

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

# Programming Languages

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*Generalizing Prior Topics*

# Generalizing

Our examples of first-class functions so far have all:

- Taken one function as an argument to another function
- Processed a number or a list

But first-class functions are useful anywhere for any kind of data

- Can pass several functions as arguments
- Can put functions in data structures (tuples, lists, etc.)
- Can return functions as results
- Can write higher-order functions that traverse your own data structures

Useful whenever you want to abstract over “what to compute with”

- No new language features

# *Returning functions*

- Remember: Functions are first-class values
  - For example, can return them from functions

Silly example:

```
fun double_or_triple f =  
  if f 7  
  then fn x => 2*x  
  else fn x => 3*x
```

Has type `(int -> bool) -> (int -> int)`

But the REPL prints `(int -> bool) -> int -> int`  
because it never prints unnecessary parentheses and  
`t1 -> t2 -> t3 -> t4` means `t1->(t2->(t3->t4))`

# Other data structures

- Higher-order functions are not just for numbers and lists
- They work great for common recursive traversals over your own data structures (datatype bindings) too
- Example of a higher-order *predicate*:
  - Are all constants in an arithmetic expression even numbers?
  - Use a more general function of type  
`(int -> bool) * exp -> bool`
  - And call it with `(fn x => x mod 2 = 0)`