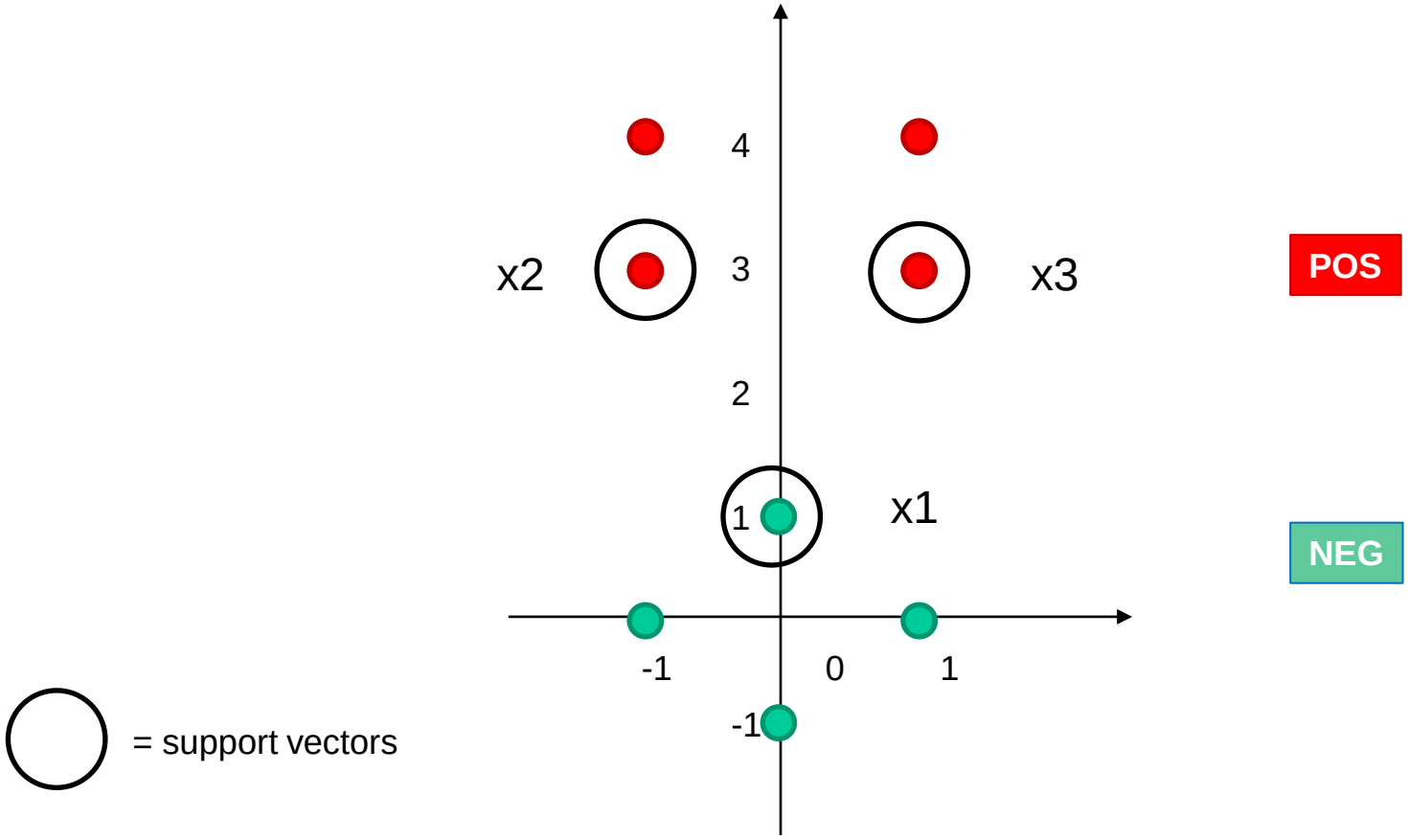
CS 1674: Intro to Computer Vision

Support Vector Machines: Exercise

Prof. Adriana Kovashka
University of Pittsburgh
October 13, 2020

Example

Simplified case: Support vectors are given



Example adapted from Dan Ventura

Solving for the alphas

- We know for the support vectors, f(x) = 1 or -1 exactly
- Add a 1 in the feature representation for the bias
- The support vectors have coordinates and labels:
  - x1 = [? ? 1], y1 = -1
  - x2 = [? ? 1], y2 = +1
  - x3 = [? ? 1], y3 = +1

Solving for the alphas

- For support vectors, $w^T x_j = y_j$ so $\Sigma_i \alpha_i y_i \text{ dot}(x_i, x_j) = y_j$
- Thus we can form the following system of linear equations (one for each of three j's), with α1, α2, α3 as the unknowns:
- α1 = ?, α2 = ?, α3 = ?

Solving for w, b

We know $w = \alpha_1 y_1 x_1 + \ldots + \alpha_N y_N x_N$ where N = # SVs

Thus w = ?, b = ?

Plotting the boundary

For SVMs, we used this eq for a line: $ax + cy + b = 0$
where $w = [a\ c]$

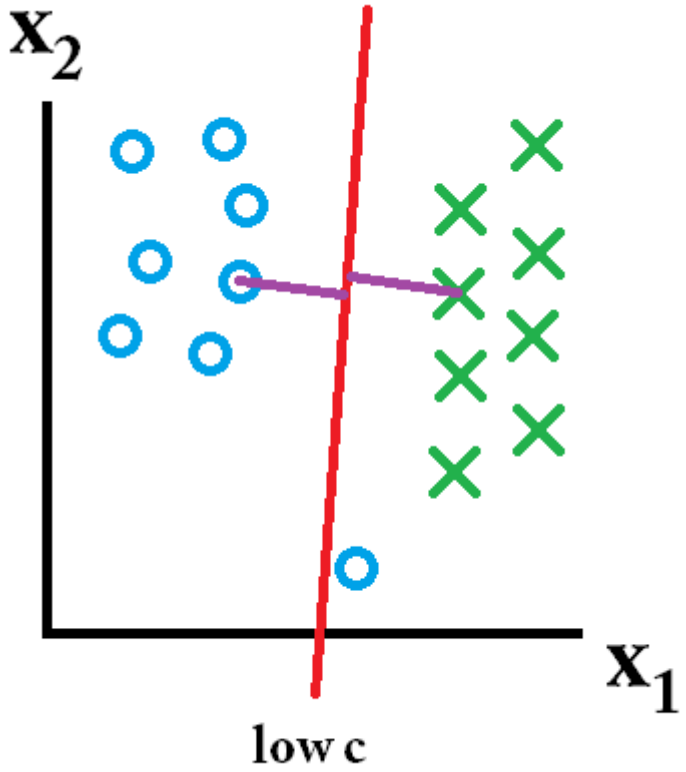
Thus $ax + b = -cy$ ➔ $y = (-a/c)\ x + (-b/c)$

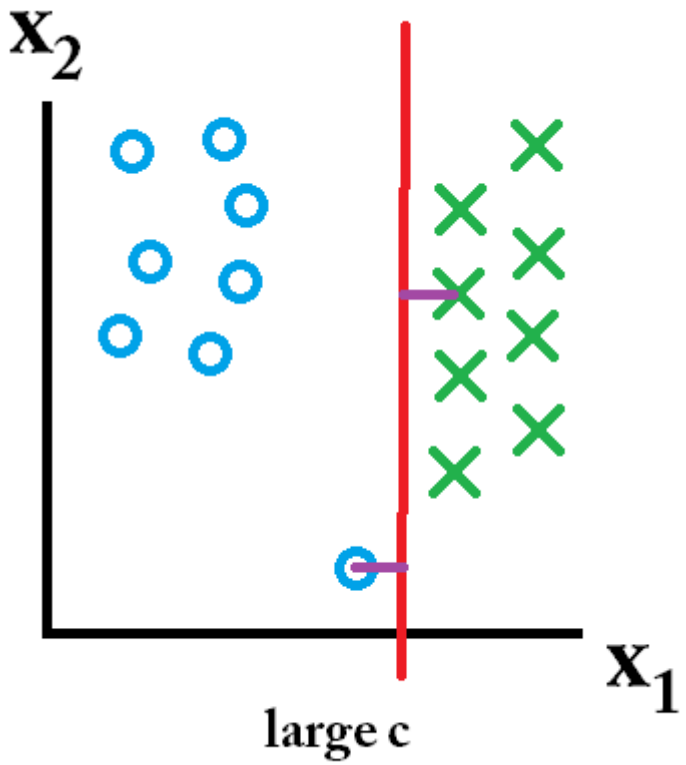
Thus y-intercept is ?

Slope of decision boundary?

Effect of margin size vs miscl. cost (c)

Training set





Misclassification ok, want large margin

Misclassification not ok

Image: Kent Munthe Caspersen

Effect of margin size vs miscl. cost (c)

Find a test set A which is better classified using a small cost c

Find a test set B which is better classified using a large cost c