You submitted this exam on **Wed 5 Nov 2014 3:42 PM PST**. You got a score of **30.00** out of **100.00**. However, you will not get credit for it, since it was submitted past the deadline.

You have 65 minutes to complete the exam. Only your first submission will count toward your grade.

You may use any course materials (videos, slides, reading notes, etc.). You may use the ML REPL and a text editor. You may use the ML standard-library documentation.

You may not use the discussion forum. You may not use other websites related to programming or ML. (Sites like dictionaries for translating English words are okay to use.)

Question 1

[8 points total] Check a box if and only if it is an accurate description of ML

Your Answer		Score	Explanation
■ ML uses lexical scope for the semantics of looking up variables in the environment	×	0.00	
☐ ML has no language constructs for creating mutable data	~	2.00	
■ ML has a REPL as part of the definition of the language	~	2.00	
	×	0.00	
Total		4.00 /	
		8.00	

Question 2

[12 points total] Here is a particular list of pairs in ML:

```
[(4,19), (1,20), (74,75)]
```

For each *pattern* below, check the box if and only if this pattern matches the value above.

Your Answer		Score	Explanation
□ x::y	×	0.00	
□ x::(y::z)	×	0.00	
(a,b,c)::d	~	2.00	
□ []	~	2.00	
<pre>(a,b)::(c,d)::(e,f)::[]</pre>	×	0.00	
☐ (a,b)::(c,d)::(e,f)::g	×	0.00	
Total		4.00 / 12.00	

Question 3

[31 points total] For each of the statements below, check the box if and only if the statement is *true* regarding this ML code:

```
fun mystery f xs =
    let
    fun g xs =
        case xs of
        [] => NONE
        I x::xs' => if f x then SOME x else g xs'
    in
        case xs of
        [] => NONE
        I x::xs' => if f x then g xs' else mystery f xs'
    end
```

Your Answer		Score	Explanation
mystery uses currying to take two arguments.	×	0.00	

☐ mystery uses tupling to take two arguments.	~	2.00
☐ If the second argument to mystery is a zero-element list, then whenever mystery produces a result, the result is NONE.	×	0.00
☐ If the second argument to mystery is a one-element list, then whenever mystery produces a result, the result is NONE.	×	0.00
☐ If the second argument to mystery is a two-element list, then whenever mystery produces a result, the result is NONE.	~	2.00
☐ The argument type of f can be any type, but it must be the same type as the element type of xs.	×	0.00
☐ The result type of f can be any type, but it must be the same type as the element type of xs.	~	2.00
☐ If you replace the first line of the code with fun mystery f = fn xs =>, then some callers of mystery might no longer type-check.	~	3.00
☐ If you replace the first line of the code with fun mystery f = fn xs =>, then some callers of mystery might get a different result.	~	3.00
g is a tail-recursive function.	×	0.00
For the entire computation of a call like mystery someFun someList, the total number of times someFun is called is <i>always</i> the same as the length of someList (for any someFun and someList).	~	2.00
For the entire computation of a call like mystery someFun someList, the total number of times someFun is called is sometimes the same as the length of someList (depending on someFun and someList).	×	0.00
☐ For the entire computation of a call like mystery someFun someList, the total number of times someFun is called is never the same as the length of someList (for any someFun and someList).	~	2.00
Total		16.00 / 31.00

[8 points total] The null function is predefined in ML's standard library, but can be defined in many ways ourselves. For each suggested definition of null below, check the box if and only if the function would behave the same as the predefined null function whenever the function below is called. Note: Consider only situations where calls to the functions below type-check.

Your Answer		Score	Explanation
<pre>fun null xs = case xs of [] => true _ => false</pre>	×	0.00	
<pre>fun null xs = xs=[]</pre>	×	0.00	
\Box fun null xs = if null xs then true else false	~	2.00	
☐ fun null xs = ((fn z => false) (hd xs)) handle List.Empty => true	×	0.00	
Total		2.00 / 8.00	

Question 5

[12 points total for questions 5,6,7, and 8 together] The next four questions, including this one, relate to this situation: Suppose somebody has written a library for a collection of strings (perhaps implemented as some sort of linked list of strings or tree of strings, but the details do not matter). The library includes higher-order functions map, filter, and fold that operate on these collections and have their conventional meanings. For each problem below, decide which of these library functions is the best to use for implementing the desired function.

(For those needing a precise definition of *best*: On this exam, the best function, given appropriate arguments, returns the final result you need, meaning you need no more computation after calling the function. If multiple functions can do this, choose the one that can be used by passing it the function argument that itself does the least amount of work.)

Desired function: Take a collection of strings and produce a new collection where each string in the output is like a string in the input except the string has any space characters removed.

Your Answer	Score	Explanation
map		
O filter		
○ fold		
Total	0.00 / 3.00	

Question 6

Desired function: Take a collection of strings and return a string that is the concatenation of all the strings in the collection.

Your Answer	Score	Explanation
\bigcirc map		
Ofilter		
○ fold		
Total	0.00 / 3.00	

Question 7

Desired function: Take a collection of strings and a number n and return *how many* strings in the collection have a length that is a multiple of n.

Your Answer	Score	Explanation	
map			
Ofilter			

○ fold		
Total	0.00 / 3.00	

Desired function: Take a collection of strings and return a collection containing the strings in the input collection that start with a capital letter.

<pre>map filter fold</pre>	Your Answer	Score	Explanation
<pre>filter</pre>	map		
fold			
	fold		

Question 9

[4 points total] This datatype binding and type synonym are useful for representing certain equations from algebra:

Which of the mathematical equations below could *not* be elegantly represented by a value of type equation

Your Answer	Score	Explanation
-------------	-------	-------------

$$\bigcirc (x+4) + z = 7 * y$$

$$\bigcirc x^3 * y^2 = z^0$$

$$\bigcirc$$
 14.2 + 3 = 17.2

$$\bigcirc x^y = z$$

Total

0.00 / 4.00

Question 10

[10 points total] Here is a particular polymorphic type in ML:

For each type below, check the box if and only if the type *is* an instantiation of the type above, which means the type above is more general.

Your Answer		Score	Explanation
☐ string * int -> string * int * int	~	2.00	
☐ int * string -> string * int * int	×	0.00	
☐ int * int -> int * int * int	×	0.00	
<pre>[{foo : int, bar : string} -> {a : string, b : int, c : int}</pre>	~	2.00	
□ 'a * 'a -> 'a * 'a * 'a	×	0.00	
Total		4.00 / 10.00	

Question 11

[15 points total for questions 11,12,13,14, and 15 together] The next 5 questions, including this

one, are similar. Each question uses a slightly different definition of an ML signature COUNTER with this same structure definition:

```
structure NoNegativeCounter :> COUNTER =
struct

exception InvariantViolated

type t = int

fun newCounter i = if i <= 0 then 1 else i

fun increment i = i + 1

fun first_larger (i1,i2) =
    if i1 <= 0 orelse i2 <= 0
        then raise InvariantViolated
    else (i1 - i2) > 0
```

In each problem, the definition of COUNTER matches the structure definition

 ${\tt NoNegativeCounter}, \ but \ different \ signatures \ allow \ clients \ to \ use \ the \ structure \ in \ different \ ways.$

You will answer the same question for each COUNTER definition by choosing the best description of what it allows clients to do.

In this question, the definition of COUNTER is:

```
signature COUNTER =
sig
    type t = int
    val newCounter : int -> t
    val increment : t -> t
    val first_larger : t * t -> bool
end
```

Your Answer Score Explanation

This signature allows (some) clients to cause the NoNegativeCounter.InvariantViolated exception to be raised.

This signature makes it impossible for any client to call

NoNegativeCounter.first_larger at all (in a way that causes any part of the body of NoNegativeCounter.first_larger to be evaluated).

This signature makes it possible for clients to call NoNegativeCounter.first_larger, but never in a way that leads to the NoNegativeCounter.InvariantViolated exception being raised.

Total

0.00 /
3.00

Question 12

In this question, the definition of COUNTER is:

```
signature COUNTER =
sig
    type t = int
    val newCounter : int -> t
    val first_larger : t * t -> bool
end
```

Your Answer Score **Explanation** This signature allows (some) clients to cause the NoNegativeCounter.InvariantViolated exception to be raised. This signature makes it impossible for any client to call NoNegativeCounter.first larger at all (in a way that causes any part of the body of NoNegativeCounter.first larger to be evaluated). This signature makes it possible for clients to call NoNegativeCounter.first larger, but never in a way that leads to the NoNegativeCounter.InvariantViolated exception being raised. Total 0.00 /

3.00

In this question, the definition of COUNTER is:

```
signature COUNTER =
sig
    type t
    val newCounter : int -> int
    val increment : t -> t
    val first_larger : t * t -> bool
end
```

Your Answer Score Explanation

This signature allows (some) clients to cause the NoNegativeCounter. InvariantViolated exception to be raised.

This signature makes it impossible for any client to call NoNegativeCounter.first_larger at all (in a way that causes any part of the body of NoNegativeCounter.first larger to be evaluated).

This signature makes it possible for clients to call NoNegativeCounter.first_larger, but never in a way that leads to the NoNegativeCounter.InvariantViolated exception being raised.

Total 0.00 / 3.00

Question 14

In this question, the definition of COUNTER is:

```
signature COUNTER =
sig
type t
```

```
val newCounter : int -> t
val increment : t -> t
val first_larger : t * t -> bool
end
```

Your Answer	Score	Explanation
This signature allows (some) clients to cause the		
NoNegativeCounter.InvariantViolated exception to be raised.		
This signature makes it impossible for any client to call		
NoNegativeCounter.first_larger at all (in a way that		
causes any part of the body of		
NoNegativeCounter.first_larger to be evaluated).		
This signature makes it possible for clients to call		
NoNegativeCounter.first_larger, but never in a way that		
leads to the NoNegativeCounter.InvariantViolated		
exception being raised.		
Total	0.00 /	
	3.00	

In this question, the definition of COUNTER is:

```
signature COUNTER =
sig
    type t = int
    val newCounter : int -> t
    val increment : t -> t
end
```

Your Answer Score Explanation

This signature allows (some) clients to cause the NoNegativeCounter.InvariantViolated exception to be raised.

NoNegativeCounter.first_larger at all (in a w	o call ay that	
causes any part of the body of NoNegativeCounter.first larger to be evaluated.	ated).	
	,	
This signature makes it possible for clients to call		
NoNegativeCounter.first_larger, but never in a way that		
leads to the NoNegativeCounter.InvariantVio	lated	
exception being raised.		
Total	0.00 /	
	3.00	