

Exercise 3.2-1:

$$\because \forall n_1 < n_2, f(n_1) < f(n_2), g(n_1) < g(n_2)$$

$$\therefore \forall n_1 < n_2, f(n_1) + g(n_1) < f(n_2) + g(n_2)$$

$$\because \forall n_1 < n_2, g(n_1) < g(n_2)$$

$$\therefore f(g(n_1)) < f(g(n_2))$$

$$\therefore \forall n_1 < n_2, f(g(n_1)) < f(g(n_2))$$

$$\therefore f(n) + g(n) \text{ and } f(g(n)) \text{ are monotonically increasing.}$$

If $f(n)$ and $g(n)$ are both non-negative.

$$\therefore f(n_1) < f(n_2), g(n_1) < g(n_2)$$

$$\therefore f(n_1)g(n_1) < f(n_2)g(n_2)$$

$$\therefore f(n)g(n) \text{ is monotonically increasing.}$$