4.3.37

EE25BTECH11047 - RAVULA SHASHANK REDDY

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Question: Find the equation of the line passing through the points

$$\mathbf{A} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 3 \\ 6 \end{pmatrix}.$$

Solution:

$$\begin{pmatrix} \mathbf{A} & \mathbf{B} \end{pmatrix}^T \mathbf{n} = \begin{pmatrix} c \\ c \end{pmatrix} \tag{1}$$

$$\begin{pmatrix} 1 & 2 \\ 3 & 6 \end{pmatrix} \mathbf{n} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \tag{2}$$

$$\begin{pmatrix} 1 & 2 & 0 \\ 3 & 6 & 0 \end{pmatrix} \xrightarrow{R_2 - 3R_1} \begin{pmatrix} 1 & 2 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$
 (3)

$$n_1 + 2n_2 = 0 (4)$$

Let $n_2 = 1$

$$n_1 = -2, (5)$$

$$\mathbf{n} = \begin{pmatrix} -2\\1 \end{pmatrix} \tag{6}$$

Equation of a Line is

$$\mathbf{n}^T \mathbf{x} = c \tag{7}$$

$$(-2 1) \begin{pmatrix} 1 \\ 2 \end{pmatrix} = c$$

$$c = 0$$

$$(-2 1) \mathbf{x} = 0$$

$$(10)$$

$$c = 0 (9)$$

$$\begin{pmatrix} -2 & 1 \end{pmatrix} \mathbf{x} = 0 \tag{10}$$

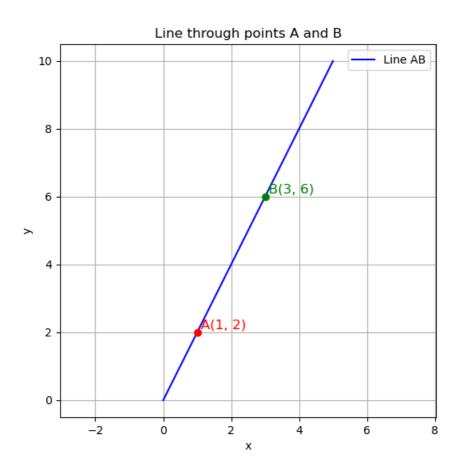


Figure 1: Caption