

**Exercise 3.1-1:**

$\because$  We might assume that  $f(n) \geq g(n)$

$$\therefore \max(f(n), g(n)) = f(n)$$

$$\therefore \exists c_1 > 0, \text{ s.t. } f(n) \geq c_1(f(n) + g(n))$$

$$\therefore \max(f(n), g(n)) = \Omega(f(n) + g(n))$$

$$\because f(n) \leq f(n) + g(n)$$

$$\therefore \max(f(n), g(n)) = O(f(n) + g(n))$$

$$\therefore \max(f(n), g(n)) = \Theta(f(n) + g(n))$$