

# Probability and Random Processes

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Q) If A and B are such that

$$\Pr(A' \cup B') = \frac{2}{3} \text{ and } \Pr(A \cup B) = \frac{5}{9}$$

then  $\Pr(A') + \Pr(B') =$

**Solution:** Using de Morgan's law and axioms of probability.

$$\Pr(A'B') = \Pr((A + B)') \quad (1)$$

$$\Pr(A' + B') = \Pr(A') + \Pr(B') - \Pr(A'B') \quad (2)$$

We have,

$$\Pr(A'B') = \Pr((A + B)') \quad (3)$$

$$\Pr(A'B') = 1 - \Pr(A + B) \quad (4)$$

$$= 1 - \frac{5}{9} \quad (5)$$

$$= \frac{4}{9} \quad (6)$$

$$\Pr(A' + B') = \Pr(A') + \Pr(B') - \Pr(A'B') \quad (7)$$

$$\Pr(A') + \Pr(B') = \Pr(A' + B') + \Pr(A'B') \quad (8)$$

$$= \frac{2}{3} + \frac{4}{9} \quad (9)$$

$$= \frac{10}{9} \quad (10)$$