```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
    [] => []
    | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman 2013

Delay and Force

Best of both worlds

Assuming some expensive computation has no side effects, ideally we would:

- Not compute it until needed
- Remember the answer so future uses complete immediately Called *lazy evaluation*

Delay and force

An ADT represented by a mutable pair

- #f in car means cdr is unevaluated thunk
 - Really a one-of type: thunk or result-of-thunk
- Ideally hide representation in a module

Using promises

```
(define (f p)
  (... (if (...) 0 (... (my-force p) ...))
        (if (...) 0 (... (my-force p) ...))
        ...
        (if (...) 0 (... (my-force p) ...))))
```

```
(f (my-delay (lambda () e)))
```

Lessons From Example

See code file for example that does multiplication using a very slow addition helper function

- With thunking second argument:
 - Great if first argument 0
 - Okay if first argument 1
 - Worse otherwise
- With precomputing second argument:
 - Okay in all cases
- · With thunk that uses a promise for second argument:
 - Great if first argument 0
 - Okay otherwise