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Assignment 2

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Abstract—This document explains the concept of a straight line equation that is parallel to a line and is passing through a point.

Download the python code from

https://github.com/ee17btech11034/AI5106/blob/main/Assignment_2/AI_assignment_2.py

and latex-tikz codes from

https://github.com/ee17btech11034/AI5106/blob/main/Assignment_2/assignment_2.tex

1 Problem

Find the equation of a line parallel to (2 5)x = 11 passing through the middle point of the join of the points $\begin{pmatrix} -7 \\ 3 \end{pmatrix}$, $\begin{pmatrix} 5 \\ -11 \end{pmatrix}$.

2 EXPLANATION

General equation of straight line is given by:

$$\mathbf{n}^T \mathbf{x} = c \tag{2.0.1}$$

n will be same because both lines are parallel.

$$\mathbf{n} = \begin{pmatrix} 2 \\ 5 \end{pmatrix} \tag{2.0.2}$$

Passing through mid point M of A, B:

$$\mathbf{M} = \frac{\mathbf{A} + \mathbf{B}}{2} \tag{2.0.3}$$

$$\mathbf{n}^T(\mathbf{x} - \mathbf{M}) = 0 \tag{2.0.4}$$

$$\mathbf{n}^T \mathbf{x} = \mathbf{n}^T \mathbf{M} \tag{2.0.5}$$

3 Solution

So, the mid point M is:

$$\mathbf{M} = \frac{\begin{pmatrix} -7\\3 \end{pmatrix} + \begin{pmatrix} 5\\-11 \end{pmatrix}}{2} = \begin{pmatrix} -1\\-4 \end{pmatrix} \tag{3.0.1}$$

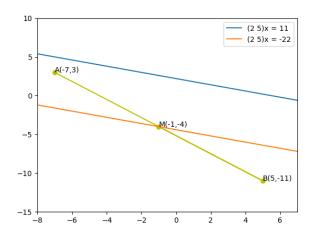


Fig. 0: Parallel Lines

$$\mathbf{n}^T \mathbf{x} = \begin{pmatrix} 2 & 5 \end{pmatrix} \begin{pmatrix} -1 \\ -4 \end{pmatrix} = -22 \tag{3.0.2}$$

So, the equation of line is:

$$(2 5) \mathbf{x} = -22 (3.0.3)$$