Beginner's guide to rSalvador 1.8 for Windows and Linux (November 26, 2020)

This guide helps you get started with rSalvador. For more advanced usage, you should consult the accompanying technical manual or use the inbuilt help facility. To get inbuilt help for a function, e.g., newton.LD, type the R command ?newton.LD.

1 Installing rSalvador on the Windows Platform

- Download and install R 3.6.1 or higher.
- Install Rtools 3.5 by downloading and executing the file Rtools35.exe.
- Launch R.
- Install the R package devtools by executing the following command from within R.

```
install.packages('devtools')
```

• Execute the following devtools command from within R.

```
devtools::install_github("eeeeeric/rSalvador", subdir = "rsalvador")
```

2 Installation on the Linux Platform

To begin with, install R and the two R packages (hypergeo, gdata) as described in the above section. Now, follow the following five steps:

1. Make an installation directory and copy the installation file rSalvadorV1.8.tar into the installation directory. For example:

```
mkdir myrsalvador
```

- 2. Untar the installation file that is already in your installation directory (e.g., /myrsalvador): tar xvf rSalvadorV1.8.tar
- 3. A sub-directory rsalvador is now created under the installation directory (e.g., ~myrsalvador), but continue to stay in the installation directory. From the installation directory, install rSalvador by executing

```
R CMD INSTALL rsalvador
```

4. If installation is not successful, go to subdirectory \(\)myrsalvador/rsalvador/src and delete all files of the form *.o, *.so and *.rds. Then repeat the above steps.

3 Starting rSalvador

Each time you invoke an R session, you need to load rSalvador with the R command library (rsalvador).

4 Your First rSalvador Calculations

Here we use the Demerec data to demonstrate the basic capabilities of rSalvador. To view this data set, type demerec.data.

• to find the maximum likelihood estimate of m:

```
newton.LD (demerec.data)
```

• to find the 95% confidence interval for m:

```
confint.LD (demerec.data)
```

• To view the iteration details:

```
newton.LD (demerec.data, show.iter=TRUE)
```

• to display the log-likelihood function:

```
plot.likelihood.LD(demerec.data)
```

5 Importing and Exporting Data

There are three ways to transfer data into rSalvador.

• creating a sequence of numbers within R:

```
y=c(0, 16, 20, 2, 2, 56, 3, 361, 9)
```

• importing data from a text file. This data file should have just one column of numbers. It can have one or more memo lines. (Use built-in help for details.)

```
y=import.text.data('example1.txt')
```

• Typically, you may have saved your data in an Excel spreadsheet file, like the accompanying example file example2.xlsx. (See built-in help for details.) To import data from that file, type

```
y=import.excel.data('example2.xlsx')
```

• Now you can repeat the calculations in the above section by replacing demerce.data with the new data variable y.

• Occasionally it may be desirable to save your data (say in y) into a plain text file for future use. This can be done by

```
export.text.data('mytest.txt',y)
```

To read this data file back into rSalvador for analysis:

```
import.text.data('mytest.txt')
```

6 Adjusting for Plating efficiency

We use data from experiment #16 of Luria and Delbruck as an example. This experiment has a plating efficiency of 0.4. You can view the data by typing luria.16.data and learn more by typing ?luria.16.data.

• to find the maximum likelihood estimate of m:

```
newton.LD.plating(luria.16.data, e=0.4)
```

• to find the 95% confidence interval for m:

```
confint.LD.plating(luria.16.data, e=0.4)
```

• To view the iteration details:

```
confint.LD.plating(luria.16.data, e=0.4, show.iter=TRUE)
```

• to view the log-likelihood function graphically:

```
plot.likelihood.LD.plating(luria.16.data,e=0.4)
```

7 Adjusting for Relative Fitness

For the sake of illustration, assume that from a fitness assay the experimentalist learns that the relative fitness is w = 0.21 for the Demerec data. To get a maximum likelihood estimate of m, execute the R command

```
newton.MK (demerec.data, w=0.21) The output is \hat{m}=25.86. To set up a 95% CI for m, execute confint.MK (demerec.data, w=0.21) which yields a 95% CI for m: (22.98, 28.81).
```

8 Comparison of mutation rates

Two mutation rates can be compared by checking whether the two 84% confidence intervals overlap.

```
confint.LD.plating(crane.data[[1]],e=0.1,alpha=0.16)/3.6e9
confint.LD.plating(crane.data[[2]],e=0.1,alpha=0.16)/3.9e9
```

The two confidence intervals for the two mutation rates overlap, and hence the difference is not significant. If terminal cell population sizes are the same in the two experiments, compare.LD performs a likelihood ratio test. In the Newcombe experiments, the difference in N_t between Experiments F and H are small, so a likelihood ratio test is possible.

```
compare.LD(newcombe.data[[6]], newcombe.data[[8]])
```

The likelihood ratio test statistic is $\Lambda = 0.0119$ and the p-value is 0.9130.

If final cell population sizes differ noticeably, a more flexible approach is to conduct a likelihood ratio test (LRT) that accounts for the difference in final cell population size. rSalvador provides three functions for that purpose, namely, LRT.LD, LRT.LD.plating and LRT.MK. All these functions require a value of R, the ratio of the two cell population sizes. The function names are intended as a mnemonic aid, e.g., LRT.LD.plating indicates that the underlying distribution is the usual Luria-Delbrück distribution with plating efficiency less than perfect. Take the Werngren-Hoffner data for example, Here we have plating efficiency $\epsilon = 0.4$. Immediately prior to plating, the first experiment had final cell density 2.3×10^8 per mL, and the second experiment had final cell density 0.5×10^8 per mL. Therefore, R=0.5/2.3. To compare mutation rates in these two experiments, one executes the following

```
R=0.5/2.3 
 LRT.LD.plating (wh.data[[1]], wh.data[[2]], R=R, e1=0.4, e2=0.4) which gives \Lambda=15.16 and p=9.86\times 10^{-5}.
```

9 Accounting for excessive variation in N_t

When the initial inoculum size N_0 is too small (< 10, say), the final cell count N_t can vary considerably. If N_0 cannot be increased, the gamma mixture model can be used to reduce the potential bias caused by large variation in N_t . An estimate of the coefficient of variation (cv) for N_t is needed. For example, if the cv for N_t in the Demerec experiment were (hypothetically) 0.2, one can proceed as follows.

```
newton.B0 (demerec.data, cv=0.2)
```

which produces an ML estimate of 10.96 for the parameter m. Similarly, a 95% likelihood ratio CI can be obtained by

```
confint.B0 (demerec.data, cv=0.2) which yields (8.70, 13.41).
```

10 Estimating m with uncertainty about relative fitness w

The relative fitness parameter w is often measured by a competition/fitness assay in the laboratory. When the sample size is relatively large, the fundamental parameter m can be estimated while w is treated as an unknown parameter of secondary interest. For example, to find the joint ML estimate of m and w for the Demerec data, one executes:

```
newton.joint.MK(demerec.data)
```

The output is a pair of numbers, (9.852, 1.12), representing an ML estimate of (m, w).

To find a 95% profile likelihood confidence interval for m, one issues the command

```
confint.profile.m(demerec.data)
```

which yields an interval of the form (6.98, 13.01). The corresponding command for finding a 95% profile CI for the relative fitness w is

```
confint.profile.w (demerec.data)
```

which yields an interval of the form (0.887, 1.447).

11 Determining sample size

We can use the expected Fisher information for m to determine sample size. The expected Fisher information is computed by truncating an infinite series that defines the expected Fisher information. The sample size is chosen by a ψ score that indicates the quality of the resulting 95% confidence interval for m. Mathematically, the ψ score is defined by

$$\psi = \frac{\text{half width of a 95\% CI for } m}{\text{anticipated magnitude of } m}.$$

By default the expected Fisher information for m is computed by including 3000 terms.

For example, if the experimentalist believes that $m \approx 4$ and $w \approx 0.75$. By choosing $\psi = 0.25$, one computes the required sample size by executing

samp.size.MK (m=4, w=0.75, psi=0.25), which yields a sample size of 31. On the other hand, if 10% of each culture is to be plated and m is believed to be 50, then

```
samp.size.LD.plating(m=50,e=0.1,psi=0.25) yields a sample size of 15.
```

12 Determining confidence intervals for mutation rate ratio

The ratio of two mutation rates coming from two independent experiments is often of considerable interest to the investigator. As both mutation rates have their own confidence intervals, the ratio of the two rates must also be given a confidence interval to reflect the inherent uncertainty about the estimated ratio (also called a mutation rate fold change). rSalvador employs a profile likelihood approach to compute confidence intervals for mutation rate ratios. For example, to consider the mutation rate ratio from the first and the second experiment in the Werngren-Hoffner study, executing the following.

```
y1 = wh.data[[1]]; y2 = wh.data[[2]]; N1 = 2.3e8; N2 = 0.5e8;
confint.foldchange.LD.plating(y1, y2, N1, N2,
e1 = 0.4, e2 = 0.4, init.base = 2e-8, show.iter = TRUE)
```

The output is a triple of the form (1.606249, 2.484488, 3.766413). The middle number is the ratio, and the other two numbers are the lower and upper confidence limits of the confidence interval for the mutation rate ratio.