Assignment(matrix theory)

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A Fill in the blanks

1. The larger of $\cos(\ln\theta)$ and $\ln(\cos\theta)$ if $e^{\frac{-\pi}{2}} < \theta < \frac{\pi}{2}$ is ..... $(1983-1Mark)$
2. The function $y = 2x^2 - \ln|x|$ is monotonically increasing for values of $x(\neq 0)$ satisfying the inequalities ..... and monotonically decreasing for values of x satisfying the inequalities ..... $(1983-2Marks)$
3. The set of all x for which $\ln(1+x) \leq x$ is equal to ..... $(1987-2Marks)$
4. Let P be a variable point on the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ with foci F_1 and F_2. If A is the area of the triangle PF_1F_2 then the maximum value of A is ..... $(1994-2Marks)$
5. Let C be the curve y^3 - 3xy + 2 = 0. If H is the set of points on the curve C where the tangent is horizontal and V is the set of the point on the curve C where the tangent is vertical then H = ... and V = ... $(1994-2Marks)$

B True / False

1. If x-r is a factor of the polynomial f(x) = $a_nx^4+....+a_0$, repeated m times $(1 < m \leq n)$, then r is a root of f'(x)=0 repeated m times. $(1983-1Mark)$
2. For $0 < a < x$, the minimum value of the function $log_a x + log_x a$ is 2. $(1984-1Mark)$

C MCQs with One Correct Answer

1. If a+b+c = 0, then the quadratic equation $3ax^2$ + 2bx + c = 0 has $(1983-1Mark)$
   a. at least one root in [0,1]
   b. one root in [2,3] and other in [-2,-1]
   c. imaginary roots
   d. none of these

2. AB is a diameter of a circle and C is any point on the circumference of the circle. Then $(1983-1Mark)$
   a. the area ofΔ ABC is maximum when it is isosceles
   b. the area of Δ ABC is minimum when it is isosceles
   c. the perimeter of Δ ABC is minimumwhen it is isosceles
   d. none of these

3. The normal to the curve x = a($\cos\theta + \theta\sin\theta$), y = a($\sin\theta$ - $\theta\cos\theta$) at any point 'θ' is such that $(1983-1Mark)$
   a. it makes constant angle with the x - axis
   b. it passes through the origin
   c. it is at a constant distance from the origin
   d. none of these

4. If $y = a\ln x + bx^2 + x$ has its extremum values at x = -1 and x = 2, then $(1983-1Mark)$
   a. a = 2, b = -1
   b. a = 2, b = $\frac{-1}{2}$
   c. a = -2, b = $\frac{1}{2}$
   d. none of these

5. Which one of the following curves cut the parabola $y^2 = 4ax$ at right angles? (1994)
   a. $x^2 + y^2 = a^2$
   b. $e^{\frac{-x}{2a}}$
   c. y = ax
   d. $x^2 = 4ay$

6. The function defined by f(x) = $(x+2)\ e^{-x}$ is (1994)
   a. decreasing for all x
   b. decreasing in $(-\infty,-1)$ and increasing in $(-1,\infty)$
   c. increasing for all x
   d. decreasing in $(-1,\infty)$ and increasing in $(-\infty,-1)$

7. The function f(x) = $\frac{\ln(\pi+x)}{\ln(e+x)}$ is $(1995S)$
   a. increasing on $(0,\infty)$
   b. decreasing on $(0,\infty)$
   c. increasing on $\left(0,\frac{\pi}{e}\right)$, decreasing on $\left(\frac{\pi}{e},\infty\right)$
   d. decreasing on $\left(0,\frac{\pi}{e}\right)$, increasing on $\left(\frac{\pi}{e},\infty\right)$

8. On the interval [0, 1] the function $x^{25}(1-x)^{25}$ takes its maximum value at the point $(1995S)$

a. 0 b. $\frac{1}{4}$ c. $\frac{1}{2}$ d. $\frac{1}{3}$