## 16. Applications of derivatives

## EE24BTECH11065 - spoorthi

## **Section-B JEE Main/AIEEE**

| , .  | min. When the thickness o                                     | •  |   |                      |
|--|---|--|---|----------------------|
| a) $\frac{1}{36\pi} \ cm/min$ .  | b) $\frac{1}{18\pi}$ cm/min.                                  | c) $\frac{1}{54\pi}$ cm/min.                   | d) $\frac{5}{6\pi}$ cm/min.                     |                      |
| equation $na_n x^{n-1}$ + a) greater than $\alpha$ b) smaller than $\alpha$ c) greater than or $\alpha$ d) equal to $\alpha$ | _   | =0 has a positive root, wh                     |   | [2005]               |
| 3) The function $f(x)$   | $=\frac{x}{2}+\frac{2}{x}$ has a local minim                  | num at   |   | [2006]               |
| a) $x = 2$   | b) $x = -2$   | c) $x = 0$                                     | d) $x = 1$                                      |                      |
|  | s enclosed on two sides by tence are of same length $x$ .     |  | -   | oank. The<br>[2006]  |
| a) $\frac{3}{2}x^2$  | b) $\sqrt{\frac{x^3}{8}}$                                     | c) $\frac{1}{2}x^2$                            | d) $\pi x^2$                                    |                      |
| 5) A value of <i>c</i> for w the interval [1, 3] i   | which conclusion of Mean s                                    | Value Theorem holds for                        | the function $f(x) =$                           | $\log_e x$ on [2007] |
| a) $\log_3 e$  | b) $\log_e 3$   | c) 2log <sub>3</sub> <i>e</i>                  | d) $\frac{1}{2}\log_3 e$                        |                      |
| 6) The function $f(x)$   | $= \tan^{-1}(\sin x + \cos x)$ is an                          | increasing function in                         |   | [2007]               |
| a) $(0,\frac{\pi}{2})$   | b) $\left(\frac{-\pi}{2},\frac{\pi}{2}\right)$                | c) $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$ | d) $\left(\frac{-\pi}{2}, \frac{\pi}{4}\right)$ |                      |
| 7) If <i>p</i> and <i>q</i> are pos [2007]   | sitive real numbers such th                                   | $nat p^2 + q^2 = 1, then the$                  | maximum value of                                | (p+q) is             |
| a) $\frac{1}{2}$   | b) $\frac{1}{\sqrt{2}}$                                       | c) $\sqrt{2}$                                  | d) 2  |                      |
| 8) Suppose the cubic of the following he   | $x^3$ - $px$ + $q$ has three distinctions olds?               | inct real roots where $p >$                    | 0 and $q > 0$ . Then w                          | which one [2008]     |
|  | ninima at $\sqrt{\frac{p}{3}}$ and maxima                     | ·  |   |                      |
|  | ninima at - $\sqrt{\frac{p}{3}}$ and maxim                    |  |   |                      |
|  | ninima at both $\sqrt{\frac{p}{3}}$ and -                     |  |   |                      |
|  | axima at both $\sqrt{\frac{p}{3}}$ and - $\sqrt{\frac{p}{3}}$ |  | 760 01 0  | F <b>A</b> 0003      |
| 9) How many real so  | lutions does the equation :                                   | $x' + 14x^3 + 16x^3 + 30x - 5$                 | 560 = 0  have  ?                                | [2008]               |

[2009]

d) 5

| d) Statement-1  | is true, Statement-2 is true   | Statement-2 is a correct                 | explanation for Staten      | nent-1.             |  |
|---|--|--|-----------------------------|---------------------|--|
| P(1), then in t   | $a^{4} + ax^{3} + bx^{2} + cx + d$ such the interval [-1, 1]:                |  | real root of $P^1(x) = 0$ . | If $P(-1) < [2009]$ |  |
|   | minimum but $P(1)$ is the  |  |                             |                     |  |
|   | minimum but $P(1)$ is not 1) is the minimum nor $P(1)$                       |  |                             |                     |  |
|   | minimum and $P(1)$ is the  |  |                             |                     |  |
| 12) The equation of   | f the tangent to the curve   | $y = x + \frac{4}{x^2}$ , that is parall | el to the x-axis, is        | [2010]              |  |
| a) $y = 1$  | b) $y = 2$   | c) $y = 3$                               | d) $y = 0$                  |                     |  |
| 13) Let $f: R \to R$ $\begin{cases} k - 2x & \text{if } x \\ 2x + 3 & \text{if } x \end{cases}$   | be defined by $f(x) =$<br>$x \le -1$<br>x > -1<br>minimum at $x = -1$ , then |  |                             |                     |  |
| If f has a local  | minimum at $x = -1$ , then   | a possible value of $k$ is               |                             | [2010]              |  |
| a) 0  | b) $-\frac{1}{2}$  | c) -1                                    | d) 1                        |                     |  |
| 14) Let $f: R \to R$ be a continuous function defined by $f(x) = \frac{1}{e^x + 2e^{-x}}$<br>Statement-1: $f(c) = \frac{1}{3}$ , for some $c \in R$ . Statement-2: $0 < f(x) \le \frac{1}{2\sqrt{2}}$ , for all $x \in R$ |  |  |                             |                     |  |
|   | is true, Statement-2 is true   |  |                             | atement-1.          |  |
| b) Statement-1  | is true, Statement-2 is fals   | e.                                       | •                           |                     |  |
|   | is false, Statement-2 is true  |  |                             |                     |  |
|   | is true, Statement 2 is true; stance between line $y - x = \frac{1}{2}$      |  |                             | [2011]              |  |
| _   |  |  | 6                           | [2011]              |  |
| a) $\frac{3\sqrt{2}}{8}$  | b) $\frac{8}{3\sqrt{2}}$   | c) $\frac{4}{\sqrt{3}}$                  | d) $\frac{\sqrt{3}}{4}$     |                     |  |
|   |  |  |                             |                     |  |
|   |  |  |                             |                     |  |
|   |  |  |                             |                     |  |
|   |  |  |                             |                     |  |

c) 3

**statement-1:** gof is differentiable at x = 0 and its derivative is continuous at that point. **statement-2:** 

a) Statement-1 is true, Statement-2 is true; statement-2 is not a correct explanation for statement-1.

b) 1

a) 7

10) Let f(x)=x|x| and  $g(x)=\sin x$ .

gof is twice differential at x = 0.

b) Statement-1 is true, Statement-2 is false.c) Statement-1 is false, Statement-2 is true.