

$$f: X \longrightarrow Y$$

↑
domain
↑
codomain

Remember to always
explicitly write out domain
and codomain!

$$\underbrace{\forall x \in X}_{\text{for all of the elements in } X}, \underbrace{\exists ! y \in Y}_{\substack{\text{there is} \\ \text{exactly 1} \\ \text{element of } Y}}, \underbrace{y = f(x)}_{\text{which } f \text{ assigns to } x}$$

totality
existence
uniqueness

In high school likely all the functions you dealt with were from $\mathbb{R} \rightarrow \mathbb{R}$. So you might have gotten into the habit of not specifying the domain and codomain. This is bad!!! \therefore

$f(x) = x^2$ has completely different

properties when $f: \mathbb{N} \rightarrow \mathbb{R}$ vs. $f: \mathbb{R} \rightarrow \mathbb{R}$

vs $f: \{2\} \rightarrow \mathbb{N}$ vs ...

At the very least, forgetting to specify the domain and codomain is just a sad way to lose points