

## Lecture 5A: (7/17/23)

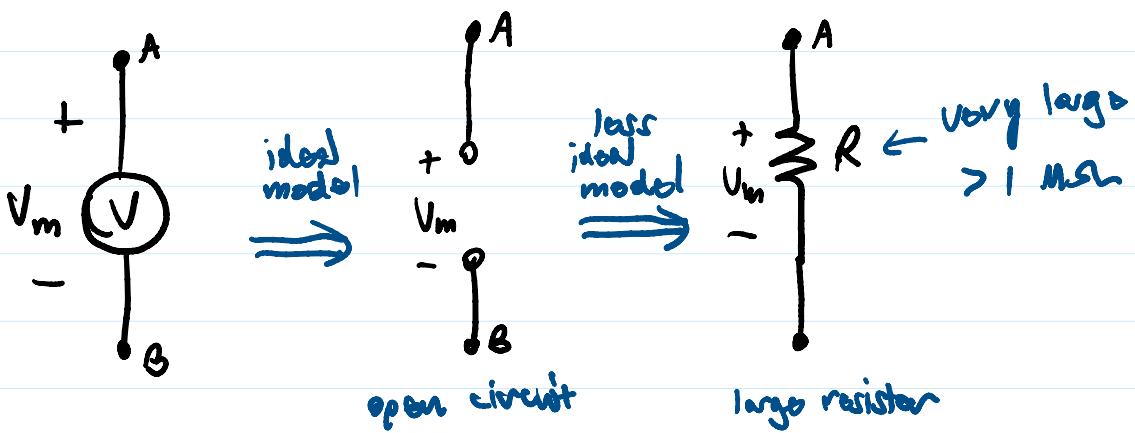
### Announcements:

- Quest: grades are released. Mean: 82.1% Median: 87.3%
- You have until Wednesday at midnight to request a regrade
- Midterm: Next Monday from 7-9 pm, Dwinelle 145
- Lab - Touch 1 (Tues) and Touch 2 (Thurs)
  - Please consider moving sections
- Office Hours - Mon/Wed 1-2pm in Cory 144MA  
HW Party - Friday 10am-noon ↴
- Today's Topics:
  - Voltage/Current Measurement (Note 13)
  - 1D Resistive Touchscreen (Note 13)
  - 2D Resistive Touchscreen (Note 14)
  - Superposition (Note 15)

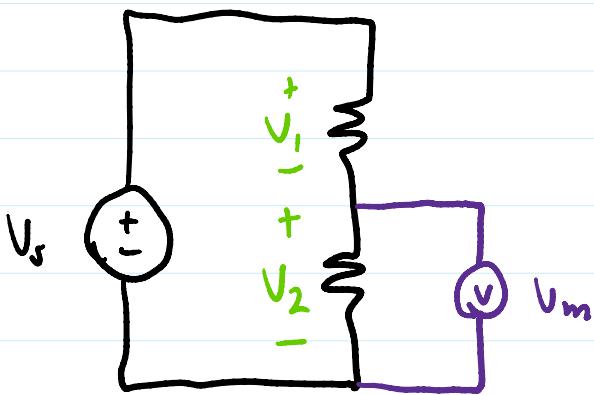
### Measuring Voltage and Current

Voltmeter: device which measures voltage across it

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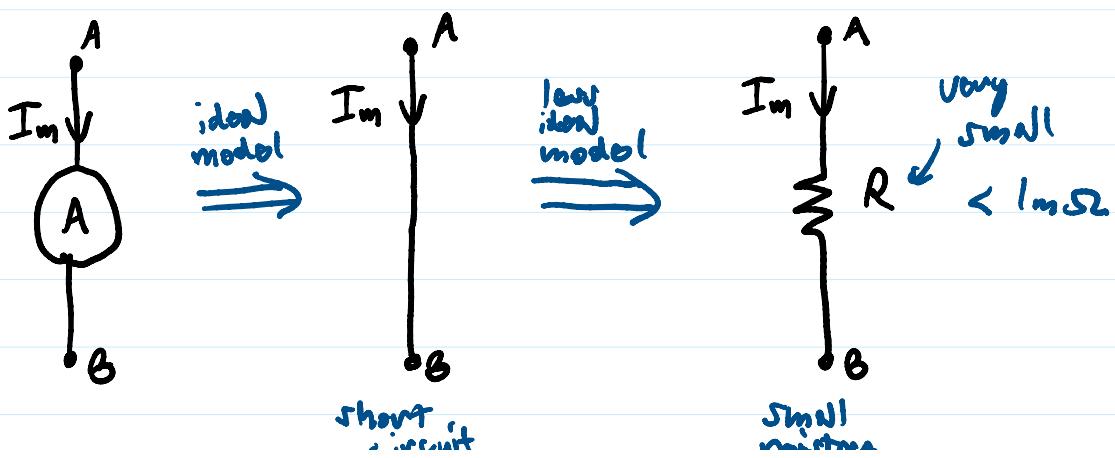
Ex).



$$V_m = V_2$$

If voltmeter is open circuit then  
 $P = V \cdot I = 0$  ↗  
 no energy loss

ammeter: device which measures current (amp) through it



• B

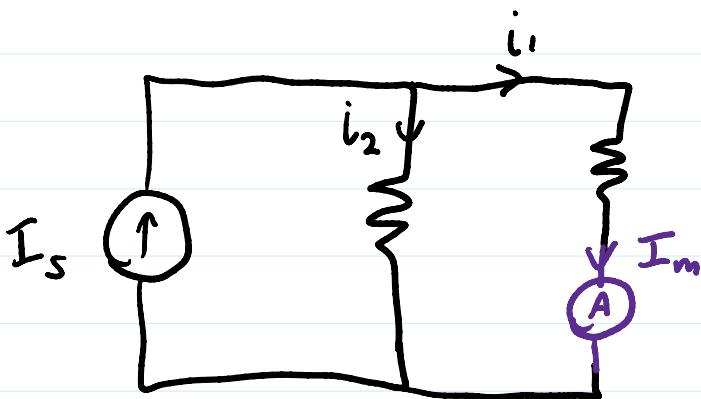
• B

• B

short  
circuit

short  
circuit

Ex).

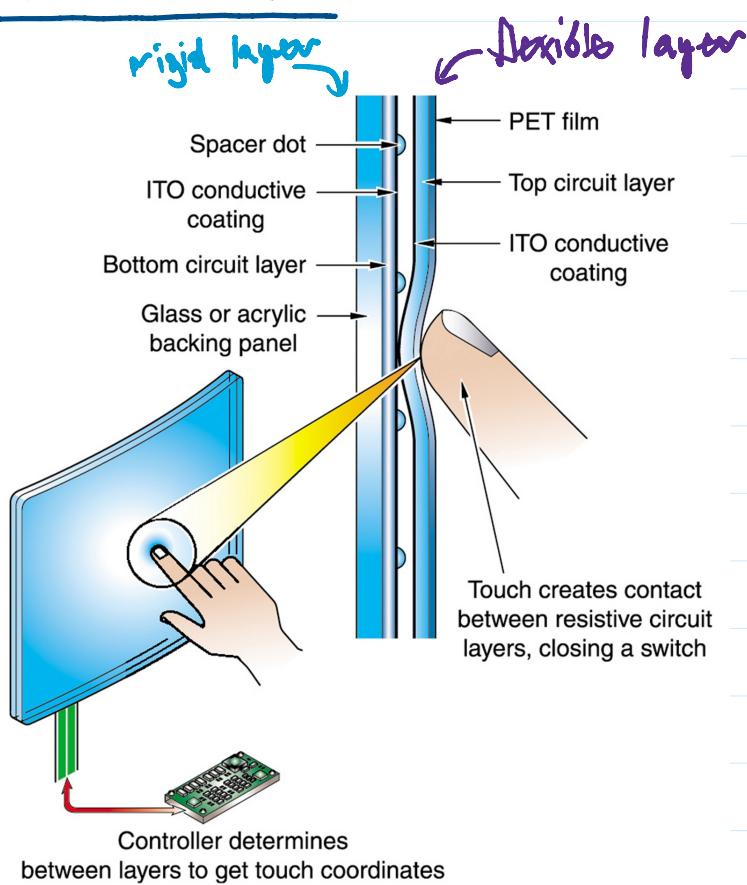


$$I_m = i_1$$

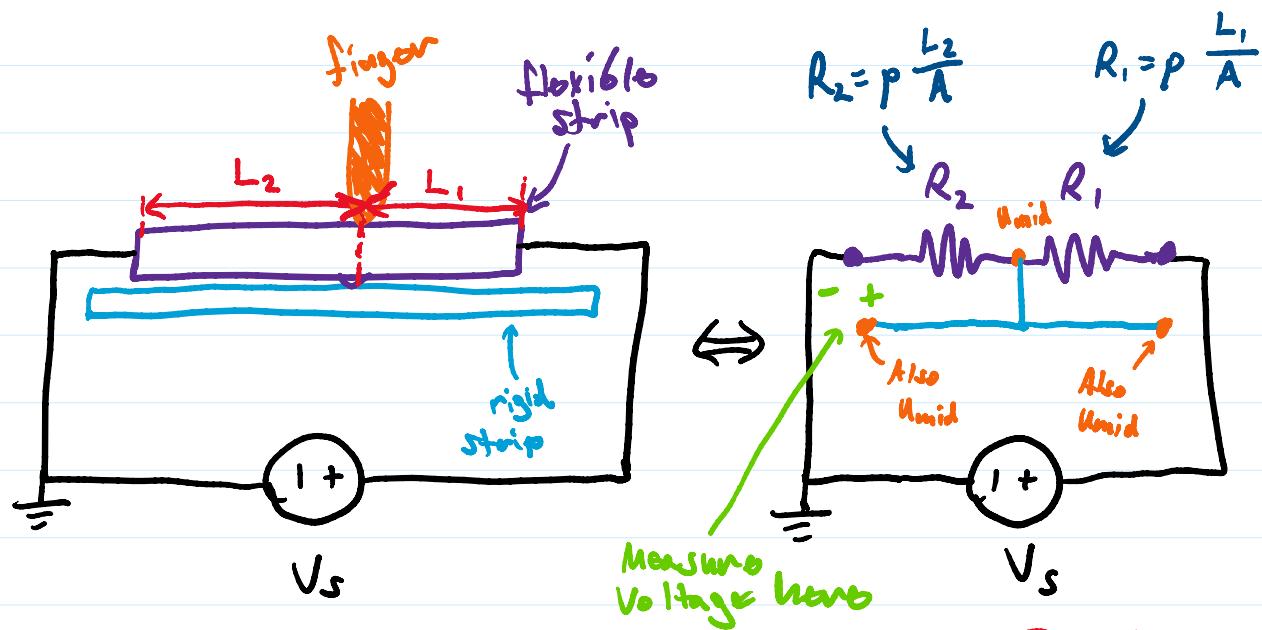
If unmotor is  
short circuit, then

$$\rho = V \cdot i = 0 \text{ J} \\ = 0 \text{ no energy loss}$$

## 1D Resistive Touch



Both layers are  
resistive!

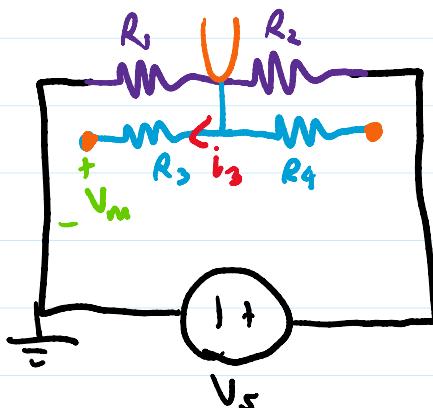


$$V_{mid} = \frac{R_2}{R_1 + R_2} V_s = \frac{\left(\rho \frac{L_2}{A}\right)}{\left(\rho \frac{L_1}{A}\right) + \left(\rho \frac{L_2}{A}\right)} V_s = \frac{L_2}{L_1 + L_2} V_s = \frac{L_2}{L_{total}} V_s$$

relative position

How can we actually measure  $V_{mid}$ ?

Use rigid layer ← Doesn't this have resistance too? !!



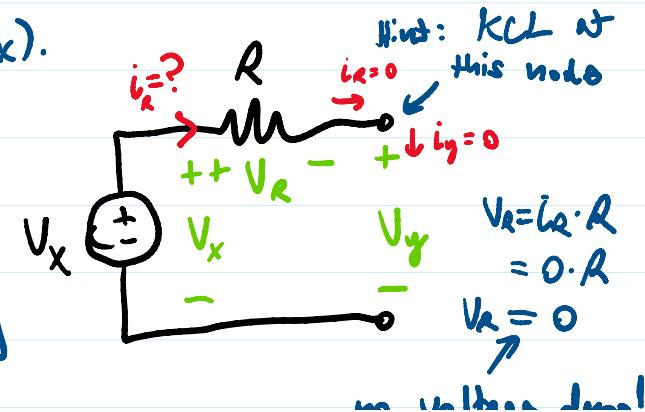
Does measured  $V_m$  change because of  $R_3$  and  $R_4$ ?

How much current flows through  $R_3$ ?  $i_3 = 0$ !

Current flow requires closed loops

The resistance of the rigid layer is inconsequential

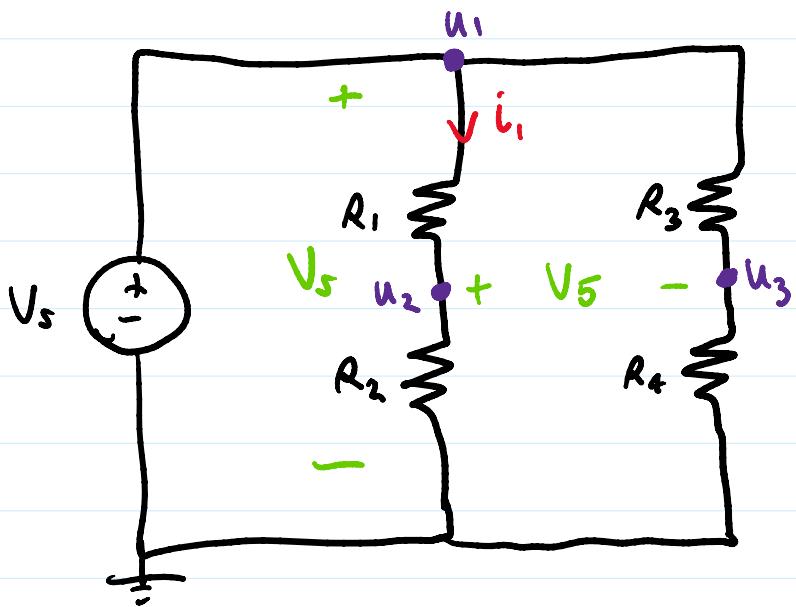
Ex).



rigid layer is inconsequential

$$v_R = v \rightarrow \text{no voltage drop!}$$

### Interesting Circuit:



What is  $u_2$ ?

$$u_2 = \frac{R_2}{R_1 + R_2} V_s$$

Add second branch:

What is  $u_3$ ?

$$u_3 = \frac{R_4}{R_3 + R_4} V_s$$

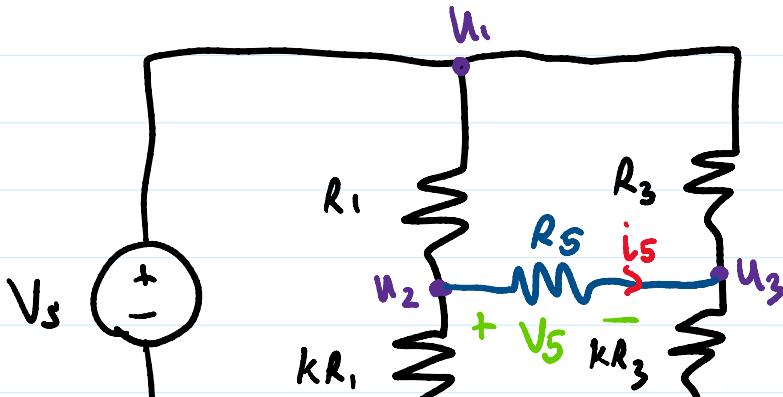
Does  $u_2$  change?  
(Does  $i_1$  change?)

No

$$i_1 = \frac{V_s}{R_1 + R_2} \quad u_2 = i_1 \cdot R_2 = \frac{R_2}{R_1 + R_2} V_s$$

If you add (or subtract) to the circuit, the circuit voltages and currents likely change.  $\leftarrow$  Need to check

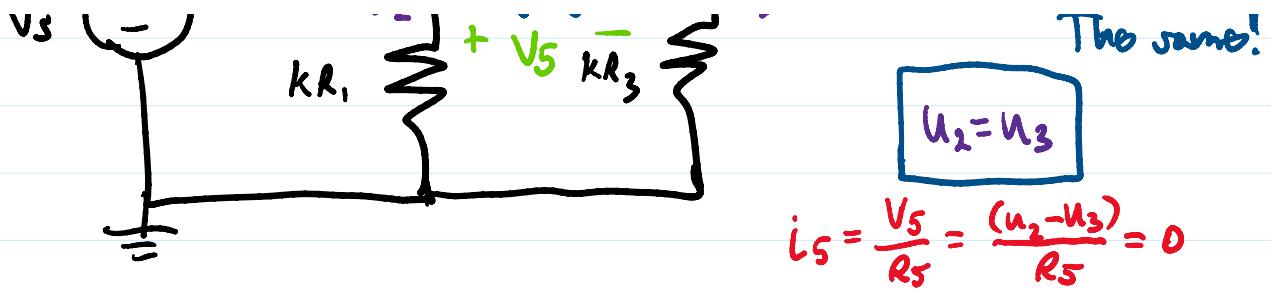
What if  $R_2 = k \cdot R_1$  and  $R_4 = k \cdot R_3$ ?



$$u_2 = \frac{kR_1}{kR_1 + R_2} V_s = \frac{k}{1+k} V_s$$

$$u_3 = \frac{kR_3}{R_3 + kR_3} V_s = \frac{k}{1+k} V_s$$

The same!



Let's add a resistor  $R_5$  between  $U_2$  and  $U_3$ .

What's the current through this resistor?

Foolproof way  $\Rightarrow$  Perform full NVA

Sneaky way  $\Rightarrow$  Do  $U_2$  and  $U_3$  change?

Before:

$$V_5 = U_2 - U_3 = 0$$

After:

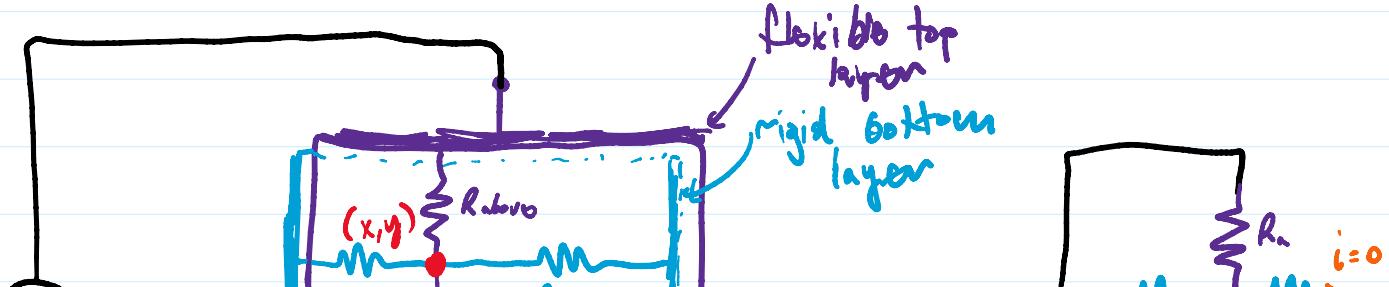
$$V_5 = U_2 - U_3 = 0$$

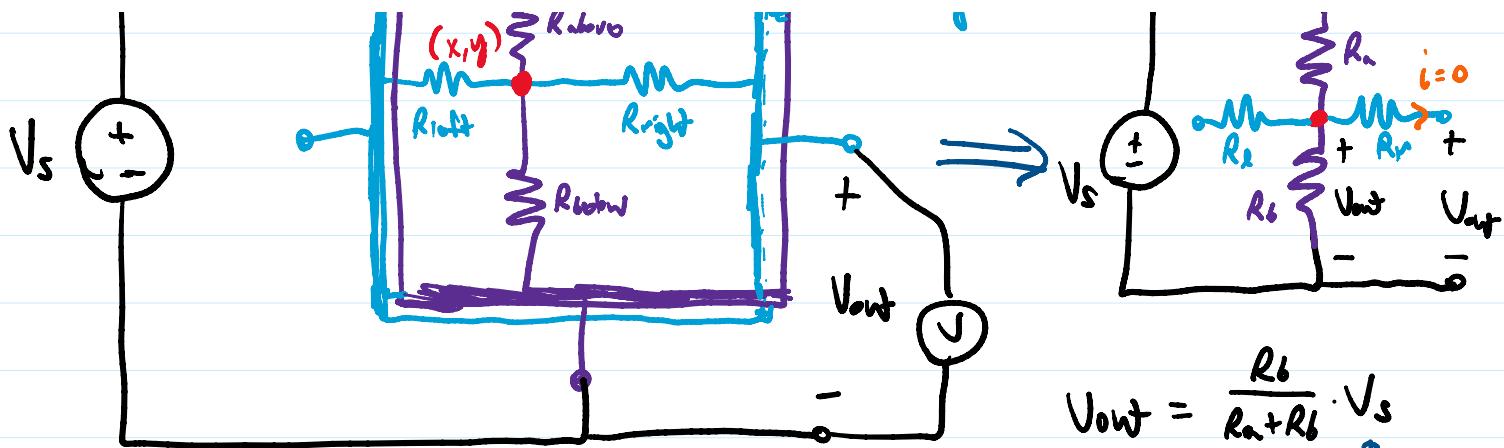
Trick: If you connect a resistor between two nodes with the same voltage, then it does not change the circuit  $\leftarrow$  "virtual open circuit"

since  $i=0$  ALWAYS

I-V characteristic  
of open circuit

## 2D Resistive Touch





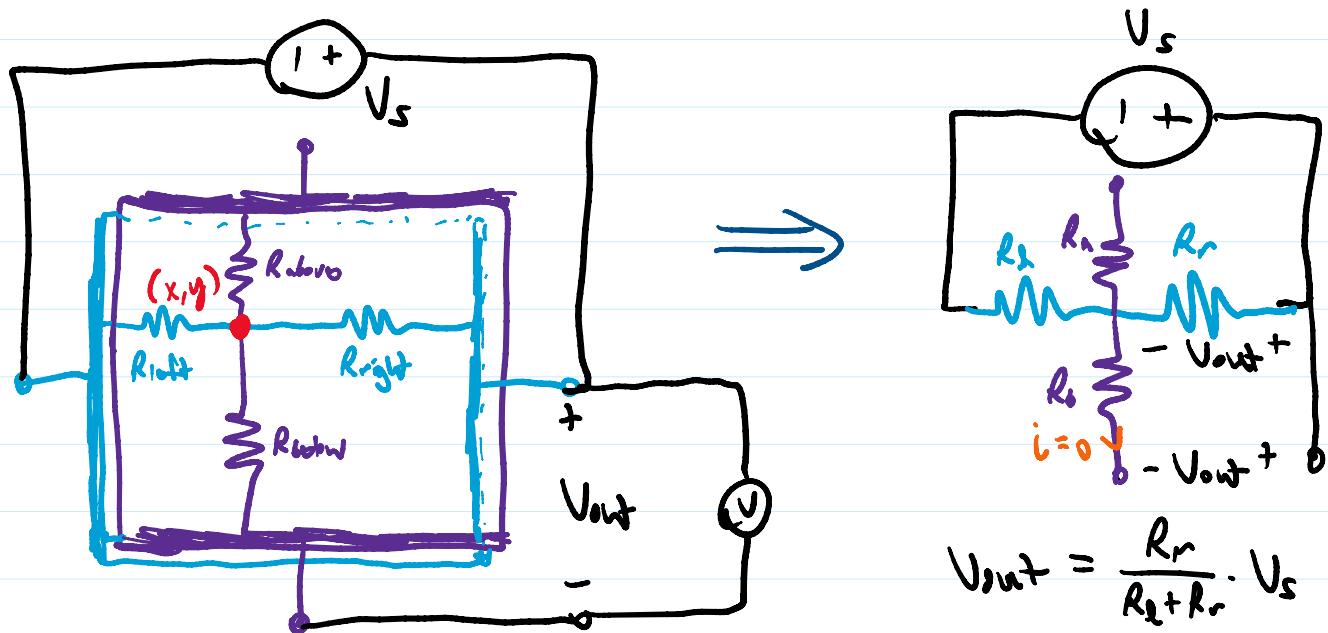
$$V_{out} = \frac{R_b}{R_a + R_b} \cdot V_s$$

$\uparrow$  known       $\uparrow$  known  
can determine  $y$  value

This circuit measures vertical position.

How can we measure horizontal position?

- Connect voltage source to bottom layer.



$$V_{out} = \frac{R_r}{R_l + R_r} \cdot V_s$$

This circuit measures horizontal position

Switch between two circuits to get both  $x$  and  $y$ .