

*CS 1674: Intro to Computer Vision*

# **Geometric Transformations and Multiple Views**

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September 29, 2020

# Why multiple views?

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- Structure and depth are inherently ambiguous from single views.

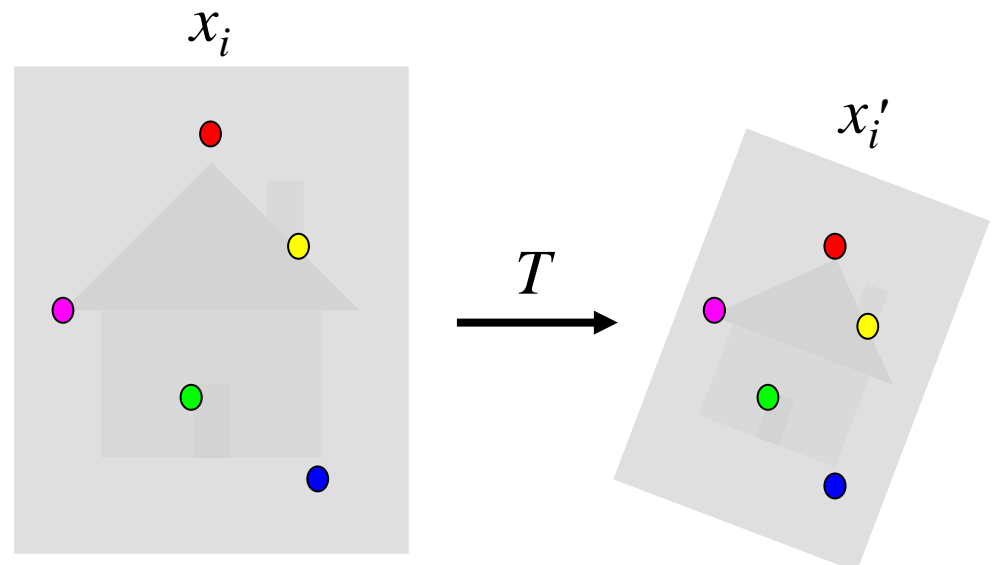


- Multiple views help us perceive 3d shape and depth.

# Alignment problem

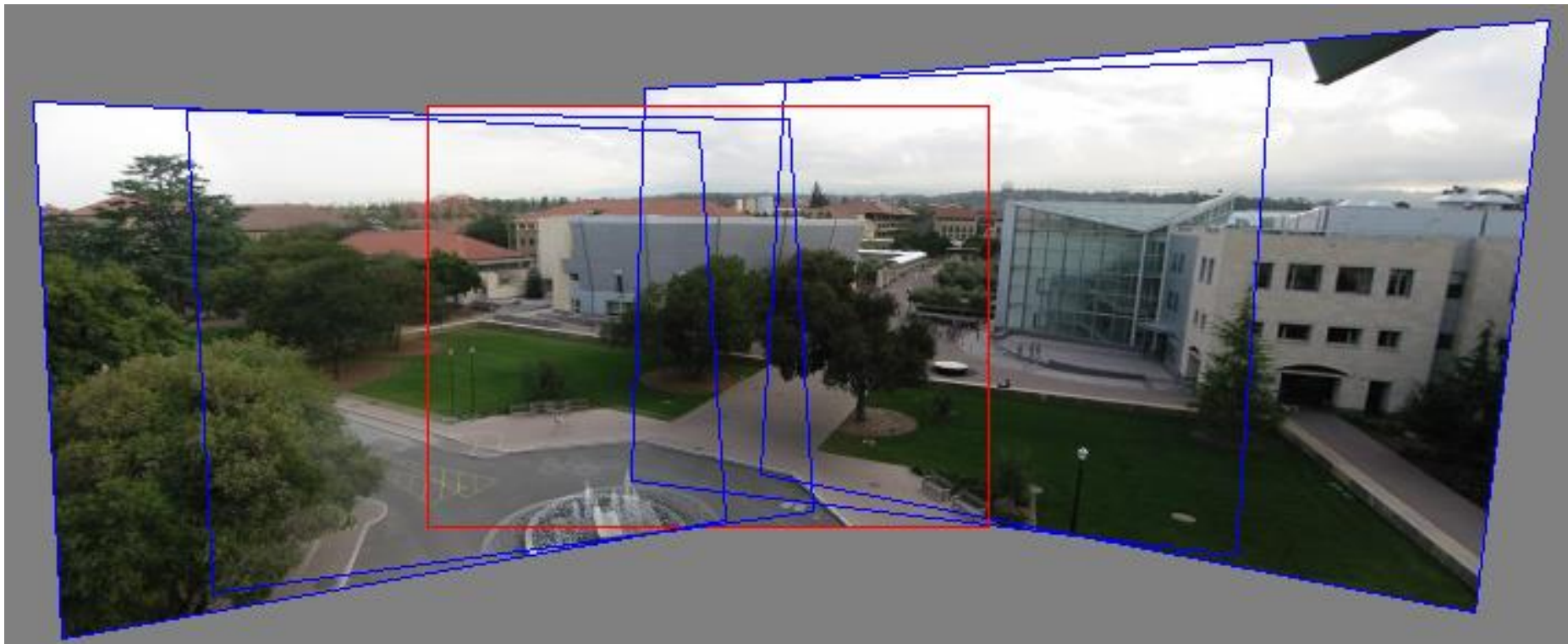
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- We previously discussed how to match features across images, of the same or different objects
- Now let's focus on the case of “two images of the same object” (e.g.  $x_i$  and  $x_i'$ )
- What transformation relates  $x_i$  and  $x_i'$ ?
- In *alignment*, we will **fit the parameters of some transformation** according to a set of matching feature pairs (“correspondences”).



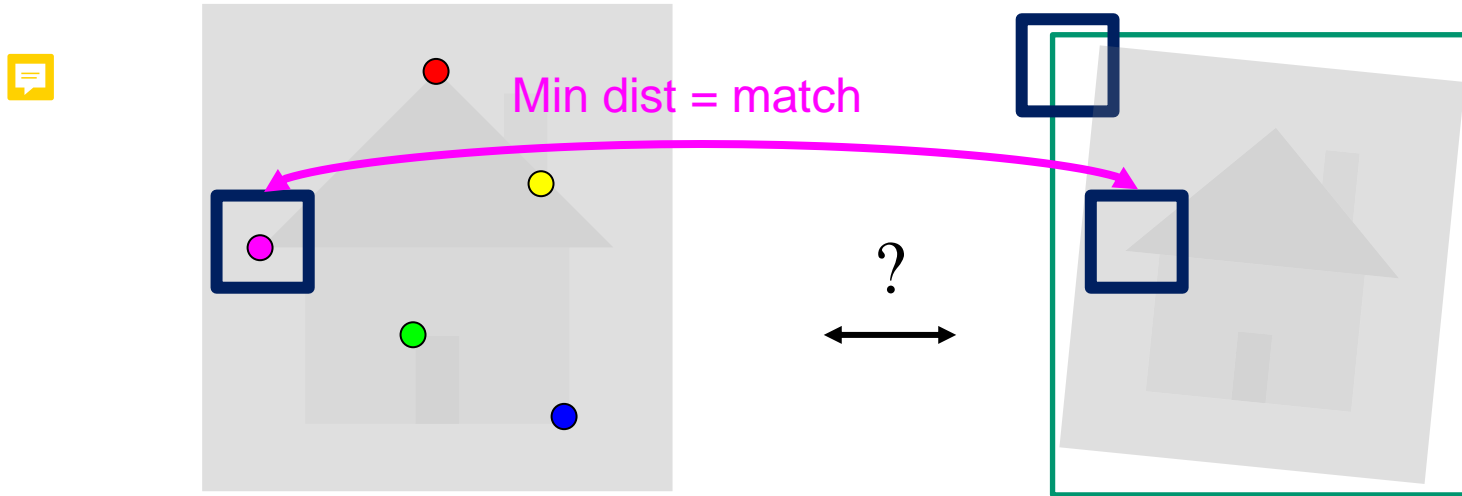
# Motivation: Image mosaics

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# First, what are the correspondences?

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- Compare content in **local** patches, find best matches.
  - Scan  $x'_i$  with template formed from a point in  $x_i$ , and compute e.g. Euclidean distance between pixel intensities in the patch
  - Or compare SIFT features

# Second, what are the transformations?

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Examples of transformations:



translate



rotate



change aspect ratio



squish/shear



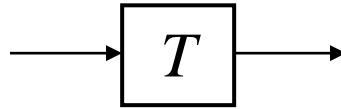
change perspective

# Parametric (global) warping

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$$\mathbf{p} = (x, y)$$



$$\mathbf{p}' = (x', y')$$

Transformation  $T$  is a coordinate-changing machine:



$$\mathbf{p}' = T(\mathbf{p})$$

What does it mean that  $T$  is **global**?

- It is the same for any point  $\mathbf{p}$
- It can be described by just a few numbers (parameters)

Let's represent  $T$  as a matrix:

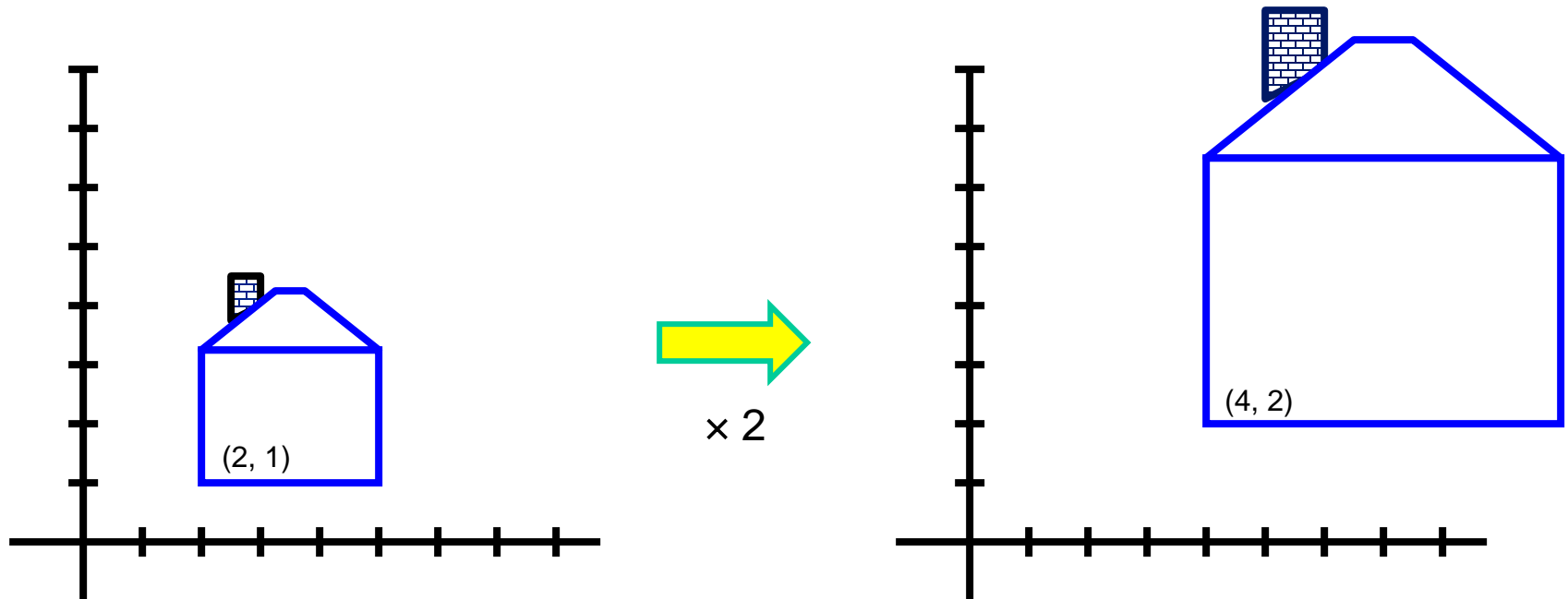
$$\mathbf{p}' = \mathbf{M}\mathbf{p}$$
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \mathbf{M} \begin{bmatrix} x \\ y \end{bmatrix}$$

# Scaling

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*Scaling* a coordinate means multiplying each of its components by a scalar

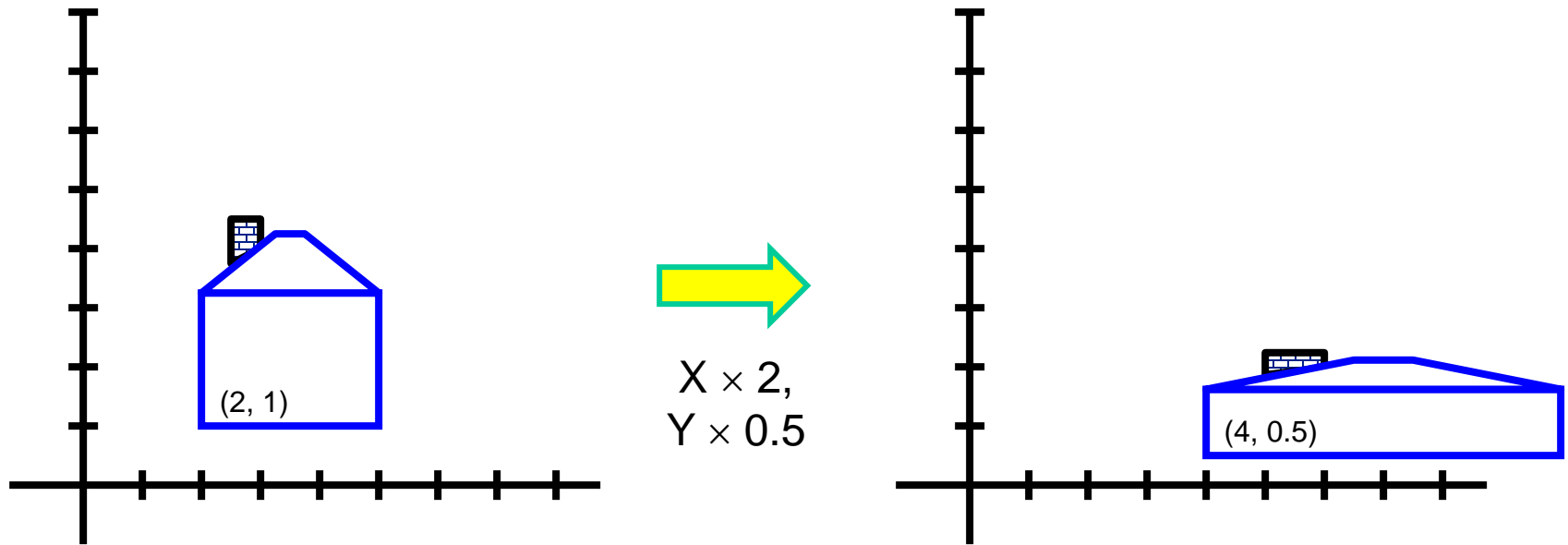
*Uniform scaling* means this scalar is the same for all components:





# Scaling

*Non-uniform scaling*: different scalars per component



# Scaling

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Scaling operation:

$$x' = ax$$

$$y' = by$$

Or, in matrix form:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}}_{\text{scaling matrix } S} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$x' = mx + ny$$

$$y' = px + qy$$



*scaling matrix S*

# 2D Linear transformations

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$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Only linear 2D transformations can be represented with a 2x2 matrix.

Linear transformations are combinations of ...

- Scale,
- Rotation,
- Shear, and
- Mirror

# What transforms can we write w/ 2x2 matrix?

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## 2D Scaling?

$$x' = s_x * x$$

$$y' = s_y * y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

## 2D Rotate around (0,0)? (see next slide)

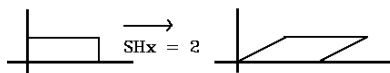


$$x' = \cos \Theta * x - \sin \Theta * y$$

$$y' = \sin \Theta * x + \cos \Theta * y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta \\ \sin \Theta & \cos \Theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

## 2D Shear?



$$x' = x + sh_x * y$$

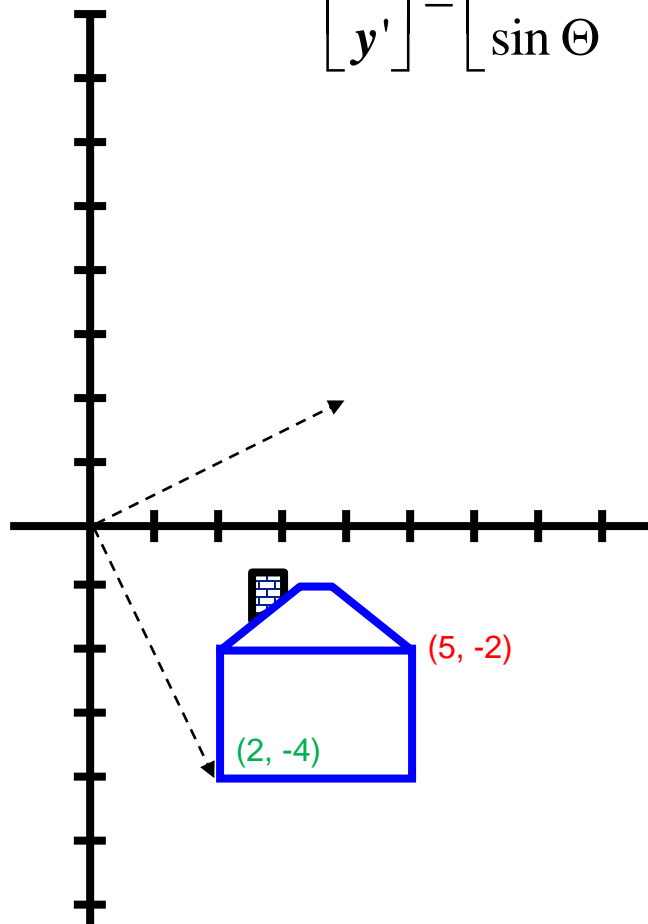
$$y' = sh_y * x + y$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & sh_x \\ sh_y & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

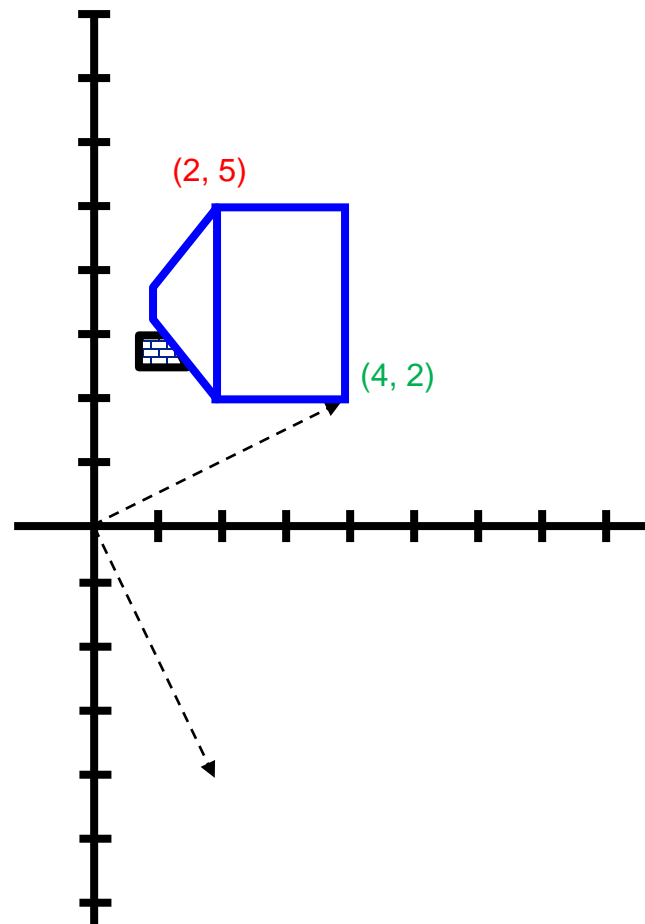
# 2D Rotation: Example

$\Theta = 90 \rightarrow M = [0 \ -1; 1 \ 0]$ , i.e.  $x' = -y, y' = x$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta \\ \sin \Theta & \cos \Theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$



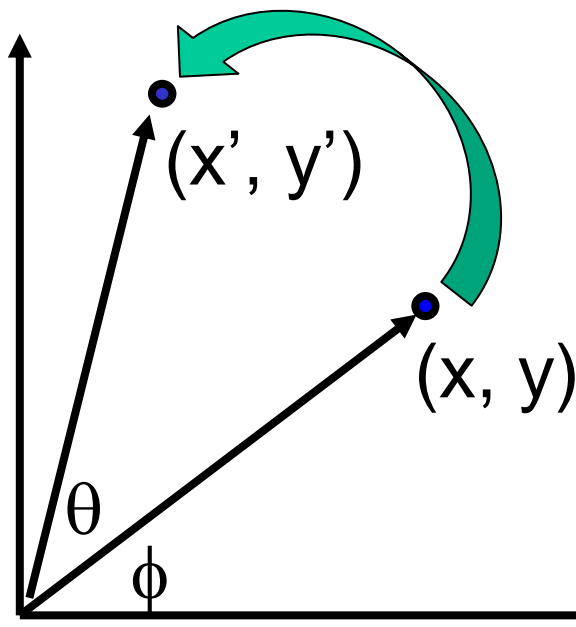
$$\begin{aligned} X' &= -Y, \\ Y' &= X \end{aligned}$$



# 2D Rotation: How to write

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$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta \\ \sin \Theta & \cos \Theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$



Polar coordinates...

$$x = r \cos(\phi)$$

$$y = r \sin(\phi)$$

$$x' = r \cos(\phi + \theta)$$

$$y' = r \sin(\phi + \theta)$$

Trig Identity...

$$x' = r \cos(\phi) \cos(\theta) - r \sin(\phi) \sin(\theta)$$

$$y' = r \sin(\phi) \cos(\theta) + r \cos(\phi) \sin(\theta)$$

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

Substitute...

$$x' = x \cos(\theta) - y \sin(\theta)$$

$$y' = x \sin(\theta) + y \cos(\theta)$$

# What transforms can we write w/ 2x2 matrix?

---

2D Mirror about Y axis?

$$\begin{aligned}x' &= -x \\ y' &= y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Mirror over (0,0)?

$$\begin{aligned}x' &= -x \\ y' &= -y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Translation?

$$\mathbf{x}' = \mathbf{x} + \mathbf{t}_x$$

$$\mathbf{y}' = \mathbf{y} + \mathbf{t}_y$$

**CAN'T DO!**

# Homogeneous coordinates

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To convert to homogeneous coordinates:

$$(x, y) \Rightarrow \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

homogeneous image  
coordinates

Converting *from* homogeneous coordinates

$$\begin{bmatrix} x \\ y \\ w \end{bmatrix} \Rightarrow (x/w, y/w)$$

Simple example:

$$y = mx + b \quad \text{vs} \quad y = \mathbf{m}\mathbf{x} \quad \text{where} \quad \mathbf{m} = [m \ b], \quad \mathbf{x} = \begin{bmatrix} x \\ 1 \end{bmatrix}$$



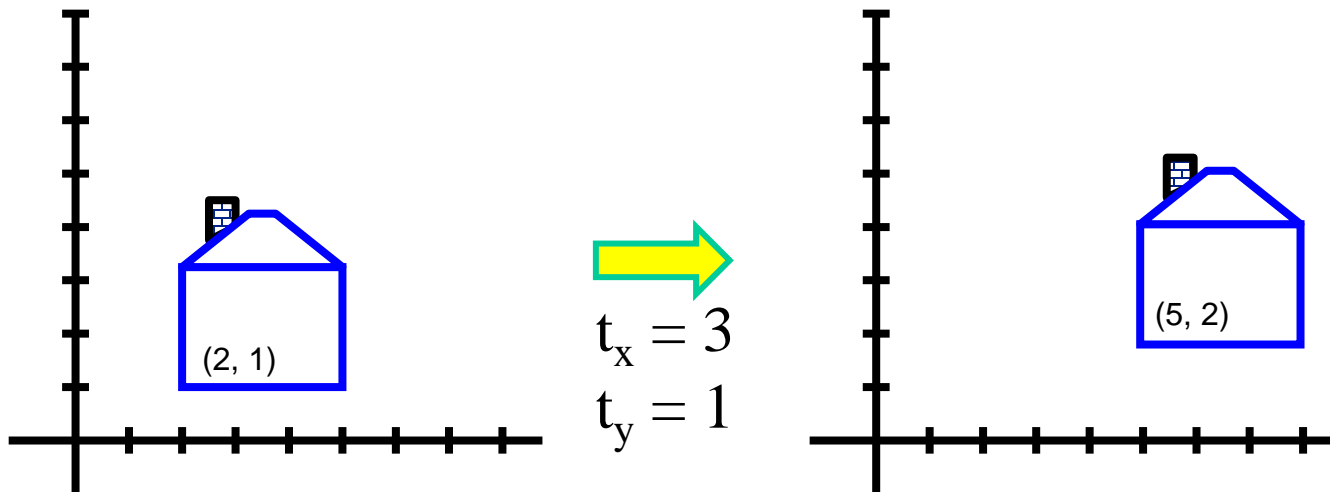


# Translation

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## Homogeneous Coordinates

$$\begin{array}{c} \downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \\ \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x + t_x \\ y + t_y \\ 1 \end{bmatrix} \end{array}$$



# 2D affine transformations

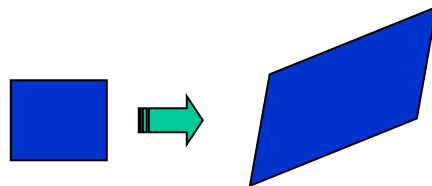
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$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Affine transformations are combinations of ... 

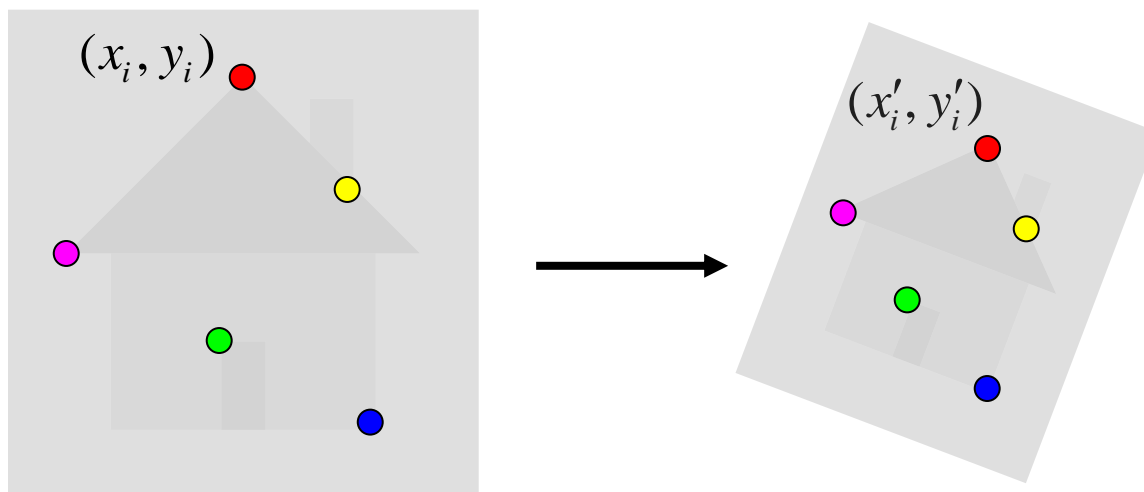
- Linear transformations, and
- Translations

Maps lines to lines, parallel lines remain parallel



# Fitting an affine transformation

- Assuming we know the correspondences, how do we get the transformation?



$$\begin{bmatrix} x'_i \\ y'_i \end{bmatrix} = \begin{bmatrix} m_1 & m_2 \\ m_3 & m_4 \end{bmatrix} \begin{bmatrix} x_i \\ y_i \end{bmatrix} + \begin{bmatrix} t_1 \\ t_2 \end{bmatrix}$$

[



$$\begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ t_1 \\ t_2 \end{bmatrix} = \begin{bmatrix} \end{bmatrix}$$



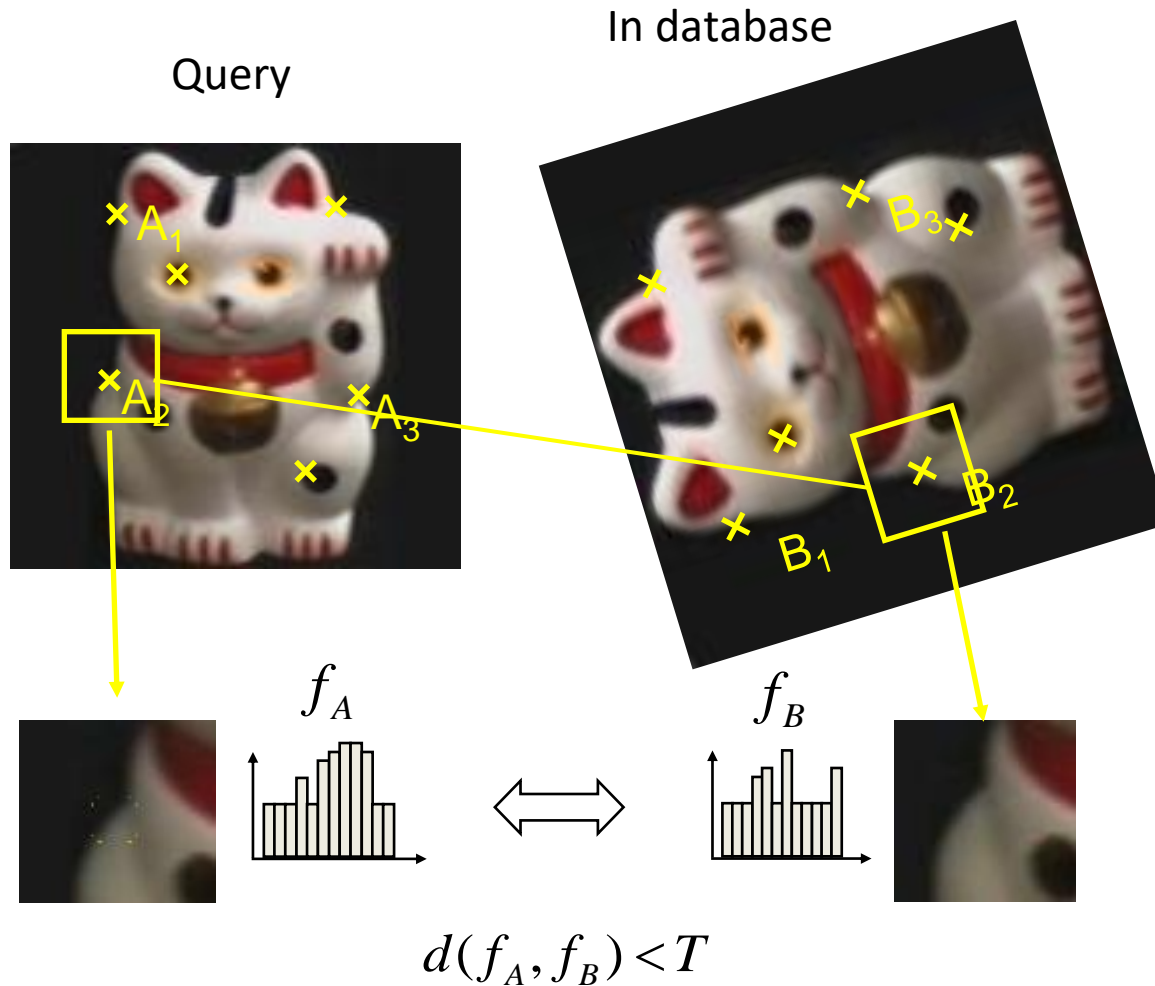
# Fitting an affine transformation

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$$\begin{bmatrix} \dots & & & & & \\ x_i & y_i & 0 & 0 & 1 & 0 \\ 0 & 0 & x_i & y_i & 0 & 1 \\ \dots & & & & & \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \\ m_3 \\ m_4 \\ t_1 \\ t_2 \end{bmatrix} = \begin{bmatrix} \dots \\ x'_i \\ y'_i \\ \dots \end{bmatrix}$$

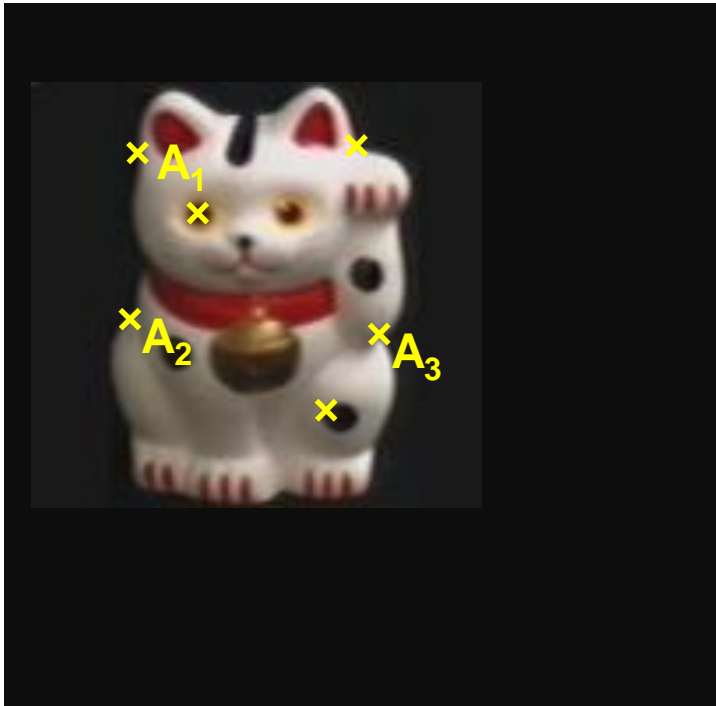
- How many matches (correspondence pairs) do we need to solve for the transformation parameters? 
- Once we have solved for the parameters, how do we compute  $(x'_{new}, y'_{new})$  given  $(x_{new}, y_{new})$ ? 

# Detour: Keypoint matching for search



1. Find a set of distinctive key-points
2. Define a region around each keypoint (window)
3. Compute a local descriptor from the region
4. Match descriptors

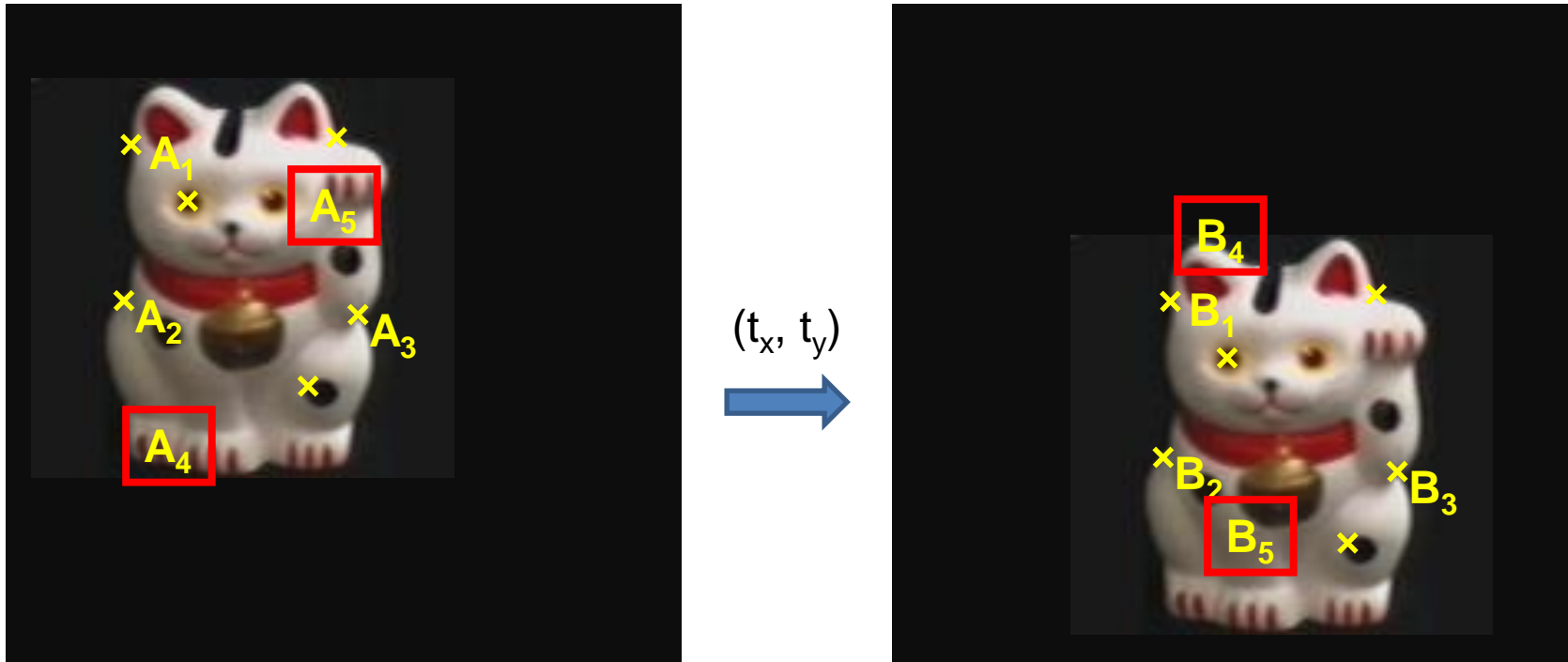
# Detour: solving for translation with outliers



Given matched points in  $\{A\}$  and  $\{B\}$ , estimate the translation of the object

$$\begin{bmatrix} x_i^B \\ y_i^B \end{bmatrix} = \begin{bmatrix} x_i^A \\ y_i^A \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

# Detour: solving for translation with outliers

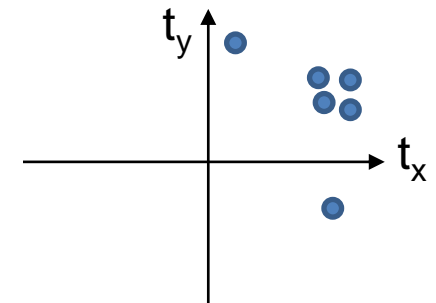


**Problem: outliers**

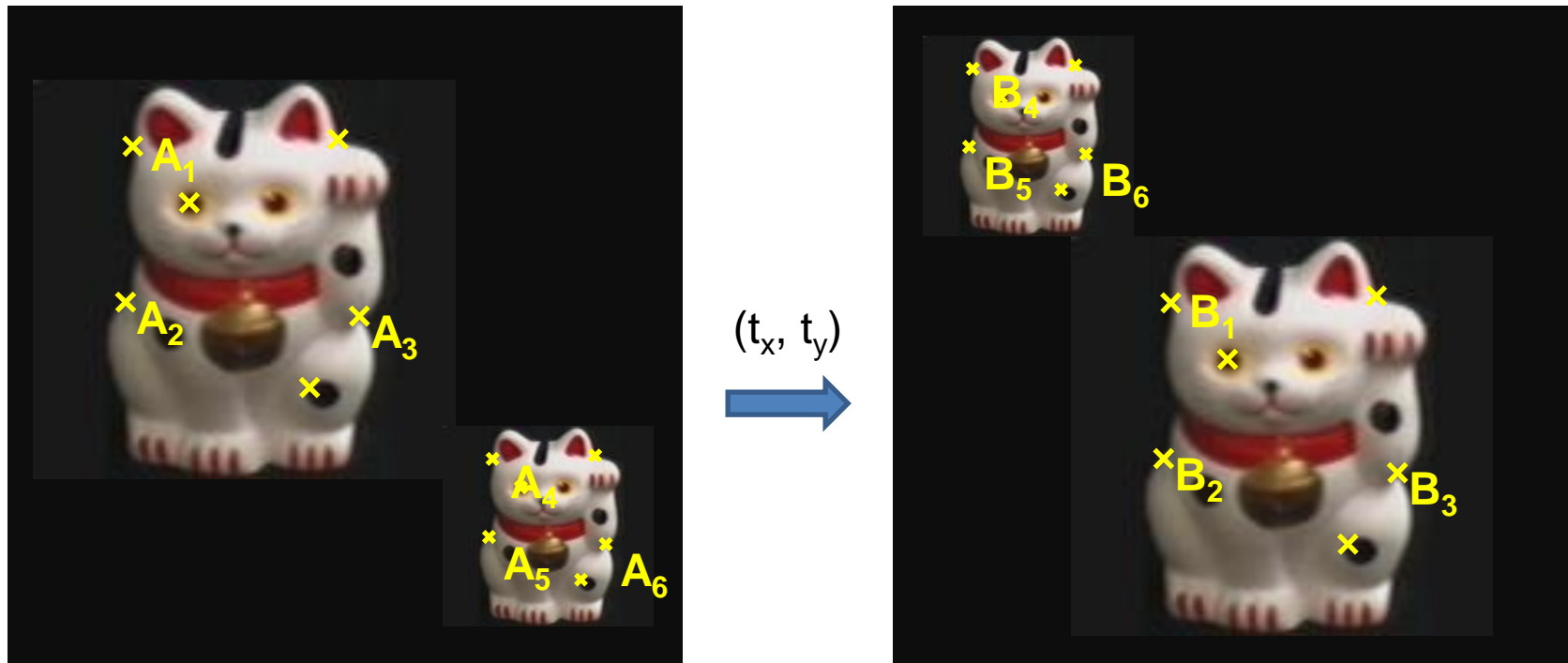
$$\begin{bmatrix} x_i^B \\ y_i^B \end{bmatrix} = \begin{bmatrix} x_i^A \\ y_i^A \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

## Hough transform solution

1. Initialize a grid of parameter values
2. Each matched pair casts a vote for consistent values
3. Find the parameters with the most votes



# Detour: solving for translation with outliers

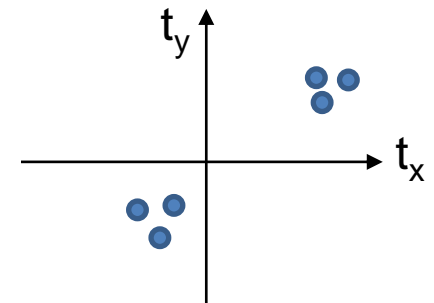


**Problem: multiple objects**

$$\begin{bmatrix} x_i^B \\ y_i^B \end{bmatrix} = \begin{bmatrix} x_i^A \\ y_i^A \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

## Hough transform solution

1. Initialize a grid of parameter values
2. Each matched pair casts a vote for consistent values
3. Find the parameters with the most votes





# 2D projective transformations

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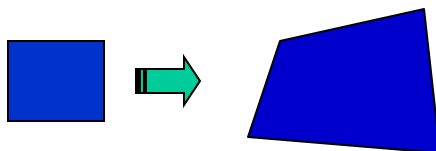


$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Projective transformations:

- Affine transformations, and
- Projective warps

Parallel lines do not necessarily remain parallel



# Projective transformations

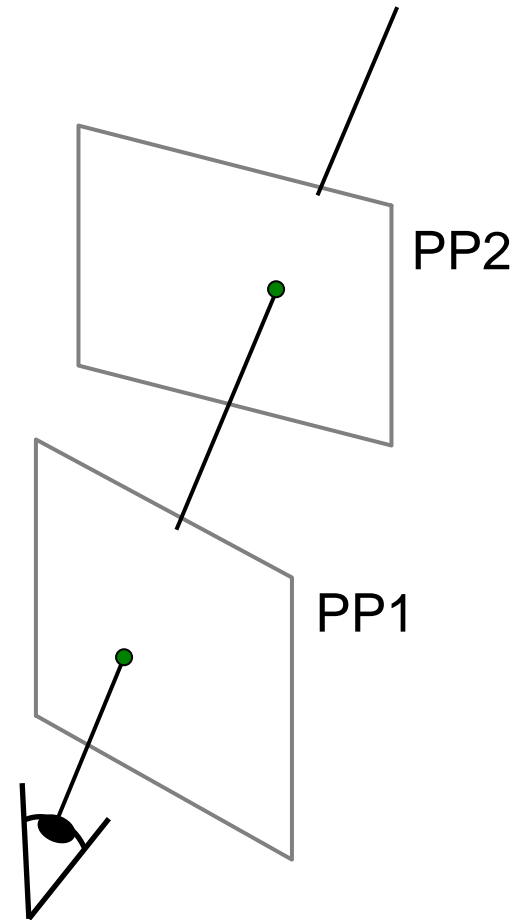
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A projective transformation is a mapping between any two projective planes with *the same center of projection*

Also called **Homography**

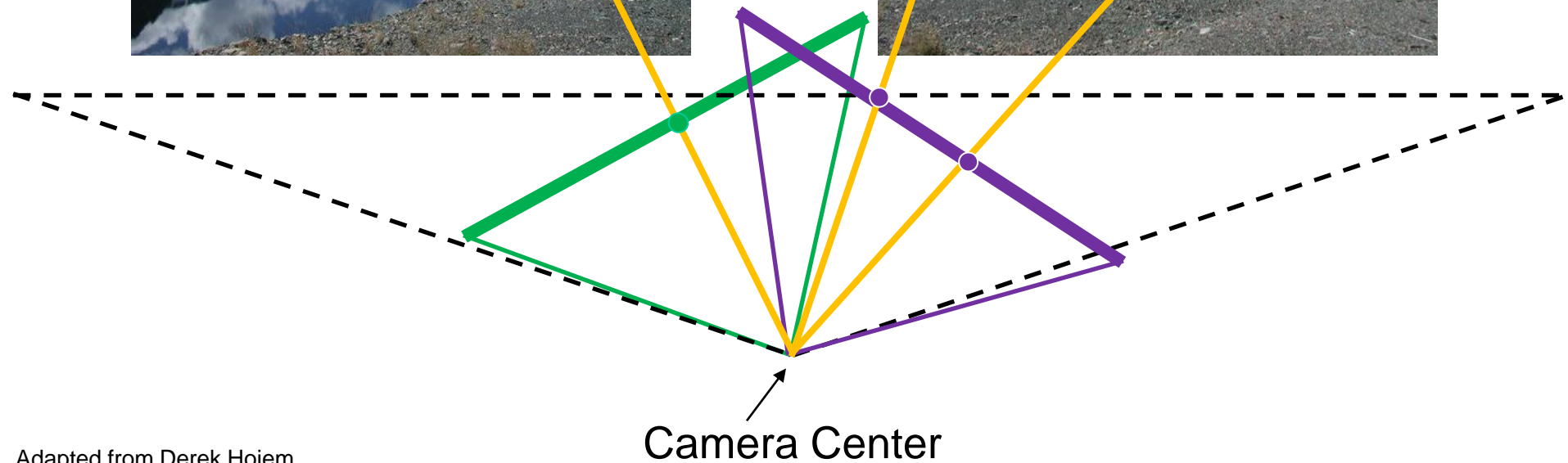
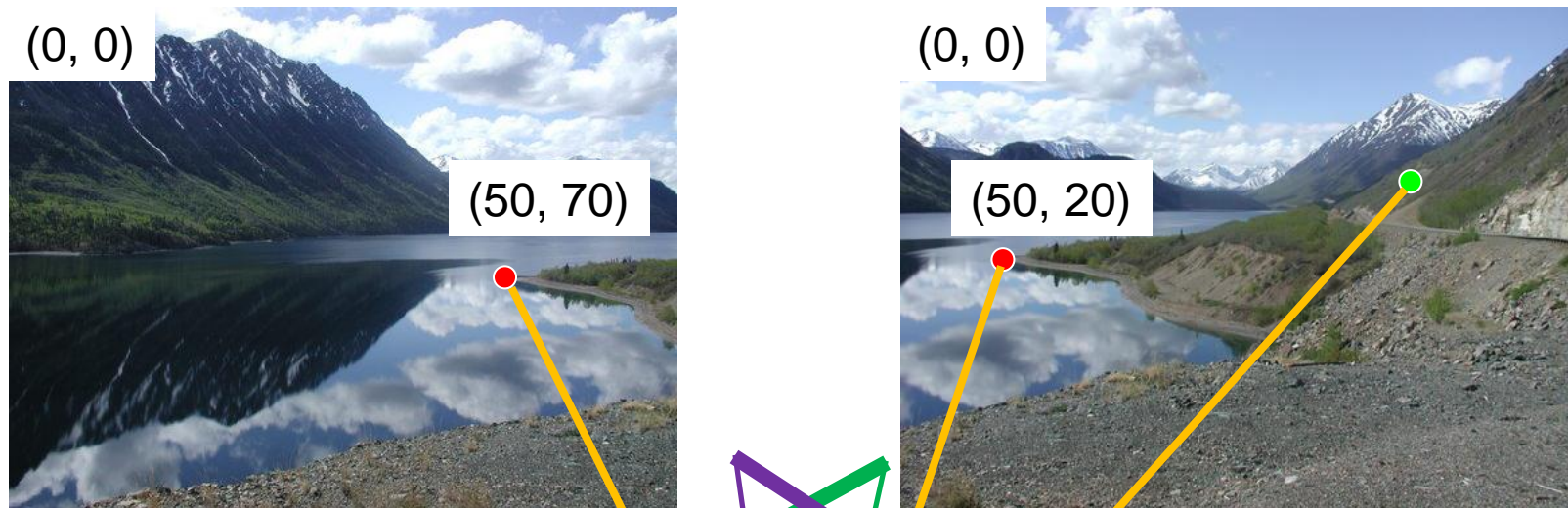
$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} * & * & * \\ * & * & * \\ * & * & * \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$\mathbf{p}' \qquad \mathbf{H} \qquad \mathbf{p}$

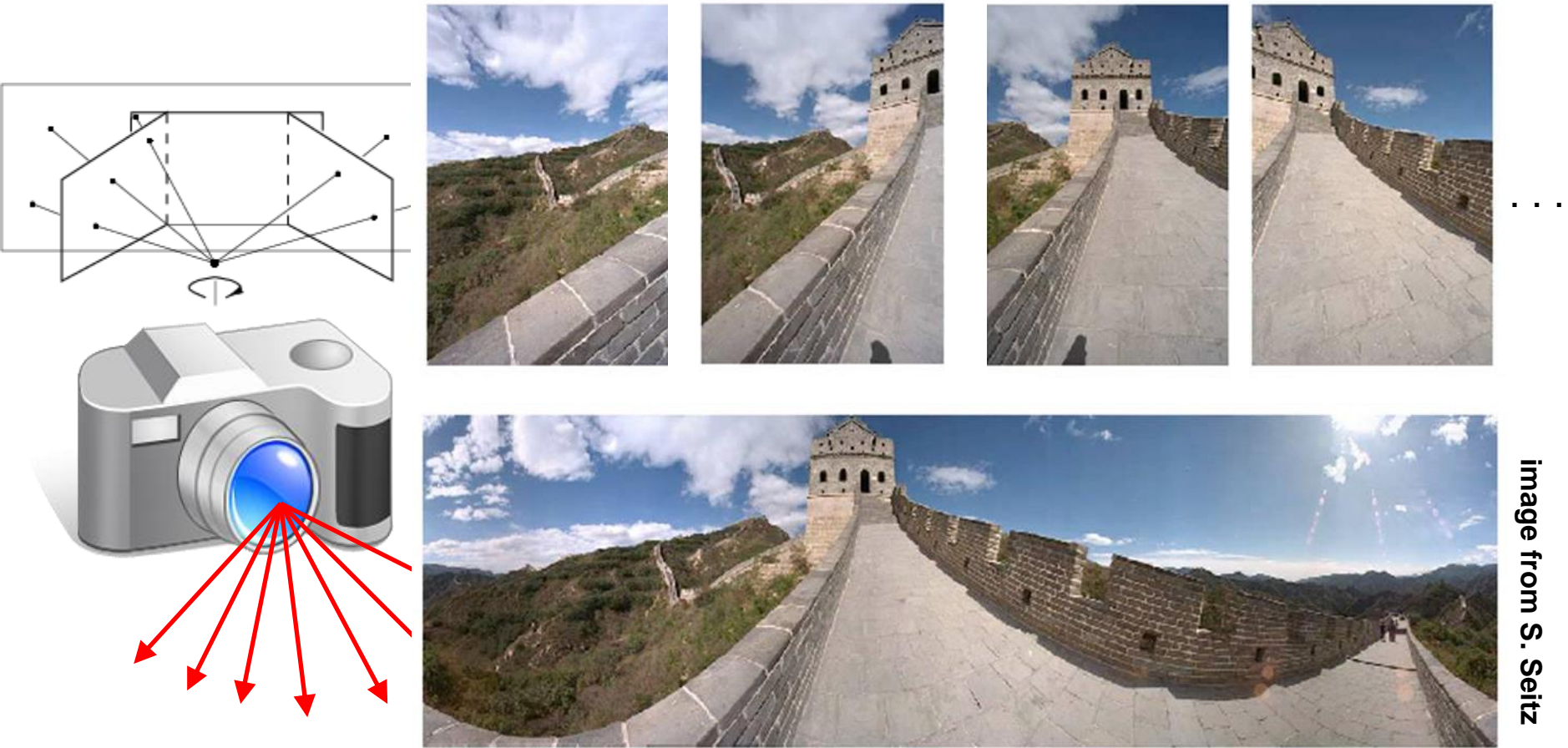


# Image mosaics: Camera setup

Two images with camera rotation but no translation



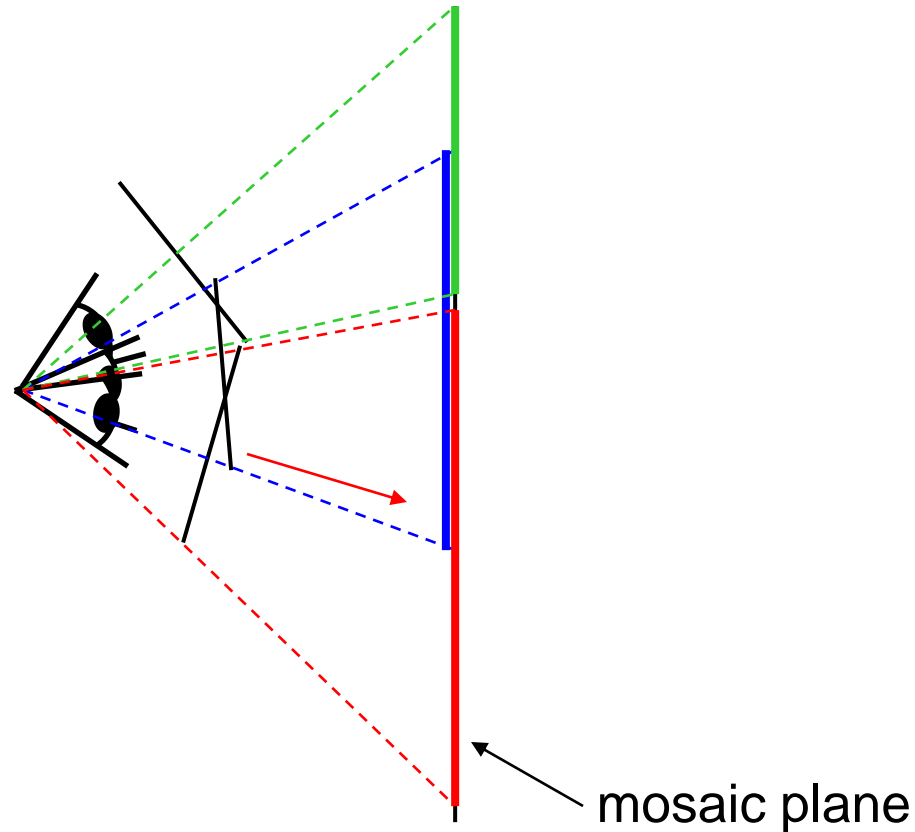
# Image mosaics: Goals



Obtain a wider angle view by combining multiple images.

# Image mosaics: Many 2D views, one 3D object

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The mosaic has a natural interpretation in 3D

- The images are reprojected onto a common plane
- The mosaic is formed on this plane
- Mosaic is a *synthetic wide-angle camera*

# How to stitch together panorama (mosaic)?

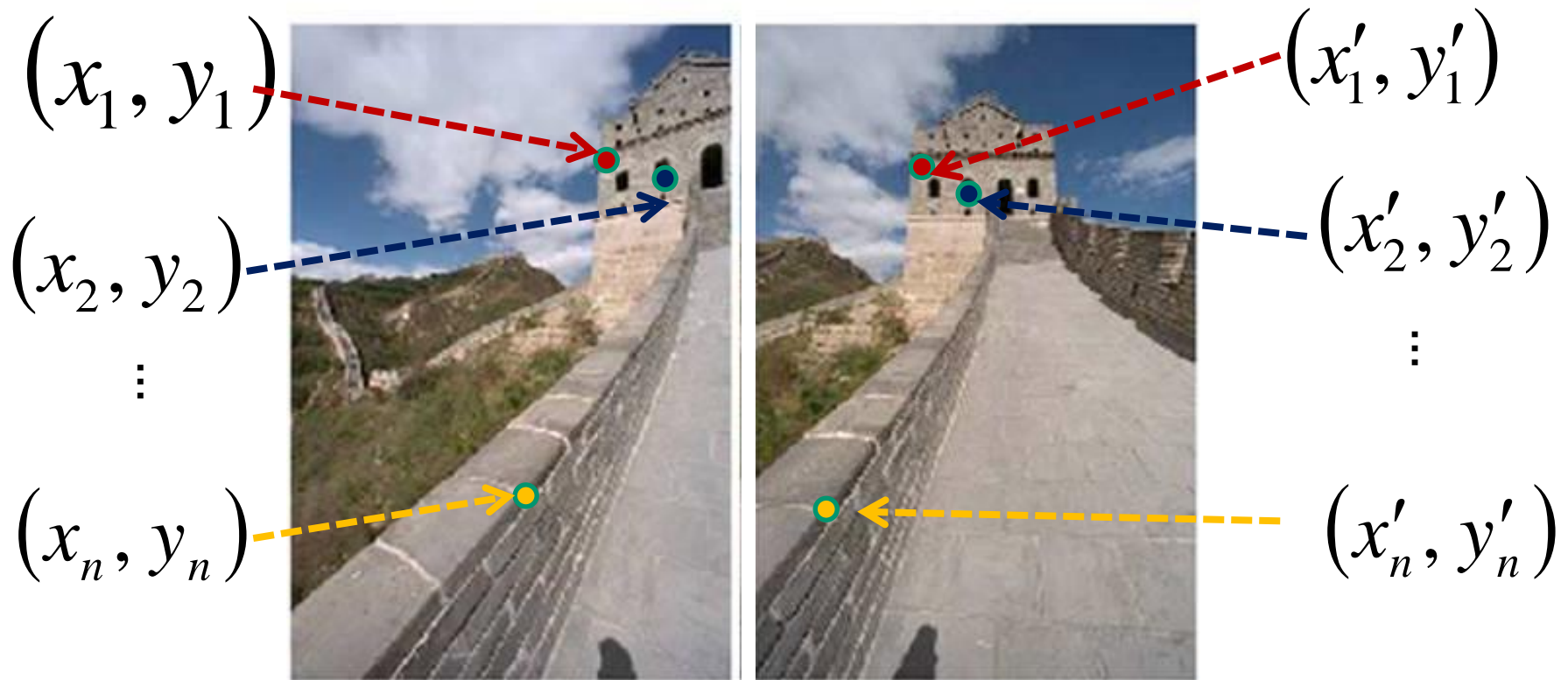
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## Basic Procedure

- Take a sequence of images from the same position
  - Rotate the camera about its optical center
- **Compute the homography (transformation) between first and second image**
- **Combine images (draw first image onto second's canvas)**
- Blend the two together to create a mosaic (post-process)
- (If there are more images, repeat)



# Computing the homography



To **compute** the homography given pairs of corresponding points in the images, we need to set up an equation where the parameters of **H** are the unknowns...



# Computing the homography

- Assume we have four matched points:  
How do we compute homography  $\mathbf{H}$ ?


$$\mathbf{p}' = \mathbf{H} \mathbf{p} \quad \mathbf{p}' = \begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} \quad \mathbf{H} = \begin{bmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & h_9 \end{bmatrix} \quad \mathbf{p} = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \quad \mathbf{h} = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \\ h_4 \\ h_5 \\ h_6 \\ h_7 \\ h_8 \\ h_9 \end{bmatrix}$$


$$\begin{bmatrix} wx' \\ wy' \\ w \end{bmatrix} = \begin{bmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & h_9 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Can set scale factor  $h_9 = 1$ .

So, there are 8 unknowns.

Need at least 8 eqs, but the more the better...

  $\mathbf{A}$   $\dots$

  $\begin{bmatrix} -x & -y & -1 & 0 & 0 & 0 & xx' & yx' & x' \\ 0 & 0 & 0 & -x & -y & -1 & xy' & yy' & y' \end{bmatrix} \mathbf{h} = \mathbf{0}$  **DEMO**

$\dots$



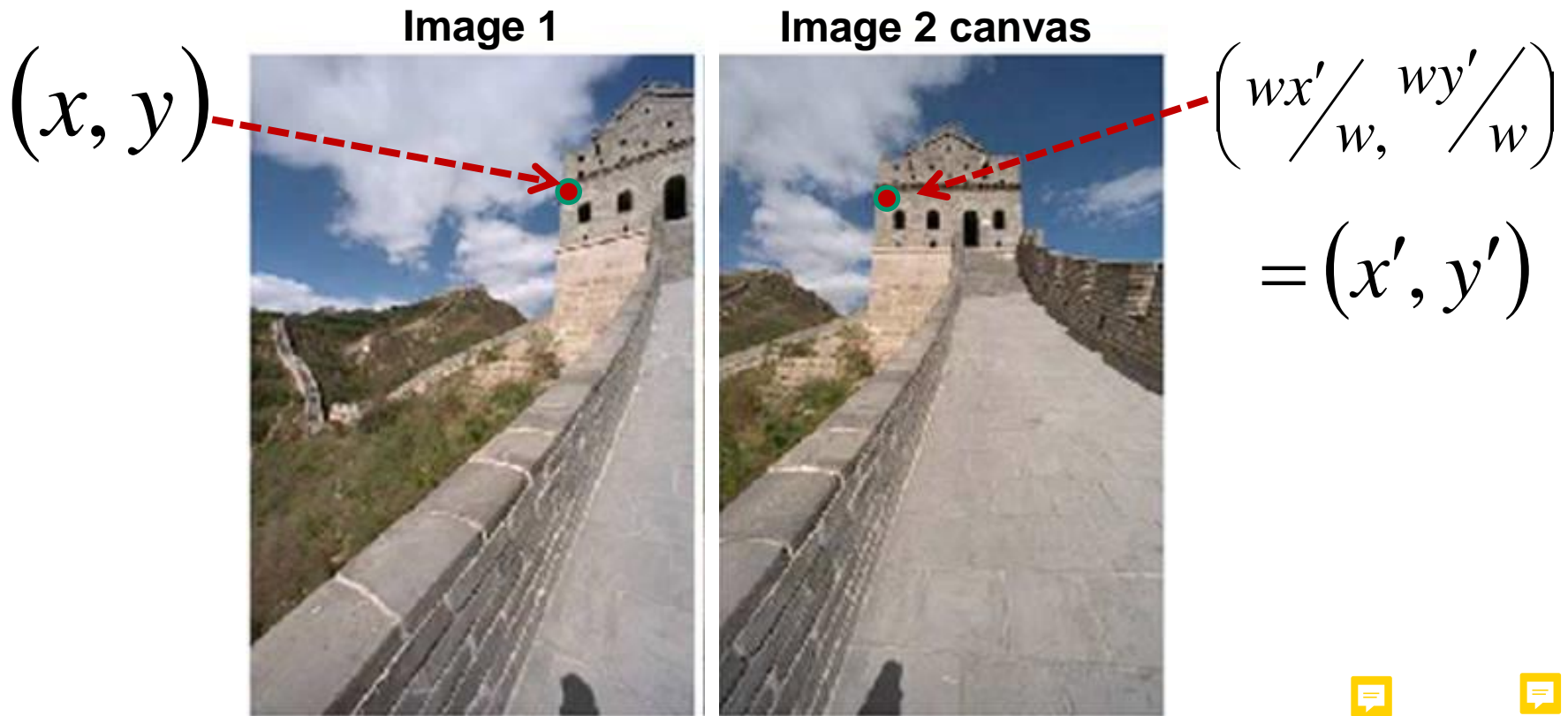
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# Combining images



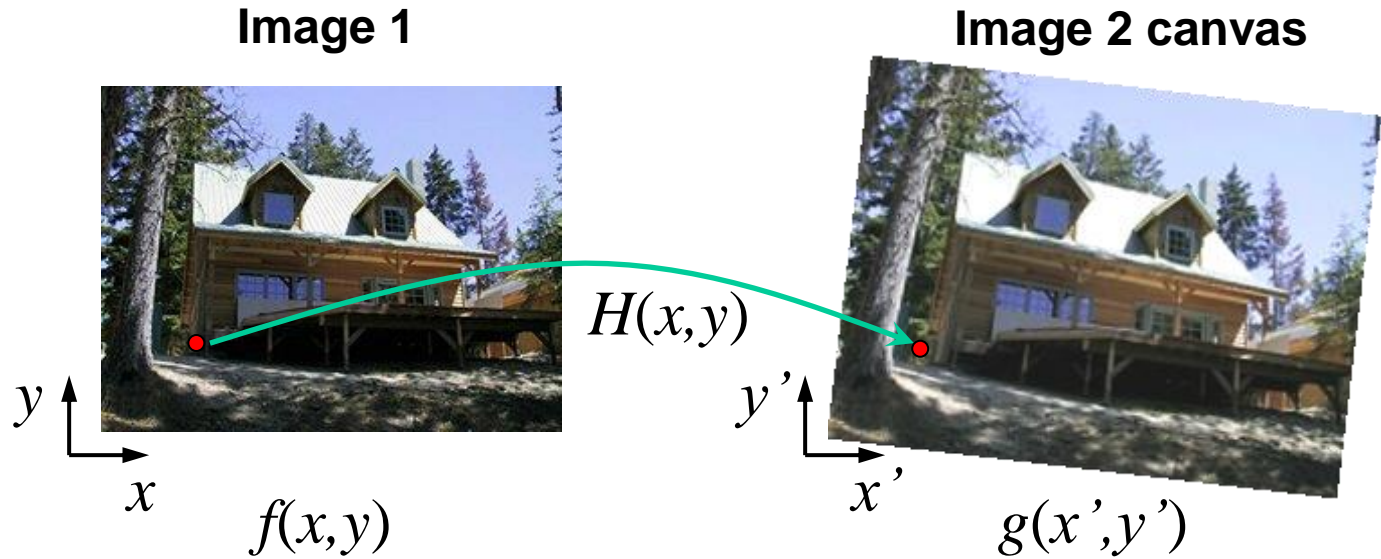
To **apply** a given homography **H**

- Compute  $\mathbf{p}' = \mathbf{H}\mathbf{p}$  (regular matrix multiply)
- Convert  $\mathbf{p}'$  from homogeneous to image coordinates

$$\begin{bmatrix} wx' \\ wy' \\ w \\ \mathbf{p}' \end{bmatrix} = \begin{bmatrix} * & * & * \\ * & * & * \\ * & * & * \\ \mathbf{H} \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \\ \mathbf{p} \end{bmatrix}$$



# Combining images



## Forward warping:

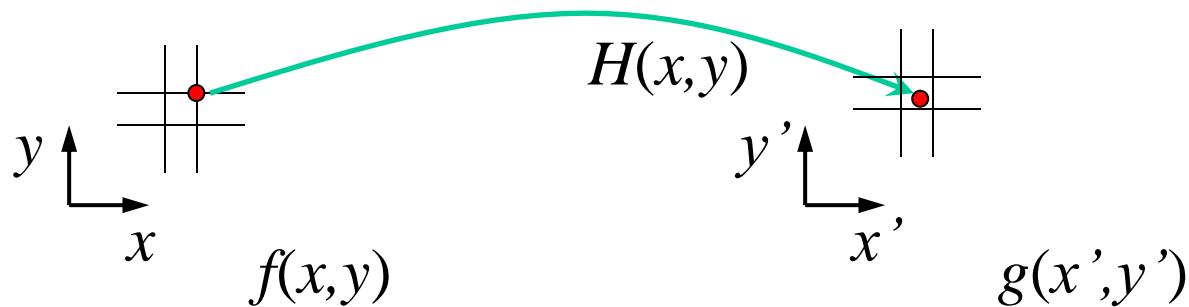
Send each pixel  $f(x, y)$  to its corresponding location

$(x', y') = H(x, y)$  in the right image



# Combining images

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## Forward warping:

Send each pixel  $f(x,y)$  to its corresponding location

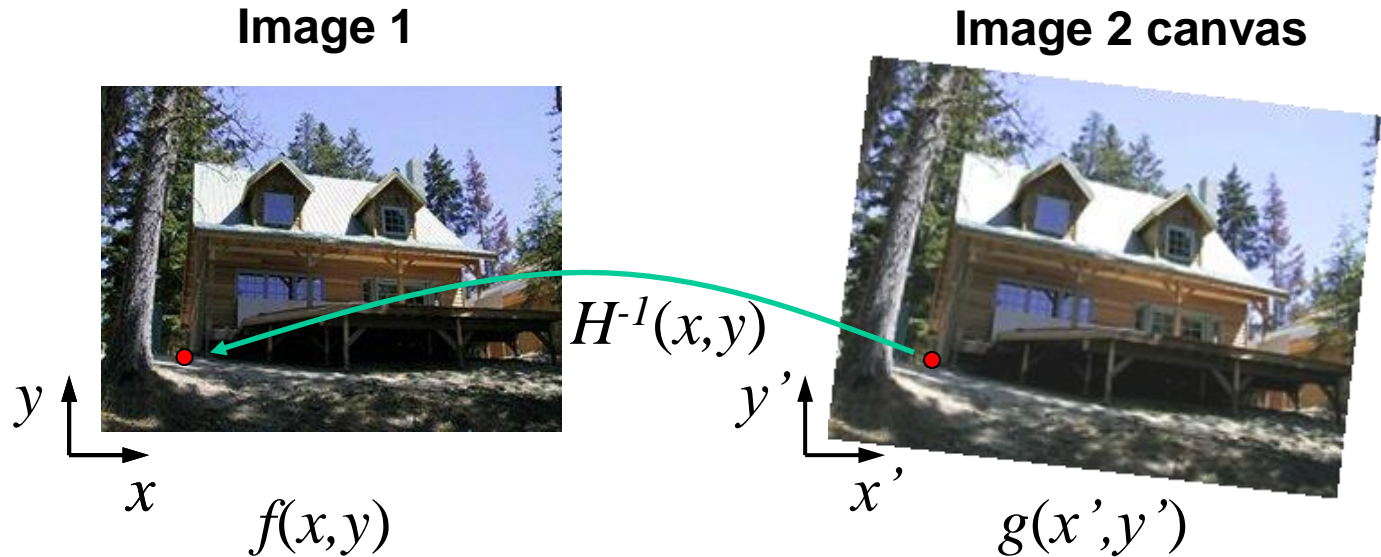
$$(x',y') = H(x,y) \text{ in the right image}$$

Q: what if pixel lands “between” two pixels?

A: *round* values of  $(x',y')$  or *distribute* color among neighbors



# Combining images



## Inverse warping:

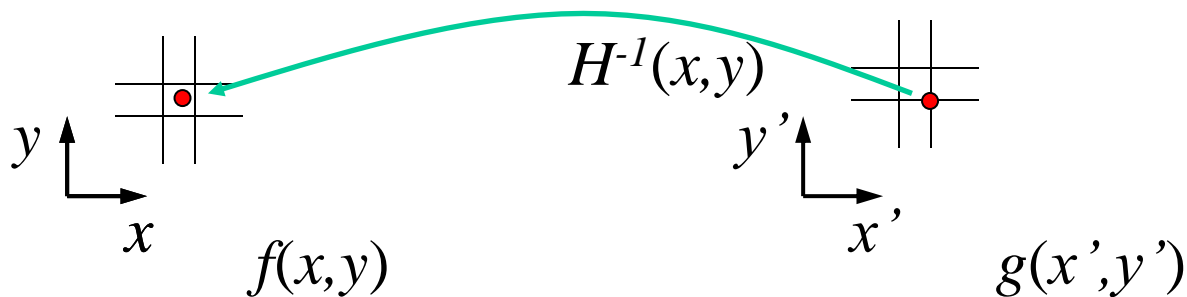
Get each pixel  $g(x', y')$  from its corresponding location

$(x, y) = H^{-1}(x', y')$  in the left image



# Combining images

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## Inverse warping:

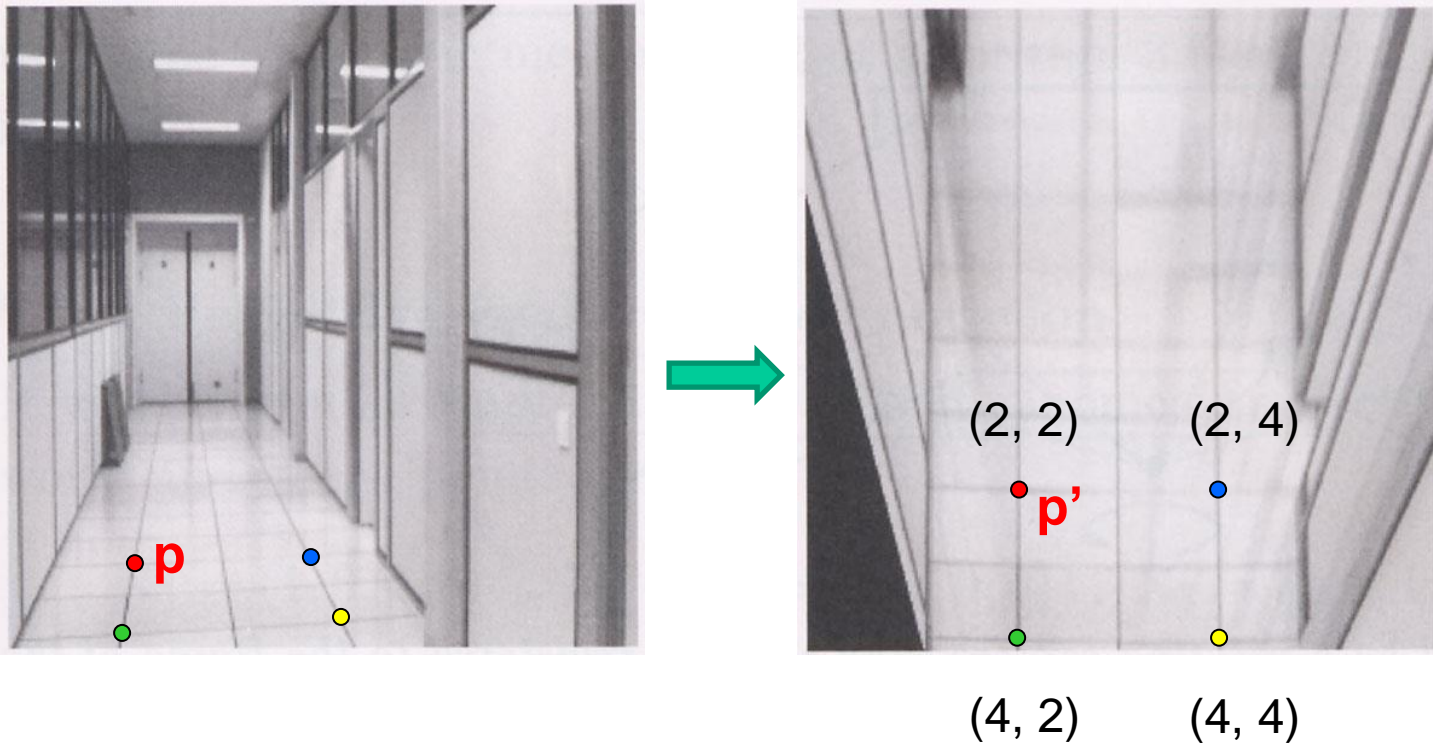
Get each pixel  $g(x',y')$  from its corresponding location

$$(x,y) = H^{-1}(x',y') \text{ in the left image}$$

Q: what if pixel comes from “between” two pixels?

A: *interpolate* color value from neighbors

# Homography example: Image rectification



To unwarp (rectify) an image solve for homography  $H$  given  $p$  and  $p'$ :  $p' = Hp$

# Summary of affine/projective transforms

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- Write **2d transformations** as matrix-vector multiplication (including translation when we use homogeneous coordinates)
- **Fitting transformations**: solve for unknown parameters given corresponding points from two views – linear, affine, projective (homography)
- **Mosaics**: uses homography and image warping to merge views taken from same center of projection
  - Perform **image warping** (forward, inverse)



# Next: Stereo vision

- Homography: Same camera center, but camera rotates
- Stereo vision: Camera center is not the same (we have multiple cameras)
- Epipolar geometry
  - Relates cameras from two positions/cameras
- Stereo depth estimation
  - Recover depth from disparities between two images

# Stereo photography and stereo viewers

Take two pictures of the same subject from two slightly different viewpoints and display so that each eye sees only one of the images.



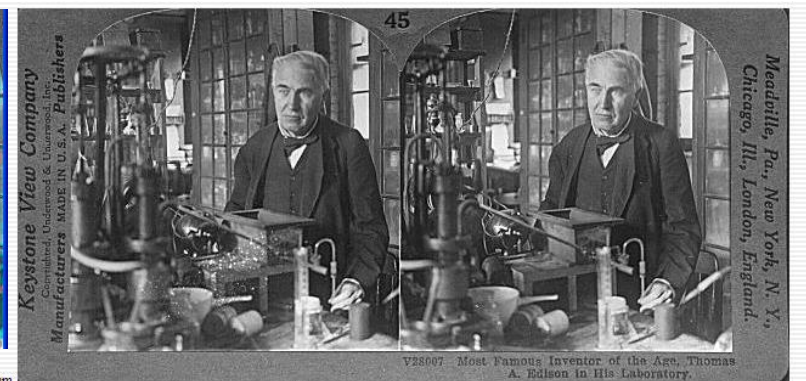
Invented by Sir Charles Wheatstone, 1838



Image from fisher-price.com



© Copyright 2001 Johnson-Shaw Stereoscopic Museum



# Depth from stereo for computers



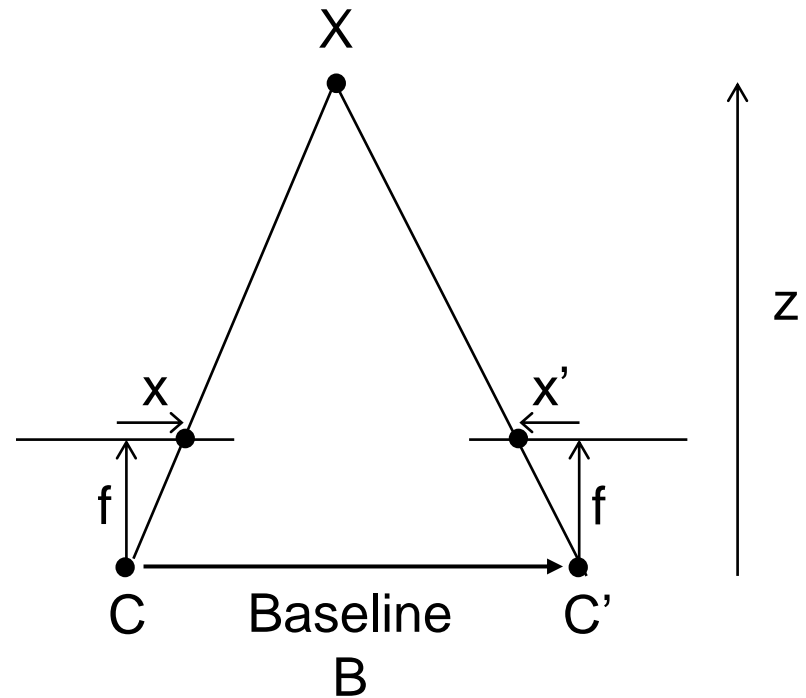
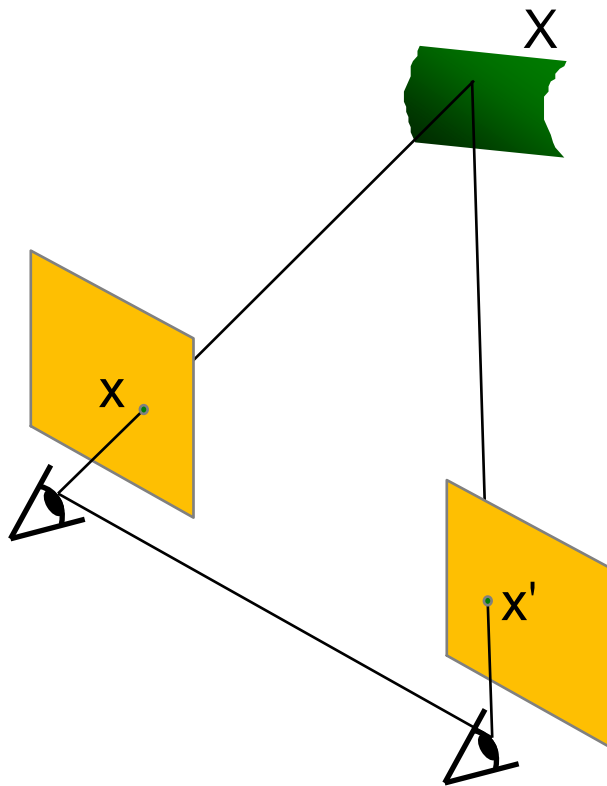
Two cameras, simultaneous views



Single moving camera and static scene

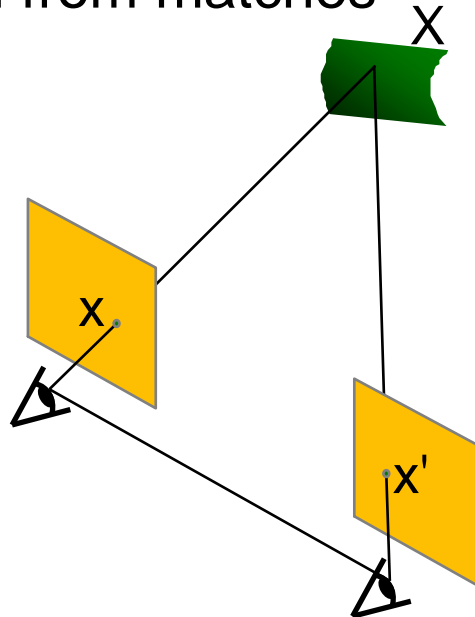
# Depth from stereo

- Goal: recover depth by finding image coordinate  $x'$  that corresponds to  $x$



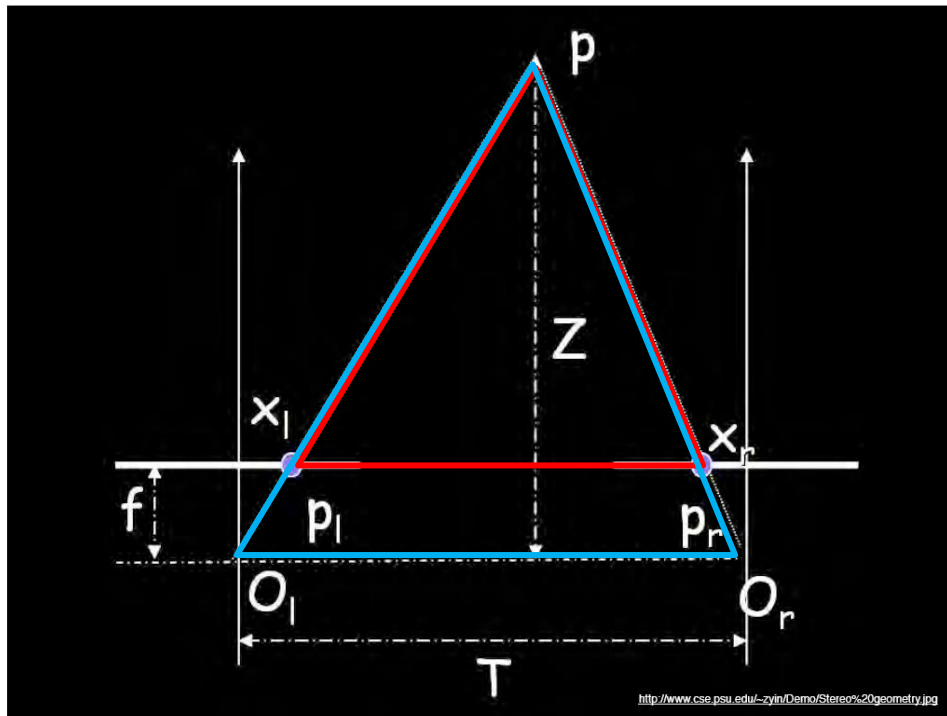
# Depth from stereo

- Goal: recover depth by finding image coordinate  $x'$  that corresponds to  $x$
- Sub-Problems
  1. Calibration: How do we recover the relation of the cameras (if not already known)?
  2. Correspondence: How do we search for the matching point  $x'$ ?
  3. Estimate depth from matches



# Geometry for a simple stereo system

- Assume parallel optical axes, known camera parameters (i.e., calibrated cameras). **What is expression for  $Z$ ?**



Similar triangles  $(p_l, P, p_r)$  and  $(O_l, P, O_r)$ :

$$\frac{T + x_l - x_r}{Z - f} = \frac{T}{Z}$$

depth  $\rightarrow$   $Z$

disparity  $\rightarrow$   $x_r - x_l$

$$Z = f \frac{T}{x_r - x_l}$$

Depth is inversely proportional to disparity.





# Depth from disparity

- We have two images from different cameras.
- If we could find the **corresponding points** in two images, we could **estimate relative depth**...
- How do we match a point in the first image to a point in the second **efficiently**?

image  $I(x,y)$



Disparity map  $D(x,y)$

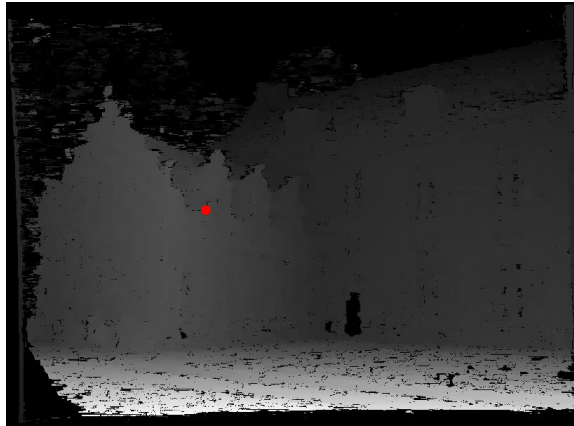
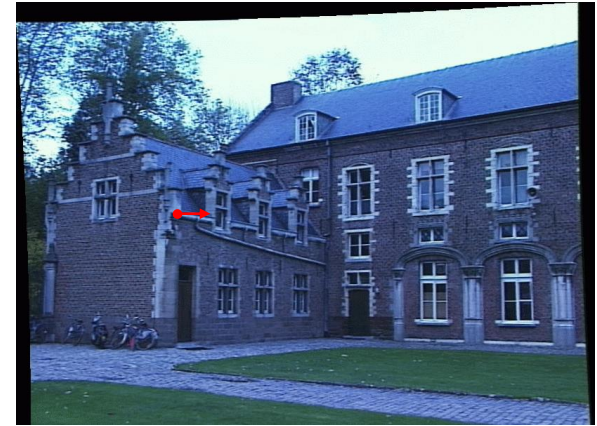
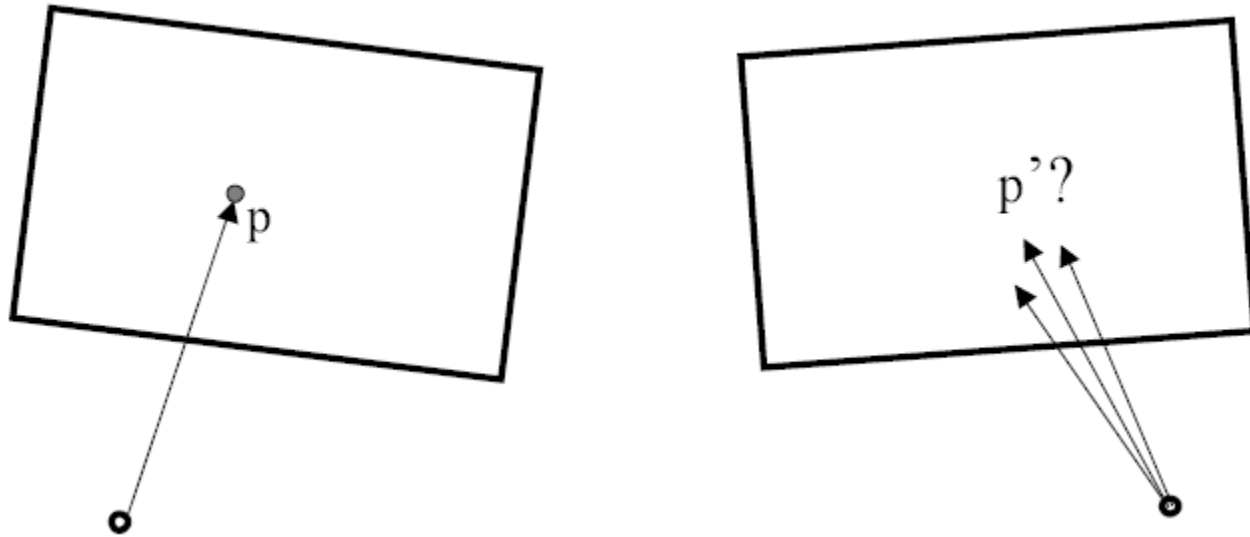


image  $I'(x',y')$



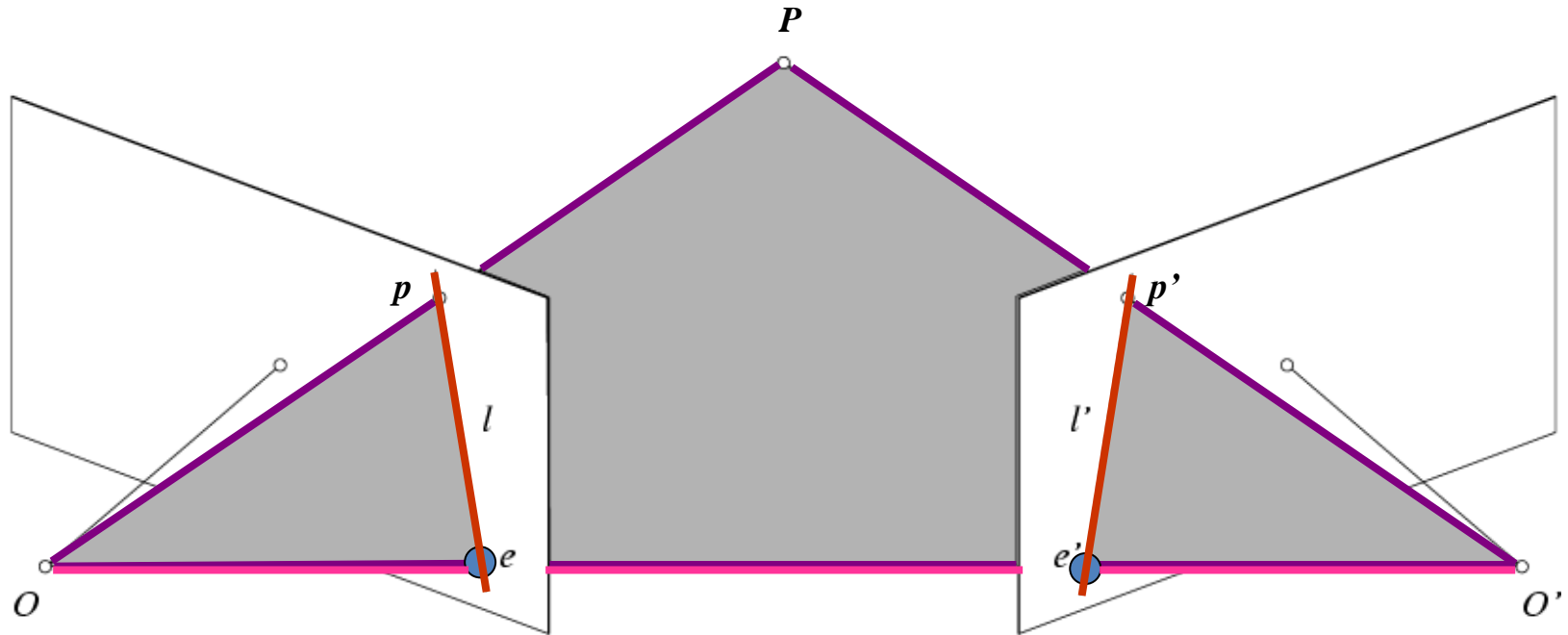
# Stereo correspondence constraints



- Given  $p$  in left image, where can corresponding point  $p'$  be?

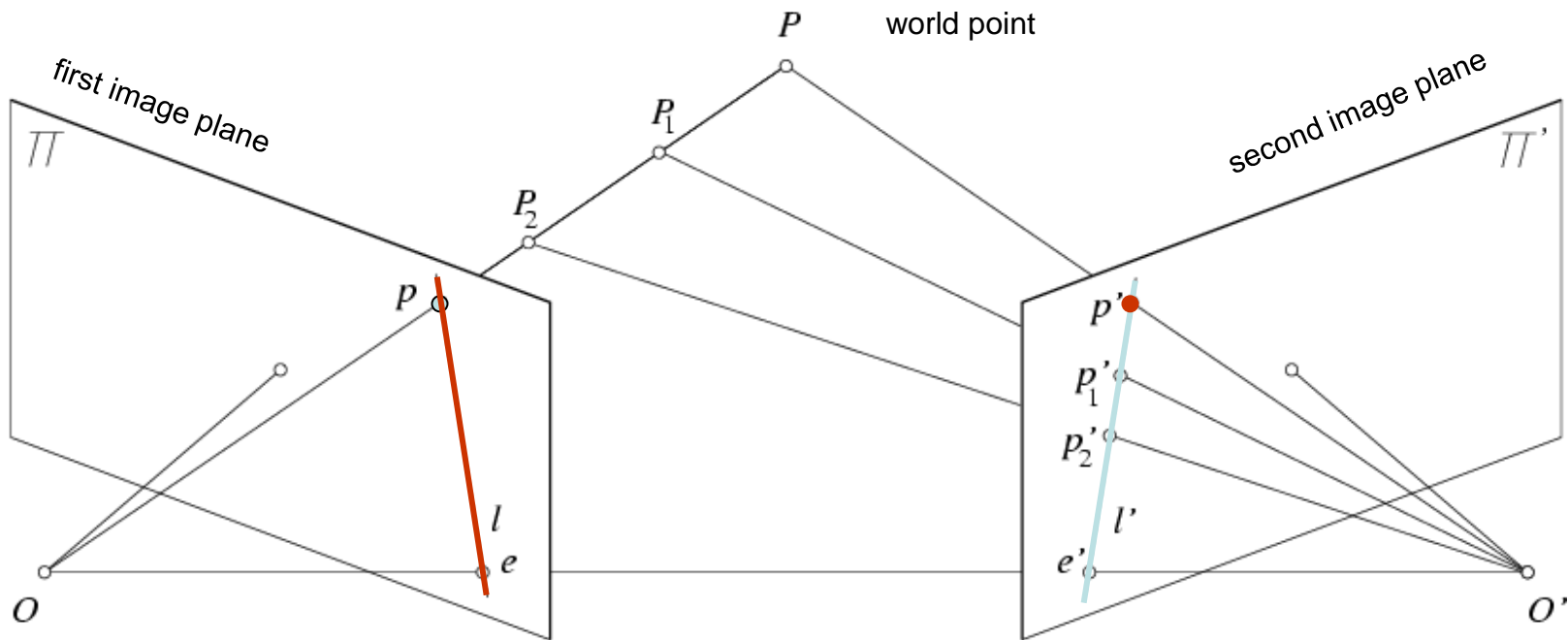


# Epipolar geometry: notation



- **Baseline** – line connecting the two camera centers
- **Epipoles**  
= intersections of baseline with image planes  
= projections of the other camera center
- **Epipolar Plane** – plane containing baseline
- **Epipolar Lines** - intersections of epipolar plane with image planes (always come in corresponding pairs)

# Epipolar constraint



Geometry of two views constrains where the corresponding pixel for some image point in the first view must occur in the second view.

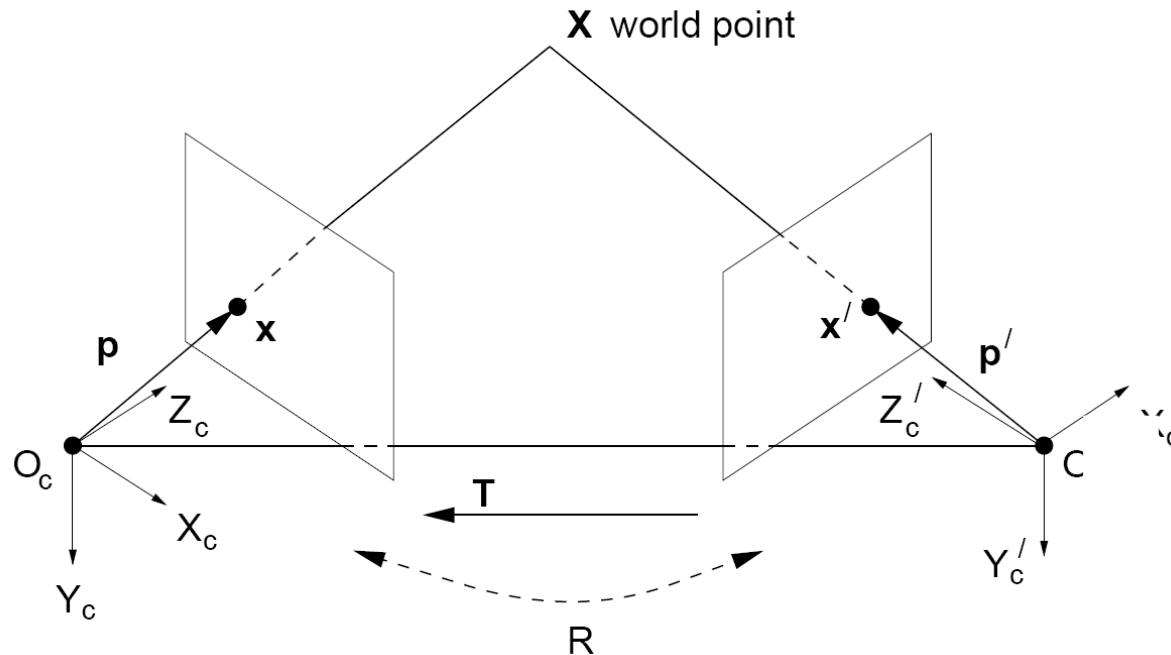
- It must be on the line where (1) the plane connecting the world point and optical centers, and (2) the image plane, intersect.
- Potential matches for  $p$  have to lie on the corresponding line  $l'$ .
- Potential matches for  $p'$  have to lie on the corresponding line  $l$ .

# Epipolar constraint



The epipolar constraint is useful because it reduces the correspondence problem to a 1D search along an epipolar line.

# Stereo geometry, with calibrated cameras



- If the stereo rig is calibrated, we know how to **rotate** and **translate** camera reference frame 1 to get to camera reference frame 2
  - Rotation: 3x3 matrix  $\mathbf{R}$ ; translation: 3x1 vector  $\mathbf{T}$ .

$$\mathbf{X}' = \mathbf{R}\mathbf{X} + \mathbf{T}$$

(See hidden slides for how we get to the next slide.)

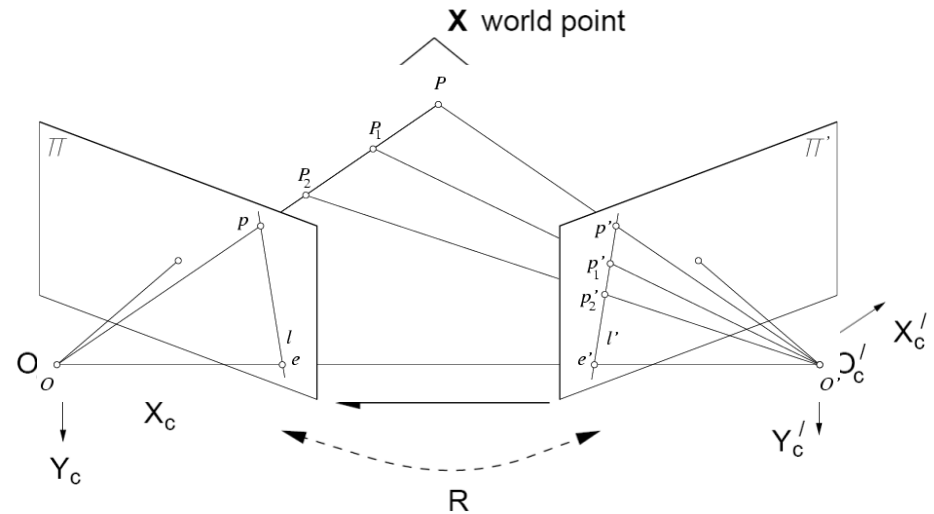
# Essential matrix

$$\mathbf{X}' \cdot (\mathbf{T} \times \mathbf{R}\mathbf{X}) = 0$$

$$\mathbf{X}' \cdot ([\mathbf{T}_x] \mathbf{R}\mathbf{X}) = 0$$

Let  $\mathbf{E} = [\mathbf{T}_x] \mathbf{R}$

$$\mathbf{X}' \cdot \mathbf{E}\mathbf{X} = \mathbf{X}'^T \mathbf{E}\mathbf{X} = 0$$

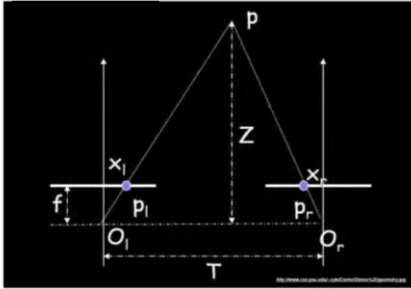


$\mathbf{E}$  is called the **essential matrix**, and it relates corresponding image points between both cameras, given the rotation and translation.

Before we said: If we observe a point in one image, its position in other image is constrained to lie on line defined by above. It turns out that:

- $\mathbf{E}^T \mathbf{x}$  is the epipolar line  $l'$  through  $\mathbf{x}'$  in the second image, corresponding to  $\mathbf{x}$ .
- $\mathbf{E} \mathbf{x}'$  is the epipolar line  $l$  through  $\mathbf{x}$  in the first image, corresponding to  $\mathbf{x}'$ .

# Essential matrix example: parallel cameras



$$\mathbf{R} =$$

$$\mathbf{T} =$$

$$\mathbf{E} = [\mathbf{T}_x] \mathbf{R} =$$

$$\mathbf{p} = [x, y, f]$$

$$\mathbf{p}' = [x', y', f]$$

$$\mathbf{p}'^T \mathbf{E} \mathbf{p} = 0$$

For the parallel cameras,  
image of any point must lie  
on same horizontal line in  
each image plane.

image  $I(x,y)$



Disparity map  $D(x,y)$

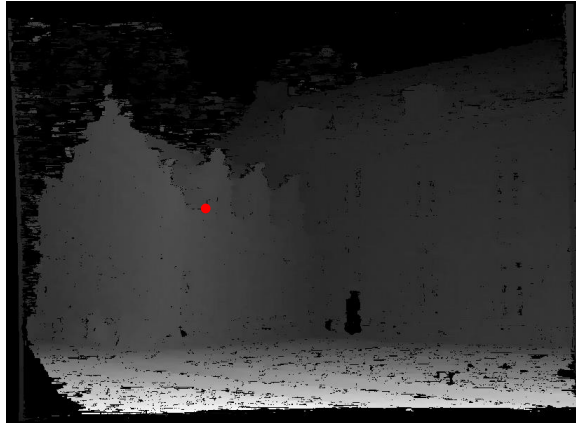
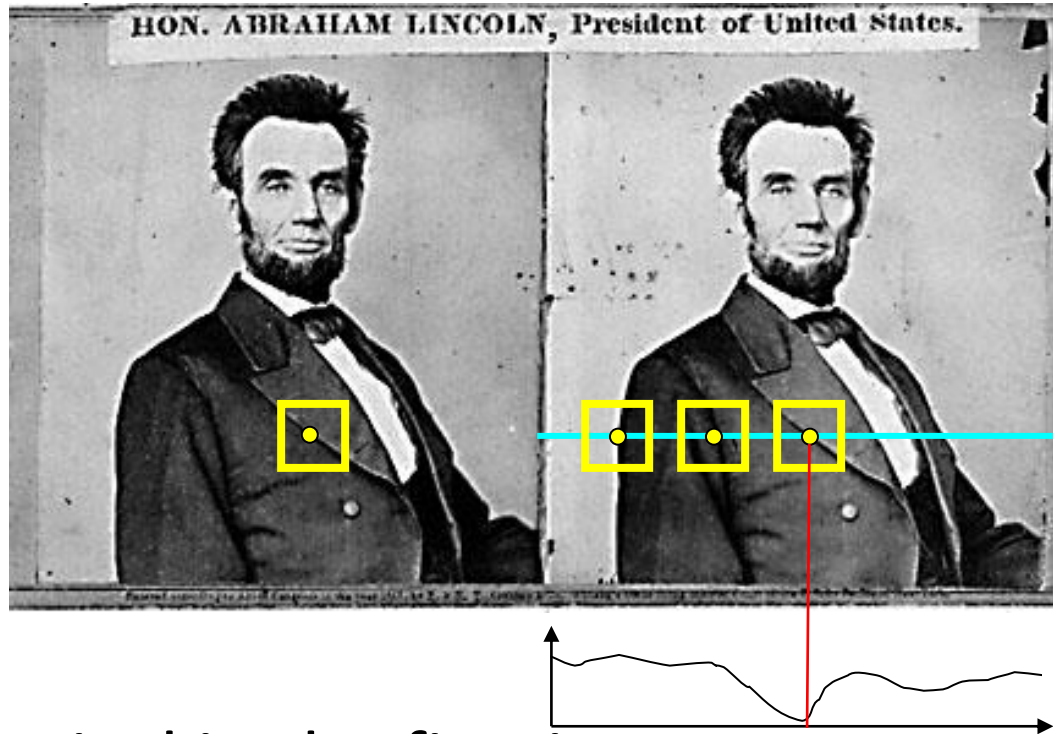


image  $I'(x',y')$



$$(x', y') = (x + D(x, y), y)$$

# Basic stereo matching algorithm



- For each pixel in the first image
  - Find corresponding epipolar scanline in the right image
  - Search along epipolar line and pick the best match  $x'$ : slide a window along the right scanline and compute Euclidean distance between contents of that window with the reference window in the left image; take the window corresponding to the minimum as the match
  - Compute disparity  $x - x'$  and set  $\text{depth}(x) = f * T / (x - x')$

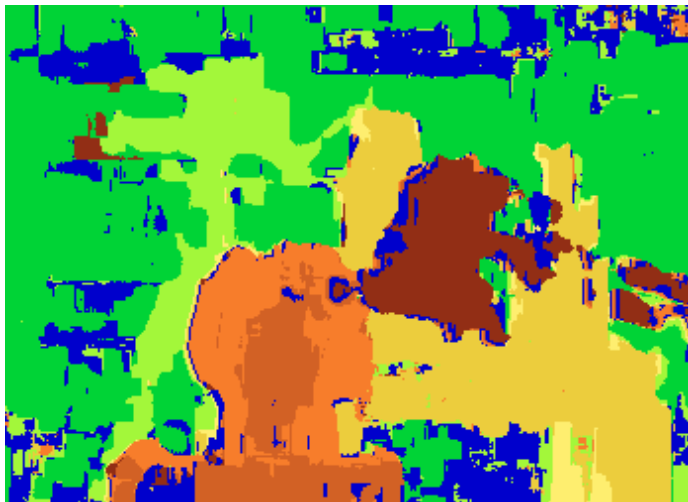


# Results with window search

Data



Predicted depth



Ground truth



# Summary of stereo vision

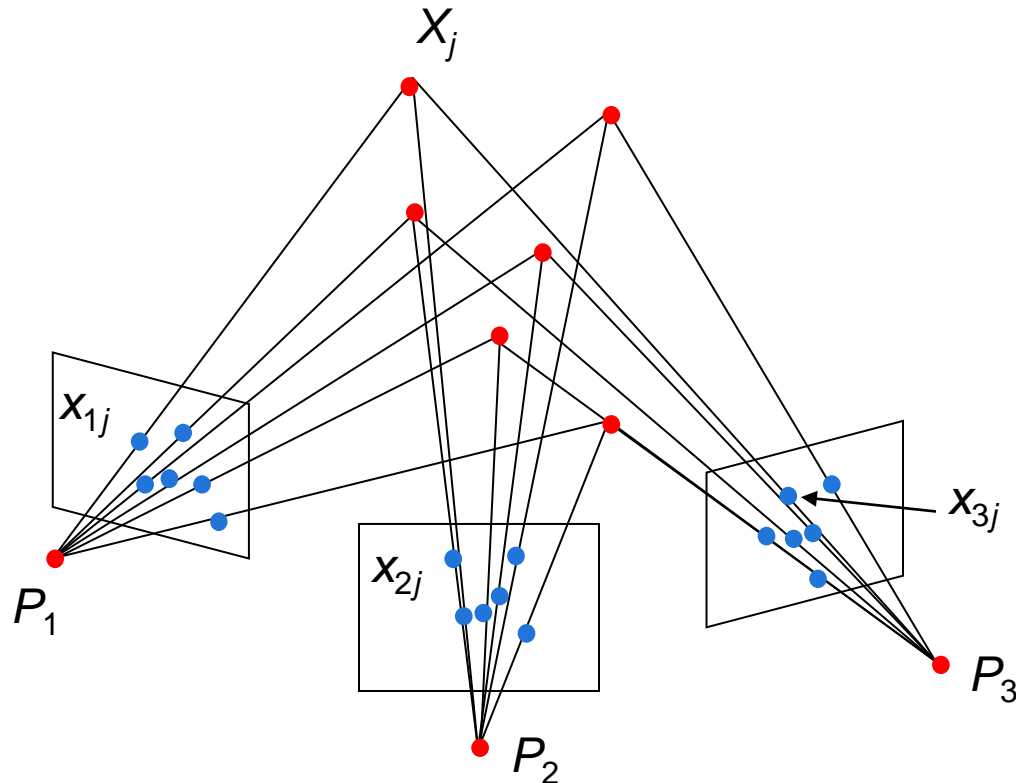
- **Epipolar geometry**
  - Epipoles are intersection of baseline with image planes
  - Matching point in second image is on a line passing through its epipole
  - Epipolar constraint limits where points from one view will be imaged in the other, which makes search for correspondences quicker
  - Essential matrix  $E$  maps from a point in one image to a line (its epipolar line) in the other
- **Stereo depth estimation**
  - Find corresponding points along epipolar scanline
  - Estimate disparity (depth is inverse to disparity)

# Projective structure from motion

- Given:  $m$  images of  $n$  fixed 3D points

$$\mathbf{x}_{ij} = \mathbf{P}_i \mathbf{X}_j, \quad i = 1, \dots, m, \quad j = 1, \dots, n$$

- Problem: estimate  $m$  projection matrices  $\mathbf{P}_i$  and  $n$  3D points  $\mathbf{X}_j$  from the  $mn$  corresponding 2D points  $\mathbf{x}_{ij}$



# Photo tourism

Noah Snavely, Steven M. Seitz, Richard Szeliski, "[Photo tourism: Exploring photo collections in 3D](#)," SIGGRAPH 2006



## Photo Tourism

Exploring photo collections in 3D

**Microsoft®**



(a)



(b)



(c)

<http://phototour.cs.washington.edu/>

# 3D from multiple images

Sameer Agarwala, Noah Snavely, Ian Simon, Steven M. Seitz, Richard Szeliski, "[Building Rome in a Day](#)," ICCV 2009

