

# Probability and Random Processes

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Q) Ten coins are tossed. What is the probability of getting atleast 8 heads?

**Solution:**

Parameter	Value	Description
$n$	10	number of tosses
$p$	$\frac{1}{2}$	Probability for Heads
$q$	$\frac{1}{2}$	Probability for Tails
$\mu = np$	5	mean of the distribution
$\sigma^2 = npq$	2.5	variance of the distribution
$X$	$0 \leq X \leq 10$	Number of heads

## Gaussian Distribution

For  $X \geq 8$

1) With a 0.5 correction:

$$\Pr(X \geq 8) = 1 - \Pr(X < 7.5) \quad (1)$$

$$\Pr(X \geq 8) = Q\left(\frac{7.5 - \mu}{\sigma}\right) \quad (2)$$

$$\Pr(X \geq 8) = Q(\sqrt{2.5}) = Q(1.5811) \quad (3)$$

$$\Rightarrow \Pr(X \geq 8) = 0.0569276 \quad (4)$$

2) Without correction:

$$\Pr(X \geq 8) = 1 - \Pr(X < 8) \quad (5)$$

$$\Pr(X \geq 8) = Q\left(\frac{8 - \mu}{\sigma}\right) \quad (6)$$

$$\Pr(X \geq 8) = Q\left(\frac{3}{\sqrt{2.5}}\right) = Q(1.8973) \quad (7)$$

$$\Rightarrow \Pr(X \geq 8) = 0.0288898 \quad (8)$$

## Binomial Distribution

$$\Pr(X \geq 8) = 1 - \Pr(X < 8) \quad (9)$$

$$= \sum_{k=8}^{10} \binom{n}{k} p^k (1-p)^{n-k} \quad (10)$$

$$= 0.0546875 \quad (11)$$

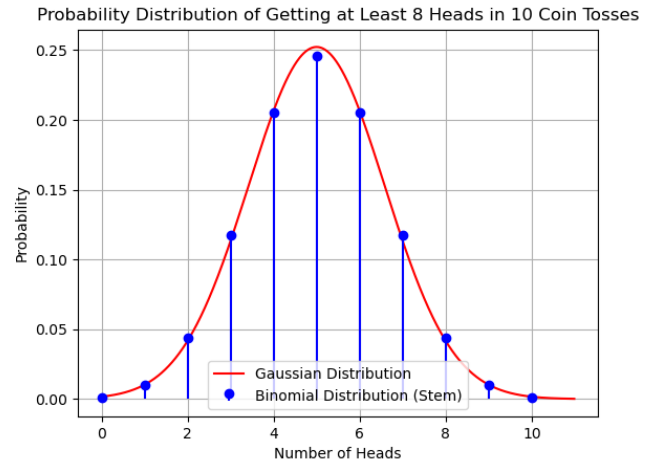


Fig. 1: Binomial vs Gaussian