

**Exercise 2.2-3:**

Here is my linear search in python.

```
def linear_search(a, key):  
    n = len(a)  
    for i in xrange(n):  
        if a[i] == key:  
            return i  
    return -1
```

For an array of size  $N$ , let  $X$  be the number of searches needed for a key.

$$\because P\{X = i\} = \frac{1}{N}, i \in \{1, 2, \dots, N\}$$

$$\therefore E(X) = \sum_{i=1}^N \frac{i}{N} = \frac{N(N+1)/2}{N} = \frac{N+1}{2}$$

$\therefore$  The average time complexity is  $\Theta(n)$

$\because$  Worst case requires  $N$  searches

$\therefore$  It is  $\Theta(n)$  as well