

16. Applications of derivatives

EE24BTECH11065 - spoorthi

Section-B JEE Main/AIEEE

- 1) A spherical iron ball 10cm in radius is coated with a layer of ice of uniform thickness that melts at a rate of $50 \text{ cm}^3 / \text{min}$. When the thickness of ice is 5cm, then the rate at which the thickness of ice decreases is [2005]
 - a) $\frac{1}{36\pi} \text{ cm/min}$.
 - b) $\frac{1}{18\pi} \text{ cm/min}$.
 - c) $\frac{1}{54\pi} \text{ cm/min}$.
 - d) $\frac{5}{6\pi} \text{ cm/min}$.
- 2) If the equation $a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x = 0$, $a_1 \neq 0, n \geq 2$, has a positive root $x = \alpha$, then the equation $na_n x^{n-1} + (n-1)a_{n-1} x^{n-2} + \dots + a_1 = 0$ has a positive root, which is [2005]
 - a) greater than α
 - b) smaller than α
 - c) greater than or equal to α
 - d) equal to α
- 3) The function $f(x) = \frac{x}{2} + \frac{2}{x}$ has a local minimum at [2006]
 - a) $x = 2$
 - b) $x = -2$
 - c) $x = 0$
 - d) $x = 1$
- 4) A triangular park is enclosed on two sides by a fence and on third side by a straight river bank. The two sides having fence are of same length x . The maximum area enclosed by the park is [2006]
 - a) $\frac{3}{2}x^2$
 - b) $\sqrt{\frac{x^3}{8}}$
 - c) $\frac{1}{2}x^2$
 - d) πx^2
- 5) A value of c for which conclusion of Mean Value Theorem holds for the function $f(x) = \log_e x$ on the interval $[1, 3]$ is [2007]
 - a) $\log_3 e$
 - b) $\log_e 3$
 - c) $2\log_3 e$
 - d) $\frac{1}{2}\log_3 e$
- 6) The function $f(x) = \tan^{-1}(\sin x + \cos x)$ is an increasing function in [2007]
 - a) $(0, \frac{\pi}{2})$
 - b) $(\frac{-\pi}{2}, \frac{\pi}{2})$
 - c) $(\frac{\pi}{4}, \frac{\pi}{2})$
 - d) $(\frac{-\pi}{2}, \frac{\pi}{4})$
- 7) If p and q are positive real numbers such that $p^2 + q^2 = 1$, then the maximum value of $(p + q)$ is [2007]
 - a) $\frac{1}{2}$
 - b) $\frac{1}{\sqrt{2}}$
 - c) $\sqrt{2}$
 - d) 2
- 8) Suppose the cubic $x^3 - px + q$ has three distinct real roots where $p > 0$ and $q > 0$. Then which one of the following holds ? [2008]
 - a) The cubic has minima at $\sqrt{\frac{p}{3}}$ and maxima at $-\sqrt{\frac{p}{3}}$
 - b) The cubic has minima at $-\sqrt{\frac{p}{3}}$ and maxima at $\sqrt{\frac{p}{3}}$
 - c) The cubic has minima at both $\sqrt{\frac{p}{3}}$ and $-\sqrt{\frac{p}{3}}$
 - d) the cubic has maxima at both $\sqrt{\frac{p}{3}}$ and $-\sqrt{\frac{p}{3}}$
- 9) How many real solutions does the equation $x^7 + 14x^5 + 16x^3 + 30x - 560 = 0$ have ? [2008]

