EECS 16A Imaging 3

Insert your names here

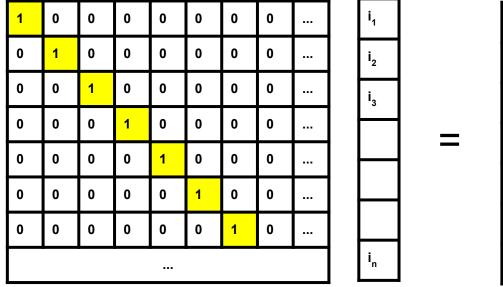
Announcements

- Buffer labs will be 3/2 to 3/4
 - You can make up **one** missed lab from the Imaging Module, if needed (unless you have received approval to make-up multiple labs)
 - Fill out the sign-up form (linked at the end of the lab notebook) if you plan to attend a buffer section

Announcements

- Optional Imaging Labs!
 - Opportunity to build a desktop scanner and scan a page using just an LED and an ambient light sensor!
- Fill out the sign-up form (linked at the end of the lab notebook) if you plan to attend an optional lab section
- See upcoming Piazza post for more details on Imaging Buffer and the Optional Imaging Lab

Last time: Matrix-vector multiplication



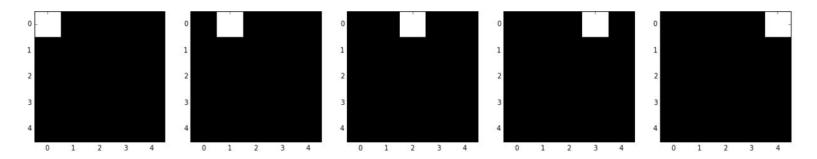
s, S_3

Masking Matrix H

Unknown, vectorized image, \vec{l}

Recorded Sensor readings, \hat{S}

Last time: Single-pixel scanning



- Setup a masking matrix where each row is a mask
 - Measured each pixel individually once

$$\vec{s} = H\vec{\iota}$$

How did we reconstruct our image, once we had s?

Poll Time! (this is review)

What are the requirements of our masking matrix H? (multiple choice)

- A. H is invertible
- B. H has linearly independent columns
- C. H has a trivial nullspace
- D. Determinant of H is 0.

$$\vec{s} = H\vec{\iota}$$

Our system

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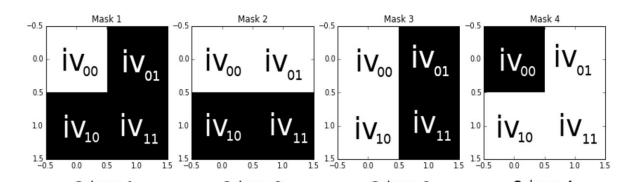
Our system

Questions from Imaging 2

Goal: Understand which measurements are good measurements

- ✓ Can we always reconstruct our image → need invertible H
- ? Are all invertible matrices equally good as scanning matrices?
- ? What happens if we mess up a single scan?
- ? What if we use multiple pixel instead of single pixel scan?

Today: Multi-pixel scanning



- Can we measure multiple pixels at a time?
 - Measurements are now linear combinations of pixels

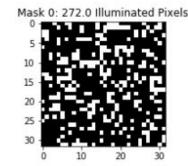
- How can we reconstruct our scanned image?
 - Is multi-pixel mask still possible to be linearly independent, aka invertible?

Why do we care?

- Improve image quality by averaging
 - Good measurements → good average
- Redundancy is useful
 - Averaging measurements is better than using bad measurement values
 - Does not "solve" bad measurements, but makes us tolerant of some errors

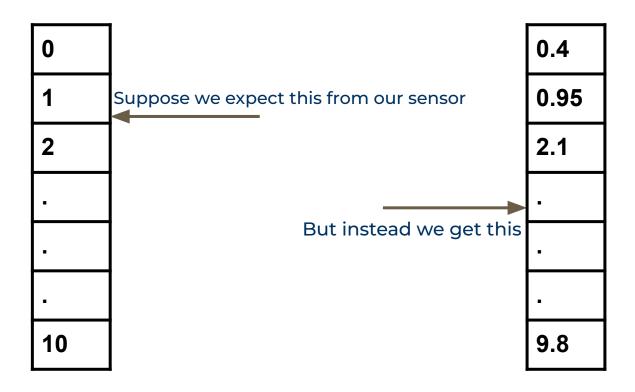
How do we do it?

 Change masks to illuminate multiple pixels per scan

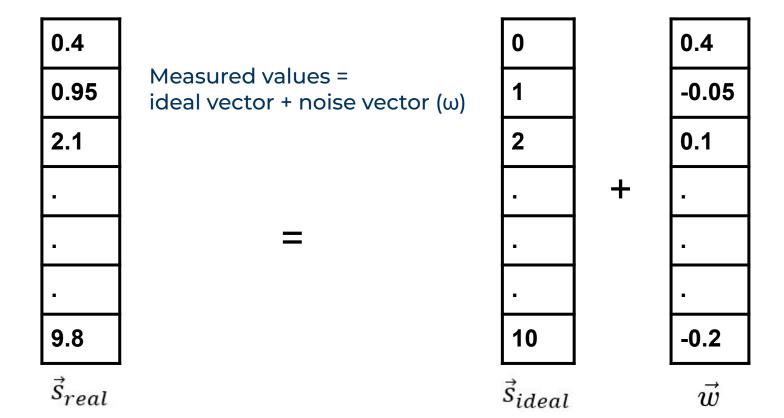


- Multiple 1's in each row of masking matrix H
- Measure linear combinations of pixels instead of single pixels
- BUT multiple pixels → more noise
 - Noise = random variation in our measurement that we don't want (ex: room light getting into box)
 - Signal = data that we do want (light from pixel illumination)
- Too much noise → hard to distinguish signal from noise
 - Want high signal, low noise
 - **Extremely important** → High signal-to-noise ratio (SNR)

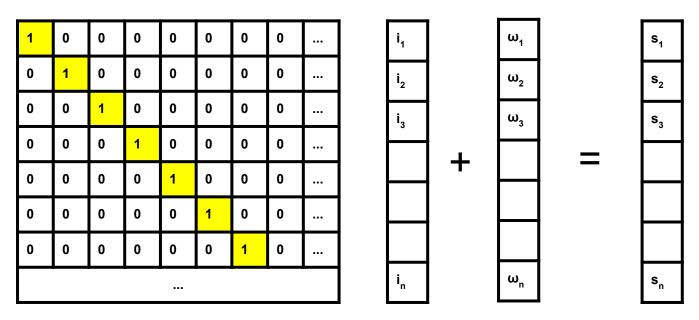
What is noise?



What is noise?



How does noise affect our system?



Masking Matrix H

Unknown, vectorized image, →

Random noise vector, \vec{w}

Recorded Sensor readings, \vec{S}

A more realistic system

Sensor readings = image vectors applied to H + noise vector

$$ec{s} = Hec{i} + ec{w}$$

We can't reconstruct i, but we can estimate it

$$ec{i}_{est} = H^{-1}ec{s} = ec{i} + H^{-1}ec{w}$$

Be careful about the noise term or else it could blow up !!

Eigenvalues for inverse matrices

- H Is an NxN matrix that we know is linearly independent (invertible).
 - No eigenvalue = 0
- Assume H has N linearly independent eigenvectors
- $Hv_i = \lambda_i v_i$ for i = 1...N
- N lin. ind. vectors can span \mathbb{R}^N
 - They span the noise vector
- The inverse of H has eigenvalues $\frac{1}{\lambda_1} \cdots \frac{1}{\lambda_N}$ (as proven in homework)

$$H^{-1}v_i = \frac{1}{\lambda_i}v_i \text{ for } i = 1...N$$

How do eigenvalues affect noise?

The noise vector can be written as:

$$\overrightarrow{\omega} = \alpha_1 \overrightarrow{v_1} + \alpha_2 \overrightarrow{v_2} + \cdots \alpha_n \overrightarrow{v_n}$$

Including effect of H^{-1}

$$H^{-1}\overrightarrow{\omega} = H^{-1}(\alpha_1\overrightarrow{v_1} + \alpha_2\overrightarrow{v_2} + \cdots + \alpha_n\overrightarrow{v_n})$$

Rewritten with eigenvalues:

$$H^{-1} \overrightarrow{\omega} = \frac{1}{\lambda_1} \alpha_1 \overrightarrow{v_1} + \frac{1}{\lambda_2} \alpha_2 \overrightarrow{v_2} + \cdots \frac{1}{\lambda_n} \alpha_n \overrightarrow{v_n}$$

Linking it all together

$$\vec{\iota}_{est} = H^{-1}\vec{s} + \boxed{H^{-1}\vec{\omega}}$$

$$H^{-1}\vec{\omega} = \frac{1}{\lambda_1}\alpha_1\vec{v_1} + \frac{1}{\lambda_2}\alpha_2\vec{v_2} + \cdots + \frac{1}{\lambda_n}\alpha_n\vec{v_n}$$

- Remember: want small noise term for high signal-to-noise ratio
- The noise is directly related to the eigenvalues

Poll Time!

- Do we want small or large eigenvalues for the H matrix in order to get a good image?
 - A. Large
 - B. The magnitude doesn't matter
 - C. Small
- Which of the following equations correctly model our imaging system? (multiple choice)
 - A. $s_{ideal} = H.i$
 - B. $s_{real} = s_{ideal} + w = H.i + w$
 - C. $s_{real} = s_{ideal} + w = H.i + H.w$
 - D. $i_{est} = H^{-1}.s_{real} = H^{-1}.s_{ideal} + H^{-1}.w$
 - E. $i_{est} = H^{-1}.s_{real} = H^{-1}.s_{ideal} + w$

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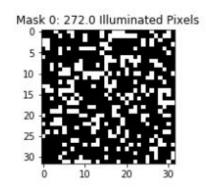
B. s_{real} = s_{ideal} + w = H.i + w

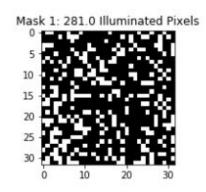
C. s_{real} = s_{ideal} + w = H.i + H.w

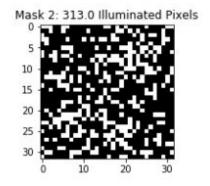
D. i_{est} = H^{-1}.s_{real} = H^{-1}.s_{ideal} + H^{-1}.w

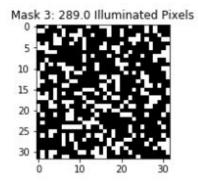
E. i_{est} = H^{-1}.s_{real} = H^{-1}.s_{ideal} + w
```

Possible scanning matrix: Random







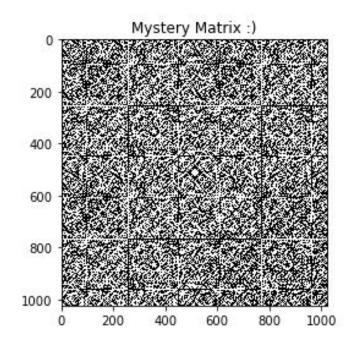


- Illuminate ~300 pixels per scan
 - Usually invertible
 - But what are its eigenvalues?

A more systematic scanning matrix

Hadamard matrix!

- Constructed to have large eigenvalues
 - o Just what we need!



Projector Setup

USE DIFFERENT AMBIENT LIGHT SENSORS

- Instead of the sensor in your kit, grab one from the TA desk and return it during checkoff
- Ambient light sensors from the TA desk should not leave the lab
- Project masks (rows of H) onto image and "measure" s using matrix multiplication
- Multiply with H inverse to find i (=H⁻¹s)
- SAME EXACT HARDWARE SETUP AS IMG 2
 - Don't forget to adjust projector settings!

Pointers

- READ CAREFULLY Long lab with lots of reading; heavily tests understanding of eigen-stuff (important for the exam)
- 2. Choose an image that focuses on a single object and is not too detailed
- 3. In case the kernel crashes, simply save your notebook and restart it. You should navigate to the previous import block and run all blocks starting there.

Pointers / Debugging

- 1. Make sure wires/resistors/light sensor are not loose
- 2. Light sensor orientation: short leg goes into +
- 3. Check COM Port
- Reupload code to launchpad after making any change in circuit
- 5. Check Baud Rate in Serial Monitor (115200)
- Projector might randomly restart in the middle of the lab. Make sure brightness 0 contrast 100.
- 7. Cover box with jacket for dark scanning conditions
- 8. If you see a very bright corner in the scan, move the light sensor away from the projector