


# [SPOILERS] Practice Problems for Section 3 -- Solutions

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```
(** High-Order Fun **)

(* There Can Be Only One *)

fun fold_map f = List.foldr (fn (x, acc) => f x :: acc) []

fun fold_filter p = List.foldr (fn (x, acc) => if p x then x :: acc else acc) []

(* The Evil Twin *)
fun unfold f state =
  case f state of
    NONE => []
  | SOME (state', x) => x :: unfold f state'

(* A Novel Approach *)
val factorial = (List.foldl (op * ) 1) o (unfold (fn x => if x = 0 then NONE else SOME
(x - 1, x)))

(* Answer to bonus question: No. Simple tail-recursive
factorial works in constant space, while unfold here
constructs a list of size n. In later sessions we
will study a data structure that would make
virtually the same implementation efficient. *)

(* Unforeseen Developments *)
fun unfold_map f =
  let
    fun helper param =
      case param of
        [] => NONE
      | x :: xs => SOME (xs, f x)
```

```

    in
        unfold helper
    end

(* So Imperative *)
fun do_until f p x =
    if p x
    then x
    else do_until f p (f x)

(* Yet Another Factorial *)
fun imp_factorial n = #1 (do_until (fn (acc, x) => (acc * x, x - 1)) (fn (_, x) => x =
    0) (1, n))

(* Fixed Point *)
fun fixed_point f = do_until f (fn x => f x = x)

(* Newton's Method *)
fun my_sqrt n =
    let
        fun fixed_point f x = do_until f (fn x => abs (f x - x) < 0.0001) x
    in
        fixed_point (fn x => 0.5 * (x + n / x)) n
    end

(* Deeper into the woods *)

(* provided definition *)
datatype 'a tree = leaf | node of { value : 'a, left : 'a tree, right : 'a tree }

fun tree_fold f base t =
    case t of
        leaf => base
      | node { value = value, left = left, right = right } => f (tree_fold f base left
, value, tree_fold f base right)

fun tree_unfold f state =
    case f state of
        NONE => leaf
      | SOME (lstate, value, rstate) => node { value = value, left = tree_unfold f lstate, right = tree_unfold f rstate }

(** A Grand Challenge **)

(* provided definitions *)

```

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datatype expr = literal_bool | literal_int | binary_bool_op of expr * expr | binary_int_op of expr * expr | comparison of expr * expr | conditional of expr * expr * expr
datatype expr_type = type_bool | type_int

exception TypeError

fun infer_type expr =
  case expr of
    literal_bool => type_bool
  | literal_int => type_int
  | binary_bool_op (x1, x2) =>
      if infer_type x1 = type_bool andalso infer_type x2 = type_bool
      then type_bool
      else raise TypeError
  | binary_int_op (x1, x2) =>
      if infer_type x1 = type_int andalso infer_type x2 = type_int
      then type_int
      else raise TypeError
  | comparison (x1, x2) =>
      if infer_type x1 = type_int andalso infer_type x2 = type_int
      then type_bool
      else raise TypeError
  | conditional (x1, x2, x3) =>
      let
        val t2 = infer_type x2
        val t3 = infer_type x3
      in
        if infer_type x1 = type_bool andalso t2 = t3
        then t2
        else raise TypeError
      end

(** Back To The Future! 2 **)

(* GCD -- Final Redux *)

(* provided helper function *)
fun gcd (a : int, b : int) =
  if a = b
  then a
  else
    if a < b
    then gcd (a, b - a)
    else gcd (a - b, b)

```

```

fun gcd_list xs = List.foldl gcd (hd xs) (tl xs)

(* Element Of A List -- Final Redux *)

(* provided helper function *)
fun is_divisible_by (a : int, b : int) = a mod b = 0

fun any_divisible_by (xs, divisor) = List.exists (fn x => is_divisible_by (x, divisor))
) xs

(* Quirky Addition -- Continued -- Final Redux *)
val add_all_opt =
  let
    fun helper param =
      case param of
        (SOME x, SOME acc) => SOME (acc + x)
      | (NONE, acc) => acc
      | (x, _) => x
  in
    List.foldl helper NONE
  end

(* Flip Flop -- Final Redux *)
val alternate = #2 o (List.foldl (fn (x, (factor, acc)) => (~factor, factor * x + acc))
) (1, 0))

(* Minimum/Maximum -- Final Redux *)
fun min_max (x :: xs) = List.foldl (fn (x, (min, max)) => (if x < min then x else min,
  if x > max then x else max)) (x, x) xs

(* Lists And Tuples, Oh My! -- Final Redux *)
fun unzip xs = List.foldr (fn ((x, y), (xs, ys)) => (x :: xs, y :: ys)) ([], []) xs

(* Lists And Tuples, Oh My! -- Continued (1) -- Final Redux *)
fun zip xs =
  let
    fun helper param =
      case param of
        (x :: xs, y :: ys) => SOME ((xs, ys), (x, y))
      | _ => NONE
  in
    unfold helper xs
  end

(* BBBCA -- Final Redux *)

```

```

fun repeats_list xs =
  let
    fun helper param =
      case param of
        (_ :: xs, 0 :: reps) => helper (xs, reps)
      | (x :: xs, n :: reps) => SOME ((x :: xs, n - 1 :: reps), x)
      | _ => NONE
  in
    unfold helper xs
  end

(* 38 Cons Cells -- Final Redux *)
fun length_of_a_list xs = List.foldl (fn (_, x) => x + 1) 0 xs

(* Forest For The Trees -- Final Redux *)

fun tree_height t = tree_fold (fn (l, _, r) => 1 + Int.max (l, r)) 0 t

fun sum_tree t = tree_fold (fn (l, v, r) => l + v + r) 0 t

(* provided definition *)
datatype flag = leave_me_alone | prune_me

fun gardener t =
  let
    fun helper state =
      case state of
        node { value = prune_me, left = _, right = _ } => NONE
      | node { value = value, left = left, right = right } => SOME (left, value, right)
      | _ => NONE
  in
    tree_unfold helper t
  end

```

↑ 0 ↓ · flag

[Nikolai Saeverud](#) · 6 days ago 🔗

I guess I am busy doing practice problems today. I did the `unfold_map` and came up with two alternative solutions. I wondered if you could comment on the style and signature of the two alternatives. Why would the `unfold_map2` have `'a` instead of `'a?`

```

val unfold_map2 = fn : ('a -> 'b) -> 'a list -> 'b list
fun unfold_map2 f = unfold (fn xs => if xs = [] then NONE else SOME (tl xs, f (hd xs)))

```

```
val unfold_map3 = fn : ('a -> 'b) -> 'a list -> 'b list
fun unfold_map3 f = unfold (fn xs => case xs of [] => NONE | x :: xs' => SOME (xs', f x))
```

↑ 0 ↓ · flag



Pavel Lepin COMMUNITY TA · 6 days ago 🔒

Only the values in so-called "equality types" can be compared for equality by using `=`. A list type is an equality type if and only if the type of values contained in the list is also an equality type. This constraint is expressed as `'a list`. Since your first version of `unfold` compares `xs` to an empty list using `=`, SML's type system infers that `xs` must belong to an equality type. I'd recommend reviewing "Polymorphic and Equality Types" in section 2 if this doesn't make a whole lot of sense.

↑ 1 ↓ · flag

Nikolai Saeverud · 6 days ago 🔒

I will review it that lecture. It is a lot to take in, but is it ever rewarding when things start to come together. Is it ok, though to use the anonymous function in `unfold_map3` instead of the `let` expression in the provided solution?

↑ 0 ↓ · flag



Pavel Lepin COMMUNITY TA · 6 days ago 🔒

Certainly, I just prefer to define a named function for expressions involving `case` / pattern matching.

↑ 1 ↓ · flag



Pavel Lepin COMMUNITY TA · 6 days ago 🔒

To clarify a little: overall, I was trying to make the reference solutions very close in style to examples on the grading rubric for peer assessment, to avoid sending fellow learners any conflicting signals. But certain personal idiosyncrasies do inevitably shine through, and one of the messages of peer assessments is the fact that there's a fairly wide variety of reasonable styles and approaches to solving the problems anyway.

If you do find anything in the solutions that seems not very readable to you, or could be otherwise "objectively" improved upon, please do let me know, I'll consider doing something about this at the very least.

↑ 1 ↓ · flag

Nikolai Saeverud · 5 days ago 🔒

Thank you Pavel. That's perfect. I am practicing doing all the different styles that we have learned, and I am not really at the stage of personal preferences of style. But thank you for the confirmation that one solution is more or less equal to the other. It gives a broader perspective on the possibilities of sml.

↑ 0 ↓ · flag

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