#### 1

# Probability and Random Processes

# Gude Prayarsh EE22BTECH11023\*

Q)Ten coins are tossed. What is the probability of getting atleast 8 heads?

## **Solution:**

| Parameter        | Value            | Description                  |
|------------------|------------------|------------------------------|
| n                | 10               | number of tosses             |
| p                | $\frac{1}{2}$    | Probability for Heads        |
| q                | $\frac{1}{2}$    | Probability for Tails        |
| $\mu = np$       | 5                | mean of the distribution     |
| $\sigma^2 = npq$ | 2.5              | variance of the distribution |
| X                | $0 \le X \le 10$ | Number of heads              |

### **Gaussian Distribution**

$$X \approx Y \sim \mathcal{N}(5, 2.5) \tag{1}$$

1) With a 0.5 correction:

$$\Pr(Y \ge 8) = Q\left(\frac{7.5 - \mu}{\sigma}\right) \qquad (2)$$

$$\Pr(Y \ge 8) = Q(\sqrt{2.5}) = Q(1.5811)$$
 (3)

$$\implies \Pr(Y > 8) = 0.0569276$$
 (4)

2) Without correction:

$$\Pr(Y \ge 8) = Q\left(\frac{8-\mu}{\sigma}\right) \quad (5)$$

$$\Pr(Y \ge 8) = Q\left(\frac{3}{\sqrt{25}}\right) = Q(1.8973)$$
 (6)

$$\implies \Pr(Y \ge 8) = 0.0288898$$
 (7)

### **Binomial Distribution**

$$\Pr(X \ge 8) = \sum_{k=8}^{10} {n \choose k} p^k (1-p)^{n-k}$$
 (8)

$$= 0.0546875$$
 (9)

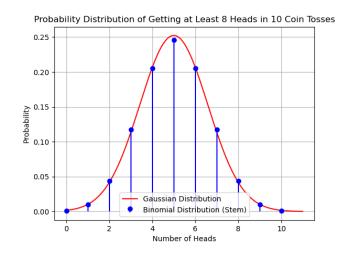


Fig. 1: Binomial vs Guassian