# Assignment 3

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Abstract—This document explains the concept of the equation of a circle passing through three points.

Download the python code from

https://github.com/ee17btech11034/AI5106/blob/ main/Assignment 4/AI assignment 4.py

and latex-tikz codes from

https://github.com/ee17btech11034/AI5106/blob/ main/Assignment 4/assignment 4.tex

#### 1 Problem

Find the equation to the circle which has its centre at  $\binom{3}{4}$  and touches the straight line  $(5 \ 12)\mathbf{x} = 1$ .

### 2 EXPLANATION

General equation of line and circle are given by:

$$\mathbf{n}^T \mathbf{x} - d = 0 \tag{2.0.1}$$

$$\mathbf{x}^T \mathbf{x} - 2\mathbf{c}^T \mathbf{x} + f = 0 \tag{2.0.2}$$

The straight line touches the circle so the radius of circle:

$$r = \left| \frac{\mathbf{n}^T \mathbf{c} - d}{\|\mathbf{n}\|} \right| \tag{2.0.3}$$

$$f = ||\mathbf{c}||^2 - r^2 \tag{2.0.4}$$

## 3 Solution

So, the radius of circle is:

$$r = \left| \frac{\left(5 \quad 12\right) \left(\frac{3}{4}\right) - 1}{\sqrt{(5)^2 + (12)^2}} \right|$$
 (3.0.1)  
$$r = \frac{62}{13}$$
 (3.0.2)

$$r = \frac{62}{13} \tag{3.0.2}$$

$$f = (3)^2 + (4)^2 - (\frac{62}{13})^2$$
 (3.0.3)

$$f = \frac{381}{169} \tag{3.0.4}$$

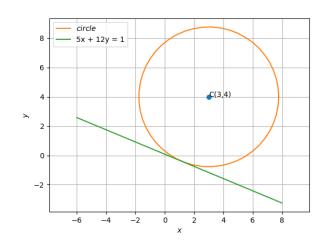


Fig. 0: Circle touches a line

Equation of circle is:

$$\mathbf{x}^T \mathbf{x} - 2(3 \quad 4)\mathbf{x} + \frac{381}{169} = 0$$
 (3.0.5)