

Exercise 3.1-2:

$$\text{Let } r = \frac{(n+a)^b}{n^b} = (1 + \frac{a}{n})^b$$

$$\therefore \text{When } a \geq 0, 1 \leq r \leq (1 + a)^b$$

$$\therefore \text{When } a < 0, (1 + a)^b \leq r \leq 1$$

$$\therefore \forall a, b \in \mathbb{R}, b > 0, \exists c_1, c_2 > 0, \text{s.t. } c_1 n^b \leq (n + a)^b \leq c_2 n^b$$

$$\therefore (n + a)^b = \Theta(n^b)$$