Question 2.3.3

AI25BTECH11040 - Vivaan Parashar

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Question: 1

If \mathbf{a} , \mathbf{b} , \mathbf{c} are three non-zero unequal vectors such that $\mathbf{a}^{\mathrm{T}}\mathbf{b} = \mathbf{a}^{\mathrm{T}}\mathbf{c}$, then find the angle between \mathbf{a} and $\mathbf{b} - \mathbf{c}$.

2 **Solution:**

The angle θ between two vectors **a** and **b** is given by the formula:

$$\theta = \arccos\left(\frac{\|\mathbf{a}^{\mathrm{T}}\mathbf{b}\|}{\|\mathbf{a}\| \|\mathbf{b}\|}\right) \tag{1}$$

In this case, we would need to find

$$\theta = \arccos(\frac{\|\mathbf{a}^{\mathrm{T}}(\mathbf{b} - \mathbf{c})\|}{\|\mathbf{a}\| \|\mathbf{b} - \mathbf{c}\|})$$
(2)

$$\theta = \arccos\left(\frac{\left\|\mathbf{a}^{\mathsf{T}}\mathbf{b} - \mathbf{a}^{\mathsf{T}}\mathbf{c}\right\|}{|\mathbf{a}||\mathbf{b} - \mathbf{c}|}\right)$$

$$\theta = \arccos(0) = 90^{\circ}$$
(3)

$$\theta = \arccos(0) = 90^{\circ} \tag{4}$$

$$\mathbf{a}^{\mathrm{T}}\mathbf{b} = \mathbf{a}^{\mathrm{T}}\mathbf{c} \text{ and } |\mathbf{a}| \neq 0, |\mathbf{b} - \mathbf{c}| \neq 0$$
(5)

Therefore, the angle between the vectors \mathbf{a} and $\mathbf{b} - \mathbf{c}$ is 90°.