

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

Dan Grossman  
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*Nested Patterns Precisely*

# *(Most of) the full definition*

The **semantics** for pattern-matching takes a pattern  $p$  and a value  $v$  and decides (1) does it match and (2) if so, what variable bindings are introduced.

Since patterns can nest, the **definition is elegantly recursive**, with a separate rule for each kind of pattern. Some of the rules:

- If  $p$  is a variable  $x$ , the match succeeds and  $x$  is bound to  $v$
- If  $p$  is  $\_$ , the match succeeds and no bindings are introduced
- If  $p$  is  $(p1, \dots, pn)$  and  $v$  is  $(v1, \dots, vn)$ , the match succeeds if and only if  $p1$  matches  $v1$ , ...,  $pn$  matches  $vn$ . The bindings are the union of all bindings from the submatches
- If  $p$  is  $C\ p1$ , the match succeeds if  $v$  is  $C\ v1$  (i.e., the same constructor) and  $p1$  matches  $v1$ . The bindings are the bindings from the submatch.
- ... (there are several other similar forms of patterns)

# Examples

- Pattern `a :: b :: c :: d` matches all lists with  $\geq 3$  elements
- Pattern `a :: b :: c :: []` matches all lists with 3 elements
- Pattern `((a,b), (c,d)) :: e` matches all non-empty lists of pairs of pairs