

## 4.5.6

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# Question

Find the equations of the line that passes through the point  $(3,0,1)$  and parallel to the planes  $x + 2y = 0$  and  $3y - z = 0$ .

# Solution

We know that the normal form of a plane is  $\mathbf{n}^T \mathbf{x} = 0$

The plane  $x + 2y = 0$  can be expressed in vector form as:

$$\begin{pmatrix} 1 \\ 2 \\ 0 \end{pmatrix}^T \mathbf{x} = 0 \quad (1)$$

therefore,

$$\mathbf{n}_1 = \begin{pmatrix} 1 \\ 2 \\ 0 \end{pmatrix} \quad (2)$$

The plane  $3y - z = 0$  can be expressed in vector form as:

$$\begin{pmatrix} 0 \\ 3 \\ -1 \end{pmatrix}^T \mathbf{x} = 0 \quad (3)$$

# Solution

therefore,

$$\mathbf{n}_2 = \begin{pmatrix} 0 \\ 3 \\ -1 \end{pmatrix} \quad (4)$$

The vector parallel to both planes will be perpendicular to the normal vectors of both planes. Therefore it can be expressed as

$$\mathbf{n}_1 \times \mathbf{n}_2 \quad (5)$$

To calculate the cross product of the two vectors  $\mathbf{a}$  and  $\mathbf{b}$ , we use the following determinant:

$$\begin{pmatrix} |\mathbf{A}_{11} \mathbf{B}_{23}| \\ |\mathbf{A}_{11} \mathbf{B}_{23}| \\ |\mathbf{A}_{11} \mathbf{B}_{23}| \end{pmatrix}$$

Where  $X_{ij} = \begin{pmatrix} x_i \\ x_j \end{pmatrix}$ .

# Solution

Expanding the determinants, we get:

$$\begin{pmatrix} ((-2) - 0) \\ (1 - 0) \\ (3 - 0) \end{pmatrix} = \begin{pmatrix} -2 \\ 1 \\ 3 \end{pmatrix} \quad (6)$$

Since the line passes through (3,0,1), the line can therefore be expressed as:

$$\frac{x - 3}{-2} = \frac{y}{1} = \frac{z - 1}{3} \quad (7)$$

codes permalink

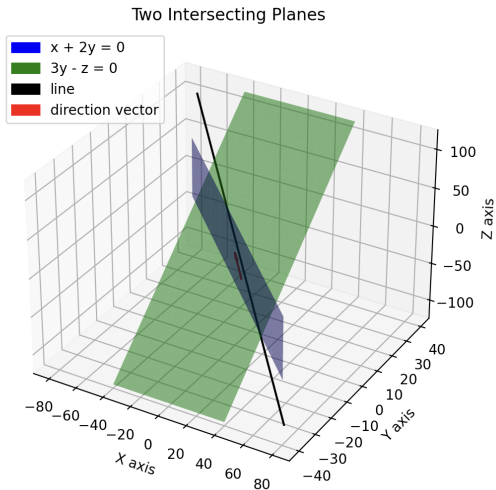


Figure: Plot