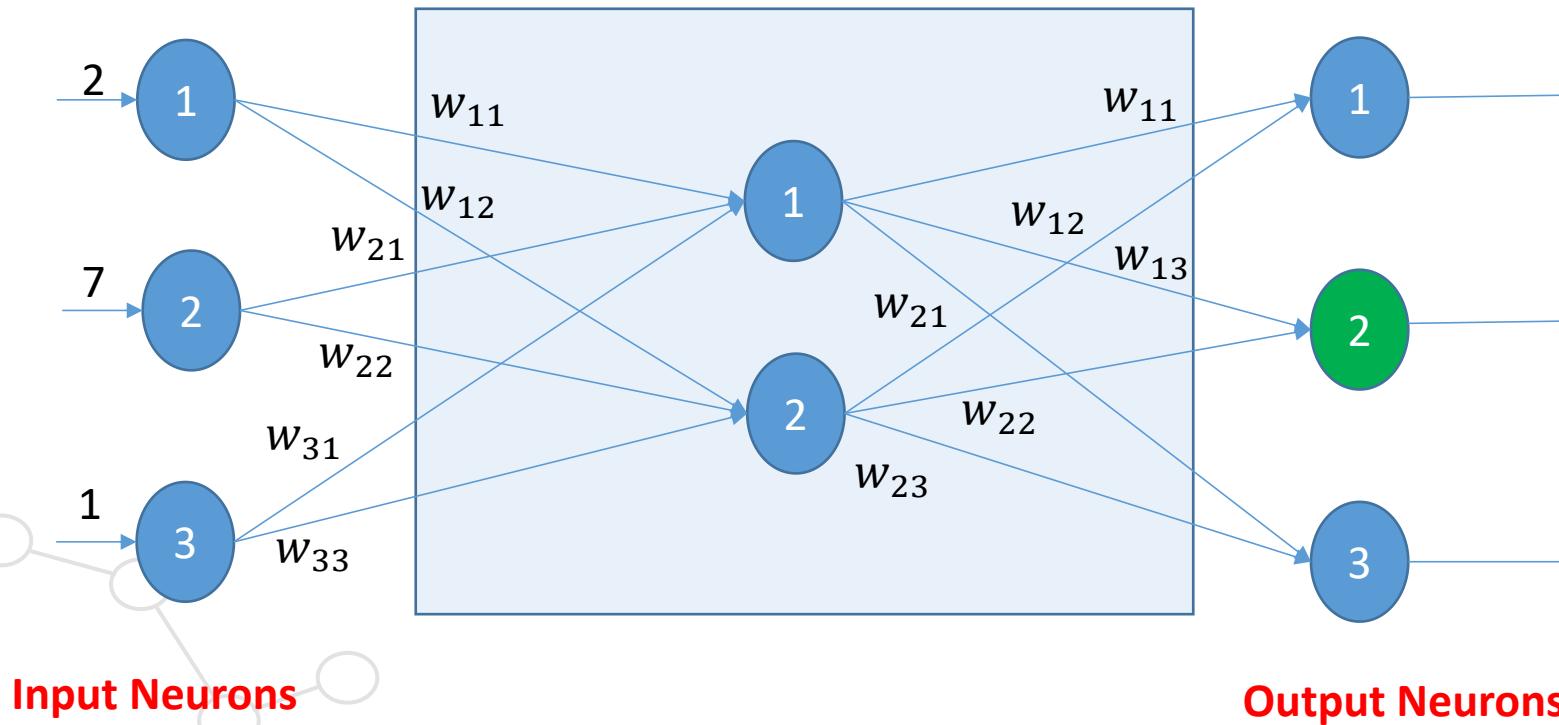
$$S(y_i) = \frac{e^{y_i}}{\sum_j e^{y_j}}$$



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

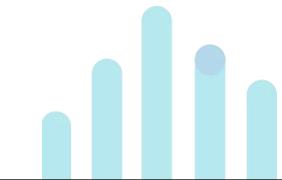
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network
- φ

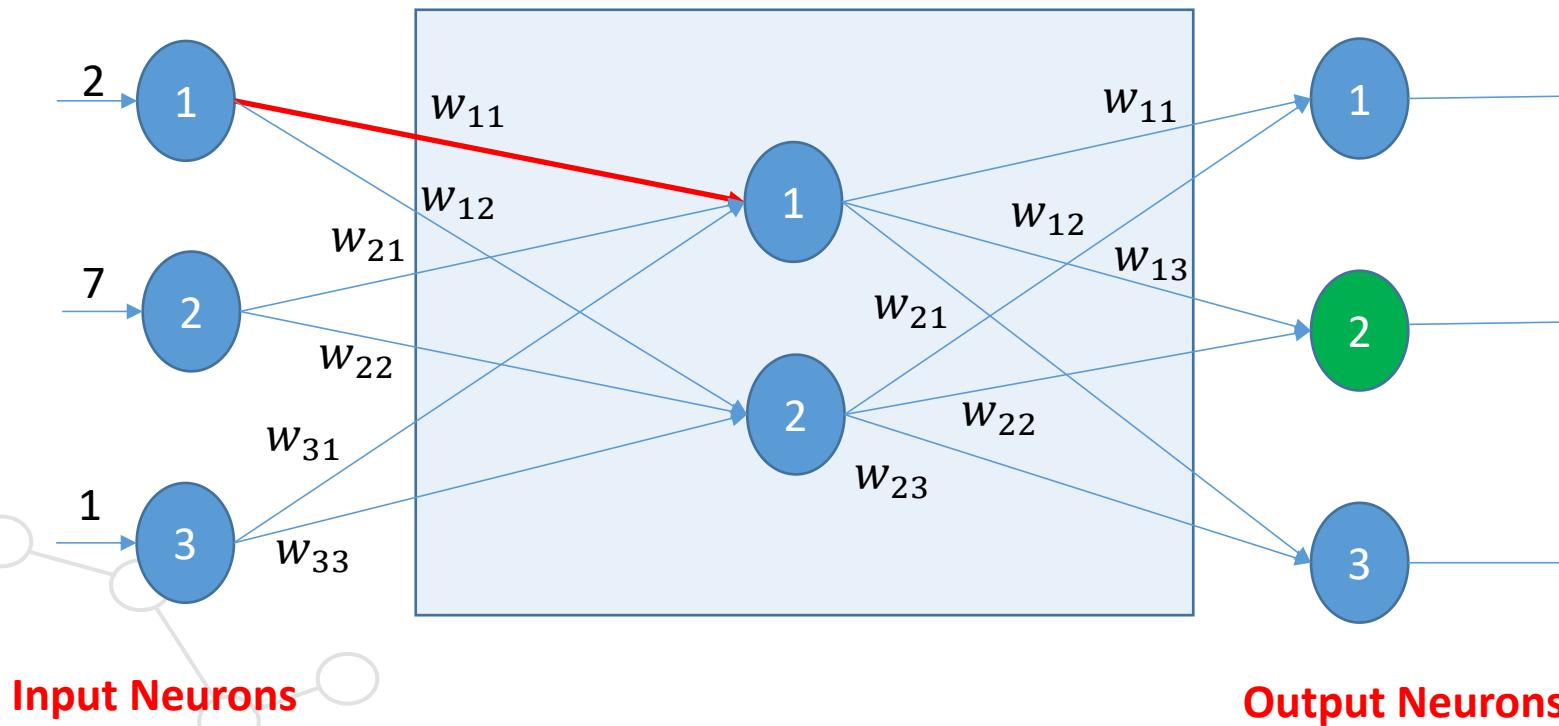
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

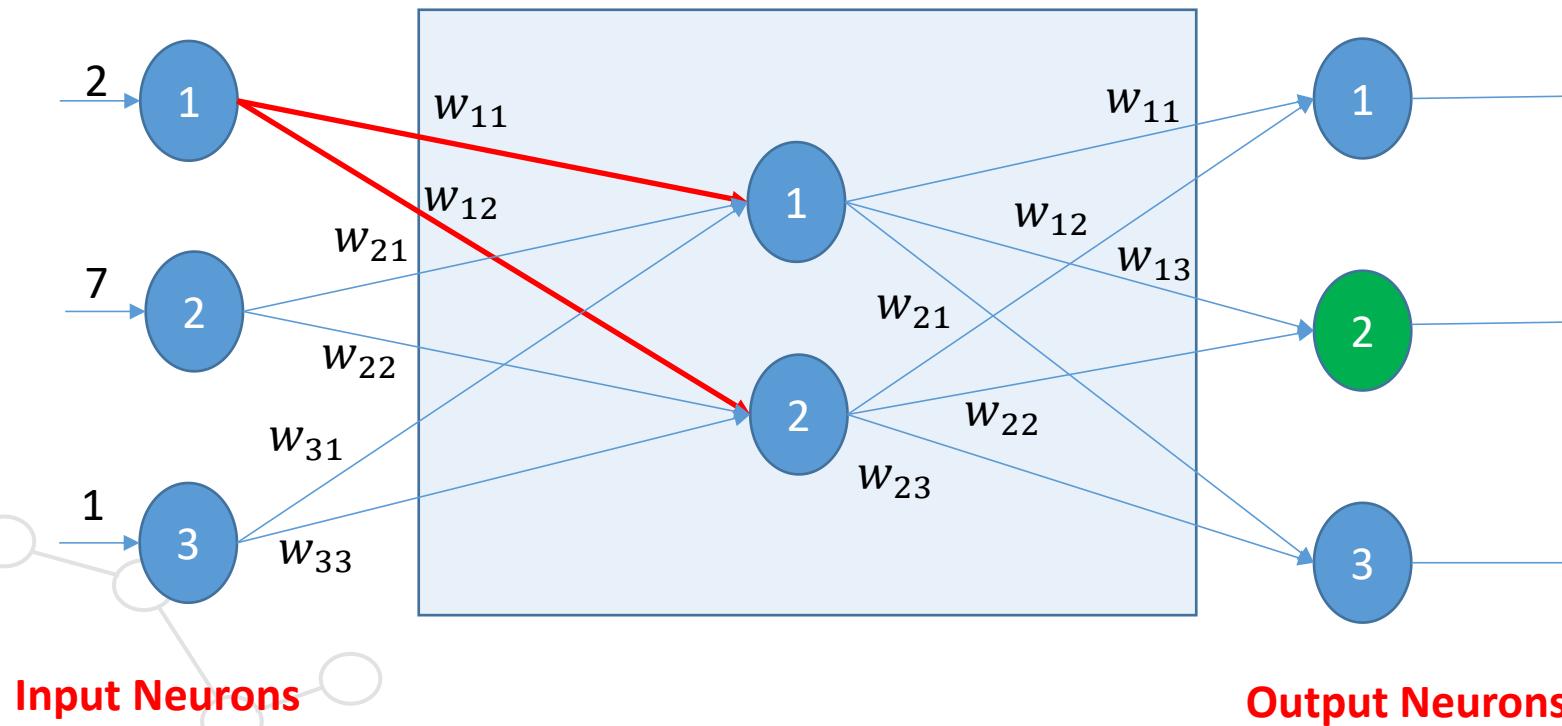
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

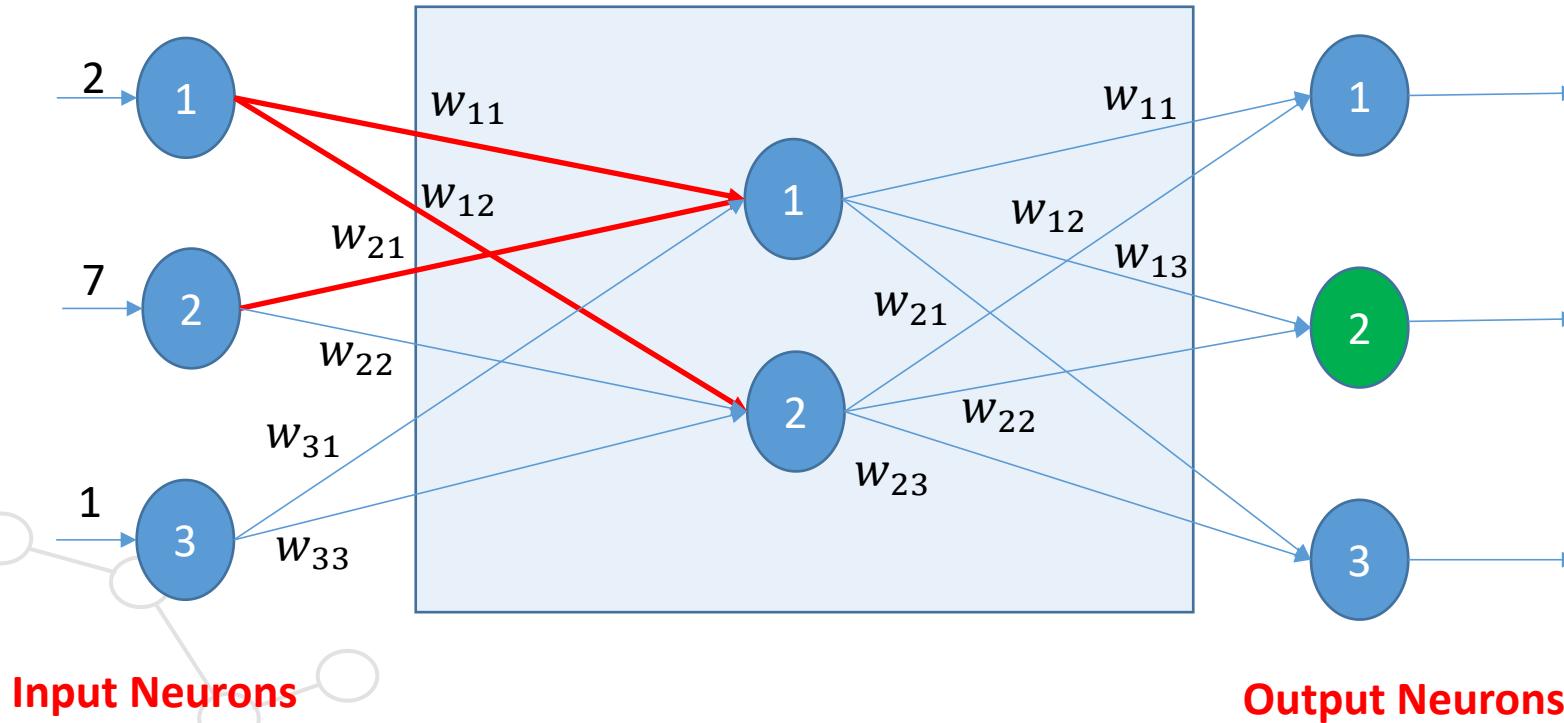
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

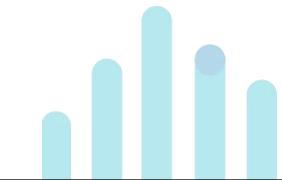
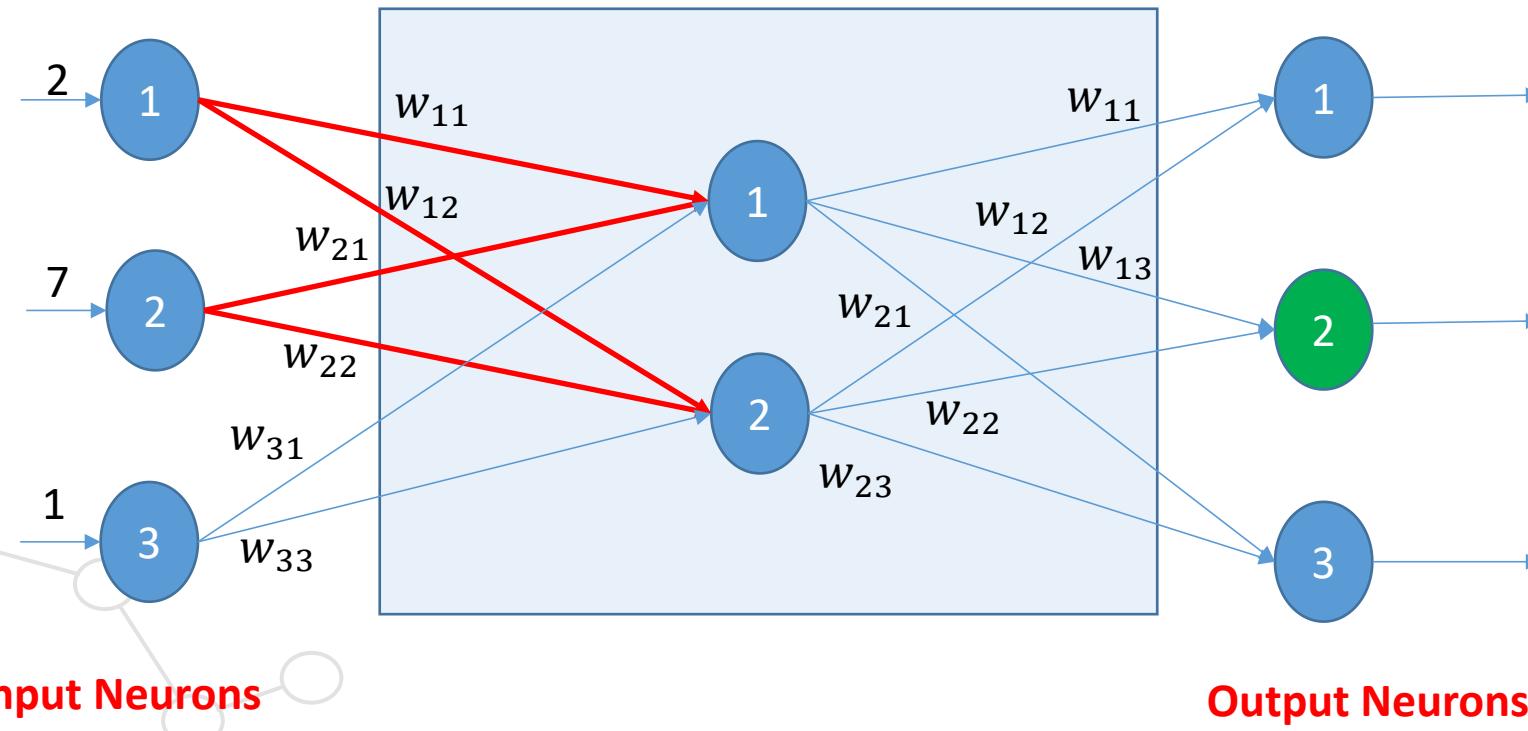
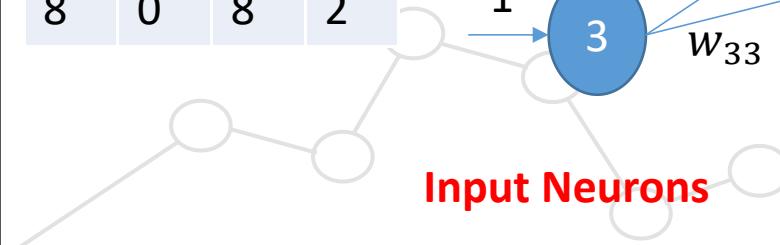
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

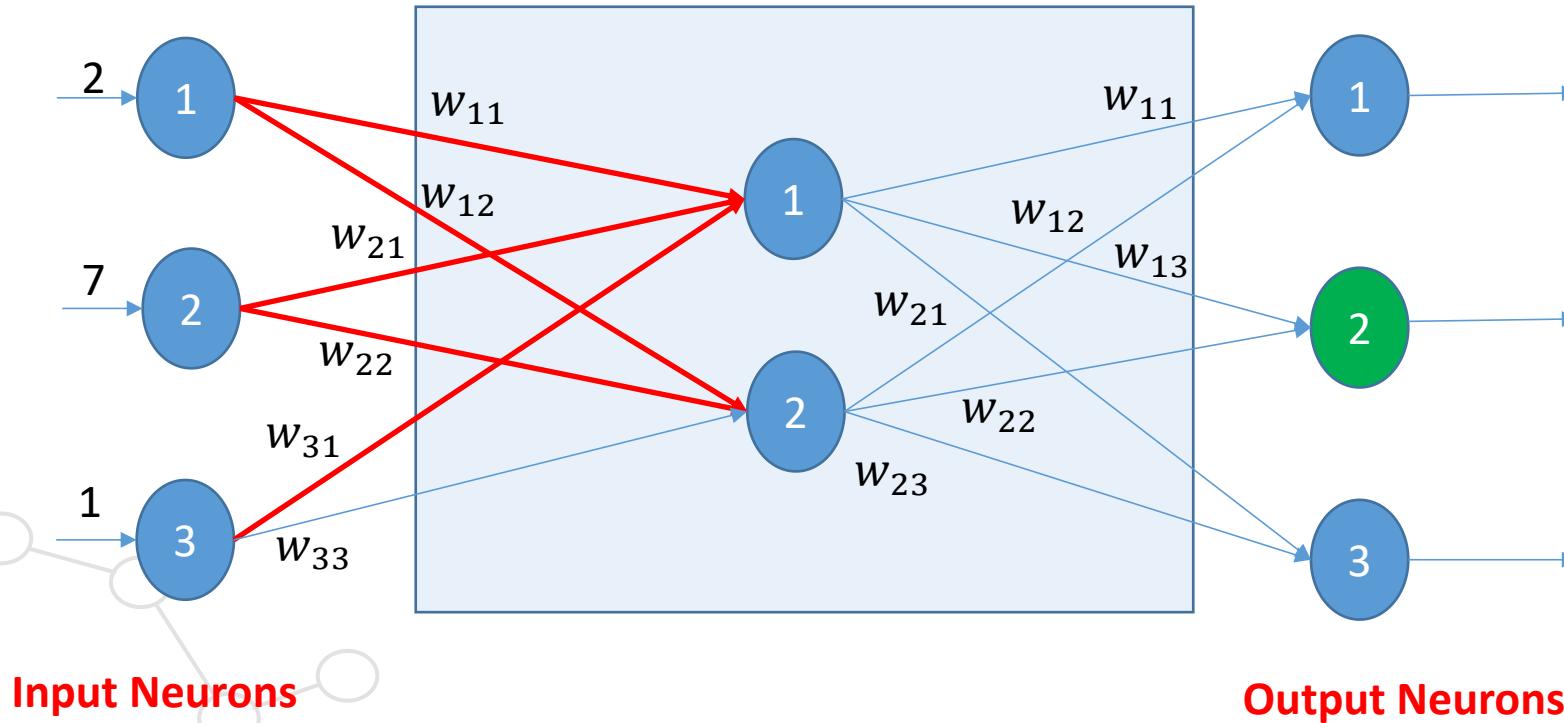
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

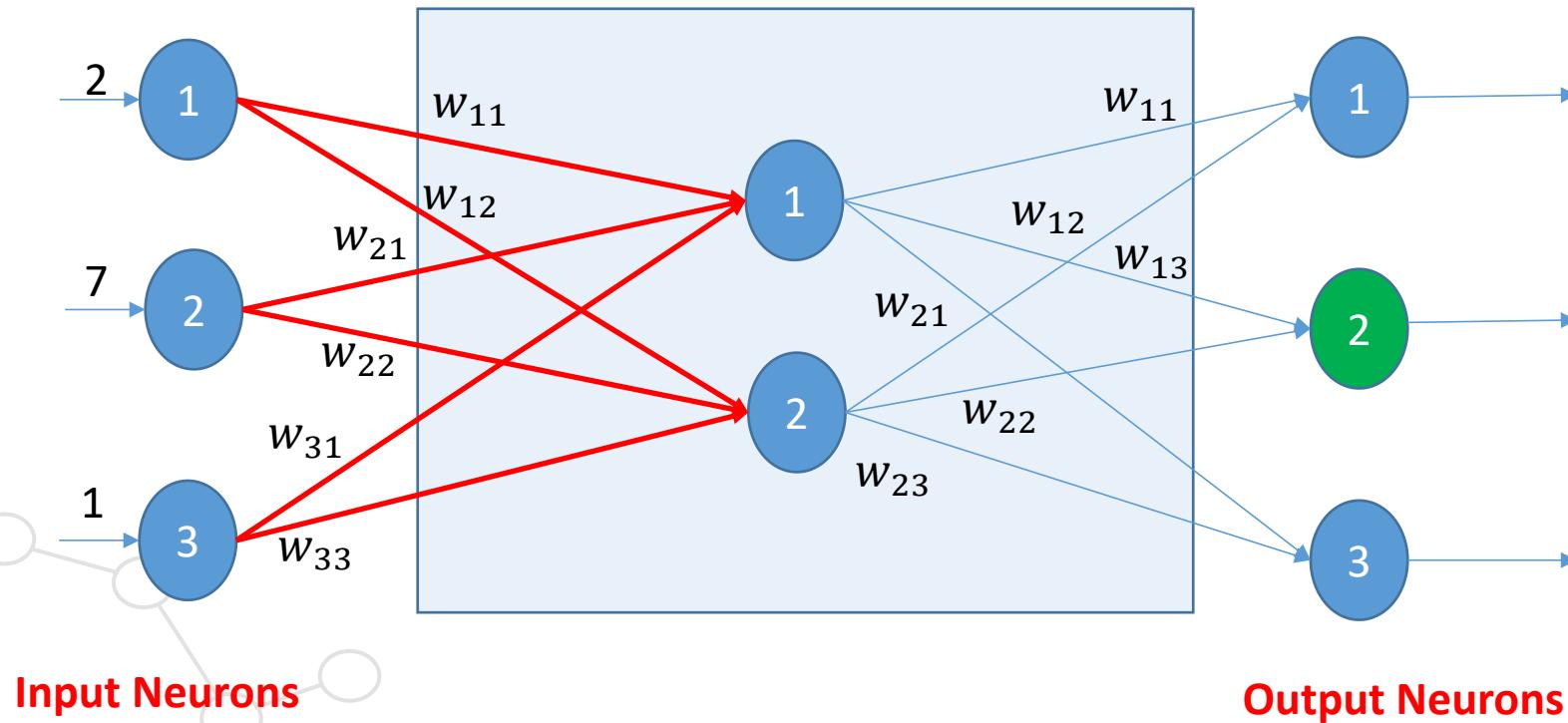
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

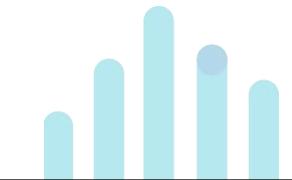
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

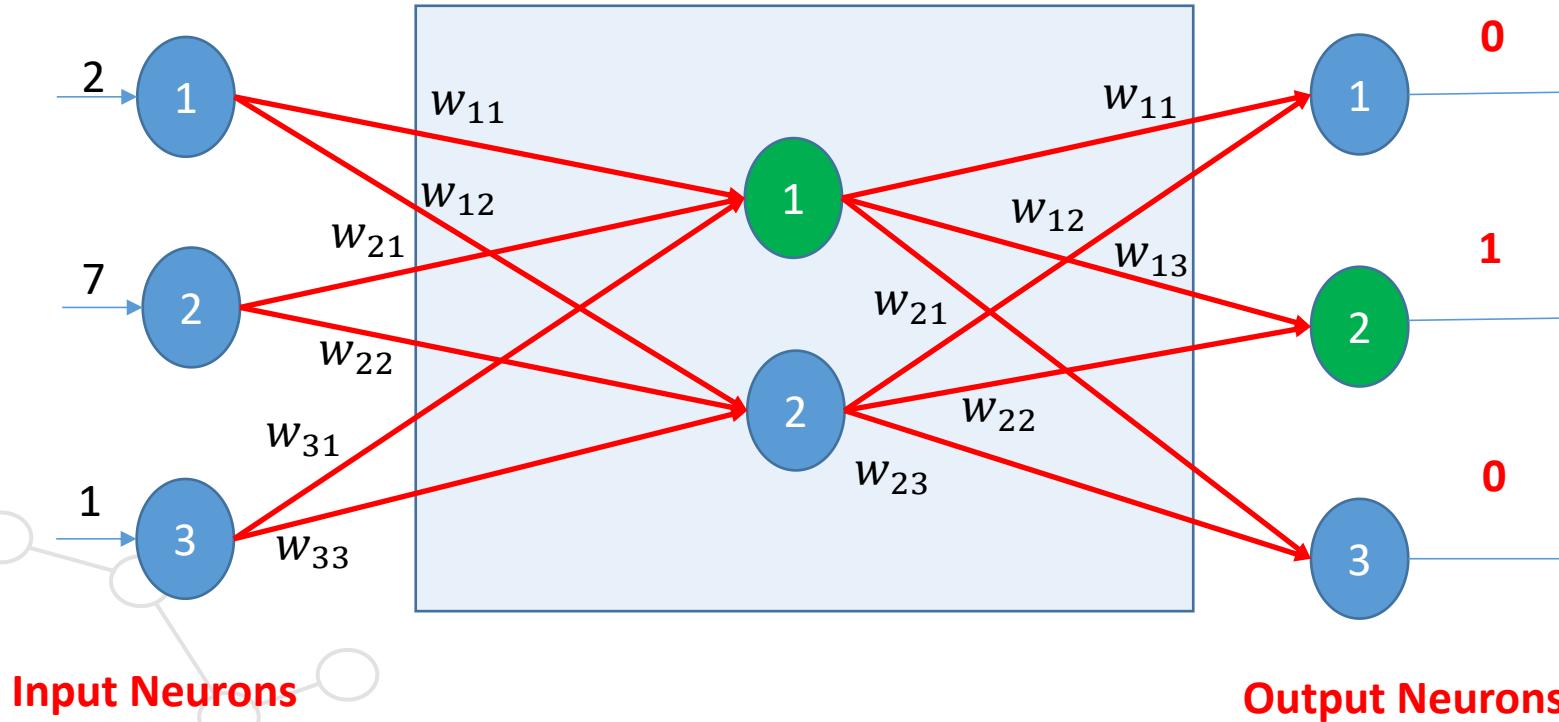
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 1: Propagate the input forward through the network

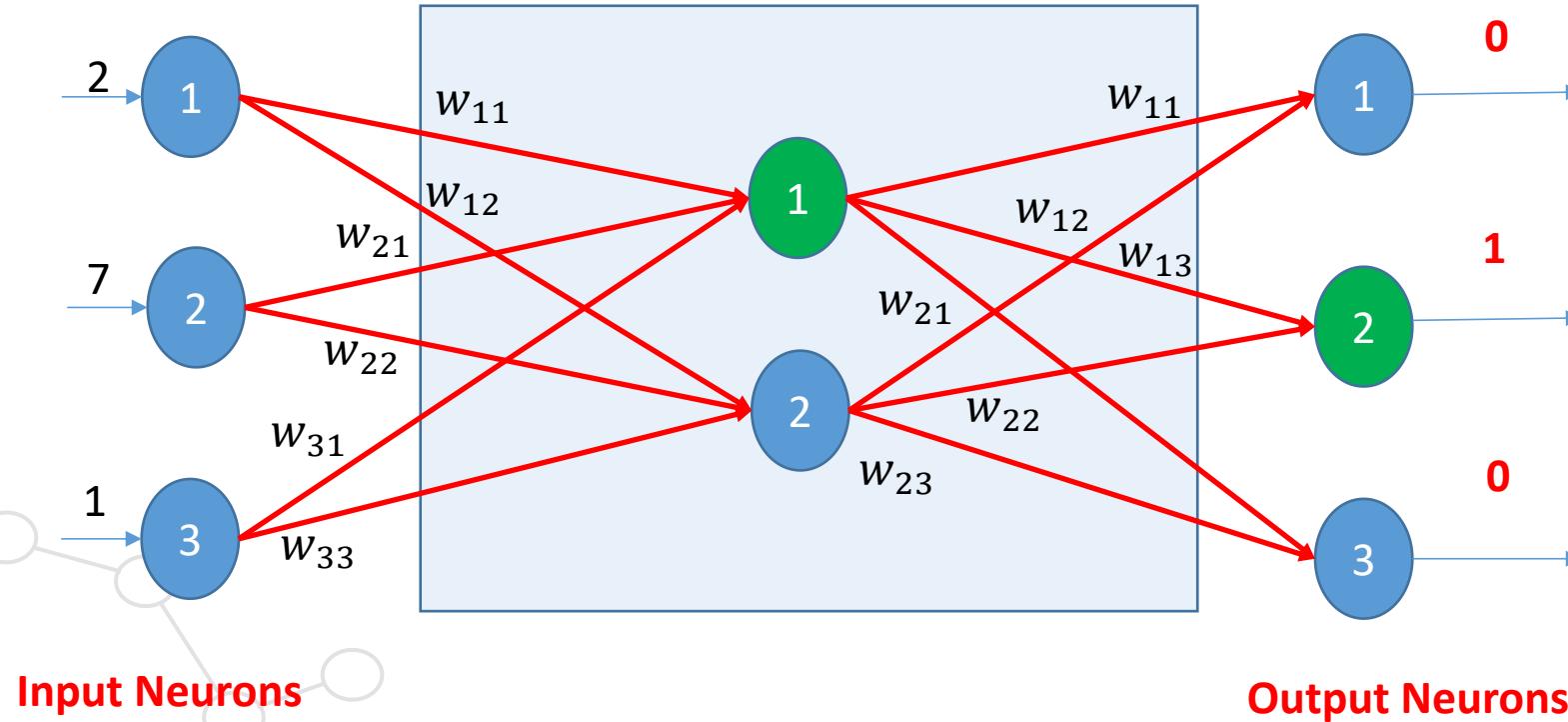
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 2: Propagate the input forward through the network

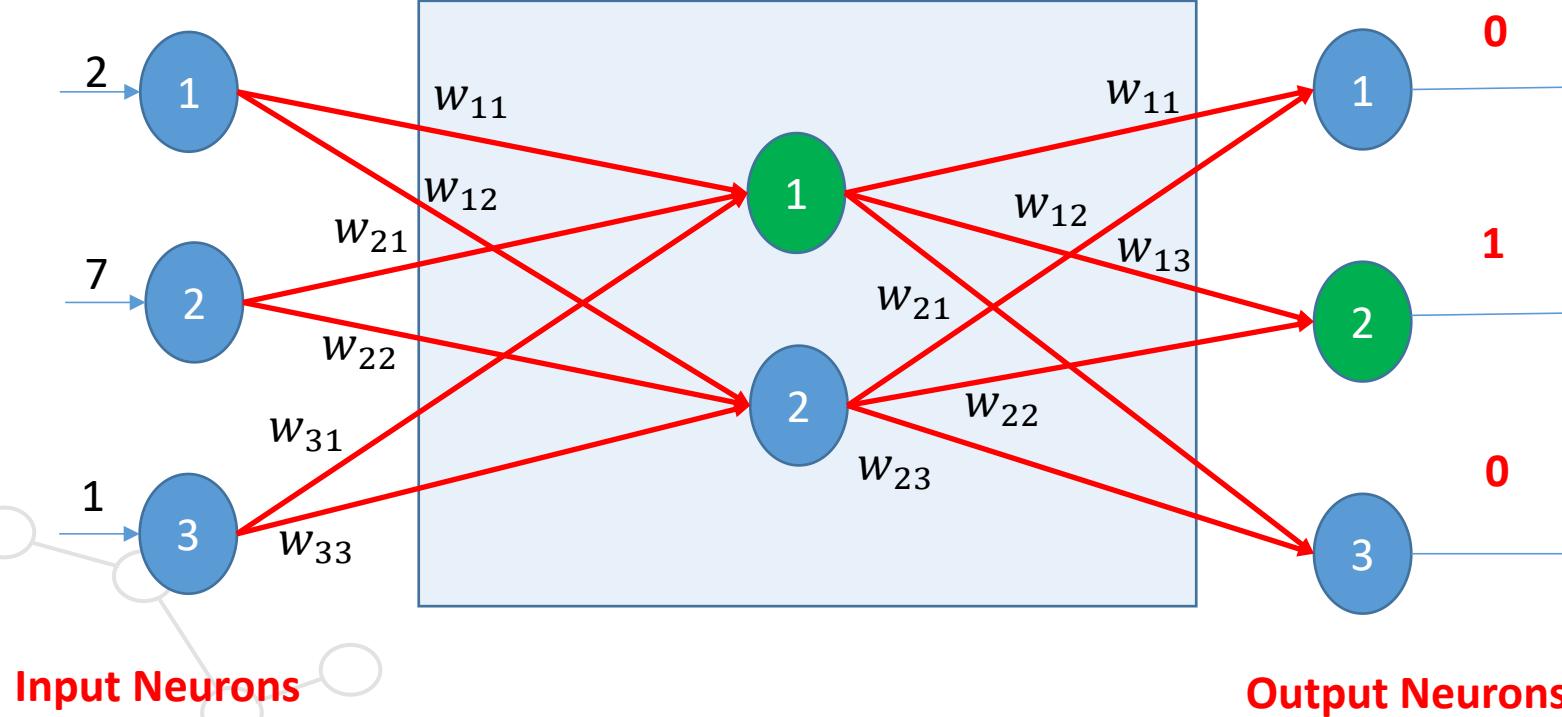
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Multilayer networks-Learning Process

- Step 3: Learning Process (propagate the **error** backward)

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2

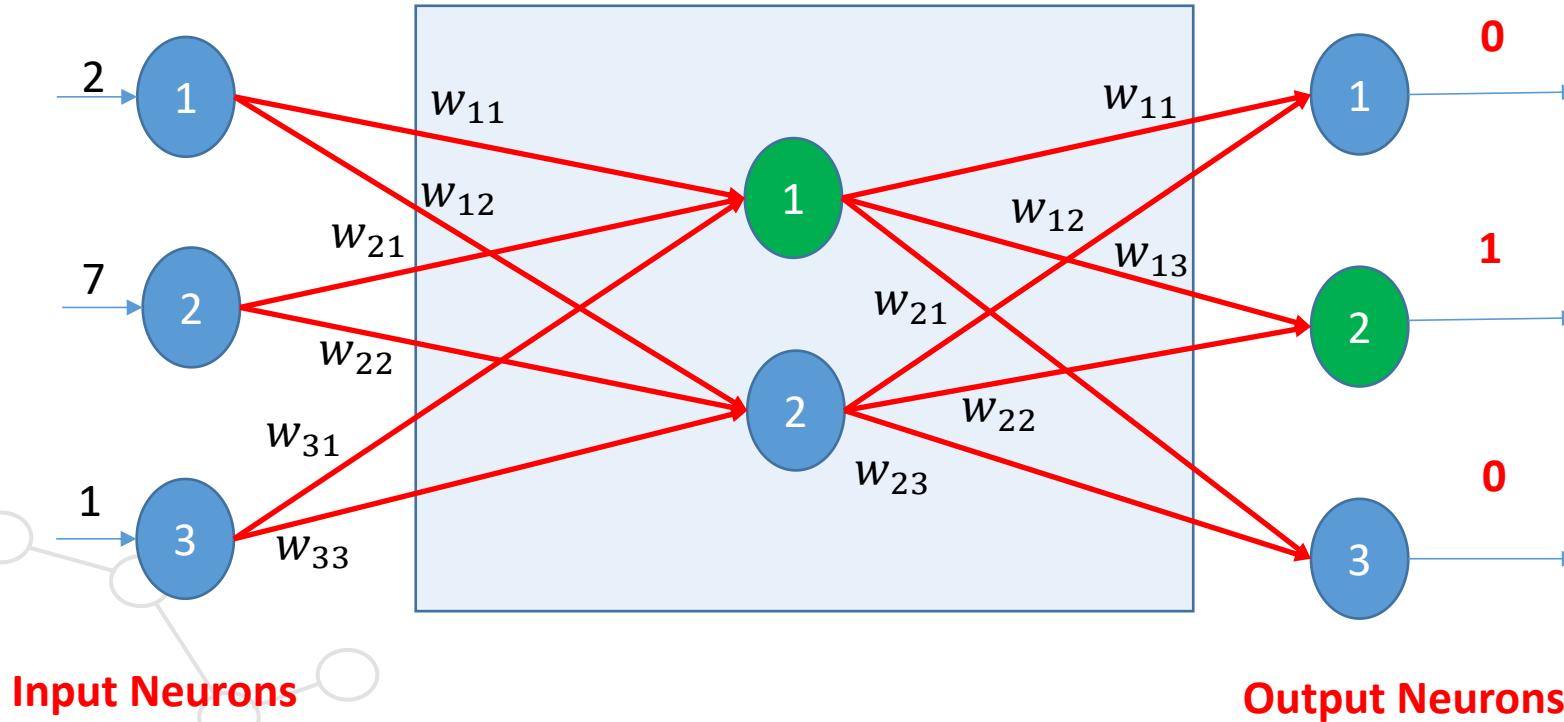


Multilayer networks-Learning Process

- Like single perceptron, we want to update the weights in this form:

$$\Delta w_{ji} = -\eta \frac{\partial E_d}{\partial w_{ji}}$$

X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



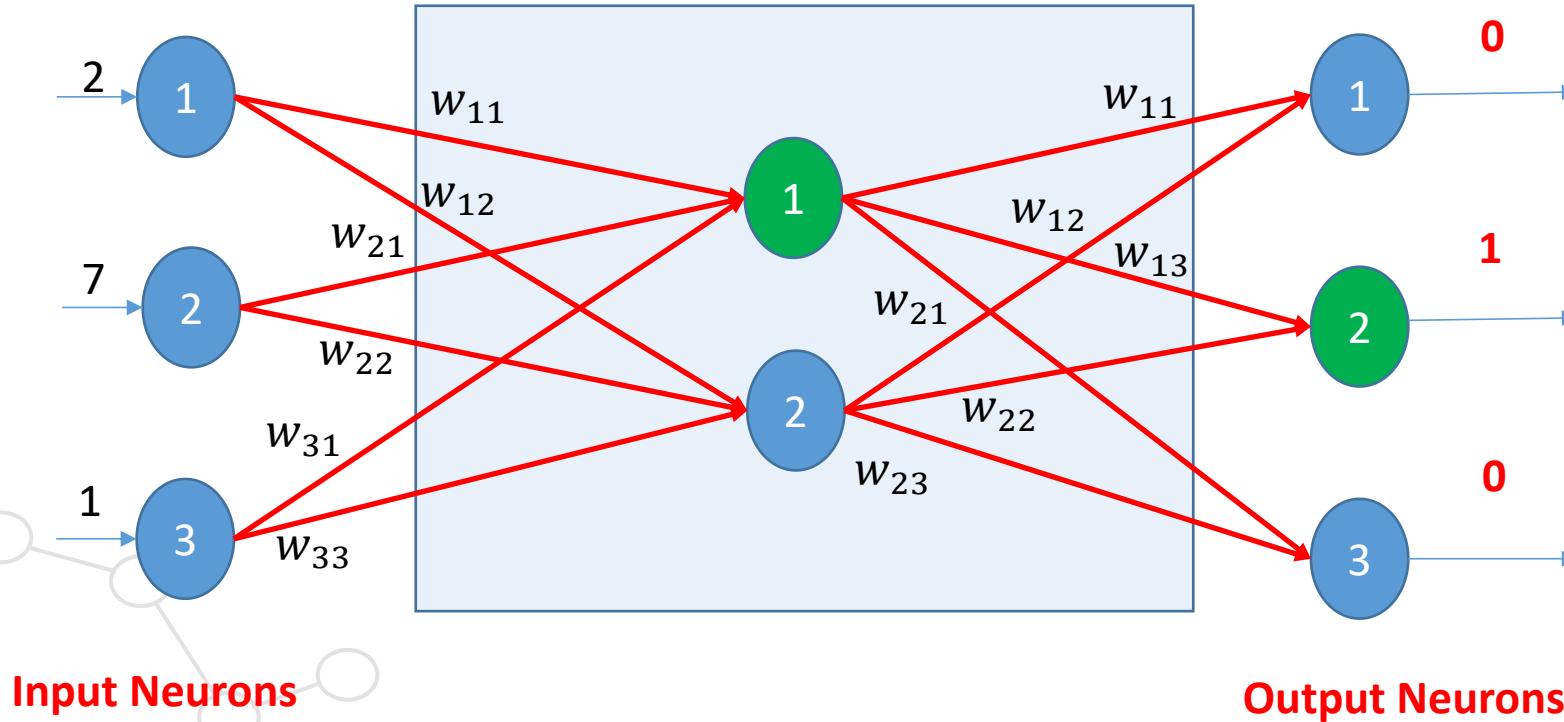
Multilayer networks-Learning Process

- Like single perceptron, we want to update the weights in this form:

$$\Delta w_{ji} = -\eta \frac{\partial E_d}{\partial w_{ji}}$$

BACKPROPAGATION METHOD

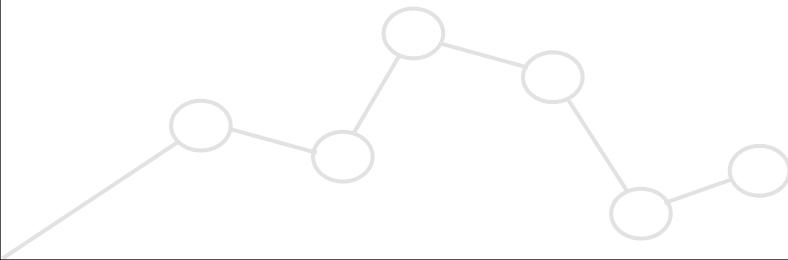
X1	X2	X3	c
2	7	1	0
3	6	5	1
5	4	7	2
6	8	5	0
7	9	7	1
8	0	8	2



Design the neural network architecture

Assume a problem with the following dataset:

x1	x2	x3	x4	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

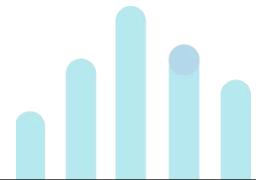


Design the neural network architecture

Assume a problem with the following dataset:

x1	x2	x3	x4	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

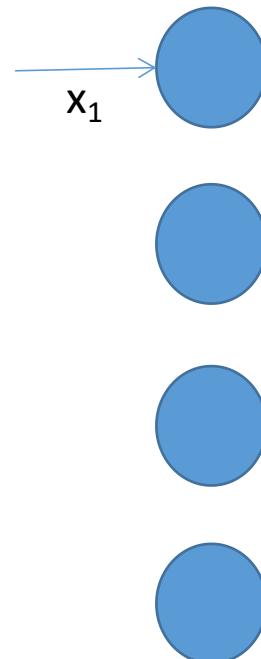
We have three
classes and feature
vectors in \mathbb{R}^4



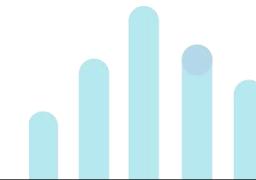
Design the neural network architecture

Assume a problem with the following dataset:

x1	x2	x3	x4	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1



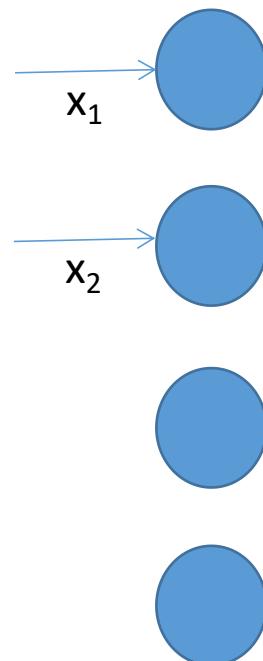
We have three classes and feature vectors in \mathbb{R}^4



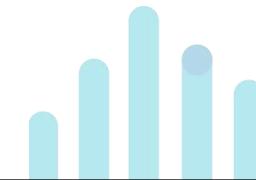
Design the neural network architecture

Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1



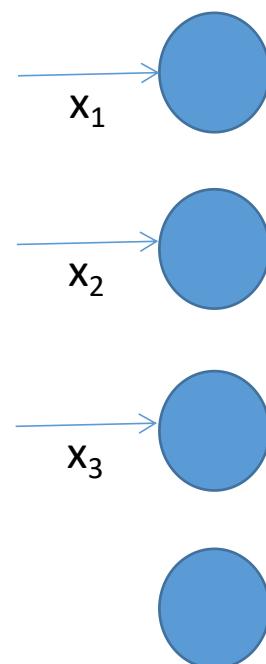
We have three classes and feature vectors in \mathbb{R}^4



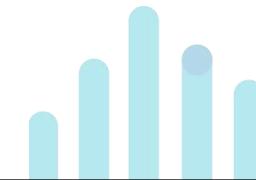
Design the neural network architecture

Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1



We have three classes and feature vectors in \mathbb{R}^4

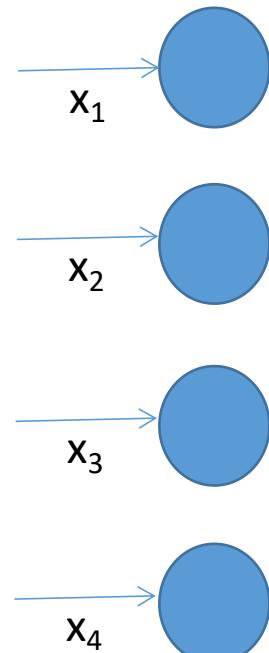


Design the neural network architecture

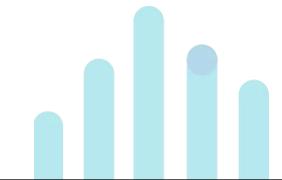
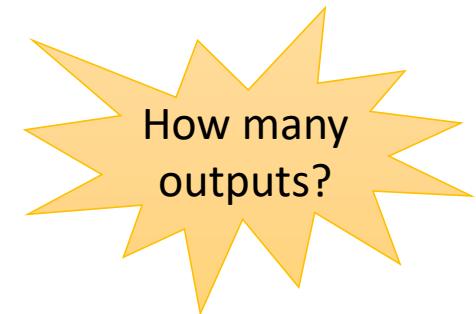
Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

We have three classes and feature vectors in \mathbb{R}^4



Input
neurons

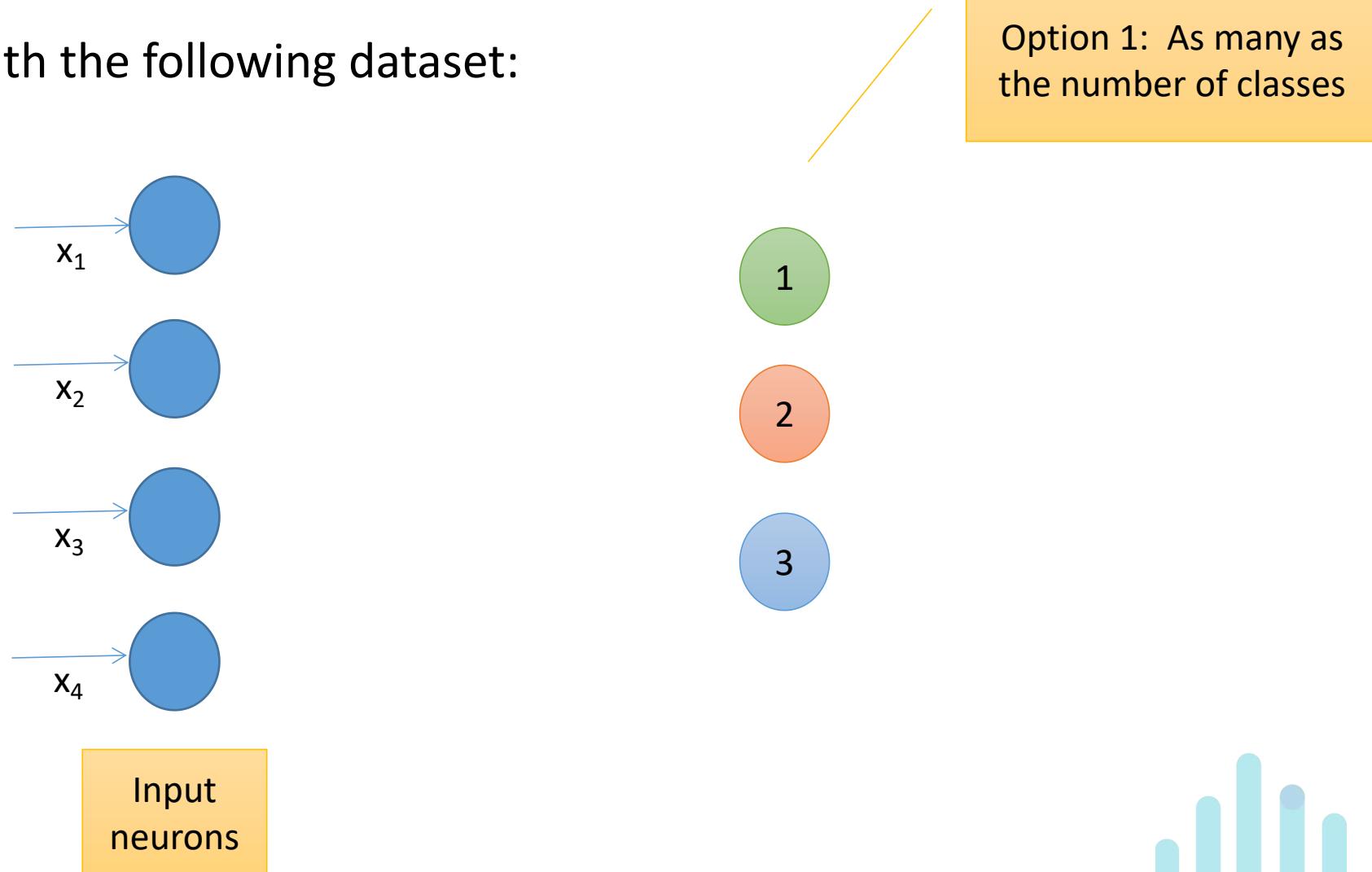


Design the neural network architecture

Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

We have three classes and feature vectors in \mathbb{R}^4

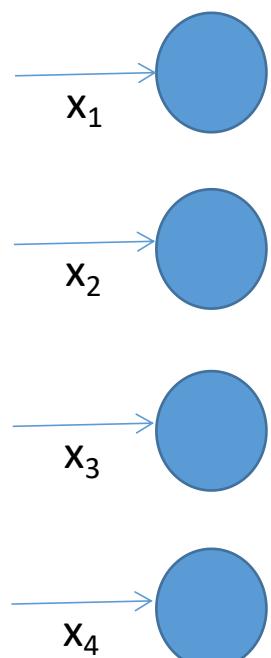


Design the neural network architecture

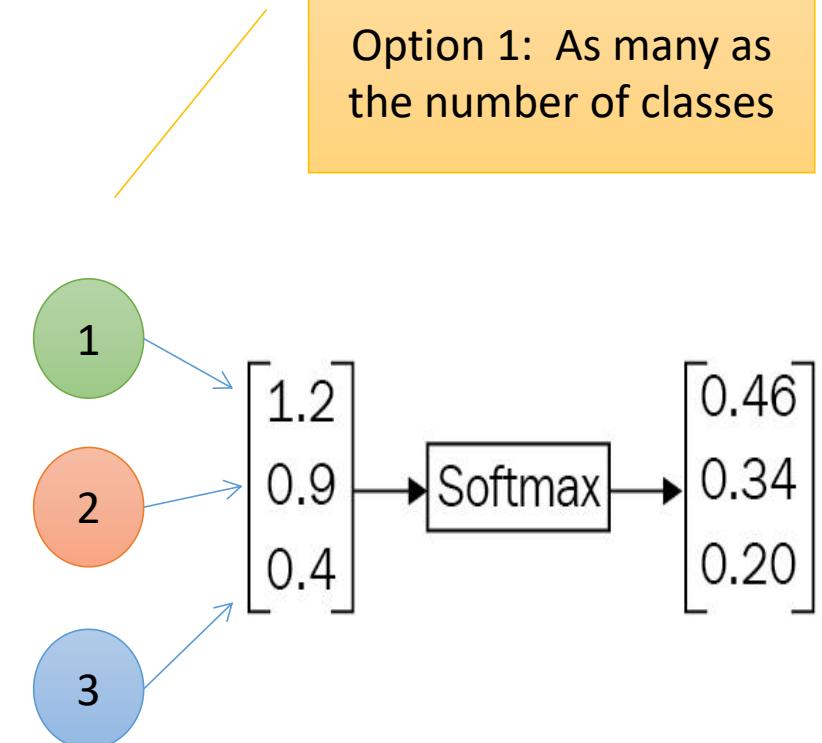
Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

We have three classes and feature vectors in \mathbb{R}^4



Input neurons



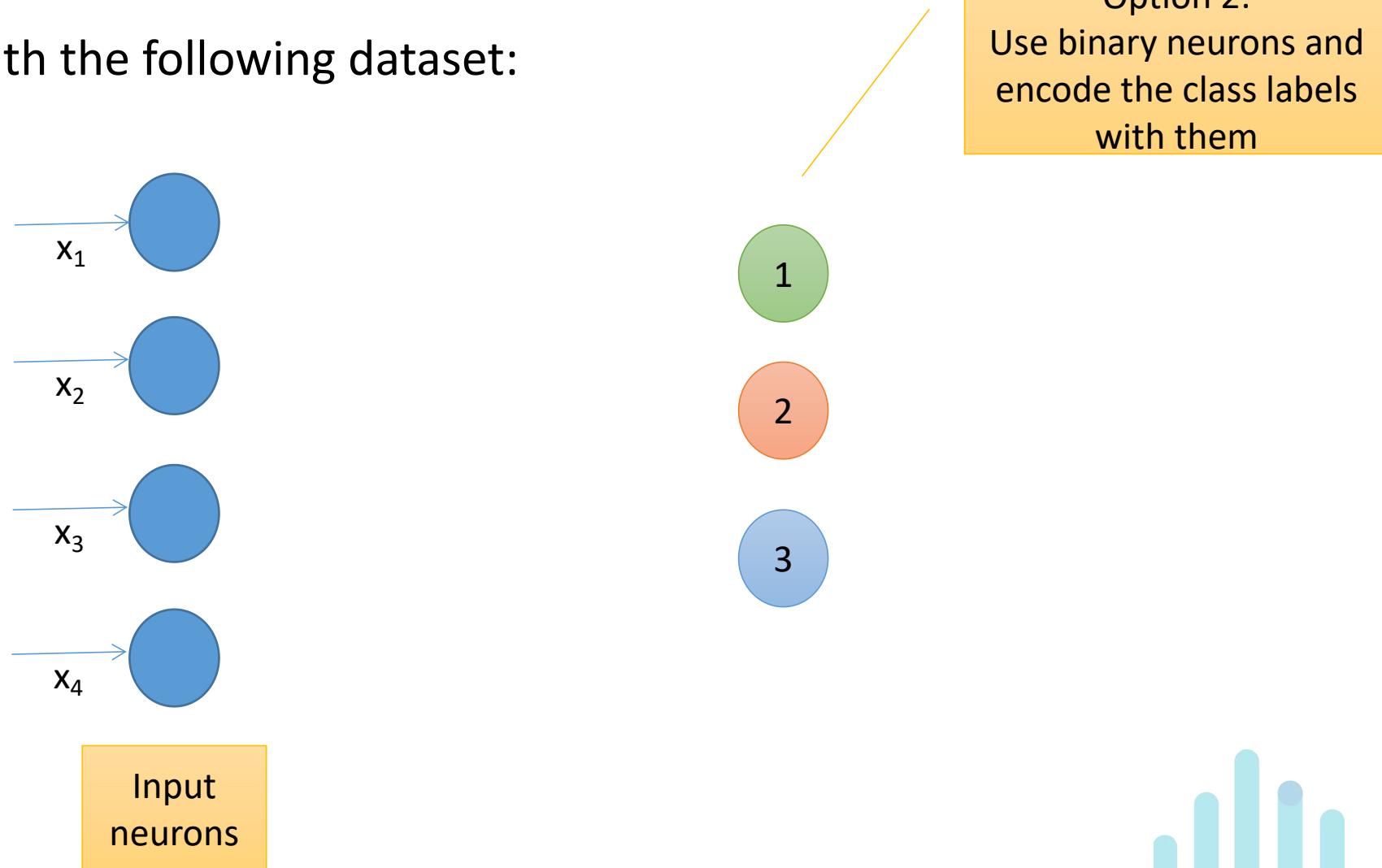
Option 1: As many as the number of classes

Design the neural network architecture

Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

We have three classes and feature vectors in \mathbb{R}^4

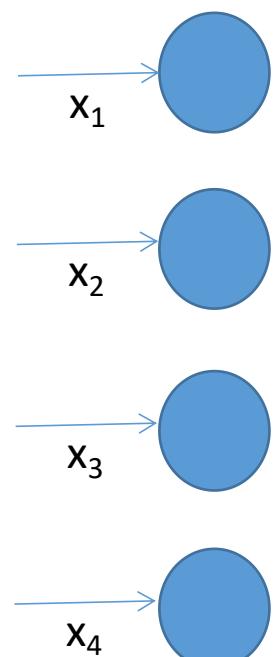


Design the neural network architecture

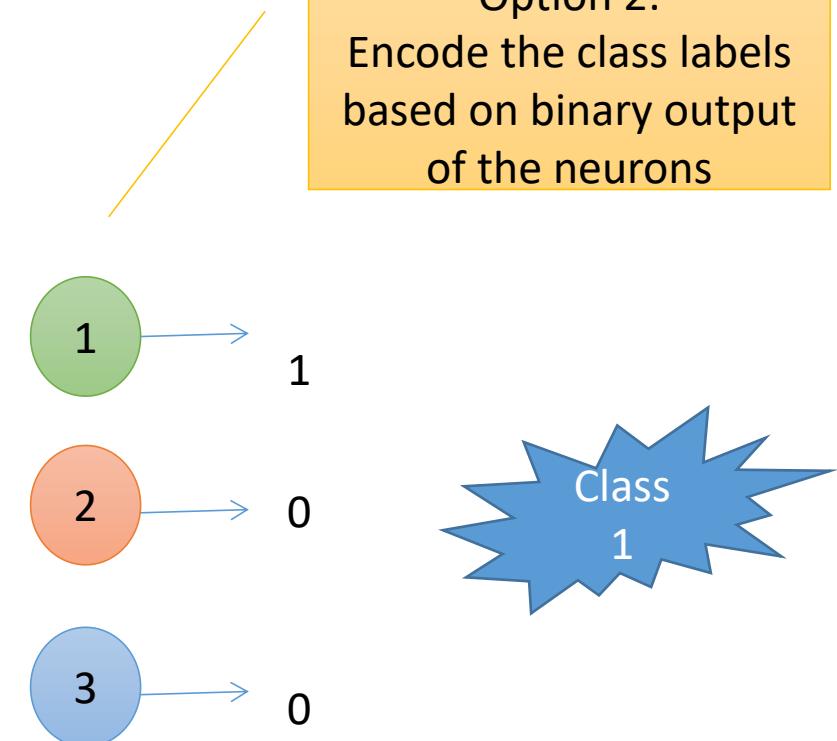
Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

We have three classes and feature vectors in \mathbb{R}^4



Input
neurons



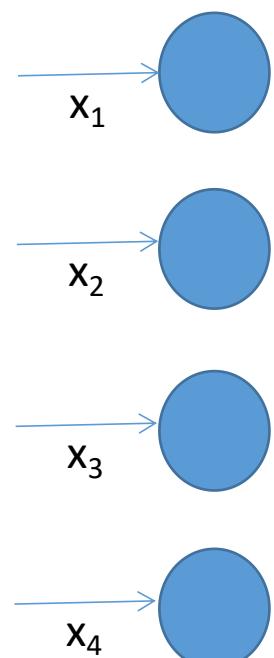
Option 2:
Encode the class labels
based on binary output
of the neurons

Design the neural network architecture

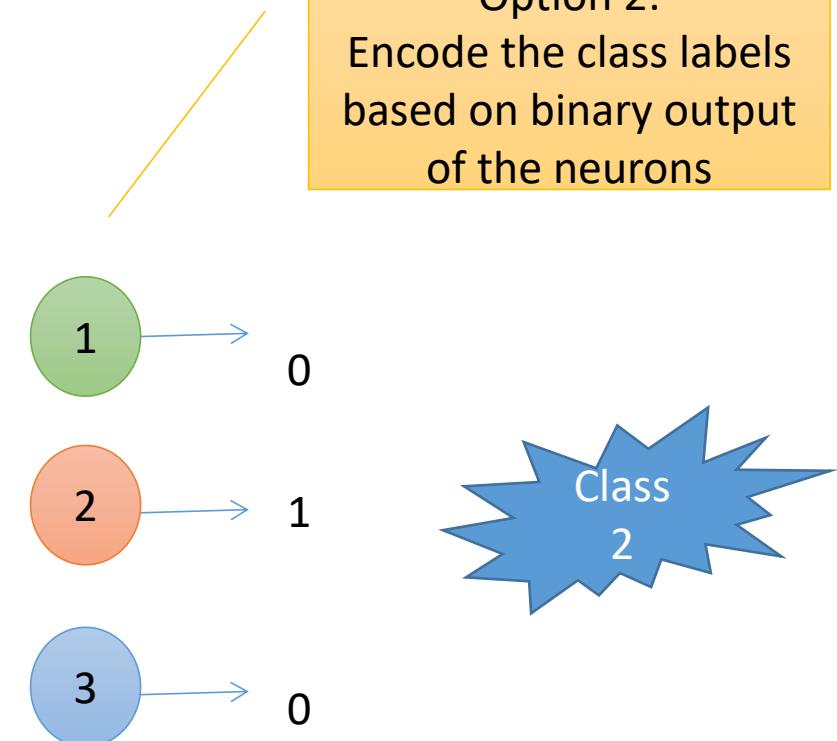
Assume a problem with the following dataset:

x ₁	x ₂	x ₃	x ₄	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

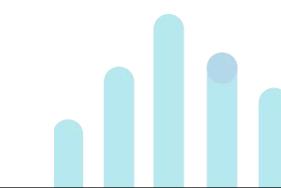
We have three classes and feature vectors in \mathbb{R}^4



Input
neurons



Option 2:
Encode the class labels
based on binary output
of the neurons

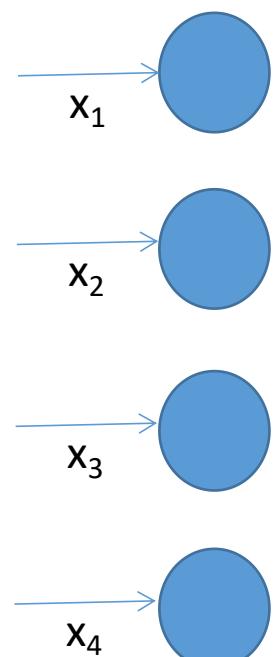


Design the neural network architecture

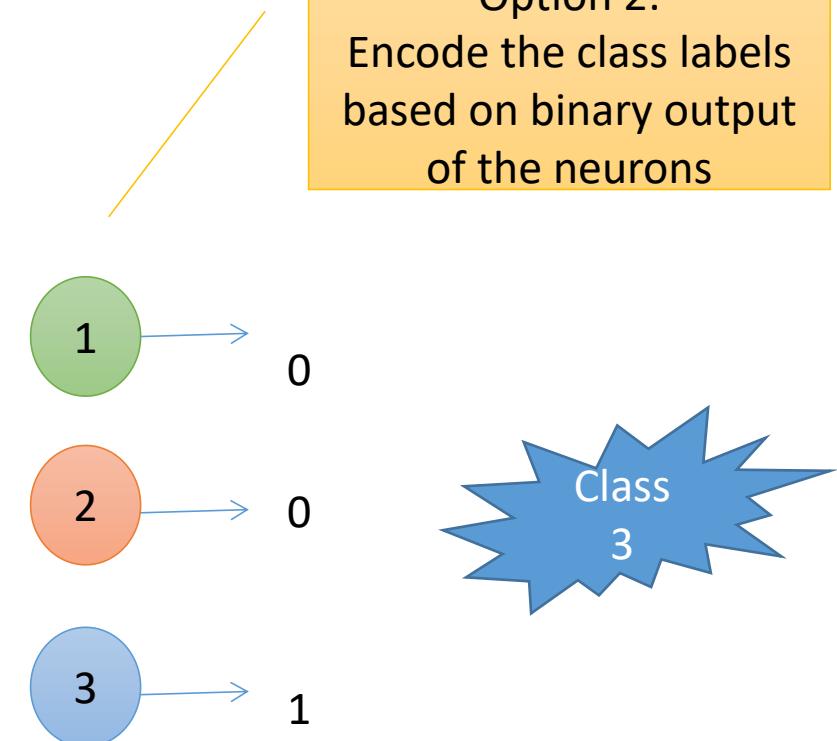
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Input
neurons



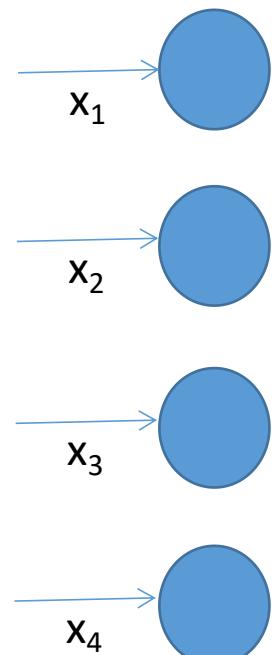
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Design the neural network architecture

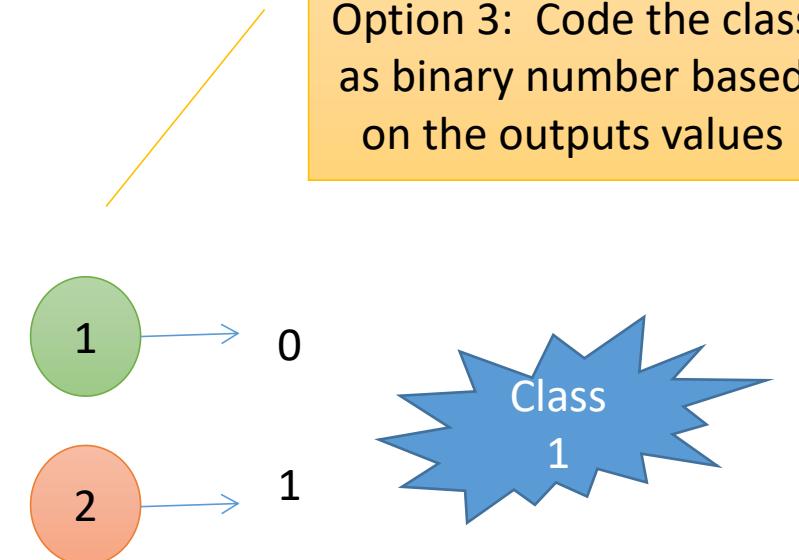
Assume a problem with the following dataset:

x1	x2	x3	x4	y
3	6	12	5	3
5	5	1	7	2
1	8	4	3	1
4	9	5	9	3
6	10	7	4	1

We have three classes and feature vectors in \mathbb{R}^4



Input neurons



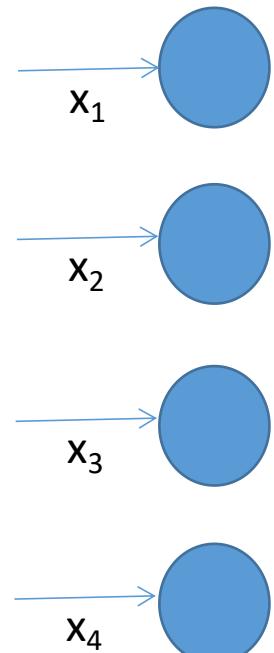
Option 3: Code the class as binary number based on the outputs values

Design the neural network architecture

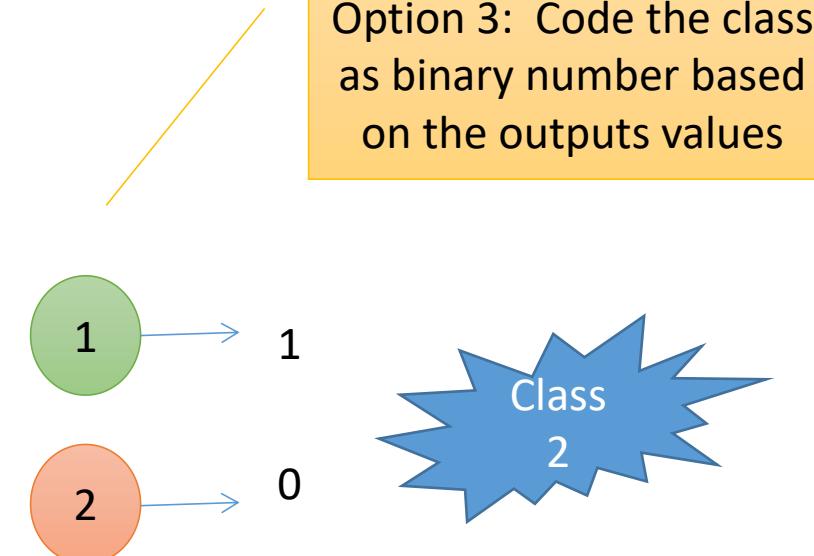
Assume a problem with the following dataset:

x1	x2	x3	x4	y
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We have three classes and feature vectors in \mathbb{R}^4



Input neurons



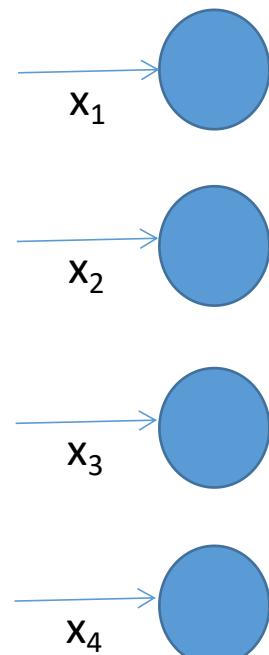
Option 3: Code the class as binary number based on the outputs values

Design the neural network architecture

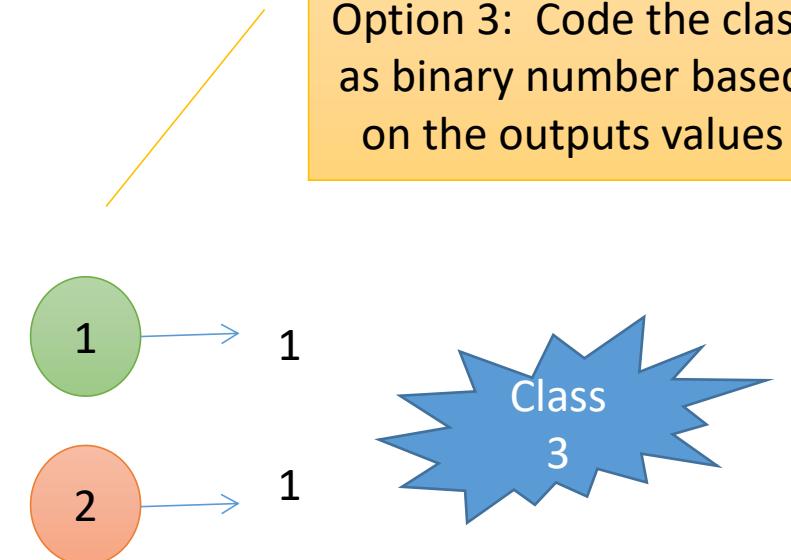
Assume a problem with the following dataset:

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We have three classes and feature vectors in \mathbb{R}^4



Input
neurons



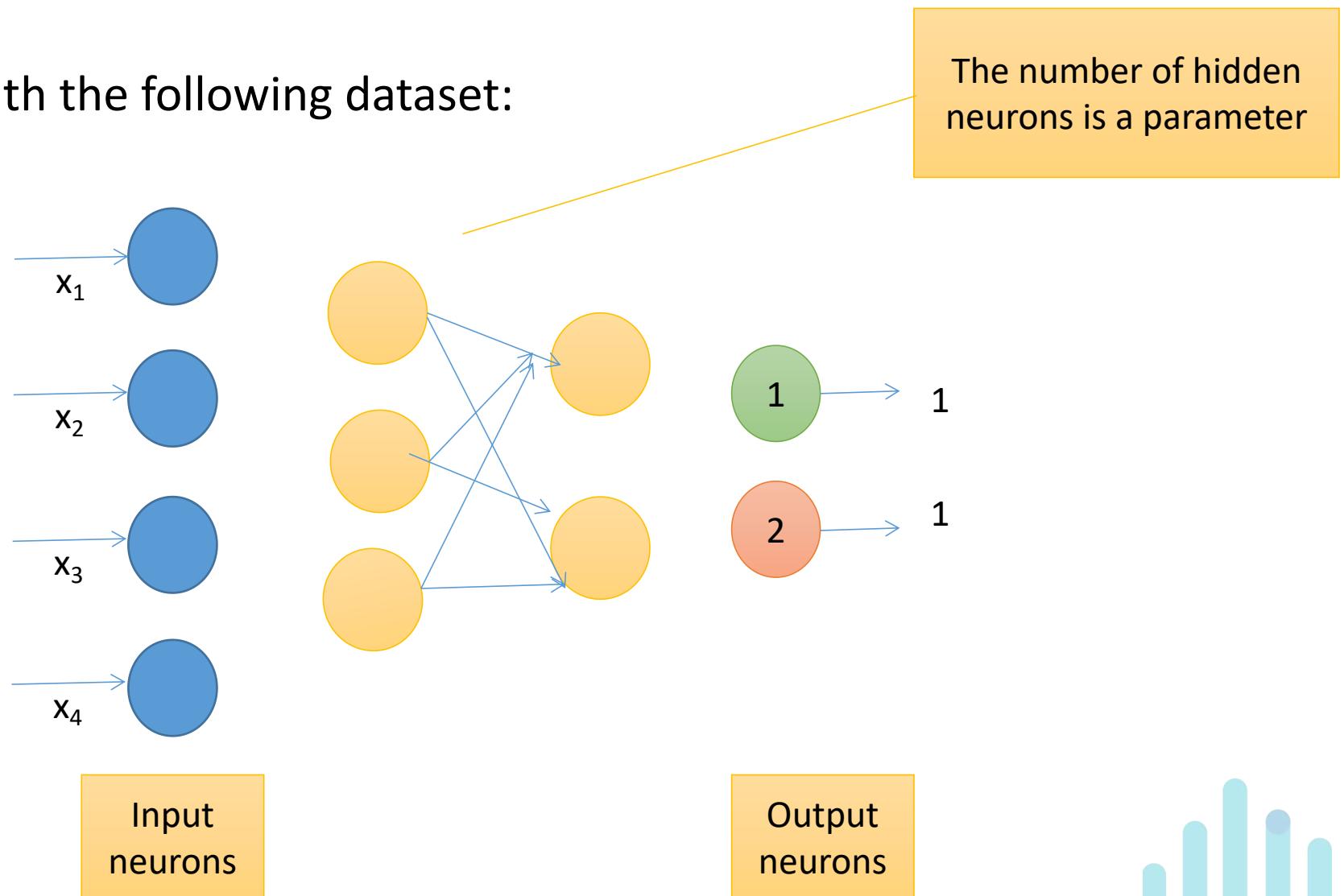
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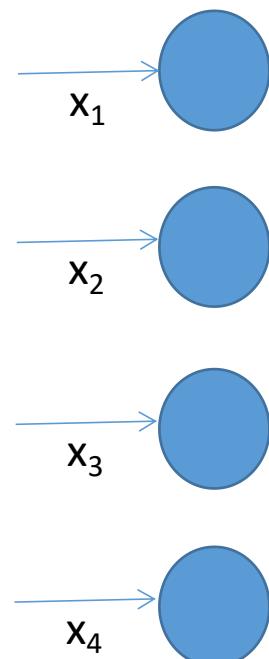


Design the neural network architecture

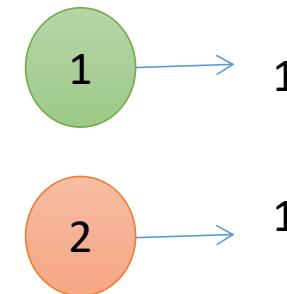
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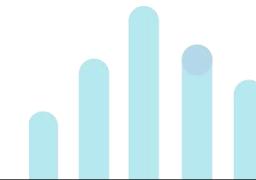
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Input
neurons

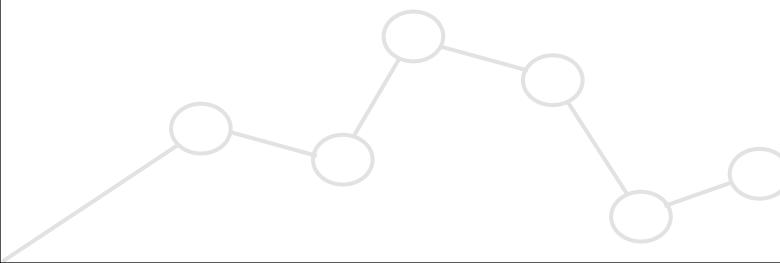


Output
neurons



Loss Function

- The MLPN use different type of error functions in order to update the weights.
- What loss function to use? Depends on the problem
- For classification problems (binary and multiclass), you can use **Cross-Entropy**
- For regression problems, we can use **Mean Squared Error**.



Loss Function- Cross Entropy

- Cross entropy measures the similarity distance between two probability vectors by means of **cross-entropy**.
- In neural networks, we can use this measure to determine the loss (error) of a neural model. This measure is defined as:

$$D(\hat{y}, y) = -\sum_j y_j \ln \hat{y}_j$$

$\hat{y} \begin{bmatrix} 0.1 \\ 0.5 \\ 0.4 \end{bmatrix}$
↓
 $y \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$

Model Prediction

Actual Values

