## Probability and Random Processes

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Q) Verify that

$$\frac{BG}{GE} = \frac{CG}{GF} = \frac{AG}{GD} = 2$$

Solution: Three vertices of the triangle and midpoints are:

$$\mathbf{A} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}, \qquad \mathbf{B} = \begin{pmatrix} -4 \\ 6 \end{pmatrix} \tag{1}$$

$$\mathbf{C} = \begin{pmatrix} -3 \\ -5 \end{pmatrix}, \qquad \mathbf{D} = \begin{pmatrix} -3.5 \\ 0.5 \end{pmatrix} \tag{2}$$

$$\mathbf{E} = \begin{pmatrix} -1 \\ -3 \end{pmatrix}, \qquad \mathbf{F} = \begin{pmatrix} -1.5 \\ 2.5 \end{pmatrix} \tag{3}$$

$$\mathbf{G} = \begin{pmatrix} -2\\0 \end{pmatrix} \tag{4}$$

We have to find AG and GD.

$$AG = \|\mathbf{G} - \mathbf{A}\| \tag{5}$$

$$= \left\| \begin{pmatrix} -2 \\ 0 \end{pmatrix} - \begin{pmatrix} 1 \\ -1 \end{pmatrix} \right\| \tag{6}$$

$$= \left\| \begin{pmatrix} -3\\1 \end{pmatrix} \right\| = \sqrt{10} \tag{7}$$

$$GD = ||\mathbf{D} - \mathbf{G}|| \tag{8}$$

$$= \left\| \begin{pmatrix} -3.5 \\ 0.5 \end{pmatrix} - \begin{pmatrix} -2 \\ 0 \end{pmatrix} \right\| \tag{9}$$

$$= \left\| \begin{pmatrix} -1.5 \\ 0.5 \end{pmatrix} \right\| = \sqrt{2.5} \tag{10}$$

We have to find BG and GE.

$$BG = \|\mathbf{G} - \mathbf{B}\| \tag{11}$$

$$= \left\| \begin{pmatrix} -2\\0 \end{pmatrix} - \begin{pmatrix} -4\\6 \end{pmatrix} \right\| \tag{12}$$

$$= \left\| \begin{pmatrix} 2 \\ -6 \end{pmatrix} \right\| = \sqrt{40} \tag{13}$$

$$GE = ||\mathbf{E} - \mathbf{G}|| \tag{14}$$

$$= \left\| \begin{pmatrix} -1 \\ -3 \end{pmatrix} - \begin{pmatrix} -2 \\ 0 \end{pmatrix} \right\| \tag{15}$$

$$= \left\| \begin{pmatrix} 1 \\ -3 \end{pmatrix} \right\| = \sqrt{10} \tag{16}$$

2) The ratio of  $BG: GE = \frac{\sqrt{40}}{\sqrt{10}} = 2:1$  We have to find CG and GF.

$$CG = \|\mathbf{G} - \mathbf{C}\| \tag{17}$$

$$= \left\| \begin{pmatrix} -2\\0 \end{pmatrix} - \begin{pmatrix} -3\\-5 \end{pmatrix} \right\| \tag{18}$$

$$= \left\| \begin{pmatrix} 1 \\ 5 \end{pmatrix} \right\| = \sqrt{26} \tag{19}$$

$$GF = ||\mathbf{F} - \mathbf{G}|| \tag{20}$$

$$= \left\| \begin{pmatrix} -1.5 \\ 2.5 \end{pmatrix} - \begin{pmatrix} -2 \\ 0 \end{pmatrix} \right\| \tag{21}$$

$$= \left\| \begin{pmatrix} 0.5 \\ 2.5 \end{pmatrix} \right\| = \sqrt{6.5} \tag{22}$$

- 3) The ratio of  $CG : GF = \frac{\sqrt{26}}{\sqrt{6.5}} = 2:1$
- 4) Therefore  $\frac{BG}{GE} = \frac{CG}{GF} = \frac{AG}{GD} = 2$

1) The ratio of  $AG: GD = \frac{\sqrt{10}}{\sqrt{2.5}} = 2:1$